THE OFFICIAL ACT PREP GUIDE

The ONLY Official Prep Guide from the Makers of the ACT

WILEY
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Preface

You want to do your best on the ACT® test, and this book can help. It supplements our free booklet, Preparing for the ACT, and our ACT Online Prep™ (a web-based preparation program for the ACT). This book features three actual ACT tests—all of which include the optional writing test—which you can use for practice, and it gives detailed explanatory answers to every question to help you review.

Using this book will help you become familiar with the following:

- The content of the ACT
- The procedures you’ll follow when you’re actually taking the ACT
- The types of questions you can expect to find on the ACT
- Suggestions on how to approach the questions
- General test-taking strategies

This book is intended to help you know what to expect when you take the ACT so you can relax and concentrate on doing your best. The more you know about what to expect on any test you take, the more likely it is that your performance on that test will accurately reflect your overall preparation and achievement in the areas it measures. Knowing what to expect can help reduce any nervousness you may feel as you approach the test.

The ACT measures your understanding of what you’ve been taught in core high school courses that you should have completed by the time you finish high school. Because it has taken you years to learn all this material, it might take you some time to review for the ACT. You can't expect to cram for the ACT in a night or two. However, any review should be helpful to you, even if it just makes you more comfortable when you actually sit down to take the ACT. We hope this book helps you to gauge how much reviewing you feel you need to do and identify subject areas on which to focus your efforts.
How This Book Is Arranged

This book is divided into five parts:

Part One: Getting Acquainted with the ACT. Chapters in this part introduce the ACT, explain how to prepare, and present general test-taking techniques and strategies for you to consider.

Part Two: Taking and Evaluating Your First Practice Test. This part includes a practice test along with guidance on how to use the test to identify areas where you may need to invest more time and effort.

Part Three: Improving Your Score. Chapters in this part present test-taking strategies tailored for each subject test—English, math, reading, and science—along with suggestions for taking the optional writing test.

Part Four: Taking Additional Practice Tests. In this part, you have the opportunity to take two additional practice tests, see the results, and interpret your scores to determine how well prepared you are to take the ACT.

Part Five: Moving Forward to Test Day. This part prepares you for test day by explaining how to register for the ACT and describing what to expect on the day of the test, so you show up on time with everything you need.

The parts are identified by bars on the edge of their right-hand pages.

Before You Begin

There is no standardized way to prepare for the ACT. Everyone learns and prepares differently. Some people prepare best when they are by themselves. Others need to work with fellow students to do their best. Still others function best in a structured class with a teacher leading them through their work. Use whatever method works best for you. Keep in mind, though, that when you actually take the ACT, it will be just you and the test.

As you use this book to prepare for the ACT, consider working in 1-hour segments (except when you're taking the timed practice tests, of course). If you want to invest more than 1 hour a day, that's fine, but take breaks to stretch and give your mind a chance to absorb the material. Toiling to the point of burnout is counterproductive.
Part One:
Getting Acquainted with the ACT Test

In This Part
This part introduces you to the ACT, the five tests that it is composed of (English, mathematics, reading, science, and the optional writing test), and testing procedures. It also features test-taking strategies and skills that apply to all of the component tests. Specifically, you will do the following:

Find out what is covered on the tests
Determine when you can use a calculator and the types of calculators you are permitted to use and prohibited from using
Get a preview of what you can expect on test day
Obtain guidance on how to prepare for test day
Learn test-taking strategies that may improve your scores on all of the tests
Chapter 1: About the ACT

The ACT measures your achievement in core academic areas important for your college and career success: English, math, reading, science, and (optionally) writing. It isn't an IQ test—it doesn't measure your basic intelligence. It's an achievement test that's been carefully designed—using surveys of classroom teachers, reviews of curriculum guides for schools all over the country, and advice from curriculum specialists and college faculty members—to be one of several effective tools for evaluating your college and career readiness.

The individual tests that make up the ACT consist of questions that measure your knowledge and skills. You're not required to memorize facts or vocabulary to do well on the ACT. Of course, all the terms, formulas, and other information you learned in your classes will be useful to you when you take the ACT. However, last-minute cramming (such as memorizing 5,000 vocabulary words or the entire periodic table of elements) won’t directly improve your performance on the ACT.
Description of the ACT

The ACT consists of four multiple-choice tests—English, mathematics, reading, and science—and an optional writing test. Topics covered on these five tests correspond very closely to topics covered in typical high school classes. Table 1.1 gives you a snapshot of all five tests.

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<td>60 min</td>
<td>Measures mathematical skills students have typically acquired in courses taken up to the beginning of grade 12</td>
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<tr>
<td>Reading</td>
<td>40</td>
<td>35 min</td>
<td>Measures reading comprehension</td>
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<tr>
<td>Science</td>
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<td>35 min</td>
<td>Measures the interpretation, analysis, evaluation, reasoning, and problem-solving skills required in the natural sciences</td>
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<tr>
<td>Writing (optional)</td>
<td>1</td>
<td>40 min</td>
<td>Measures writing skills emphasized in high school English classes and in entry-level college composition courses</td>
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Questions on the tests are intended to help assess college and career readiness. The following sections provide an overview of what you should know to perform well on each test. For additional details, check out the ACT College and Career Readiness Standards presented in chapter 12.

**English Test**

*75 questions, 45 minutes*

The English test consists of five essays or passages, each of which is accompanied by a sequence of multiple-choice test questions. Different passage types are employed to provide a variety of rhetorical situations. Passages are chosen not only for their appropriateness in assessing writing skills but also to reflect students’ interests and experiences.

Passages and their accompanying questions test knowledge and skills related to production of writing; knowledge of language; and conventions of Standard English grammar, usage, and punctuation.

**Production of Writing**

Production of writing tests knowledge and skills in two areas of English composition:

- Topic development in terms of purpose and focus
- Organization, unity, and cohesion
Topic Development in Terms of Purpose and Focus
Examples of knowledge and skills tested include the following:

- Determine the relevance of material to the topic or the focus of the passage or paragraph
- Identify the purpose of a word or phrase (for example, identify a person, define a term, or describe an object)
- Determine whether a passage has met a specific goal
- Use a word, phrase, or sentence to accomplish a specific purpose, such as convey a feeling or attitude or illustrate a given statement

Organization, Unity, and Cohesion
Examples of knowledge and skills tested include the following:

- Determine the need for transition words or phrases to define relationships in terms of time or logic
- Determine the most logical place for a sentence in a paragraph
- Provide a suitable conclusion for a paragraph or passage (for example, summarizing the main idea)
- Provide a suitable introduction for a paragraph or passage
- Rearrange sentences in a paragraph or paragraphs in a passage to establish a logical flow
- Determine the most logical place to divide a paragraph to achieve the stated goal

Knowledge of Language
Knowledge of language questions tests your ability to clearly and succinctly express yourself in written English. Knowledge and skills tested include the following:

- Revise unclear, clumsy, and confusing writing
- Delete redundant and wordy material
- Revise an expression to make it conform to the style and tone used throughout the passage
- Determine the need for conjunctions to create logical connections between clauses
- Choose the most appropriate word or phrase in terms of the sentence content
Conventions of Standard English Grammar, Usage, and Punctuation

Conventions of Standard English Grammar, Usage, and Punctuation questions test knowledge and skills such as the following:

- Determine the need for punctuation or conjunctions to join clauses or to correct awkward-sounding fragments, fused sentences, and faulty subordination and coordination of clauses
- Recognize and correct inappropriate shifts in verb tense
- Recognize and correct disturbances in sentence structure, such as faulty placement of adjectives, participial phrase fragments, missing or incorrect relative pronouns, dangling or misplaced modifiers, faulty parallelism, run-on sentences, and weak conjunctions between independent clauses
- Maintain consistent and logical verb tense and voice and pronoun person within a paragraph or passage

Note: Spelling, vocabulary, and rote recall of grammar rules are not tested.

Mathematics Test

60 questions, 60 minutes

The mathematics test presents multiple-choice questions that require you to use reasoning skills to solve practical math problems. Some questions may belong to a set of several questions (for example, several questions about the same graph or chart).

Conceptual knowledge and computational skills are assumed as background for the problems, but recall of complex formulas and extensive computation is not required.

Math questions test knowledge and skills in the areas of number and quantity, algebra and functions, geometry, and statistics and probability, as described in the following sections.

Number and Quantity

Math questions in this category test your knowledge of numbers and fundamental math concepts and operations, including the following:

- Perform calculations on whole numbers and decimals
- Recognize equivalent fractions and fractions in lowest terms
- Locate rational numbers (whole numbers, fractions, decimals, and mixed numbers) on the number line
- Recognize single-digit factors of a number
- Identify a digit’s place value
• Demonstrate knowledge of elementary number concepts, including rounding, ordering of decimals, pattern identification, primes, and greatest common factor
• Write powers of 10 using exponents
• Comprehend the concept of length on the number line, and find the distance between two points
• Understand absolute value in terms of distance
• Find the distance between two points with the same x-coordinate or y-coordinate in the coordinate plane
• Add, subtract, and multiply matrices (tables of numbers)
• Order fractions
• Find and use the least common multiple
• Demonstrate knowledge of complex numbers and multiply two complex numbers
• Comprehend the concept of irrational numbers, such as π
• Apply properties of rational exponents
• Use relations involving addition, subtraction, and scalar multiplication of vectors and matrices
• Analyze and draw conclusions based on number concepts

**Algebra and Functions**

The mathematics test contains questions that require knowledge of and skills in algebra, functions, or both. Algebra involves formulas and equations in which letters and other symbols are used to represent unknown or unspecified values. A function is a rule, equation, or expression that produces exactly one output for any given input; for example, $2x$ is a function in that any input used for $x$ results in an output that is twice the input’s value.

**Algebra**

Algebra knowledge and skills tested include the following:

• Demonstrate knowledge of basic expressions, such as $b + g$ to identify a total
• Solve equations in the form $x + a = b$, where $a$ and $b$ are whole numbers or decimals
• Use substitution to evaluate mathematical expressions
• Combine like terms, such as $2x + 5x$
• Add and subtract algebraic expressions
• Multiply two binomials
• Match inequalities with their graphs on the number line
• Demonstrate knowledge of slope
• Solve real-world problems by using first-degree equations
• Solve inequalities
• Match linear or compound inequalities with their graphs on the number line
• Add, subtract, and multiply polynomials
• Solve quadratic equations
• Factor quadratics
• Work with squares/square roots and cubes/cube roots of numbers
• Work with scientific notation
• Solve problems involving positive integer exponents
• Determine the slope of a line from an equation
• Solve linear inequalities when the method involves reversing the inequality sign
• Solve systems of two linear equations
• Solve absolute value equations and inequalities
• Match quadratic inequalities with their graphs on the number line

Functions
Questions that involve functions test your ability to do the following:
• Understand the concept of a function having a well-defined output value at each valid input value
• Extend a given pattern by a few terms for patterns that have a constant increase or decrease between terms or that have a constant factor between terms
• Evaluate linear, quadratic, and polynomial functions expressed in function notation at the integer level
• Interpret statements that use function notation in terms of their context
• Find the domain of polynomial functions and rational functions
• Find the range of polynomial functions
• Find where a rational function’s graph has a vertical asymptote
• Use function notation for simple functions of two variables
• Relate a graph to a situation described qualitatively in terms of faster change or slower change
• Build functions for relations that are inversely proportional or exponential
• Find a recursive expression for the general term in a sequence described recursively
• Evaluate composite functions of integer values
• Compare actual values and the values of a modeling function to judge model fit and compare models
• Demonstrate knowledge of geometric sequences
• Demonstrate knowledge of unit circle trigonometry
• Match graphs of basic trigonometric functions with their equations
• Use trigonometric concepts and basic identities to solve problems
• Demonstrate knowledge of logarithms
• Write an expression for the composite of two simple functions

Algebra and Functions
Questions that involve both algebra and functions test your ability to do the following:
• Solve problems using whole numbers and decimals in the context of money
• Solve one- or two-step arithmetic problems using positive rational numbers, such as percent
• Relate a graph to a situation described quantitatively
• Solve two- or three-step arithmetic problems involving concepts such as rate and proportion, sales tax, percentage off, and estimation
• Perform word-to-symbol translations
• Solve multistep arithmetic problems that involve planning or converting units of measure (for example, feet per second to miles per hour)
• Build functions and write expressions, equations, or inequalities with a single variable for common pre-algebra settings, such as rate and distance problems and problems that involve proportions
• Match linear equations with their graphs in the coordinate plane
• Solve word problems containing several rates, proportions, or percentages
• Build functions and write expressions, equations, and inequalities for common algebra settings
• Interpret and use information from graphs in the coordinate plane
• Solve complex math problems involving percent of increase or decrease or requiring integration of several concepts
• Build functions and write expressions, equations, and inequalities when the process requires planning and/or strategic manipulation
• Analyze and draw conclusions based on properties of algebra and/or functions
• Analyze and draw conclusions based on information from graphs in the coordinate plane
• Identify characteristics of graphs based on a set of conditions or on a general equation such as $y = ax^2 + c$
• Given an equation or function, find an equation or function whose graph is a translation by specified amounts up or down

**Geometry**

Geometry questions are based primarily on the mathematical properties and relationships of points, lines, angles, two-dimensional shapes, and three-dimensional objects. Knowledge and skills tested include the following:

• Estimate the length of a line segment based on other lengths in a geometric figure
• Calculate the length of a line segment based on the lengths of other line segments that go in the same direction (for example, overlapping line segments and parallel sides of polygons with only right angles)
• Perform common conversions of money and of length, weight, mass, and time within a measurement system (for example, inches to feet and hours to minutes)
• Compute the area and perimeter of triangles, rectangles, and other polygons
• Use properties of parallel lines to find the measure of an angle
• Exhibit knowledge of basic angle properties and special sums of angle measures (for example, $90^\circ$, $180^\circ$, and $360^\circ$)
• Use geometric formulas when all necessary information is given
• Locate points in the coordinate plane
• Translate points up, down, left, and right in the coordinate plane
• Use several angle properties to find an unknown angle measure
• Count the number of lines of symmetry of a geometric figure
• Use symmetry of isosceles triangles to find unknown side lengths or angle measures
• Recognize that real-world measurements are typically imprecise and that an appropriate level of precision is related to the measuring device and procedure
• Compute the perimeter of composite geometric figures with unknown side lengths
• Compute the area and circumference of circles
• Given the length of two sides of a right triangle, find the length of the third side
• Express the sine, cosine, and tangent of an angle in a right triangle as a ratio of given side lengths
• Determine the slope of a line from points or a graph
• Find the midpoint of a line segment
• Find the coordinates of a point rotated 180° around a given center point
• Use relationships involving area, perimeter, and volume of geometric figures to compute another measure (for example, surface area for a cube of a given volume and simple geometric probability)
• Use the Pythagorean theorem
• Apply properties of 30°–60°–90°, 45°–45°–90°, similar, and congruent triangles
• Apply basic trigonometric ratios to solve right-triangle problems
• Use the distance formula
• Use properties of parallel and perpendicular lines to determine an equation of a line or coordinates of a point
• Find the coordinates of a point reflected across a vertical or horizontal line or across $y = x$
• Find the coordinates of a point rotated 90° across a vertical
• Recognize special characteristics of parabolas and circles (for example, the vertex of a parabola and the center or radius of a circle)
• Use relationships among angles, arcs, and distances in a circle
• Compute the area of composite geometric figures when planning and/or visualization is required
• Use scale factors to determine the magnitude of a size change
• Analyze and draw conclusions based on a set of conditions
• Solve multistep geometry problems that involve integrating concepts, planning, and/or visualization

Statistics and Probability

Statistics is a branch of mathematics that involves the collection and analysis of large quantities of numerical data. Probability is a branch of mathematics that involves calculating the likelihood of an event occurring or a condition existing. Statistics and probability questions test your ability to do the following:
• Calculate averages
• Read and extract relevant data from a basic table or chart and use the data in a computation
• Use the relationship between the probability of an event and the probability of its complement
• Calculate the missing data value given the average and all other data values
• Translate from one representation of data to another (for example, from a bar graph to a circle graph)
• Compute probabilities
• Describe events as combinations of other events (for example, using and, or, and not)
• Demonstrate knowledge of and apply counting techniques
• Calculate the average given the frequency counts of all the data values
• Manipulate data from tables and charts
• Use Venn diagrams in counting
• Recognize that when data summaries are reported in the real world, results are often rounded and must be interpreted as having appropriate precision
• Recognize that when a statistical model is used, model values typically differ from actual values
• Calculate or use a weighted average
• Interpret and use information from tables and charts, including two-way frequency tables
• Recognize the concepts of conditional and joint probability and of independence expressed in real-world contexts
• Distinguish among mean, median, and mode for a list of numbers
• Analyze and draw conclusions based on information from tables and charts, including two-way frequency tables
• Understand the role of randomization in surveys, experiments, and observational studies
• Demonstrate knowledge of conditional and joint probability
• Recognize that part of the power of statistical modeling comes from looking at regularity in the differences between actual values and model values

**Reading Test**

**40 questions, 35 minutes**

The reading test measures your reading comprehension in three general areas:

• Key ideas and details
• Craft and structure
• Integration of knowledge and ideas

The test comprises four sections, each containing one long or two shorter prose passages that are representative of the level and kinds of text commonly encountered in first-year college curricula. Passages on topics in social studies, natural sciences, literary narrative (including prose fiction), and the humanities are included, and the passages vary in terms of how challenging and complex they are.

**Key Ideas and Details**

Questions that test reading comprehension focus primarily on identifying key details in the passage and grasping the overall meaning of the passage. Reading skills tested are divided into three categories:

• Close reading
• Central ideas, themes, and summaries
• Relationships

**Close Reading**

Close-reading skills involve your ability to do the following:

• Locate and interpret facts or details in a passage
• Draw logical conclusions
• Paraphrase statements
Central Ideas, Themes, and Summaries
Questions that focus on central ideas, themes, and summaries challenge your ability to do the following:

- Identify the topic and distinguish it from the central idea or theme
- Identify or infer the central idea or theme of a passage
- Summarize key supporting ideas or details

Relationships
Relationship questions involve the ability to do the following:

- Identify the sequence of events or place events in their correct sequence
- Identify stated or implied cause-effect relationships
- Identify stated or implied comparative relationships

Craft and Structure
Some reading questions go beyond the meaning of the passage to challenge your understanding of how the author crafted and structured the passage. Reading skills tested in this area are divided into three categories:

- Word meanings and word choice
- Text structure
- Purpose and point of view

Word Meanings and Word Choice
Reading questions may focus on the meaning or impact of a word or phrase, challenging your ability to do the following:

- Interpret the meaning of a word or phrase, including determining technical, academic, connotative, and figurative meanings
- Understand the implication of a word or phrase and of descriptive language
- Analyze how the choice of a specific word or phrase shapes the meaning or tone of a passage

Text Structure
Text-structure questions ask you to analyze how various structural elements function to serve a specific purpose in the passage. To answer such questions, you may need to do one of the following:

- Analyze how one or more sentences in passages relate to the whole passage
• Identify or infer the function of one or more paragraphs
• Analyze the overall structure of a passage

**Purpose and Point of View**
The reading test may include questions that challenge your ability to do the following:
• Identify or infer the author’s or narrator’s purpose or intent
• Determine how an author’s or narrator’s purpose or intent shapes the content and style of the passage
• Recognize an author’s or narrator’s point of view

**Integration of Knowledge and Ideas**
Reading questions may require that you go beyond simply reading and understanding a passage to analyzing one or more passages. Reading skills tested in the area of integration of knowledge and ideas are divided into two categories:
• Arguments
• Multiple texts

**Arguments**
Questions related to argumentative essays may test your ability to do the following:
• Identify or infer the central claim being presented in the passage
• Analyze how one or more sentences offer reasons for or support the claim

**Multiple Texts**
Multiple-text questions involve reading two passages and doing the following:
• Compare the two passages
• Draw logical conclusions using information from the two passages

**Science Test**
40 questions, 35 minutes
The science test measures the interpretation, analysis, evaluation, reasoning, and problem-solving skills required in the natural sciences: life science/biology; physical science/chemistry, physics; and earth and space science. (See chapter 12 for a more detailed breakdown of science content covered on the test.)
The test assumes that students are in the process of taking the core science course of study (three years or more) that will prepare them for college-level work and have completed a course in earth science and/or physical science and a course in biology. The test presents several sets of scientific information, each followed by a number of multiple-choice test questions. The scientific information is conveyed in the form of reading passages and graphic representations—graphs (charts), tables, and illustrations.

Questions on the science test can be grouped into the following three general areas:

- Interpretation of data
- Scientific investigation
- Evaluation of models, inferences, and experimental results

**Interpretation of Data**

Interpretation of data involves the following skills:

- Select data from a data presentation (for example, a food web diagram, a graph, a table, or a phase diagram)
- Identify features of a table, graph, or diagram (for example, units of measurement)
- Find information in text that describes a data presentation
- Understand scientific terminology
- Determine how the values of variables change as the value of another variable changes in a data presentation
- Compare or combine data from one or more data presentations (for example, order or sum data from a table)
- Translate information into a table, graph, or diagram
- Perform a interpolation or extrapolation using data in a table or graph (for example, categorize data from a table using a scale from another table)
- Determine and/or use a mathematical relationship that exists between data
- Analyze presented information when given new information

**Scientific Investigation**

Questions that apply to scientific investigation are typically related to experiments and other research. Such questions challenge your ability to do the following:

- Find information in text that describes an experiment
- Understand the tools and functions of tools used in an experiment
• Understand the methods used in an experiment
• Understand experimental design
• Identify a control in an experiment
• Identify similarities and differences between experiments
• Determine which experiments use a given tool, method, or aspect of design
• Predict the results of an additional trial or measurement in an experiment
• Determine the experimental conditions that would produce specified results
• Determine the hypothesis for an experiment
• Determine an alternate method for testing a hypothesis
• Understand precision and accuracy issues
• Predict the effects of modifying the design or methods of an experiment
• Determine which additional trial or experiment could be performed to enhance or evaluate experimental results

**Evaluation of Models, Inferences, and Experimental Results**

Some questions on the science test challenge your ability to evaluate models, inferences, and experimental results. (A *model* is a description of an object or phenomenon intended to explain and predict its behavior.) To answer such questions, you must be able to do the following:

• Find basic information in a model
• Identify implications in a model
• Determine which models present certain information
• Determine which hypothesis, prediction, or conclusion is, or is not, consistent with one or more data presentations, models, or pieces of information in text
• Identify key assumptions in a model
• Identify similarities and differences between models
• Determine whether presented information or new information supports or contradicts (or weakens) a hypothesis or conclusion and why
• Identify the strengths and weaknesses of models
• Determine which models are supported or weakened by new information
• Determine which experimental results or models support or contradict a hypothesis, prediction, or conclusion
• Use new information to make a prediction based on a model

Writing Test (Optional)

1 prompt, 40 minutes

The writing test is a 40-minute essay test that measures your writing skills—specifically those writing skills emphasized in high school English classes and in entry-level college composition courses.

The test asks you to produce an essay in response to a contemporary issue. You will be given a prompt that presents the issue and provides three different perspectives on it. Your task is to write an essay in which you develop a perspective on the issue and explore how it relates to at least one other perspective.

Trained readers will evaluate your essay for the evidence it provides of a number of core writing skills. These readers will consider four key dimensions of your essay:

• Ideas and Analysis
• Development and Support
• Organization
• Language Use and Conventions

Ideas and Analysis

Effective writing depends on effective ideas. It is important to think carefully about the issue in the prompt and compose an argument that addresses the issue meaningfully. In evaluating the ideas and analysis in your essay, readers will look for your ability to do the following:

• Generate a clear main idea that establishes your perspective on the issue
• Engage with multiple perspectives on the issue by analyzing the relationship between your perspective and at least one other perspective
• Clarify your understanding of the issue and differing perspectives on it by providing a relevant context for discussion
• Analyze critical elements (e.g., implications and complexities) of the issue and perspectives under consideration
Development and Support

Even the best ideas must be developed and supported to be effective in a written argument. By explaining and illustrating your points, you help the reader understand your thinking. In evaluating this dimension of your essay, readers will look for your ability to do the following:

- Clarify your ideas by explaining your reasoning
- Bolster your claims with persuasive examples
- Convey the significance of your perspective by exploring reasons why your ideas are worth considering
- Extend your argument by considering qualifications, exceptions, counterarguments, and complicating factors

Organization

Organizational choices are essential to effective writing. Guide the reader through your discussion by arranging your ideas according to the logic of your argument. As readers evaluate the organization of your essay, they will look for your ability to do the following:

- Unify your essay by making strategic use of a controlling idea and other organizational techniques (e.g., theme or motif)
- Group ideas clearly, with each paragraph limited to the discussion of related ideas
- Produce a sequence of ideas that follows a clear logic, both in terms of the argument's overall structure (e.g., introduction, body, conclusion) and within the argument itself, with each point following from the last
- Use transitions to connect ideas, both within paragraphs (e.g., relating claims to support) and across paragraphs (e.g., moving from one discussion into another)

Language Use and Conventions

Skillful language use enhances argumentative writing. Strategic choices in the vocabulary you use and the style you employ can make your essay more effective. To evaluate your use of language, readers will look for your ability to do the following:

- Make precise word choices that communicate your ideas with clarity
- Demonstrate control over a variety of sentence structures
- Match the style of your writing to the audience and purpose (e.g., more evocative language to convey emotional appeals versus a more neutral voice to convey an argument based on reason)
- Accurately apply the conventions of grammar, word usage, syntax, and mechanics
ACT Test Formats: Paper and Online

The ACT is available as a paper test and as an online test in certain states and educational districts. Regardless of format, what is most important is the knowledge and skills you have developed over your course of study. If you know the material, whether you choose answers by marking them on paper or clicking an option on a computer screen will likely make little difference.

Using a Calculator

You may use a permitted calculator only on the mathematics test, but you are not required to do so. All math problems on the test can be solved without a calculator, and you may be able to perform some of the math more quickly in your head or on scratch paper.

Note: You may use any four-function, scientific, or graphing calculator as long as it is a permitted calculator modified, if necessary, as described in the following. For additional details and ACT's most current calculator policy, visit www.act.org.

Certain types of calculators, including the following, are prohibited:

- Calculators with built-in or downloaded computer algebra system (CAS) functionality, including the TI-89, TI-92, TI-Nspire CAS, HP Prime, HP 48GII, HP 40G, HP 49G, HP 50G, fx-ClassPad 400, ClassPad 300, ClassPad 330, and all Casio models that start with CFX-9970G (Using the TI-89 is the most common reason students are dismissed from the ACT for prohibited calculator use.)
- Handheld, tablet, or laptop computers, including PDAs
- Electronic writing pads or pen-input devices (the Sharp EL 9600 is permitted)
- Calculators built into cell phones or any other electronic communication devices
- Calculators with a typewriter keypad (letter keys in QWERTY format, but letter keys not in QWERTY format are permitted)

The following types of calculators are permitted but only after they are modified as noted:

- Calculators that can hold programs or documents (remove all documents and all programs that have CAS functionality)
- Calculators with paper tape (remove the tape)
- Calculators that make noise (mute the device)
- Calculators with an infrared data port (completely cover the infrared data port with heavy opaque material such as duct tape or electrician's tape)
- Calculators that have power cords (remove all power and electrical cords)
- Accessible calculators (such as audio-talking or braille calculators) may be allowed under the accessibility policies for the ACT test. (Visit www.act.org for details.)
If you choose to use a calculator during the mathematics test, follow these guidelines:

- Use a calculator you are accustomed to using. A more powerful, but unfamiliar, calculator may be a disadvantage. If you are unaccustomed to using a calculator, practice using it when you take the practice tests in this book, so you are comfortable with using it in a test situation.
- Do not share a calculator during the test.
- Make sure your calculator works properly. If your calculator uses batteries, the batteries should be strong enough to last throughout the testing session.
- Bring a spare calculator and/or extra batteries.

**Taking the Test**

Knowing what to expect on test day can alleviate any anxiety you may feel. The following list describes the steps you will take through the testing day:

1. You must report to the test center by the reporting time.
   - If you are testing on a **national test** date the reporting time is 8:00 AM.
     - You will need to bring the following:
       - A printed copy of your ACT admission ticket
       - Acceptable photo ID
       - Sharpened no. 2 soft-lead pencils with good erasers (no mechanical pencils or ink pens)
       - A calculator, if you would like to use one
   - If you are testing during the week day at your school through **state and district** testing the reporting time will be at the same time you usually report for school.
     - You will need to bring the following:
       - Acceptable photo ID
       - Sharpened no. 2 soft-lead pencils with good erasers (no mechanical pencils or ink pens)
       - A calculator, if you would like to use one

(**Note:** You will not be admitted to test if you are late or if your ID does not meet ACT’s requirements.)
2. When all examinees present at the reporting time are checked in and seated, wait until you are notified to start the test.

3. A short break is scheduled after the first two tests. You are prohibited from using a cell phone or any electronic device during the break, and you may not eat or drink anything in the test room. (If you take the ACT with writing, you will have time before the writing test to relax and sharpen your pencils.)

4. When time has expired, tests are collected and you are dismissed.

Note: If you do not complete all your tests for any reason, tell a member of the testing staff whether or not you want your answer document scored before you leave the test center. If you do not, all tests attempted will be scored.

For more about registering for the ACT and being well prepared for test day, turn to chapter 13.

Summary
This book should help you to understand how to get ready to take the ACT. Knowing the basics should get you started. By now, you should have a fair idea of what to expect at the test center and know where to find more information: on ACT’s website at www.act.org. Now that you know the basic information, you should be ready to start preparing for the ACT.
Chapter 2: Preparation, Skills, and Strategies

Performance on the ACT is largely influenced by two factors: the knowledge and skills you acquire over your many years of formal education and your familiarity with the test format and questions.

The best preparation for the ACT is taking rigorous high school classes. If you’ve taken challenging courses, paid attention in class, and completed your assignments satisfactorily, you’ve already done much of the preparation required to do well on the ACT.

Your familiarity with the test format and questions and your comfort and confidence in tackling the ACT also play an important role in how well you do on the test. Of course, no test-taking strategy can help you choose the correct answer when you don’t understand the question or don’t have the knowledge and skills to answer it, but certain strategies and skills can help you avoid common mistakes that will lower your score, such as misreading an answer choice or spending too much time on any given question.

The suggestions in this chapter are designed to help you build on the preparation that you have already completed. They’re taken from advice gathered over years—from education specialists, testing specialists, and people who, similar to you, have taken lots of tests. Read the advice, try it out, and see whether it helps. Realize that you can choose how you will take the ACT. Then make intelligent choices about what will work for you.
Mental Preparation

The best mental preparation for the ACT is rigorous course work, but mental preparation also involves confidence and clear thinking. The following tips will help make you feel calmer and more confident so that you’ll do your very best on the ACT.

Identify Strengths and Address Areas of Improvement

One of the best ways to prepare mentally for the test is to identify your strengths and areas of improvement, then work toward addressing the areas that may hamper your performance on the test. For example, if time expires before you have a chance to answer all of the questions on a practice test, you need to work on pacing. If you struggle to comprehend word problems in math, you need to practice solving more word problems. However, if you breeze through reading comprehension questions, you might not need to spend time improving your reading comprehension skills.

The following sections explain how to identify strengths and areas of improvement and address issues that may hamper your performance on the test.

Take the First Practice Test

To evaluate your ACT readiness take the first practice test in chapter 3 and analyze the results, as instructed in chapter 4. The test-taking experience and the results will help reveal your strengths and areas of improvement. If you do well on the first practice test, you can be confident that you know the material and are comfortable with the test format. You may decide to take additional practice tests for confirmation or review the test-taking skills in this chapter and in chapters 5 through 9 to see whether they can help you do even better.

If your performance on the first practice test falls short of your goal, you may need to do additional course work in certain subject areas or invest additional time and effort developing effective test-taking strategies and skills. Do not be discouraged if you do not meet your goal on the practice test. Be thankful that your areas for improvement were identified prior to test day and that you now have the information you need to formulate your improvement plan.

Identify Subject Areas to Review

Some students do better in certain subjects than in others. The practice tests in this book will help you identify your stronger and weaker subjects. As you take and score the practice tests, create a list of the subject areas and types of questions you struggle to answer. For example, if you had trouble answering math questions about angles in a triangle, the circumference of a circle, the volume of a cube, the relationships among parallel and perpendicular lines, and so forth, you may need a refresher course in plane geometry.

Chapter 1 includes a list of subject areas covered on each portion of the ACT to help you categorize the questions you answered incorrectly and identify subject areas you need to study or review.
Plan Your Practice and Study Time

To stay on track leading up to test day, set up a reasonable schedule to practice and study for the ACT. Set aside small amounts of time for studying over an extended period—days, weeks, or even months—so you won't feel the need to cram in the days leading up to the test.

Make your schedule flexible enough to allow for a surprise homework assignment or some unexpected fun. And find a way to reward yourself as you get the work done, even if it's just a checklist you can mark to show your progress. A flexible schedule with regular rewards will prevent burnout while keeping you motivated.

Develop a Positive Mental Attitude

Approach the ACT confident that you will do your best. Although confidence alone obviously isn't enough to ensure good performance on a test, doubt and fear can hurt your performance. Be confident in your ability to do well on the ACT. You will do well! You just need to be prepared.

Some small changes can make a surprising difference. For example, how you imagine yourself taking the exam may affect how well you actually do. Negative thoughts have a way of generating negative results. So practice positive thinking; imagine yourself meeting the challenge of the exam with ease. The day of the test, tell yourself you intend to do your best, and believe it.

Keep the Test in Perspective

Remembering that the ACT is only one part of the process of your education and training will help you keep it in perspective. So will remembering that the ACT and tests similar to it are designed to provide you with feedback and direction. Your scores can help make decisions about your future education and career choices. Think of the test as an opportunity to get to know more about yourself, not as a potential barrier to your future plans.

Another way to keep the ACT in perspective is to use the test as an opportunity to identify careers that match your interests, abilities, and values; explore suitable college majors; and start choosing high school courses that align with your future education and career goals. ACT Profile (www.actprofile.org) can help. ACT Profile is a free college and career planning website, where you can do the following:

- Find majors and careers that match your unique interests, abilities, and values
- Explore personalized major and career maps to see which education and career options might be a good fit
- Search for majors, careers, and schools
- Compare college costs
- Gather key information about occupations, including salary, outlook, and required training
• See the big picture of how your interests, skills, and values fit with your favorite occupations and majors
• Connect with counselors, teachers, parents, and others in your planning network

To get started, create your free account at www.actprofile.org. Remember, the ACT is more than just a test, and you are more than a score. The test and your score are just a few of the many tools ACT has designed to help you make smarter decisions about your future.

**General Test-Taking Strategies and Skills**

How you approach the ACT and various types of questions, how well you manage your time, whether you change answers, and other factors may affect how well you do on the ACT. The following sections present a few test-taking strategies and skills to help you perform to the best of your ability.

**Remain Calm**

When you’re under pressure during a test, an unexpected question or a minor incident such as breaking a pencil can be very upsetting. For many students, the natural tendency at such times is to panic. Panic detracts from test performance by causing students to become confused and discouraged and to have trouble recalling information they know.

It’s a good idea to have a strategy ready for dealing with incidents that might rattle your nerves. One effective strategy is to take a brief time out to center yourself. Take slow, deep breaths and let yourself relax. Put the test temporarily out of mind. Close your eyes if you want. Visualize yourself confidently resuming work on the test, turning in a completed answer sheet, and leaving the room with a feeling of having done your best work. Allow 20 to 30 seconds for your time out, which is probably all you’ll need to regain your composure.

**Pace Yourself**

The ACT, similar to many tests, must be completed within a specific and limited amount of time. Working quickly and efficiently is one of the skills necessary for conveying how much you’ve learned in the subject area being tested.

To develop an effective, efficient pace, time yourself as you take the practice tests. If time expires before you have a chance to answer all the questions, you know that you need to work faster next time. If you rushed through the test, had time remaining at the end, and made careless mistakes, you know that you will need to work at a more relaxed pace and be more careful in answering questions.

**Warning:** Don’t try to push yourself to work so fast that you make errors. Answering fifty questions carefully and correctly and leaving ten unanswered is better than answering sixty questions too quickly and missing twenty because of mistakes.

Although you won’t want to lose time by being distracted, you shouldn’t obsess about time either. Use all of the time available so you can do your very best on the test.
Some people suggest more formal methods for pacing yourself by allocating a certain amount of time per question or set of questions, as in the following examples:

- **Divide the available time by the number of questions.** For example, on the mathematics test, divide 60 minutes by 60 questions, and you know you have 1 minute per question.

- **Divide the available time into different stages of the writing process.** If you’re taking the optional writing test, you may want to allocate the time to planning, writing, and revising/editing your essay. Keep in mind that you probably won’t have enough time to fully draft, revise, and then recopy your essay, so spending a few minutes planning your essay before you start writing it is usually wise.

Keep in mind that these strategies are not foolproof, that some questions will take you longer to answer than others, and that doing the math to calculate your time allocations takes time. You may be better off developing a feel for the time and occasionally checking the clock to make sure you’re on track to finish, perhaps with a few minutes remaining at the end to check answers you were unsure of. If you want to keep track of your pace while taking the ACT, bring a watch. Not all testing centers have wall clocks.

**Know the Directions Ahead of Time**

You can save yourself precious moments on the ACT by being familiar with the directions ahead of time. Then, when taking the test, you can read the directions to refresh your memory instead of having to spend time and mind power processing those directions. For example, the ACT English, reading, and science tests ask for the “best” answer, and the mathematics test asks for the “correct” answer. This simple difference in the instructions signals an important distinction to keep in mind as you’re working through those tests. Because only one answer is “correct” in the mathematics test, you’ll want to be sure your understanding of the question and your calculations are precise—so that your answer matches one, and only one, of the possible answers. In the other tests, more than one of the possible answers may be correct to some degree, and you’ll need to be careful to select the “best” answer among those potentially “correct” ones. You’ll find the directions for each test in the practice ACT tests in this book.

The directions for the writing test are also very important, because they spell out the aspects of writing that will be evaluated. They also tell you where in the test booklet you can plan your essay and where you should write your final version. The directions for the writing test and a sample answer document appear in the practice ACT tests in this book.

Before you take the ACT, become familiar with the answer document. Knowing in advance how to use the answer document will save you time and prevent worry when you take the actual ACT.

**Read Carefully and Thoroughly**

Just as it’s important to read and understand the directions for a test, it’s also important to read and understand each question and answer choice on the test. As you’ve probably discovered somewhere along the line, you can miss even the simplest test question by reading carelessly and...
overlooking an important word or detail. Some questions on the ACT, for instance, require more
than one step, and the answer to each preliminary step may be included as an answer choice. If
you read these questions too quickly, you can easily make the mistake of choosing a plausible
answer that relates to a preliminary step but is the incorrect answer to the question.

Take the time to read each question carefully and thoroughly before choosing your answer. Make
sure you understand exactly what the question asks and what you are to do to answer it. You may
want to underline or circle key words in the test booklet (see the later section “Write Notes in
Your Test Booklet”). Reread the item if you are confused.

Watch the question’s wording. Look for words such as not or least, especially when they are not
clearly set off with underlining, capital letters, or bold type. Don’t make careless errors because
you only skimmed the question or the answer choices. Pay close attention to qualifying words
such as all, most, some, none; always, usually, seldom, sometimes, never; best, worst; highest, lowest;
smaller, larger. (There are many other qualifying words; these are only a few examples of related
groups.) When you find a qualifier in one of the responses to a question, a good way to determine
whether or not the response is the best answer is to substitute related qualifiers and see which
makes the best statement. For example, if a response says, “Tests are always difficult,” you might
test the truth of the word always by substituting sometimes and the other words related to always.
If any of the words other than the one in the answer makes the best statement, then the response
is not the best answer.

Pay close attention to modifying or limiting phrases in the statement. For instance, a question in
the reading test might have the following as a possible answer: “Lewis and Clark, the great British
explorers, began their historic trip to the West Coast by traveling up the Mississippi.” The answer
is incorrect because Lewis and Clark were not British but were US citizens. (You would not be
expected to know from memory that Lewis and Clark were US citizens; that information
would be included in the passage.)

Read all the answer choices before selecting one. Questions on the ACT often include answer
choices that seem plausible but aren’t quite correct. Even though the first answer choice may
appeal to you, the correct or best answer may be farther down the list.

When taking the writing test, read the writing prompt carefully. Before you start to plan
your essay, make sure you understand the writing prompt and the issue it asks you to
respond to.

**Choose Strategies for Answering Easier and More Difficult Questions**

A strategy for taking the ACT is to answer the easy questions first and skip the questions you
find difficult. After answering all of the easy questions, go back and answer the more difficult
questions, as time permits. When you skip a question, mark it in the test booklet (but not
on the answer sheet), so you can quickly flip back to it later. Also, make absolutely sure that
on the answer sheet, you skip the set of answer choices that correspond to the question you
skipped.
Use Logic on More Difficult Questions

When you return to more difficult questions, use logic to eliminate incorrect answer choices. Compare the remaining answer choices and note how they differ. Such differences may provide clues as to what the question requires. Eliminate as many incorrect answer choices as you can, then make an educated selection from the remaining choices. See the next section for additional guidance.

Choose a Strategy for Guessing on Multiple-Choice Questions

On some standardized tests, you’re penalized for each incorrect answer. On the ACT multiple-choice tests, however, your raw score is based on the number of questions you answer correctly—nothing is deducted for wrong answers.

Because you’re not penalized for guessing on the ACT, answering every question is advantageous. Here’s a good way to proceed:

1. If a question stumps you, try to eliminate wrong choices. Narrowing your choices increases your odds of guessing the correct answer.

2. If you still aren’t sure about the answer, take your best guess.

You don’t need a perfect reason to eliminate one answer and choose another. Sometimes an intelligent guess is based on a hunch—on something you may know but don’t have time to consciously recognize in a timed-test situation.

Maybe you’ve heard some advice about how to answer questions when you don’t know the correct answer, such as “When in doubt, choose ‘C,’” or “When in doubt, select the longest (or shortest) alternative,” or “If ‘none of the above’ (or a similar response) is among the answer choices, select it.” Although these bits of advice may hold true now and then, the questions on the ACT have been carefully written to make these strategies ineffective.

Choose a Strategy for Changing Answers

You think you marked the wrong answer choice on a certain question. Do you go with your original answer or change it to the new answer? Some people advise to always go with your first response. And surely everyone has had the experience of agonizing over a response, trying to decide whether to change it, then doing so only to find out later that the first answer was the correct one.

However, some research by education and testing specialists suggests that you should change your answer when you change your mind. If you’re like the test-takers in the study, your second answer is more likely to be the correct one.

So, how can you decide what to do? Before you change an answer, think about how you approached the question in the first place. Give some weight to the reasons why you now believe another answer is better. Don’t mechanically follow an arbitrary rule just because it works for somebody else. Know yourself; then trust yourself to make intelligent, informed decisions.
**Write Notes in Your Test Booklet**

You’re allowed to write in the test booklet, so feel free to write notes in the test booklet to flag key details or to work out a problem on paper.

**Mark Your Answers Carefully**

Only answers marked on the answer sheet during the time allowed for a particular test will count. Carefully mark your answers on the answer sheet as you work through the questions on each test.

Remember that during an actual test you may not fill in answers or alter answers on your answer sheet after “stop” is called.

For the writing test, writing (or printing) legibly in English in the correct place in the test booklet is vital. If readers cannot read what you have written, they will be unable to score your essay. You are allowed to write or print your essay, but you must do so clearly. Keep in mind, you must write your essay using a soft-lead pencil (not a mechanical pencil). You must write on the lined pages in the answer folder. If you make corrections, do so thoroughly. You may write corrections or additions neatly between the lines of your essay, but you may not write in the margins.

**Plan to Check Your Answers**

When you reach the end of one of the ACT tests with several minutes to spare, you may feel you’ve done quite enough. Resist the temptation to rest. Use the remaining time to check your work, as follows:

- For the multiple-choice tests, be sure you’ve marked all your answers in the proper places on the answer sheet.
- Be certain you’ve answered all the questions on your answer sheet, even the ones you weren’t sure about. (Of course, you must be very careful to stop marking ovals when time is called.)
- When you reach the end of the mathematics test, check your calculations. You may check your calculations using the test booklet as scratch paper or using a permitted calculator (see chapter 1).
- Check your answer sheet for stray pencil marks that may be misread by the scoring machine. Erase any such marks cleanly and completely.
- Be sure you’ve marked only one answer on your answer sheet for each question.
- If there are too many questions for you to check all of your answers, be sure to check those that you feel most uncertain about first, then any others that you have time for on that test.
• At the end of the writing test, take a few minutes to read over your essay. Correct any mistakes in spelling, grammar, usage, or punctuation. If you see any words that are difficult to read, rewrite them so they’re legible. Make any revisions neatly between the lines (but do not write in the margins).

Learn Strategies for Specific Tests

In addition to the general test-taking strategies presented in the preceding sections there are specific strategies for each of the ACT tests. For example, on the mathematics test, if a question includes an illustration, you may want to write dimensions given in the question on the illustration to help you visualize what the question is asking. In part 3 of this book, the chapters provide test-taking tips for each of the ACT tests along with additional information that reveals the types of questions you can expect to encounter on each test.

Summary

All the strategies outlined in this chapter are merely suggestions intended to give you ideas about good preparation habits and strategies for getting through the ACT in the best, most efficient manner possible. Some of the strategies will work for you, others won’t. Feel free to pick and choose from among all the strategies in this chapter, and the more specific strategies in part 3, so that you have a test-taking plan that works best for you.
Part Two: Taking and Evaluating Your First Practice Test

In This Part
In this part, you have the opportunity to take, score, and evaluate your first practice test. This exercise enables you to identify your strengths and weaknesses, so you can develop an efficient study plan that focuses on areas where you need the most improvement. In this part, you will do the following:

- Simulate testing conditions, so you become acclimated to the conditions you will experience on test day
- Take a complete practice test comprising all five ACT tests—English, mathematics, reading, science, and the optional writing test
- Score your test to gauge your overall performance
- Review explanatory answers to understand why you answered each question correctly or incorrectly
- Determine whether you need to work more on subject matter or on test-taking strategies and skills
- Analyze your performance on each test to gain better insight on the knowledge and skills in greatest need of improvement
In this chapter, you take the first of the three practice tests in this book, score the test, and review the answers with explanations. We encourage you to take the test under conditions similar to those you will encounter on test day and to try your very best.

After you take and score the test and review the answers, you will be well poised to analyze your performance in chapter 4. The results of this first practice test will help you identify subject areas you may need to review and test-taking strategies, such as pacing, that you may want to work on prior to test day.

**Simulating Testing Conditions**

Taking the practice tests can help you become familiar with the ACT. We recommend that you take the tests under conditions that are as similar as possible to those you will experience on the actual test day. The following tips will help you make the most of the practice tests:

- The four multiple-choice tests require a total of 2 hours and 55 minutes. Try an entire practice test in one sitting, with a
10-minute break between the mathematics test and the reading test. (If you are taking the writing test, you may also take a break of roughly 5 minutes after the science test.)

- Sit at a desk with good lighting. You will need sharpened no. 2 pencils with good erasers. You may not use mechanical pencils or highlight pens. Remove all books and other aids from your desk. On test day, you will not be allowed to use references or notes. If you test at a national test center, you won't need scratch paper, because each page of the mathematics test has a blank column that you can use for scratch work.

- If you plan to use a calculator on the mathematics test, review the details about permissible calculators on ACT’s website, www.act.org. Use a calculator with which you are familiar for both the practice test and on the test day. You may use any four-function, scientific, or graphing calculator on the mathematics test, except as specified on ACT’s website.

- Use a digital timer or clock to time yourself on each test. Set your timer for 5 minutes less than the allotted time for each test so you can get used to the 5-minute warning. (Students approved for extended-time should set a timer for 60-minute warnings up to the total time allowed—5 hours or 6 hours.)

- Allow yourself only the time permitted for each test.

- Detach and use one sample multiple-choice answer document.

- Read the general test directions on the first page of the practice test. These are the same directions that will appear on your test booklet on test day. After reading the directions, start your timer and begin with the English test. Continue through the science test, taking a short break between the mathematics test and the reading test. If you do not plan to take the ACT writing test, score your multiple-choice tests using the information beginning on page 101.

- If you plan to take the writing test, take a short break after the science test. Detach (or photocopy) the writing test answer document that follows the writing test planning pages. Then read the test directions on the first page of the practice ACT writing test. These are the same directions that will appear on your test booklet on test day. After reading the directions, start your timer, then carefully read the prompt. After you have considered what the prompt is asking you to do, use the pages provided to plan your essay, and then write your essay on the answer document. After you have finished, score your essay using the information beginning on page 108.
The ACT® Sample Answer Sheet

A  NAME, MAILING ADDRESS, AND TELEPHONE
(Please print.)

Last Name  First Name  MI (Middle Initial)

House Number & Street (Apt. No.); or PO Box & No.; or RR & No.

City  State/Province  ZIP/Postal Code

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Printed in U.S.A.     IM-(A)134993-001-554321
011 215 160 Rev 1 PAGE 1

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ALL examinees must complete block A – please print.

Blocks B, C, and D are required for all examinees. Find the MATCHING INFORMATION on your ticket. Enter it EXACTLY the same way, even if any of the information is missing or incorrect. Fill in the corresponding ovals. If you do not complete these blocks to match your previous information EXACTLY, your scores will be delayed up to 8 weeks.

USE A SOFT LEAD NO. 2 PENCIL ONLY.
(Do NOT use a mechanical pencil, ink, ballpoint, correction fluid, or felt-tip pen.)

B  MATCH NAME
(First 5 letters of last name)

C  MATCH NUMBER

D  DATE OF BIRTH

Do NOT mark in this shaded area.

EXAMINEE STATEMENT, CERTIFICATION, AND SIGNATURE

1. Read the following Statement: By submitting this answer sheet, I agree to comply with and be bound by the Terms and Conditions: Testing Rules and Policies for the ACT® provided in the ACT registration materials for this assessment, including those concerning test security, score cancellation, examinee remedies, arbitration, and consent to the processing of my personally identifying information, including the collection, use, transfer and disclosure of information as described in the ACT Privacy Policy (www.act.org/privacy.html).

International Examinees: By my signature I am also providing my consent to ACT to transfer my personally identifying information to the United States to ACT, or a third party service provider for processing, where it will be subject to use and disclosure under the laws of the United States. I acknowledge and agree that it may also be accessible to law enforcement and national security authorities in the United States.

I understand that ACT owns the assessment questions and responses and affirm that I will not share any assessment questions or responses with anyone by any form of communication before, during, or after the assessment administration. I understand that assuming anyone else’s identity to take this assessment is strictly prohibited and may violate the law and subject me to legal penalties.

2. Copy the Certification shown below (only the text in italics) on the lines provided. Write in your normal handwriting.

Certification: I agree to the Statement above and certify that I am the person whose name and address appear on this answer sheet.

Your Signature

Today’s Date

ACT

PO BOX 168, IOWA CITY, IOWA 52243-0168

The ONLY Official Prep Guide from the Makers of the ACT
**Marking Directions:** Mark only one oval for each question. Fill in response completely. Erase errors cleanly without smudging.  
Correct mark:          Do NOT use these incorrect or bad marks.  
Incorrect marks:  Overlapping mark:  Smudged erase:  Mark is too light:  

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ALL blocks B, C, and D must complete block A—please print.

Blocks B, C, and D are required for all examinees. Find the MATCHING INFORMATION on your ticket. Enter it EXACTLY the same way, even if any of the information is missing or incorrect. Fill in the corresponding ovals. If you do not complete these blocks to match your previous information EXACTLY, your scores will be delayed up to 8 weeks.

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   2. Copy the Certification shown below (only the text in italics) on the lines provided. Write in your normal handwriting.

   Certification: I agree to the Statement above and certify that I am the person whose name and address appear on this answer sheet.

Your Signature: ________________________

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Taking and Scoring Your First ACT Practice Test

EXAMINEE STATEMENT, CERTIFICATION, AND SIGNATURE

1. Read the following Statement: By opening this test booklet, I agree to comply with and be bound by the Terms and Conditions: Testing Rules and Policies for the ACT® provided in the ACT registration materials for this assessment, including those concerning test security, score cancellation, examinee remedies, arbitration, and consent to the processing of my personally identifying information, including the collection, use, transfer and disclosure of information as described in the ACT Privacy Policy (available at www.act.org/privacy.html).

International Examinees: By my signature I am also providing my consent to ACT to transfer my personally identifying information to the United States to ACT, or a third party service provider for processing, where it will be subject to use and disclosure under the laws of the United States. I acknowledge and agree that it may also be accessible to law enforcement and national security authorities in the United States.

I understand that ACT owns the assessment questions and responses and affirm that I will not share any assessment questions or responses with anyone by any form of communication before, during, or after the assessment administration. I understand that assuming anyone else’s identity to take this assessment is strictly prohibited and may violate the law and subject me to legal penalties.

2. Copy the Certification shown below (only the text in italics) on the lines provided. Write in your normal handwriting.

Certification: I agree to the Statement above and certify that I am the person whose name appears on this form.

3. Sign your name as you would any official document and enter today’s date.

Your Signature

Today’s Date

Directions

This booklet contains tests in English, mathematics, reading, and science. These tests measure skills and abilities highly related to high school course work and success in college. Calculators may be used on the mathematics test only.

The questions in each test are numbered, and the suggested answers for each question are lettered. On the answer document, the rows of ovals are numbered to match the questions, and the ovals in each row are lettered to correspond to the suggested answers.

For each question, first decide which answer is best. Next, locate on the answer document the row of ovals numbered the same as the question. Then, locate the oval in that row lettered the same as your answer. Finally, fill in the oval completely. Use a soft lead pencil and make your marks heavy and black. Do not use ink or a mechanical pencil.

Mark only one answer to each question. If you change your mind about an answer, erase your first mark thoroughly before marking your new answer. For each question, make certain that you mark in the row of ovals with the same number as the question.

Only responses marked on your answer document will be scored. Your score on each test will be based only on the number of questions you answer correctly during the time allowed for that test. You will not be penalized for guessing. It is to your advantage to answer every question even if you must guess.

You may work on each test only when the testing staff tells you to do so. If you finish a test before time is called for that test, you should use the time remaining to reconsider questions you are uncertain about in that test. You may not look back to a test on which time has already been called, and you may not go ahead to another test. To do so will disqualify you from the examination.

Lay your pencil down immediately when time is called at the end of each test. You may not fold or tear the pages of your test booklet.

DO NOT OPEN THIS BOOKLET UNTIL TOLD TO DO SO.
ENGLISH TEST

45 Minutes—75 Questions

DIRECTIONS: In the five passages that follow, certain words and phrases are underlined and numbered. In the right-hand column, you will find alternatives for the underlined part. In most cases, you are to choose the one that best expresses the idea, makes the statement appropriate for standard written English, or is worded most consistently with the style and tone of the passage as a whole. If you think the original version is best, choose “NO CHANGE.” In some cases, you will find in the right-hand column a question about the underlined part. You are to choose the best answer to the question.

You will also find questions about a section of the passage, or about the passage as a whole. These questions do not refer to an underlined portion of the passage, but rather are identified by a number or numbers in a box.

For each question, choose the alternative you consider best and fill in the corresponding oval on your answer document. Read each passage through once before you begin to answer the questions that accompany it. For many of the questions, you must read several sentences beyond the question to determine the answer. Be sure that you have read far enough ahead each time you choose an alternative.

PASSAGE I

What Elephants Learn

Cynthia Moss has been studying elephants, since 1972 when she started the now-famous Amboseli Elephant Research Project in Amboseli National Park in Kenya. An author, lecturer, filmmaker, and a fierce advocate for elephants—which face a daunting array of threats to their survival, from droughts to human encroachment Moss is widely considered an expert on the social behavior of these creatures.

1. A. NO CHANGE
   B. elephants, since 1972,
   C. elephants since 1972,
   D. elephants’ since 1972

2. F. NO CHANGE
   G. more-then-famous
   H. now famously
   J. famously

3. A. NO CHANGE
   B. encroachment—
   C. encroachment:
   D. encroachment,

4. At this point, the writer is considering adding the following true statement:
   Humans are among the threats to the animal’s survival.
   Should the writer make this addition here?
   F. Yes, because it presents a crucial factor in determining Moss’s interest in working with elephants.
   G. Yes, because it introduces the idea that becomes the focus of the rest of the essay.
   H. No, because the essay is focused on elephants and does not otherwise mention a human presence in their lives.
   J. No, because this information is already provided in the paragraph.

GO ON TO THE NEXT PAGE.
A key finding from her intensive field studies is the extent to which elephant survival depends on learned behavior.

As Moss has observed, however, a calf must learn how to use its trunk. At first a young elephant will drink by kneeling down at the water’s edge and it sipped directly with its mouth. The habit of pulling water into its trunk. Then releasing that water into its mouth develops only after months as if witnessing other elephants doing so.

On occasion, Moss will see a calf stick its trunk into the mouth of its mother and pull out a bit of whatever plant material she is eating. In this way, the calf learns what kinds of vegetation are safe to eat on the savanna, where poisonous plants also grow.

[1] Elephants live in family groups, each one headed by a matriarch. [2] This senior female teaches adolescent females by modeling proper care of younger elephants. [3] One of Moss’s most memorable observations in which this regard involved three elephants. [4] These were a matriarch, Echo, and two offspring: Enid, a ten-year-old female, and Ely, also named by Moss. [5] Echo showed Enid how to care for Ely by staying close to him when he was feeding and sleeping and by running to his aid when he signaled his distress. [6] Ely not only overcame his early limitations, but he also grew up to be a confident young bull.

5. A. NO CHANGE
   B. intensive field studies
   C. intensive field studies,
   D. intensive, field studies

6. F. NO CHANGE
   G. for instance,
   H. as always,
   J. by now,

7. A. NO CHANGE
   B. which it sips
   C. and sipping
   D. that sips

8. F. NO CHANGE
   G. trunk and then
   H. trunk then by
   J. trunk

9. A. NO CHANGE
   B. when witnessing
   C. of witnessing
   D. then witness

10. F. NO CHANGE
     G. in this regard
     H. ones that
     J. which

11. A. NO CHANGE
     B. a baby male.
     C. an elephant.
     D. the third.

12. F. NO CHANGE
     G. he also will have grown
     H. he also had grown
     J. also growing

GO ON TO THE NEXT PAGE.
[7] Ely was born with deformed feet that initially prevented him from walking.

Moss has brought compelling stories and information about elephants is provided to an ever-expanding audience. She hopes others will in turn become advocates for the animals she admires and understands in ways few others do.

13. For the sake of logic and cohesion, the best placement for Sentence 7 would be:
A. where it is now.
B. before Sentence 1.
C. after Sentence 3.
D. after Sentence 4.

14. F. NO CHANGE
G. is given by her to
H. is reaching
J. to

Question 15 asks about the preceding passage as a whole.

15. Suppose the writer’s goal had been to write a brief essay focusing on some aspect of animal behavior in the wild. Would this essay accomplish that goal?
A. Yes, because the essay focuses on Moss’s research on how elephants on the savanna learn to identify their various family members.
B. Yes, because the essay focuses on elephants on the savanna and some of the behaviors they display, as studied by Moss.
C. No, because the essay focuses instead on how elephants have evolved in Kenya as compared to how they have evolved in other parts of Africa.
D. No, because the essay focuses on elephants that Moss studies in zoos around the world.

PASSAGE II

The following paragraphs may or may not be in the most logical order. Each paragraph is numbered in brackets, and question 29 will ask you to choose where Paragraph 2 should most logically be placed.

Ghost Signs

[1]

Seeing remnants of outdoor advertisements from a bygone era, they are called “ghost signs.” I search for them on city streets, in town squares, and along country roads. Some are weather-beaten billboards; others are faded murals painted years ago on the sides of old buildings. Whatever words remain Fruiterer . . . Apothecary . . . Gramophones . . . Pan-Handle Coffee—are often barely

16. F. NO CHANGE
G. The sight of remnants
H. To see remnants
I. Remnants

17. A. NO CHANGE
B. era that is no more,
C. era of another time,
D. era of times past,

18. F. NO CHANGE
G. remain—
H. remain,
J. remain:

GO ON TO THE NEXT PAGE.
legible, pale fragments of yesterday’s consumer culture should strike me as silly or sad. After all, there they are: advertising products and businesses that no longer exist.

Yet, they themselves survive without apology, with instead, their simple claims and complex colors. The contrast draws me in every time.

I collect ghost signs. Not the signs themselves, but photos of them. Driving home from school one chilly October evening, my collection got its start. I had made the same drive countless times before, but I had never noticed the sign.

Then there it was, an ad for “Joe’s Café,” perched atop a metal pole, which was upright under a cape of kudzu vines. Maybe it was the way the setting sun’s illumination of the yellowing plastic.

Maybe it was the small hole, a clue to vandalism or of a hailstorm. Instead, something about the sign touched me. I pulled over. In the twilight, I got out of the car, snapped a picture with my phone, and sent it to some friends. I vowed to return with my camera to better capture the forlorn, luminous beauty of my discovery. Since that dusky evening, I have been happily haunted by ghost signs.

19. A. NO CHANGE
   B. they should
   C. should they

20. F. NO CHANGE
   G. products and businesses,
   H. products, and businesses
   J. products: businesses

21. A. NO CHANGE
   B. apology, with, instead,
   C. apology with instead,
   D. apology with instead

22. F. NO CHANGE
   G. Driving home from school one chilly October evening was the beginning of my collection.
   H. I started my collection one chilly October evening, driving home from school.
   J. The start of my collection came to me driving home from school one chilly October evening.

23. Given that all the choices are accurate, which one echoes a central point the writer makes about ghost signs?
   A. NO CHANGE
   B. was not what interested me,
   C. might have been wood,
   D. was disappearing

24. F. NO CHANGE
   G. illuminating setting sun on
   H. sun illuminated the set on
   J. setting sun illuminated

25. A. NO CHANGE
   B. evidence of
   C. evidently
   D. DELETE the underlined portion.

26. F. NO CHANGE
   G. On the other hand, something
   H. Meanwhile, something
   J. Something
Once in a while, I take a friend with me on my searches. People who know of my fascination will point me to where they think they have seen a ghost sign. Favorite finds include an ad for sliced bread, one for a “modern” motel, and yet another for fountain pen repair services. As fun as it is to have company, my best hunts have been solitude trips. I appreciate the beauty of ghost signs more when I like the signs, am alone.

29. For the sake of logic and cohesion, Paragraph 2 should be placed:
A. where it is now.
B. before Paragraph 1.
C. after Paragraph 3.
D. after Paragraph 4.

PASSAGE III
Blue Holes of the Bahamas

The Bahamas, a series of semitropical islands off the southeast coast of the United States, which are home to some of the most unusual geological formations in the world: underwater caves known as blue holes. [A] These

31. A. NO CHANGE
B. States, are
C. States are
D. States,
vertical caves were formed over thousands of years, and their cold depths provide abundant clues to the islands’ past.

During the formation process, tiny grains of calcium carbonate separated from the seawater. These grains built up, then compacted, forming the limestone that makes up the islands. Over time, rainwater permeated the porous limestone but was trapped just above sea level, buoyed by the denser seawater below. Jostled back and forth by tides, the layer of slightly acidic, brackish water eroded limestone faster than either rainwater—or seawater—could alone. As the limestone eroded caves formed.

Over time periods in which the weather changed drastically, sea levels rose and fell by hundreds of feet. This allowed the cave-creating process to be a process that repeated at different depths hundreds of feet apart. The roofs of many caves collapsed, leaving the chambers beneath exposed.

32. Given that all the following statements are true, which one, if added here, would most effectively introduce the topic of this paragraph?
   F. The Bahamas were formed from calcium carbonate, a component of seawater.
   G. Calcium carbonate, a common rock substance, is also found in seawater.
   H. Much of the land making up the Bahamas is still underwater.
   J. Most types of limestone contain calcium carbonate.

33. A. NO CHANGE
   B. are building
   C. will build
   D. build

34. F. NO CHANGE
   G. being buoyed because of
   H. it being buoyed by
   J. buoying it was

35. A. NO CHANGE
   B. rainwater, or seawater,
   C. rainwater, or seawater
   D. rainwater or seawater

36. F. NO CHANGE
   G. limestone, eroded caves
   H. limestone eroded, caves
   J. limestone eroded caves,

37. Which choice most specifically illustrates how long the cave-creating process took?
   A. NO CHANGE
   B. Between ice ages and the more temperate eras that followed them.
   C. During this extended time,
   D. As time passed,

38. F. NO CHANGE
   G. repeat again and again at various different depths.
   H. repeat at different depths that varied.
   J. repeat at different depths.
Some of these blue holes open to small contained caves, others open to miles-long interconnected tunnels.

The telltale sign of a blue hole is a circular patch of water striking darker than the water surrounding them. (The darker water indicates greater depth.)

Divers have found the remains of turtles and alligators. Now extinct on the islands, stalactites and stalagmites from a time when the caves were above sea level, and artifacts of early human inhabitants.

Hundreds of blue holes can be sighted off the Bahamas. So far, most remain unexplored by divers, owing in part to the danger of cave diving. Often the only clue to the mysteries below is the tantalizing sight of dark blue water leading deep into the sea.

39. A. NO CHANGE
   B. caves that
   C. caves;
   D. caves,

40. At this point, the writer is considering adding the following true sentence:
   At 663 feet deep, Dean’s Blue Hole in Long Island, Bahamas, is a popular cave-diving destination.

   Should the writer make this addition here?
   F. Yes, because it supports the preceding sentence by providing an example of a blue hole that is very deep.
   G. Yes, because it allows the reader to visualize a specific blue hole in the Bahamas.
   H. No, because it offers a detail that is unrelated to the paragraph’s focus on the cave-creating process.
   J. No, because it does not provide an adequate description of Dean’s Blue Hole.

41. A. NO CHANGE
   B. strikingly darker
   C. strikingly darkly
   D. striking darkly

42. F. NO CHANGE
   G. these.
   H. one.
   J. it.

43. A. NO CHANGE
   B. alligators now. Extinct on
   C. alligators now extinct on
   D. alligators now extinct. On

44. Which choice most effectively suggests the shape of blue holes as described earlier in the essay?
   F. NO CHANGE
   G. dot the waters of
   H. darken parts of
   J. appear in

45. The writer wants to add the following sentence to the essay:
   In these depths, fossils and ancient rock formations are incredibly well preserved.

   This sentence would most logically be placed at:
   A. Point A in Paragraph 1.
   B. Point B in Paragraph 2.
   C. Point C in Paragraph 4.
   D. Point D in Paragraph 5.

Question 45 asks about the preceding passage as a whole.
PASSAGE IV

The Walls of Rome

Rome, founded on the banks of the Tiber River, boasts two ancient walls that, when they were built, surrounded the city. [A] Although both were built as walls intended to defend the city protectively and stood ten meters tall they were erected under different historical circumstances.

It’s thought that the Servian Wall was constructed in the early fourth century BCE and named after Servius Tullius, who was the sixth king of Rome. The eleven-kilometer wall encircled Rome’s seven hills and stood entirely on the east side of the Tiber River. [B]

The Aurelian Wall, built in the late third century CE by the Roman Emperor Aurelian, was more sturdier than the older wall. It was nineteen kilometers long greatly expanded and surrounded the city of Rome as well as a small section of the Tiber’s west bank. Erected almost 600 years after the Servian Wall, the Aurelian Wall protected Rome while the army was away, defending the empire’s far-flung frontiers from enemy attacks. [C] The massive wall deterred many enemies who might have been tempted to attack Rome during those intervals the city was sparsely defended.

46. F. NO CHANGE
   G. defensive walls for defending the city
   H. walls to provide defensive protection
   J. defensive walls

47. A. NO CHANGE
   B. tall. They
   C. tall, they
   D. tall; they

48. F. NO CHANGE
   G. Among historians, its
   H. Its’
   J. Its

49. A. NO CHANGE
   B. Wall had been
   C. Wall, which,
   D. Wall, was

50. F. NO CHANGE
   G. much sturdier than
   H. more sturdier then
   J. much sturdier then

51. Which of the following placements for the underlined portion makes it most clear that it was Rome that had expanded?
   A. Where it is now
   B. After the words surrounded the
   C. After the word Rome
   D. After the words of the

GO ON TO THE NEXT PAGE.
The Aurelian Wall featured eighteen large gateways permitting both foot and chariot traffic in and out of the city. In other words, a series of 381 towers and eleven smaller side gates called posterns were evenly spaced along the rest of the wall. Both the posterns and the towers served as defensive positions for protecting Rome. Walkable passages lined the inner side of the wall.

The Romans used bricks to build the Aurelian Wall. However, only small portions of the Servian Wall remains, some of which can be seen inside a chain restaurant located beneath Rome’s central train station. It could, perhaps, be considered ironic that remnants

52. F. NO CHANGE
G. Therefore, a
H. Instead, a
J. A

53. A. NO CHANGE
B. Both, the posterns and the towers,
C. Both the posterns, and the towers
D. Both the posterns and the towers,

54. Which choice provides the most specific information about how posterns and towers served as defensive positions?
F. NO CHANGE
G. by providing cover for armed guards during an enemy attack.
H. in that they were designed to help Rome repel enemy attacks.
J. by keeping Rome safe from invaders.

55. Given that all the statements are true, which one provides the most effective transition to Paragraph 5?
A. NO CHANGE
B. Today, the Aurelian Wall continues to dominate the Roman landscape.
C. Emperor Aurelian did not survive long enough to see the completion of the Aurelian Wall.
D. Before the Servian and Aurelian Walls were built, ancient Rome was most likely protected by mounds of earth.

56. F. NO CHANGE
G. were remaining,
H. has remained,
J. remain,

57. At this point, the writer is considering adding the following true statement:
To hasten the construction of the Aurelian Wall, existing architectural features, such as aqueducts, were incorporated into the structure. Should the statement be added here?
A. Yes, because it adds information about the Aurelian Wall that supports the main idea of the paragraph.
B. Yes, because it demonstrates how innovative and practical the Roman engineers were.
C. No, because it provides a detail that interrupts the paragraph’s discussion of the Servian Wall in the present day.
D. No, because it provides a level of detail about the wall that is inconsistent with the level of detail in the rest of the essay.

GO ON TO THE NEXT PAGE.
of a wall that once protected the future capital of one
of the ancient world’s most famous empires are now
preserved and recognized as historically significant
by archaeologists.

58. Which choice best completes the irony that is set up in
the first part of the sentence?
A. NO CHANGE
B. as important relics of Rome’s earliest boundaries.
C. within a fast-food restaurant.
D. in such varied locations.

59. Which choice best completes the irony that is set up in
the first part of the sentence?
A. NO CHANGE
B. as important relics of Rome’s earliest boundaries.
C. within a fast-food restaurant.
D. in such varied locations.

59. Question 60 asks about the preceding passage
as a whole.

60. The writer is considering adding the following state-
ment to the essay:
The two walls can be thought of as concentric
circles emanating from the ancient Roman
Forum.

If the writer were to add this statement, it would most
logically be placed at:
F. Point A in Paragraph 1.
G. Point B in Paragraph 2.
H. Point C in Paragraph 3.
J. Point D in Paragraph 4.

61. A. NO CHANGE
B. Revolution, prisoner of war James Forten,
C. Revolution, prisoner of war James Forten
D. Revolution prisoner of war, James Forten

62. Which of the following sentences, if added here, would
provide the most logical transition from the preceding
paragraph to this paragraph?
F. Forten was one of many to serve in the American
Revolution.
G. Forten’s rejection was risky.
H. Such an offer must have been unusual.
J. Many would later admire Forten’s skills as an
innovator.

63. A. NO CHANGE
B. chances to surviving
C. chances of surviving
D. chance to survive
Forten also knew that if released at the war’s end or as part of an exchange, he, a free black man, might be captured and sold into slavery as he journeyed home to Philadelphia. Forten not only survived but became one of the most successful businessmen and ardent abolitionists in the United States. 

[3]

Forten’s rise to prosperity began upon his return home when a sailmaker hired him to design, mend, and sew sails. Forten’s knowledge of ships, gained from his experiences as a sailor during the war, paid off. He rose to the position of foreman, and in 1798, Forten bought the sailmaker’s business. [B]

[4]

Employing thirty-eight workers, white and black, Forten held his employees to a high standard. Viewed as a professional academy, his business produced skilled apprentices who constructed sails for dozens of vessels. The bulk of Forten’s business records was probably lost after the business was sold. 

Soon, many regarded Forten as the city’s premier sailmaker in Philadelphia. 

64. F. NO CHANGE
G. exchange; he as
H. exchange—he
J. exchange. He

65. If the writer were to delete the preceding sentence, the paragraph would primarily lose:
A. a description of the tactics Forten used to survive imprisonment and become a successful businessman and abolitionist.
B. a transition from a discussion of the ramifications of Forten’s decision to a discussion of his success as a sailmaker and abolitionist.
C. a comparison between Forten’s work as a businessman and his role as an abolitionist.
D. an analysis of how Forten transitioned from a prisoner to a businessman and abolitionist.

66. F. NO CHANGE
G. had arose
H. had rose
J. raised

67. A. NO CHANGE
B. workers, whom were
C. workers:
D. workers

68. The writer is considering deleting the preceding sentence. Should the sentence be kept or deleted?
F. Kept, because it establishes a correlation between Forten’s business records and the early success of Forten’s business.
G. Kept, because it provides evidence to support the claim that Forten employed thirty-eight workers.
H. Deleted, because it blurs the paragraph’s focus on the success of Forten’s business.
J. Deleted, because it contradicts the idea that Forten had high expectations for his business.

69. A. NO CHANGE
B. foremost leading sailmaker in his native Philadelphia.
C. premier sailmaker in the city of Philadelphia.
D. premier sailmaker.
A savvy businessman, Forten supported abolitionist causes. When the War of 1812 closed the port of Philadelphia, Forten used his profits in real estate and lending to support his sailmaking enterprise. When the need for smaller, quicker vessels changed sail design, he adapted. One thing Forten refused to do, however, was fit a slave ship with sails.

In fact, historians estimate that the sailmaker invested over greater than half his fortune in work to abolish slavery. [C] One of the wealthiest men in Philadelphia, Forten helped finance the Liberator, a powerful abolitionist newspaper. [D] The Revolutionary War veteran, who served in this war, believed that the United States owed all residents the right to freedom.
1. Which of the following expressions is equivalent to 
\( a(4 - a) - 5(a + 7) \) ?
A. \(-2a - 35\)
B. \(-2a + 7\)
C. \(-a^2 - a - 35\)
D. \(-a^2 - a + 7\)
E. \(-2a^3 - 35\)

2. Which of the following inequalities orders the numbers
0.2, 0.03, and \( \frac{1}{4} \) from least to greatest?
F. \(0.2 < 0.03 < \frac{1}{4}\)
G. \(0.03 < 0.2 < \frac{1}{4}\)
H. \(0.03 < \frac{1}{4} < 0.2\)
J. \(\frac{1}{4} < 0.03 < 0.2\)
K. \(\frac{1}{4} < 0.2 < 0.03\)

3. If \(x^2 + 4 = 29\), then \(x^2 - 4 = ?\)
A. \(5\)
B. \(\sqrt{21}\)
C. \(21\)
D. \(25\)
E. \(33\)
4. The vertices of a rectangle are \((-1,-2), (4,-2), (4,3),\) and \((-1,3).\) When the rectangle is graphed in the standard \((x,y)\) coordinate plane below, what percent of the total area of the rectangle lies in Quadrant III?

\[
\begin{array}{c|c|c|c}
\hline
& I & II & III \\
\hline
I & & & \\
\hline
II & & & \\
\hline
III & & & \\
\hline
IV & & & \\
\hline
\end{array}
\]

F. 8%  
G. 12%  
H. 12.5%  
J. 32%  
K. 48%

5. In 1985, the cost of clothing for a certain family was $620. In 1995, 10 years later, the cost of clothing for this family was $1,000. Assuming the cost increased linearly, what was the cost of this family’s clothing in 1991?

A. $908  
B. $848  
C. $812  
D. $810  
E. $772

6. The square root of a certain number is approximately 9.2371. The certain number is between what 2 integers?

F. 3 and 4  
G. 4 and 5  
H. 9 and 10  
J. 18 and 19  
K. 81 and 99

7. A bag contains 10 pieces of flavored candy: 4 lemon, 3 strawberry, 2 grape, and 1 cherry. One piece of candy will be randomly picked from the bag. What is the probability the candy picked is NOT grape flavored?

A. \(\frac{1}{5}\)  
B. \(\frac{1}{4}\)  
C. \(\frac{1}{2}\)  
D. \(\frac{3}{4}\)  
E. \(\frac{4}{5}\)

GO ON TO THE NEXT PAGE.
8. When points $A$ and $B(-3,4)$ are graphed in the standard $(x,y)$ coordinate plane below, the midpoint of $AB$ will be $(1,2)$. What will be the coordinates of point $A$?

F. $(-7,6)$  
G. $(-2,1)$  
H. $(-1,3)$  
J. $(-1,8)$  
K. $(5,0)$

9. Andrea manages a company that currently has 116 customers, which is 8 more than twice the number of customers the company had 1 year ago. How many customers did the company have 1 year ago?

A. 50  
B. 54  
C. 62  
D. 66  
E. 100

10. Joseph will have a 200-foot-long fence installed around his yard. The A+ Fence Company charges a $500.00 fee, plus a set amount per foot of fence. The A+ Fence Company has given Joseph an estimate of $2,200.00 to install the fence around his yard. What is the set amount per foot of fence?

F. $4.00  
G. $4.80  
H. $8.50  
J. $11.00  
K. $13.50

11. For a math homework assignment, Karla found the area and perimeter of a room of her house. She reported that the area of her rectangular living room is 180 square feet and that the perimeter is 54 feet. When drawing a sketch of her living room the next day, she realized that she had forgotten to write down the dimensions of the room. What are the dimensions of Karla’s living room, in feet?

A. 9 by 20  
B. 10 by 18  
C. 12 by 15  
D. 14 by 13  
E. 16 by 11
Carrie’s Chocolate Shop and Tamika’s Treat Shop both sell candy in boxes. The table below lists the price (the total amount the customer pays) of each box of candy sold at the shops. For each shop, there is a linear relationship between the price of a box of candies and the number of candies in that box. These are the only numbers of candies that can be purchased at the shops.

<table>
<thead>
<tr>
<th>Candies per box ((n))</th>
<th>Price at Carrie’s Chocolate Shop ((c))</th>
<th>Price at Tamika’s Treat Shop ((t))</th>
</tr>
</thead>
<tbody>
<tr>
<td>5</td>
<td>$1.50</td>
<td>$2.25</td>
</tr>
<tr>
<td>10</td>
<td>$2.50</td>
<td>$2.75</td>
</tr>
<tr>
<td>15</td>
<td>$3.50</td>
<td>$3.25</td>
</tr>
<tr>
<td>20</td>
<td>$4.50</td>
<td>$3.75</td>
</tr>
<tr>
<td>25</td>
<td>$5.50</td>
<td>$4.25</td>
</tr>
<tr>
<td>30</td>
<td>$6.50</td>
<td>$4.75</td>
</tr>
</tbody>
</table>

12. Jeremy has $10.00 in quarters to spend on candy. What is the maximum number of quarters he would have left after paying for a box of 25 candies at Tamika’s Treat Shop?
   (Note: Each quarter is worth $0.25.)
   F. 10  
   G. 17  
   H. 22  
   J. 23  
   K. 30

13. At Tamika’s Treat Shop, what is the average price per candy in a box of 20, to the nearest $0.01?
   A. $0.08  
   B. $0.19  
   C. $0.23  
   D. $0.30  
   E. $0.45

14. Which of the following equations gives the relationship between the price in dollars, \(c\), and the number of candies, \(n\), in a box of candies at Carrie’s Chocolate Shop?
   F. \(c = 0.2n + 0.5\)  
   G. \(c = 0.3n\)  
   H. \(c = 0.5n + 1.5\)  
   J. \(c = n - 3.5\)  
   K. \(c = 1.4n - 5.5\)
15. Which of the following is a solution to the equation $x^2 - 36x = 0$?
A. 72  
B. 36  
C. 18  
D. 6  
E. −6

16. In the figure below, vertices $D$ and $F$ of $\triangle DEF$ lie on $CG$, the measure of $\angle CDE$ is $148^\circ$, and the measure of $\angle EFG$ is $140^\circ$. What is the measure of $\angle DEF$?

![Triangle Diagram]

F. 72°  
G. 98°  
H. 100°  
J. 108°  
K. 116°

17. A company ships notepads in rectangular boxes that each have inside dimensions measuring 9 inches long, 9 inches wide, and 12 inches tall. Each notepad is in the shape of a cube with an edge length of 3 inches. What is the maximum number of notepads that will fit in 1 closed box?
A. 10  
B. 11  
C. 12  
D. 22  
E. 36

18. The function $f$ is defined as $f(x) = -4x^3 - 4x^2$. What is $f(-4)$?
F. −320  
G. −192  
H. 16  
J. 192  
K. 320

19. Which of the following $(x, y)$ pairs is the solution for the system of equations $x + 2y = 4$ and $-2x + y = 7$?
A. $(-2, 3)$  
B. $(-1, 2.5)$  
C. $(1, 1.5)$  
D. $(2, 1)$  
E. $(4, 0)$

20. Which of the following is a value of $x$ that satisfies $\log_3 36 = 2$?
F. 4  
G. 6  
H. 8  
J. 16  
K. 18
21. A 5-inch-by-7-inch photograph was cut to fit exactly into a 4-inch-by-6-inch frame. What is the area, in square inches, of the part of the photograph that was cut off?
   A. 2
   B. 10
   C. 11
   D. 12
   E. 24

22. A line contains the points A, B, C, and D. Point B is between points A and C. Point D is between points C and B. Which of the following inequalities must be true about the lengths of these segments?
   F. BC < AB
   G. BD < AB
   H. BD < CD
   J. CD < AB
   K. CD < BC

23. If x and y are positive integers such that the greatest common factor of $x^2y$ and $xy^3$ is 45, then which of the following could y equal?
   A. 45
   B. 15
   C. 9
   D. 5
   E. 3

24. To test a new medicine, each of 300 volunteers was assigned a distinct number from 1 to 300. Next, a calculator was used to simulate drawing 150 balls from among 300 congruent balls. The balls were numbered the same way as the volunteers so that 150 volunteers to receive the new medication would be chosen without bias. The other volunteers received a placebo. Weeks later, the 2 groups were compared. Which of the following phrases best describes the company’s testing?
   F. Randomized census
   G. Randomized experiment
   H. Nonrandomized experiment
   J. Randomized sample survey
   K. Nonrandomized sample survey

25. One caution sign flashes every 4 seconds, and another caution sign flashes every 10 seconds. At a certain instant, the 2 signs flash at the same time. How many seconds elapse until the 2 signs next flash at the same time?
   A. 6
   B. 7
   C. 14
   D. 20
   E. 40

GO ON TO THE NEXT PAGE.
26. For all nonzero values of $a$ and $b$, the value of which of the following expressions is always negative?

F. $a - b$
G. $-a - b$
H. $|a| + |b|$
J. $|a| - |b|$
K. $-|a| - |b|$

27. Graphed in the same standard $(x,y)$ coordinate plane are a circle and a parabola. The circle has radius 3 and center $(0,0)$. The parabola has vertex $(-3,-2)$, has a vertical axis of symmetry, and passes through $(-2,-1)$. The circle and the parabola intersect at how many points?

A. 0
B. 1
C. 2
D. 3
E. 4

28. 40% of 250 is equal to 60% of what number?

F. 150
G. 160
H. $166\frac{2}{3}$
J. 270
K. 375

29. Which of the following inequalities is equivalent to $-2x - 6y > 2y - 4$?

A. $x < -4y + 2$
B. $x > -4y + 2$
C. $x < 2y + 2$
D. $x < 4y + 2$
E. $x > 4y + 2$
30. For an angle with measure $\alpha$ in a right triangle, $\sin \alpha = \frac{40}{41}$ and $\tan \alpha = \frac{40}{9}$. What is the value of $\cos \alpha$?

F. $\frac{9}{41}$
G. $\frac{41}{9}$
H. $\frac{9}{40}$
J. $\frac{9}{\sqrt{1.519}}$
K. $\frac{9}{\sqrt{3.281}}$

31. The perimeter of rectangle $ABCD$ is 96 cm. The ratio of the side lengths $AB:BC$ is 3:5. What is the length, in centimeters, of $AB$?

A. 6
B. 18
C. 30
D. 36
E. 60

32. For $\triangle ABC$ shown below, base $AC$ has a length of 16 inches and altitude $BD$ has a length of 8 inches. The area of a certain square is equal to the area of $\triangle ABC$. What is the length, in inches, of a side of the square?

F. 6
G. 8
H. 12
J. 16
K. 32
In the figure shown below, \(ABCD\) is a rectangle, \(EFGH\) is a square, and \(CD\) is the diameter of a semicircle. Point \(K\) is the midpoint of \(CD\). Point \(J\) is the midpoint of both \(AB\) and \(EF\). Points \(E\) and \(F\) lie on \(AB\). The 3 given lengths are in meters.

33. The length of \(EH\) is what percent of the length of \(AD\)?
   A. 15.6%
   B. 30%
   C. 36%
   D. 43.2%
   E. 50%

34. What is the length, in meters, of \(JD\)?
   F. 13
   G. 15.6
   H. 17
   J. \(\sqrt{44}\)
   K. \(\sqrt{244}\)

35. What is the length, in meters, of arc \(CD\)?
   A. \(2.5\pi\)
   B. \(5\pi\)
   C. \(6.25\pi\)
   D. \(10\pi\)
   E. \(25\pi\)

36. The figure will be placed in the standard \((x,y)\) coordinate plane so that \(K\) is at the origin, \(AB\) is parallel to the \(x\)-axis, and 1 meter equals 1 coordinate unit. Which of the following values could be the \(y\)-coordinate of \(H\)?
   F. 1.8
   G. 3.6
   H. 8.4
   J. 10
   K. 12
37. What is the length, in coordinate units, of the altitude from C to AB in \( \triangle ABC \) shown in the standard \((x,y)\) coordinate plane below?

A. 3
B. 5
C. 6
D. \(\sqrt{10}\)
E. \(\sqrt{13}\)

38. At a local post office, on average, 3 customers are in line when the post office closes each day. The probability, \( P \), that exactly \( n \) customers are in line when the post office closes can be modeled by the equation \( P = \frac{3^n e^{-\frac{3}{2}}}{n!} \). Given that \( e^{-\frac{3}{2}} \approx 0.05 \), which of the following values is closest to the probability that exactly 2 customers are in line when the post office closes?

F. 0.08
G. 0.11
H. 0.15
J. 0.23
K. 0.45

39. What is the amplitude of the function \( f(x) = \frac{1}{2} \cos(3x + \pi) \)?

A. \(\frac{1}{3}\)
B. \(\frac{1}{2}\)
C. \(\frac{3}{2}\)
D. 2
E. 3

40. License plates on cars in a certain state consist of 3 letters taken from the 26 letters, A through Z, followed by 3 digits taken from the 10 digits, 0 through 9. Which of the following expressions gives the number of distinct license plates that are possible given that repetition of both letters and digits is allowed?

F. \(10^3 \cdot 26^3\)
G. \((10 + 26)^3\)
H. \(2(26!)^3(10!)^3\)
J. \((3 + 3)^{26} + 10\)
K. \((26! \cdot 10!)^3 + (26! \cdot 10!)^3\)
41. For 20 quiz scores in a typing class, the table below gives the frequency of the scores in each score interval. Which score interval contains the median of the scores?

<table>
<thead>
<tr>
<th>Score interval</th>
<th>Frequency</th>
</tr>
</thead>
<tbody>
<tr>
<td>96–100</td>
<td>3</td>
</tr>
<tr>
<td>91–95</td>
<td>1</td>
</tr>
<tr>
<td>86–90</td>
<td>3</td>
</tr>
<tr>
<td>81–85</td>
<td>4</td>
</tr>
<tr>
<td>76–80</td>
<td>9</td>
</tr>
</tbody>
</table>

A. 96–100  
B. 91–95  
C. 86–90  
D. 81–85  
E. 76–80

42. In the complex numbers, where \( i^2 = -1 \),

\[
\frac{1}{1+i}, \quad \frac{1-i}{1-i} = ?
\]

F. \( i - 1 \)  
G. \( 1 + i \)  
H. \( 1 - i \)  
J. \( \frac{1-i}{2} \)  
K. \( \frac{1+i}{2} \)

43. Temperatures measured in degrees Fahrenheit (\( F \)) are related to temperatures measured in degrees Celsius (\( C \)) by the formula \( F = \frac{9}{5}C + 32 \). There is 1 value of \( x \) for which \( x \) degrees Fahrenheit equals \( x \) degrees Celsius. What is that value?

A. \( -72 \)  
B. \( -40 \)  
C. \( -32 \)  
D. \( 0 \)  
E. \( 32 \)
44. The table below gives experimental data values for variables \( x \) and \( y \). Theory predicts that \( y \) varies directly with \( x \). Based on the experimental data, which of the following values is closest to the constant of variation? (Note: The variable \( y \) varies directly with the variable \( x \) provided that \( y = kx \) for some nonzero constant \( k \), called the constant of variation.)

<table>
<thead>
<tr>
<th>( x )</th>
<th>( y )</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.75</td>
<td>0.140</td>
</tr>
<tr>
<td>8.50</td>
<td>0.425</td>
</tr>
<tr>
<td>14.75</td>
<td>0.750</td>
</tr>
<tr>
<td>16.75</td>
<td>0.850</td>
</tr>
<tr>
<td>21.00</td>
<td>1.050</td>
</tr>
</tbody>
</table>

F. \(-2.61\)
G. 0.05
H. 3.61
J. 15.90
K. 20.00

45. During a snowstorm, the relationship between the depth of accumulated snow, \( y \) inches, and the elapsed time, \( x \) hours, was modeled by the equation \( 2x - 5y = -5 \). One of the following graphs in the standard \((x, y)\) coordinate plane models the equation for positive values of \( x \) and \( y \). Which one?

A. \[
\begin{array}{c|c}
\hline
x & y \\
\hline
1 & 3 \\
2 & 4 \\
3 & 5 \\
4 & 6 \\
5 & 7 \\
\hline
\end{array}
\]

B. \[
\begin{array}{c|c}
\hline
x & y \\
\hline
1 & 2 \\
2 & 4 \\
3 & 6 \\
4 & 8 \\
5 & 10 \\
\hline
\end{array}
\]

C. \[
\begin{array}{c|c}
\hline
x & y \\
\hline
1 & 3 \\
2 & 6 \\
3 & 9 \\
4 & 12 \\
5 & 15 \\
\hline
\end{array}
\]

D. \[
\begin{array}{c|c}
\hline
x & y \\
\hline
1 & 4 \\
2 & 6 \\
3 & 8 \\
4 & 10 \\
5 & 12 \\
\hline
\end{array}
\]

E. \[
\begin{array}{c|c}
\hline
x & y \\
\hline
1 & 5 \\
2 & 10 \\
3 & 15 \\
4 & 20 \\
5 & 25 \\
\hline
\end{array}
\]
46. Diana is baking bread, and the original recipe calls for 1 \( \frac{1}{2} \) teaspoons of yeast and 2 \( \frac{1}{2} \) cups of flour. Diana will use the entire contents of a packet that contains 2 \( \frac{1}{4} \) teaspoons of yeast and will use the same ratio of ingredients called for in the original recipe. How many cups of flour will Diana use?

F. 1 \( \frac{7}{8} \)
G. 3 \( \frac{1}{4} \)
H. 3 \( \frac{3}{4} \)
J. 3 \( \frac{3}{4} \)
K. 4

47. For all nonzero values of \( x \), \( \frac{12x^6 - 9x^2}{3x^2} = ? \)

A. \( 4x^3 - 3x \)
B. \( 4x^3 - 3 \)
C. \( 4x^4 - 9x^2 \)
D. \( 4x^4 - 3x \)
E. \( 4x^4 - 3 \)

48. Four matrices are given below.

\[
W = \begin{bmatrix} 1 & 2 \\ 5 & 8 \end{bmatrix}, \quad X = \begin{bmatrix} 3 & 9 \\ 7 & 4 \end{bmatrix}, \quad Y = \begin{bmatrix} 1 & 3 & 7 \\ 4 & 2 & 6 \end{bmatrix}, \quad Z = \begin{bmatrix} 5 & 8 \\ 2 & 9 \\ 3 & 7 \end{bmatrix}
\]

Which of the following matrix products is undefined?

F. \( WX \)
G. \( WY \)
H. \( YZ \)
J. \( WX \)
K. \( XZ \)
49. The 3 parabolas graphed in the standard \((x, y)\) coordinate plane below are from a family of parabolas. A general equation that defines this family of parabolas contains the variable \(n\) in addition to \(x\) and \(y\). For one of the parabolas shown, \(n = 1\); for another, \(n = 2\); and for the third, \(n = 3\). Which of the following could be a general equation that defines this family of parabolas for all \(n \geq 1\)?

A. \(y = nx^2 + 1\)
B. \(y = \frac{1}{n}x^2 + 1\)
C. \(y = x^2 + n\)
D. \(y = -nx^2 + 1\)
E. \(y = -\frac{1}{n}x^2 + 1\)

50. After polling a class of 20 music students by a show of hands, you find that 8 students play the guitar and 9 students play the piano. Given that information, what is the minimum number of students in this music class who play both the guitar and the piano?

F. \(0\)
G. \(1\)
H. \(8\)
J. \(9\)
K. \(17\)

51. A teacher assigns each of her 18 students a different integer from 1 through 18. The teacher forms pairs of study partners by using the rule that the sum of the pair of numbers is a perfect square. Assuming the 9 pairs of students follow this rule, the student assigned which number must be paired with the student assigned the number 1?

A. 16
B. 15
C. 9
D. 8
E. 3

GO ON TO THE NEXT PAGE.
52. Lucky found $8.25 in pennies, nickels, dimes, and quarters while walking home from school one week. When she deposited this money in the bank, she noticed that she had twice as many nickels as pennies, 1 fewer dime than nickels, and 1 more quarter than nickels. How many quarters did Lucky find that week?

F. 3  
G. 9  
H. 16  
J. 21  
K. 26

53. Given \(10^{(\frac{2x-1}{x})} = 1\), \(x = ?\)

A. \(-\frac{1}{2}\)  
B. \(-\frac{1}{8}\)  
C. \(\frac{1}{2}\)  
D. \(\frac{10}{19}\)  
E. \(1\)

54. The table below shows the results of a survey of 250 people who were asked whether they like to read and whether they play a musical instrument.

<table>
<thead>
<tr>
<th></th>
<th>Play a musical instrument</th>
<th>Do NOT play a musical instrument</th>
<th>Total</th>
</tr>
</thead>
<tbody>
<tr>
<td>Like to read</td>
<td>50</td>
<td>60</td>
<td>110</td>
</tr>
<tr>
<td>Do NOT like to read</td>
<td>40</td>
<td>100</td>
<td>140</td>
</tr>
<tr>
<td>Total</td>
<td>90</td>
<td>160</td>
<td>250</td>
</tr>
</tbody>
</table>

According to the results, what is the probability that a randomly selected person who was surveyed likes to read, given that the person plays a musical instrument?

F. \(\frac{1}{5}\)  
G. \(\frac{5}{9}\)  
H. \(\frac{5}{17}\)  
J. \(\frac{9}{25}\)  
K. \(\frac{11}{25}\)
55. Mario was riding a bicycle with wheels 26 inches in diameter. During 1 minute of Mario’s ride, the wheels made exactly 200 revolutions. At what average speed, in feet per second, was Mario riding during that minute?

A. \( \frac{65}{9} \pi \)
B. \( \frac{65}{18} \pi \)
C. \( \frac{130}{9} \pi \)
D. \( \frac{845}{18} \pi \)
E. \( \frac{1,690}{9} \pi \)

56. Whenever \( j \) and \( k \) are positive integers such that \( \sqrt{3^j} = 27^k \), what is the value of \( \frac{j}{k} \)?

F. \( \frac{1}{6} \)
G. \( \frac{3}{2} \)
H. 3
J. 4
K. 6

57. A finite arithmetic sequence has 7 terms, and the first term is \( \frac{3}{4} \). What is the difference between the mean and the median of the 7 terms?

A. 0
B. \( \frac{3}{4} \)
C. \( \frac{4}{3} \)
D. 3
E. 4

GO ON TO THE NEXT PAGE.
58. In the circle with center $D$ shown below, the length of radius $\overline{CD}$ is 4 cm, the length of $\overline{BC}$ is 1 cm, and $\overline{BC}$ is perpendicular to radius $\overline{AD}$ at $B$. When $\angle ADC$ is measured in degrees, which of the following expressions represents the length, in centimeters, of $\overline{AC}$?

![Diagram of a circle with a triangle inside it, showing radius $\overline{CD}$ of 4 cm, $\overline{BC}$ of 1 cm, and $\overline{BC}$ perpendicular to $\overline{AD}$ at $B$.]

F. $\frac{\pi}{45} \left( \sin^{-1} \left( \frac{1}{4} \right) \right)$

G. $\frac{\pi}{45} \left( \cos^{-1} \left( \frac{1}{4} \right) \right)$

H. $2\frac{\pi}{45} \left( \sin^{-1} \left( \frac{1}{4} \right) \right)$

J. $2\frac{\pi}{45} \left( \cos^{-1} \left( \frac{1}{4} \right) \right)$

K. $2\frac{\pi}{45} \left( \tan^{-1} \left( \frac{1}{4} \right) \right)$

59. The lengths of the triangle shown below are rounded to the nearest 0.1 cm. What is the area, to the nearest 1 cm$^2$, of this triangle?

![Diagram of a triangle with sides 4.0 cm, 5.0 cm, and 8.0 cm, and an angle of 30°.]

(Note: The area of any triangle with sides of length $a$, $b$, and $c$ opposite angles of measure $A$, $B$, and $C$, respectively, is given by $\frac{1}{2}ab \sin C$.)

A. 4
B. 5
C. 8
D. 10
E. 14
60. The probability distribution of the discrete random variable $X$ is shown in the table below. What is the expected value of $X$?

<table>
<thead>
<tr>
<th>$x$</th>
<th>Probability $P(X = x)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>$\frac{1}{6}$</td>
</tr>
<tr>
<td>1</td>
<td>$\frac{1}{12}$</td>
</tr>
<tr>
<td>2</td>
<td>$\frac{1}{4}$</td>
</tr>
<tr>
<td>3</td>
<td>$\frac{1}{12}$</td>
</tr>
<tr>
<td>4</td>
<td>$\frac{1}{12}$</td>
</tr>
<tr>
<td>5</td>
<td>0</td>
</tr>
<tr>
<td>6</td>
<td>$\frac{1}{3}$</td>
</tr>
</tbody>
</table>

F. $\frac{1}{6}$
G. $\frac{1}{3}$
H. 1
J. 2
K. $3\frac{1}{6}$
LITERARY NARRATIVE: This passage is adapted from the novel A Map of Home by Randa Jarrar (©2008 by Randa Jarrar).

I don’t remember how I came to know this story, and I don’t know how I can possibly still remember it. On August 2, the day I was born, my baba (father) stood at the nurses’ station of St. Elizabeth’s Medical Center of Boston with a pen between his fingers and filled out my birth certificate. He had raced down the stairs seconds after my birth, as soon as the doctor had assured him that I was all right. While filling out my certificate, Baba realized that he didn’t know my sex for sure but that didn’t matter; he’d always known I was a boy, had spoken to me as a boy while I was in Mama, and as he approached the box that contained the question, NAME OF CHILD, he wrote with a quivering hand and in his best English cursive, Nidal (strife; struggle). It was not my grandfather’s name, and Baba, whose name is Waheed and who was known during his childhood as Said, was the only son of the family, so the onus of renaming a son after my grandfather fell squarely upon his shoulders. It was an onus he brushed off his then-solid shoulders unceremoniously, like a piece of lint or a flake of dandruff; these are analogies my grandfather would the next day angrily pen in a letter sent from Jenin to Boston.

When he’d filled out the entire form, Baba regally relayed it to the nurse, who he remembered was called Rhonda. Then Baba, in flip-flops, turned around and raced up the white-tiled hallway, bypassed the elevator, ran up the three floors to the maternity ward, and burst into the birthing room.

“How is my queen?” said Baba, caressing my mother’s face.

“She’s lovely,” Mama said, thinking he meant me, “and eight whole pounds, the buffalo! No wonder my back was so . . .” Baba’s brow furrowed, and Mama couldn’t finish her complaint, because, eager to correct his mistake, Baba was already out the door and running down the white-tiled hallway, past new mothers and their red-faced babies, past hideous robes in uncalled-for patterns, bypassing the elevator, and sliding down the banister of the staircase. He raced on, screaming for Rhonda, where is Rhonda, help me, Rhonda, an outcry that provided the staff with three weeks’ worth of laughter.

Rhonda emerged with the birth certificate in hand, and Baba, who is not usually known for laziness, grabbed a pen and added at the end of my name a heavy, reflexive, feminizing, possessive, cursive “I.”

Moments later, Mama, who had just been informed of my nom de guerre, got out of bed and walked us to the elevator, the entire time ignoring my baba, who was screaming, “Nidali is a beautiful name, so unique, come on Ruz, don’t be so rash, you mustn’t be walking, you need to rest!”

Mama must not have fought long, or who knows: maybe she went to the nurses’ station and talked to Rhonda, and maybe Rhonda told her that the birth certificate was already sent out—that Mama would have to go to the office of the City of Boston clerk and see the registar of vital statistics, where they keep the birth and death certificates—and maybe Mama, who is the most superstitious of all humans (even more than Baba, and to that she’ll attest) shuddered at the thought of taking me, a newborn, through the heat and the Boston traffic to a place where, she must’ve imagined, people went to fill out death certificates, and she must’ve further imagined that going on such a trip, to such a place, would surely bring about my death—because I still have my name.

Whenever I imagined Baba running out just after my birth and sliding through the hallways like a movie star, I knew he must have embellished. Baba liked to do that: tell stories that were impossible but true all at once, especially if those stories made him look like a rock star. This is because he used to be a writer and was now an architect. Our little apartment was filled with blueprints and plastic models of houses instead of notebooks and poetry: a reality that filled him with great sadness. So Baba put that sadness into these stories.

Mama liked to expose him when he told such stories; she was his paparazzo, his story-cop. This was because she was the true rock star: a musician who no longer played music. Our house was filled with Baba’s blueprints and plastic models of houses and with my schoolwork and toys and dolls and a hundred half pairs of socks instead of a piano: a reality that filled her with great sadness.

I knew from the beginning that home meant embellishing, and that’s why I loved school. Teachers were there; they taught us facts based on reality.
1. The point of view from which the passage is told is best described as that of:
A. a first person narrator who re-creates a story about her parents and the birth of their first child, events which happened before the narrator was born.
B. a first person narrator who offers insight into characters’ thoughts and relates actions mainly from a time she was too young to remember.
C. an omniscient third person narrator who relates the thoughts and actions of several characters.
D. a limited third person narrator who relates events most closely from the perspective of Nidali.

2. The narrator mentions a piece of lint and a flake of dandruff primarily to:
F. imply that the narrator’s grandfather didn’t value family traditions.
G. provide examples of movements Baba made while filling out the birth certificate.
H. emphasize the importance of naming the baby after the baby’s grandfather.
J. illustrate the casual way in which the narrator’s father ignored a tradition.

3. Based on the passage, Mama’s reaction to learning the name Baba gave the baby can best be described as:
A. disapproval followed by resignation.
B. annoyance followed by amusement.
C. embarrassment followed by outrage.
D. shock followed by resentment.

4. The sequence of actions described in the seventh paragraph (lines 54–68) can best be characterized as:
F. Baba’s exaggerated account of Mama’s trip to the office of the City of Boston clerk.
G. a scenario the narrator imagines could have happened.
H. the story of how Nidali got her name from Mama’s point of view.
J. a memory that the narrator shares to reveal more about her personality.

5. The narrator concludes that Mama didn’t go to the office of the City of Boston clerk based on the fact that:
A. Baba believed it would be unlucky to change a baby’s name at that point.
B. going there would’ve required taking the baby out in a severe winter storm.
C. Mama had a tendency to change her mind quickly.
D. the narrator still has the name Nidali.

6. In line 78, the phrase these stories most nearly refers to:
F. the conflicting stories about the origins of Nidali’s name.
G. Baba’s notebooks and poetry.
H. the embellished tales Baba liked to tell.
J. the narrator’s accounts of her family’s time in Boston.

7. According to the passage, which of the following emotions do Baba and Mama share regarding their professional lives?
A. Pride
B. Anxiety
C. Sadness
D. Contentment

8. Of the following characters, which one does the narrator describe as the most superstitious?
F. Mama
G. Baba
H. Nidali
J. Rhonda

9. The narrator most strongly suggests that Mama does which of the following when Baba tells stories?
A. Yawns and rolls her eyes in mock boredom
B. Goes about her business and ignores him
C. Chimes in with exaggerations and white lies
D. Corrects him about the accuracy of details

10. In the passage, the narrator makes which of the following distinctions?
F. Home is a place of embellished stories, whereas school is a place of facts and reality.
G. Mama is a true rock star, whereas Baba is an amateur musician.
H. Being an architect made Baba happy, whereas being a writer made him miserable.
J. Writing requires great imagination, whereas playing music requires great skill.
Passage A by Laura Hillenbrand

The horseless carriage was just arriving in San Francisco, and its debut was turning into one of those colorfully unmitigated disasters that bring misery to everyone but historians. Consumers were staying away from the “devilish contraptions” in droves. In San Francisco in 1903, the horse and buggy was not going the way of the horse and buggy.

For good reason. The automobile, so sleekly efficient on paper, was in practice a civic menace, belching out exhaust, kicking up storms of dust, becoming hopelessly mired in the most innocuous-looking puddles, and tying up horse traffic. Incensed local lawmakers responded with monuments to legislative creativity. The laws of at least one town required automobile drivers to stop, get out, and fire off Roman candles every time horse-drawn vehicles came into view. Massachusetts tried and, fortunately, failed to mandate that cars be equipped with bells that would ring with each revolution of the wheels. In some towns police were authorized to disable passing cars with ropes, chains, and wires. San Francisco didn’t escape the legislative wave. Bitter local officials pushed through an ordinance banning automobiles from all tourist areas, effectively exiling them from the city.

Nor were these the only obstacles. The asking price for the cheapest automobile amounted to twice the $500 annual salary of the average citizen—some cost three times that much—and all that bought you was four wheels, a body, and an engine. “Accessories” like bumpers, carburetors, and headlights had to be purchased separately. Navigation was a nightmare. The first of San Francisco’s road signs were only just being erected, hammered up by an enterprising insurance underwriter who hoped to win clients by posting directions into the countryside, where drivers retreated for “picnic parties” held out of the view of angry townsfolk.

The first automobiles imported to San Francisco had so little power that they rarely made it up the hills. The grade of Nineteenth Avenue was so daunting for the engines of the day that watching automobiles straining for the top became a local pastime.

Passage B by Peter Carlson

In the mid-1950s, Ford Motor Company was building not one, not two, but 18 varieties of Edsel, including a convertible and a station wagon. The designers came up with some interesting ideas. They created a push-button transmission and put it in the middle of the steering wheel, where most cars have a horn. And they fiddled with the front end: Where other cars had horizontal chrome grilles, the Edsel would have a vertical chrome oval in its grille. It was new! It was different!

Unfortunately, it didn’t work. It couldn’t suck in enough air to cool the engine. “They had to keep opening up that oval to get more air in there,” says Jim Arnold, who was a trainee in Edsel’s design shop. “And it didn’t look as good.”

Edsel didn’t have its own assembly lines, so the cars were produced in Ford and Mercury plants, which caused problems. Every once in a while, an Edsel would roll past workers who were used to Mercurys or other Fords. Confused, they sometimes failed to install all the parts before the Edsel moved on down the line. Cars without parts can be a problem, of course, but other aspects of the Edsel juggernaut worked perfectly—the hype, for instance. The Edsel PR team touted the glories of the cars, but wouldn’t let anybody see them. When they finally released a photo, it turned out to be a picture of . . . the Edsel’s hood ornament. And hundreds of publications actually printed it!

On September 4, 1957, proclaimed by Ford as E-Day, nearly 3 million Americans flocked to showrooms to see the Edsel. Unfortunately, very few of them bought the Edsel. “We couldn’t even get people to drive it,” says C. Gayle Warnock, Edsel’s public relations director. “They just didn’t like the car. They just didn’t like the front end.”

But styling was hardly the worst problem. Oil pans fell off, trunks stuck, paint peeled, doors failed to close and the much-hyped “Teletouch” push-button transmission had a distressing tendency to freeze up. People joked that Edsel stood for “Every day something else leaks.”

Another major problem was caused by bad luck: The Edsel was an upscale car launched a couple months after a stock market plunge caused a recession. Sales of all premium cars plummeted.

Before E-Day, Edsel’s hypemeisters promised to sell 200,000 cars the first year. Actually, they sold 63,110. Sales dropped below 45,000 the second year. And only 2,846 of the 1960 models sold before Ford pulled the plug.
11. Which of the following statements about automobiles in San Francisco in 1903 is best supported by Passage A?
   
   A. They were affordable for the average citizen but unpopular nevertheless.
   
   B. They were used more by tourists for sightseeing purposes than by citizens for practical purposes.
   
   C. They failed to capture the public imagination in spite of huge public relations efforts.
   
   D. They were considered a public nuisance by all but a small segment of the population.

12. Which of the following terms in Passage A is used more figuratively than literally?
   
   F. Puddles (line 11)
   
   G. Monuments (line 13)
   
   H. Bells (line 18)
   
   J. Hills (line 39)

13. The purpose of the quotation marks around the word accessories in line 29 is most likely to:
   
   A. suggest that the features were actually essentials.
   
   B. indicate that the word appeared in legal documents.
   
   C. emphasize that the word was widely misunderstood.
   
   D. clarify that inexpensive automobiles had some luxury features.

16. Which of the following events referred to in Passage B occurred first chronologically?
   
   F. E-Day ended.
   
   G. The stock market plunged.
   
   H. Edsel sales dropped below 45,000.
   
   J. Edsel sales reached 2,846.

17. As it is used in the passage, the term premium cars (line 86) serves primarily as a:
   
   A. reference to what Edsels have become now that they are valued antiques.
   
   B. name for a type of car that was ushered in by the makers of the Edsel.
   
   C. label for a category of cars that the makers of the Edsel intended it to belong to.
   
   D. derisive term used sarcastically by Edsel owners who were disappointed in their purchase.

18. A similarity between the two passages is that they both:
   
   F. examine their topics from a significant distance of time.
   
   G. reveal the author’s professional background as a way of lending credibility to the text.
   
   H. assert that automobiles have contributed little that is worthwhile to society.
   
   J. incorporate information about traffic and road conditions into a discussion of automobile design.

19. An element of Passage A that is not present in Passage B is a reference to what aspect of the automobile culture?
   
   A. Related legislation
   
   B. Public opinion
   
   C. Economics
   
   D. Quotations from industry experts

20. If publicity experts had been assigned to build enthusiasm for the cars mentioned in Passage A using the methods described in Passage B, the experts would most likely have first released photos to the press that showed:
   
   F. cars going up Nineteenth Avenue in San Francisco.
   
   G. a single detail such as a gleaming headlight or a polished door handle.
   
   H. the meticulous work done along the assembly line to ensure the quality of the new car.
   
   J. an attractive young couple smiling as they enjoy a car ride past horses grazing in pastures.
The legend of Winslow Homer is that he left New York civilization to become a recluse on the coast of Maine for the last 25 years of his life. In reality, the property at Prouts Neck—which included a large, rambling hotel building—was purchased by his brother Charles for the whole extended Homer family. The artist also built a studio with an ocean view just yards away from the family house so throughout the summers he could enjoy the company of his father, his brothers and their wives, as well as the year-round guests of the many local people whose friendship he valued. Homer continued to travel frequently, spending parts of the winter in the Caribbean. But the artist always lived alone, and when he was working, which was the large part of most of his days, he could be extremely short-tempered when interrupted.

The sea outside his window now inspired the artist to create what came to be known as his greatest paintings. The Maine coast is extremely rocky and prone to monstrous gales that—at their most powerful—can whip up the waves to 40 or 50 feet. Screaming winds can rip across the breakers, creating long horizontal trails of spray. Homer rendered this sea with all the understanding of a painter who knows to simplify and synthesize. In paintings such as *Eastern Point* and *Cannon Rock* the construction of the water has been reorganized into clear graphic shapes and strong directional lines that echo the Japanese printmaking that had such a lasting effect on his work. The rocks in the paintings are massed into powerful, almost flat, designs and the brushing has become energetic, as though feeding from the physical strength of the ocean. These paintings take on an abstract grandeur that has justly made them famous. They remain, however, haunting evocations of the eternal power of the ocean.
23. Based on the passage, the way Homer depicted shapes in his early work and the way he depicted them in his later work is best described as shifting from:
   A. weak to powerful.
   B. sharp to rounded.
   C. dark to light.
   D. uplifting to melancholy.

24. According to the passage, Homer felt fascination for the subjects that inspired him at Tynemouth for:
   F. short time; Homer soon abandoned them for the genre subjects he’d been painting previously.
   G. short time; Homer found little commercial success painting those subjects.
   H. long time; Homer regularly returned to Tynemouth to paint.
   J. long time; Homer continued to be inspired by what he saw there for years.

25. According to the passage, the paintings that Tynemouth inspired Homer to create mainly featured:
   A. scenes of tourists and sunbathers enjoying the beach.
   B. the interplay between the sea and the lives of fishermen and their families.
   C. the dynamic struggle between farmers and the powerful forces of nature.
   D. the soothing yet dramatic beauty of the North Sea and its rocky shoreline.

26. The passage most strongly suggests that the main turning point in the development of Homer as an artist was his:
   F. discovery of subject matter that profoundly inspired him.
   G. sense of accomplishment at having paintings displayed at the Great Exposition.
   H. decision to spend winters in the Caribbean, where he was inspired by the sea.
   J. rejection of the belief that the world was stark and melancholy.

27. The author characterizes the immediate effect of experiences in Paris upon Homer’s work as:
   A. subtle; Homer continued to paint simple shapes and powerful designs but used more color.
   B. dramatic; Homer’s work became bolder and clearer.
   C. imperceptible; Homer’s work didn’t change until several years later.
   D. significant; Homer abandoned the subjects he’d been painting before his time in Paris.

28. The main idea of the last paragraph is that:
   F. Homer’s paintings of the Maine coast exhibit the culmination of his artistic skills.
   G. Homer’s paintings of the sea evoke the grandeur of the human spirit in the natural world.
   H. the most effective way to depict water in a painting is to use graphic shapes and directional lines.
   J. viewing two of Homer’s famous paintings of the sea had a lasting effect on the author.

29. The author speculates that Homer may have chosen to go to Tynemouth because he:
   A. wanted to return to the place that had originally inspired him to be a painter.
   B. expected to be able to work better without the distractions he struggled with in Paris.
   C. needed a break from the overcrowded Jersey coast.
   D. hoped to find the kinds of subjects he had depicted in some of his earlier popular paintings.

30. The passage states that in Prouts Neck, Homer could be irritable when:
   F. his paintings weren’t selling well.
   G. storms prevented him from painting outdoors.
   H. the sea was too rough to go boating.
   J. he was interrupted while painting.
It took humans thousands of years to explore our own planet and centuries to comprehend our neighboring planets, but nowadays new worlds are being discovered every week. To date, astronomers have identified more than 370 “exoplanets,” worlds orbiting stars other than the sun. Many are strange. There’s an Icarus-like “hot Saturn” 260 light-years from Earth, whirling around its parent star so rapidly that a year there lasts less than three days. Circling another star 150 light-years out is a scorched “hot Jupiter,” whose upper atmosphere is being blasted off to form a gigantic, comet-like tail. Three brightened planets have been found orbiting a pulsar—the remains of a once mighty star shrunk into a spinning atomic nucleus the size of a city—while untold numbers of worlds have evidently fallen into their suns or been flung out of their systems to become “floaters” that wander in eternal darkness.

Amid such exotica, scientists are eager for a hint of the familiar: planets resembling Earth, orbiting their stars at just the right distance—neither too hot nor too cold—to support life as we know it. No planets quite like our own have yet been found, presumably because they’re inconspicuous. To see a planet as small and dim as ours amid the glare of its star is like trying to see a firefly in a fireworks display; to detect its gravitational influence on the star is like listening for a cricket in a tornado. Yet by pushing technology to the limits, astronomers are rapidly approaching the day when they can find another Earth and interrogate it for signs of life.

Only 11 exoplanets, all of them big and bright and conveniently far away from their stars, have as yet had their pictures taken. Most of the others have been detected by using the spectroscopic Doppler technique, in which starlight is analyzed for evidence that the star is being tugged ever so slightly back and forth by the gravitational pull of its planets. In recent years astronomers have refined the Doppler technique so exquisitely that they can now tell when a star is pulled from its appointed rounds by only one meter a second—about human walking speed. That’s sufficient to detect a giant planet in a big orbit, or a small one if it’s very close to its star, but not an Earth at anything like our Earth’s 93-million-mile distance from its star. The Earth tugs the sun around at only one-tenth walking speed, or about the rate that an infant can crawl; astronomers cannot yet prize out so tiny a signal from the light of a distant star.

Another approach is to watch a star for the slight periodic dip in its brightness that will occur should an orbiting planet circle in front of it and block a fraction of its light. At most a tenth of all planetary systems are likely to be oriented so that these mini-eclipses, called transits, are visible from Earth, which means that astronomers may have to monitor many stars patiently to capture just a few transits. The French COROT satellite, now in the third and final year of its prime mission, has discovered seven transiting exoplanets, one of which is only 70 percent larger than Earth.

The United States’ Kepler satellite is COROT’s more ambitious successor. Launched from Cape Canaveral in March 2008, Kepler is essentially just a big digital camera with a .95-meter aperture and a 95-megapixel detector. It makes wide-field pictures every 30 minutes, capturing the light of more than 100,000 stars in a single patch of sky between the bright stars Deneb and Vega. Computers on Earth monitor the brightness of all those stars over time, alerting humans when they detect the slight dimming that could signal the transit of a planet.

Because that dimming can be mimicked by other phenomena, such as the pulsations of a variable star or a large sunspot moving across a star’s surface, the Kepler scientists won’t announce the presence of a planet until they have seen it transit at least three times—a wait that may be only a few days or weeks for a planet rapidly circling close to its star but years for a terrestrial twin. By combining Kepler results with Doppler observations, astronomers expect to determine the diameters and masses of transiting planets. If they manage to discover a rocky planet roughly the size of Earth orbiting in the habitable zone—not so close to the star that the planet’s water has been baked away, nor so far out that it has frozen into ice—they will have found what biologists believe could be a promising abode for life.

31. Which of the following descriptions best reflects the way the passage is organized?
   A. It raises the question of whether exoplanets exist and then presents to an equal extent arguments on both sides.
   B. It focuses first on the search for planets, then sharpens that focus to the search for planets like our own.
   C. It defines planets, first those in Earth’s solar system and then those familiar mostly to astronomers.
   D. It refers to mythology, then moves to a technical description of those exoplanets the size of Earth or smaller.

32. The passage makes use of both technical terms and:
   F. rhetorical questions.
   G. figurative language.
   H. excerpts from the writings of astronauts.
   J. excerpts from the writings of ancient astronomers.
33. As it is used in line 18, the term such exotica refers to:
   A. the sophisticated equipment used to locate previously unidentified planets.
   B. the contents of our solar system, in particular the planets Jupiter and Saturn.
   C. overblown claims about planets far from Earth.
   D. planets and solar systems vastly unlike Earth and its solar system.

34. What is the main idea of the second paragraph (lines 18–30)?
   F. Recently discovered exoplanets have disappointed scientists.
   G. Some exoplanets were once thought to be stars at the center of solar systems.
   H. Some recently discovered exoplanets spin on their axis at the same speed that Earth spins on its axis.
   J. Planets that resemble Earth are extremely hard to detect.

35. The passage’s description of the spectroscopic Doppler technique indicates that it is a method used to identify the:
   A. intensity of light reaching Earth from a planet outside Earth’s solar system.
   B. effect of a planet’s gravitational pull on the sun the planet is orbiting.
   C. speed at which a planet rotates on its axis.
   D. distance between an exoplanet and its former sun.

36. According to the passage, in order to confirm a possible planet using the Kepler method, scientists look for:
   F. evidence of water both as a solid and a liquid on the supposed planet.
   G. an uninterrupted light originating from the supposed planet.
   H. identical results in images of the same location taken 24 hours apart.
   J. three occurrences of a slight dimming in a star that strongly indicates a planet’s presence.

37. According to the passage, at the time the passage was written, how many exoplanets had had their picture taken?
   A. 370
   B. 95
   C. 11
   D. 0

38. According to the passage, which of the following is a capability of the Kepler?
   F. It can capture the light of more than 100,000 stars in a single patch of sky.
   G. It can determine the distance between an exoplanet and its star.
   H. It can travel up to 150 light-years away from Earth.
   J. It can determine the surface features of planets well enough to indicate the presence of water.

39. In the passage, Deneb and Vega are identified as:
   A. stars at the edges of the area examined by the Kepler.
   B. planets that are only 70 percent larger than Earth.
   C. scientists pioneering in the field of planet searching.
   D. former stars whose traveling light is still visible.

40. According to the passage, what do scientists expect to determine about any given transiting planet by combining Kepler results with Doppler observations?
   F. The length of its year
   G. Its distance from its sun
   H. Its diameter and mass
   J. Its distance from Earth

END OF TEST 3

STOP! DO NOT TURN THE PAGE UNTIL TOLD TO DO SO.
DO NOT RETURN TO A PREVIOUS TEST.
In a study of fur pigmentation in deer mice, *Peromyscus polionotus*, scientists compared the brightness of the fur of mice from populations located different distances directly inland from a coastal site. Figure 1 shows the 2 facial regions and the 2 body regions at which the fur of each mouse was evaluated (on a scale from 0 to 1.00) with respect to its brightness. Figure 1 also shows how, for each of the 4 regions, average relative brightness varied with inland distance.

*For each facial or body region, the darkest fur pigmentation was assigned a brightness value of 0, and the lightest fur pigmentation was assigned a brightness value of 1.00.

Figure 1
Taking and Scoring Your First ACT Practice Test

1. Based on Figure 2, on average, where was the brightest surface soil found?
   A. At the coastal site
   B. 50 km inland
   C. 100 km inland
   D. 150 km inland

2. According to Figure 1, the average relative brightness of the dorsal stripe was 0.25 at an inland distance that was closest to which of the following?
   F. 20 km
   G. 40 km
   H. 60 km
   J. 80 km

3. According to Figure 1, the greatest change in the average relative brightness of the fur on the rostrum occurred between which of the following inland distances?
   A. 0 km and 25 km
   B. 25 km and 50 km
   C. 50 km and 75 km
   D. 100 km and 125 km

4. Based on Figure 1, on average, was the fur pigmentation on the ventrum of *P. polionotus* lighter or darker 150 km inland than it was at the coastal site?
   F. Lighter, because the average relative brightness 150 km inland was greater.
   G. Lighter, because the average relative brightness 150 km inland was less.
   H. Darker, because the average relative brightness 150 km inland was greater.
   J. Darker, because the average relative brightness 150 km inland was less.

5. Which of the following statements best explains the geographic variation in the fur pigmentation of *P. polionotus*? At any given inland distance, the more closely the fur pigmentation of a *P. polionotus* mouse matches the soil, the:
   A. less likely the mouse will be found by a predator, and thus the less likely it will pass its fur pigmentation traits to its offspring.
   B. less likely the mouse will be found by a predator, and thus the more likely it will pass its fur pigmentation traits to its offspring.
   C. more likely the mouse will be found by a predator, and thus the less likely it will pass its fur pigmentation traits to its offspring.
   D. more likely the mouse will be found by a predator, and thus the more likely it will pass its fur pigmentation traits to its offspring.

6. Based on Figure 2, on average, was the surface soil at the coastal site lighter or darker than the standard that was used for the comparison?
   F. Lighter; the average percent relative reflectance of the soil at the coastal site was 100%.
   G. Lighter; the average percent relative reflectance of the soil at the coastal site was less than 100%.
   H. Darker; the average percent relative reflectance of the soil at the coastal site was 100%.
   J. Darker; the average percent relative reflectance of the soil at the coastal site was less than 100%.
Passage II

A high concentration of dissolved nickel (Ni\(^{2+}\)) in wastewater is an environmental concern. Students studied the removal of Ni\(^{2+}\) from wastewater, using an aqueous Ni\(^{2+}\) solution as a model of wastewater.

In water, hydroxide (OH\(^{-}\)) reacts with Ni\(^{2+}\) to form nickel hydroxide monohydrate [Ni(OH)\(_2\)·H\(_2\)O]. The balanced chemical equation for this reaction is

\[
Ni^{2+} + 2OH^- + H_2O \rightarrow Ni(OH)_2\cdot H_2O
\]

Because the monohydrate is a solid, it can be filtered from the solution. Some of the solid will eventually dissolve if it is left in contact with the solution.

The students did 2 experiments to study how reaction time and filtration method affected the removal of Ni\(^{2+}\) from the aqueous Ni\(^{2+}\) solution.

**Experiment 1**

In each of Trials 1–3, Steps 1–4 were performed:

1. Thirty-two mL of aqueous 1.0 mole/L OH\(^-\) solution and 260 mL of aqueous 0.060 mole/L Ni\(^{2+}\) solution were poured into the same flask.
2. The mixture was stirred at 22°C for 10 min, 3 days, or 7 days.
3. Solid monohydrate was recovered by **standard filtration** (see Figure 1).

**Experiment 2**

In each of Trials 4–6, Steps 1–4 in Experiment 1 were performed except that in Step 3, solid monohydrate was recovered by **vacuum filtration** (see Figure 2).

The results of Experiments 1 and 2 are shown in Table 1.

<table>
<thead>
<tr>
<th>Experiment</th>
<th>Trial</th>
<th>Reaction time</th>
<th>CNF (mg/kg)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>1</td>
<td>10 min</td>
<td>6</td>
</tr>
<tr>
<td></td>
<td>2</td>
<td>3 days</td>
<td>39</td>
</tr>
<tr>
<td></td>
<td>3</td>
<td>7 days</td>
<td>42</td>
</tr>
<tr>
<td>2</td>
<td>4</td>
<td>10 min</td>
<td>58</td>
</tr>
<tr>
<td></td>
<td>5</td>
<td>3 days</td>
<td>69</td>
</tr>
<tr>
<td></td>
<td>6</td>
<td>7 days</td>
<td>73</td>
</tr>
</tbody>
</table>

Table 1 adapted from K. Blake Corcoran, Brian E. Rood, and Bridget G. Trogden, "Chemical Remediation of Nickel(II) Waste: A Laboratory Experiment for General Chemistry Students." ©2010 by Division of Chemical Education, Inc., American Chemical Society.

7. If a reaction time of 2 days had been tested in Experiment 1, the CNF would most likely have been:
   A. less than 6 mg/kg.
   B. between 6 mg/kg and 39 mg/kg.
   C. between 39 mg/kg and 42 mg/kg.
   D. greater than 42 mg/kg.
Based on the results of Experiments 1 and 2, what combination of reaction time and filtration method resulted in the lowest concentration of dissolved nickel in the filtrate?

<table>
<thead>
<tr>
<th>reaction time</th>
<th>filtration method</th>
</tr>
</thead>
<tbody>
<tr>
<td>F. 10 min</td>
<td>standard</td>
</tr>
<tr>
<td>G. 7 days</td>
<td>standard</td>
</tr>
<tr>
<td>H. 10 min</td>
<td>vacuum</td>
</tr>
<tr>
<td>J. 7 days</td>
<td>vacuum</td>
</tr>
</tbody>
</table>

9. Was the net force exerted on the mixture in the funnel more likely greater in Trial 3 or in Trial 6?
   A. Trial 3, because the filtration apparatus was connected to a vacuum pump.
   B. Trial 3, because the filtration apparatus was not connected to a vacuum pump.
   C. Trial 6, because the filtration apparatus was connected to a vacuum pump.
   D. Trial 6, because the filtration apparatus was not connected to a vacuum pump.

10. In each trial, the students performed which of the following chronological sequences of steps?
   F. Measuring the CNF; recovering the solid by filtration; mixing the Ni$^{2+}$ and the OH$^{-}$ solutions
   G. Mixing the Ni$^{2+}$ and the OH$^{-}$ solutions; recovering the solid by filtration; measuring the CNF
   H. Recovering the solid by filtration; measuring the CNF; mixing the Ni$^{2+}$ and the OH$^{-}$ solutions
   J. Recovering the solid by filtration; mixing the Ni$^{2+}$ and the OH$^{-}$ solutions; measuring the CNF

11. A student predicted that when solid monohydrate is recovered by vacuum filtration, a greater CNF will result for a reaction time of 3 days than for a reaction time of 10 min. Do the data in Table 1 support this prediction?
   A. No; Trial 1 had a greater CNF than did Trial 2.
   B. No; Trial 5 had a greater CNF than did Trial 4.
   C. Yes; Trial 1 had a greater CNF than did Trial 2.
   D. Yes; Trial 5 had a greater CNF than did Trial 4.

12. In how many of the 6 trials was nickel hydroxide monohydrate recovered by standard filtration after OH$^{-}$ and Ni$^{2+}$ had been allowed to react for at least 3 days?
   F. 1
   G. 2
   H. 4
   J. 6

13. Based on the balanced chemical equation in the passage, as 6 OH$^{-}$ ions are consumed, how many formula units of Ni(OH)$_2$$\cdot$H$_2$O are produced?
   A. 3
   B. 6
   C. 12
   D. 18
Passage III

Star formation begins with the gravitational collapse of matter in an interstellar gas cloud. A protostar (forming star) affects gas in the surrounding portions of the cloud in 2 ways:

- The protostar’s gravitational field attracts gas, causing the gas to accrete (accumulate onto the protostar).
- Radiation pressure (RP) associated with the protostar’s emissions causes gas to be pushed away from the protostar, inhibiting accretion.

Star formation ends when the effect of RP overcomes that of gravity. At that point, the protostar can no longer gain mass by accretion and is considered a fully formed star.

Three scientists debate whether the maximum mass that a protostar can reach by accretion is great enough to account for the most massive stars observed.

Scientist 1

The effect of RP is uniform in all directions around a protostar. As a result, the maximum mass that a protostar can reach by accretion is 20 $M_\odot$ (1 $M_\odot$ = mass of the Sun). Any further increase in mass requires at least 1 stellar merger (the combination of 2 or more fully formed stars into 1). Because stars tend to form in clusters, stellar mergers are likely.

Scientist 2

Scientist 1 is correct that stellar mergers are likely. However, because a protostar rotates about its axis, a disk of gas forms in the plane of the protostar’s equator. This reduces the effect of RP in that plane, allowing gas from the disk to readily accrete. As a result, the maximum mass that a protostar can reach by accretion is 40 $M_\odot$. Any further increase in mass requires at least 1 stellar merger.

Scientist 3

Stellar mergers are very unlikely given the vast distances between stars, even within clusters. Scientist 2 is correct about the formation and the effect of the disk. In addition, a protostar produces bubble-like regions of radiation that increase the effect of RP near the protostar’s poles, promoting the flow of gas into the disk. As a result, accretion continues until the surrounding portions of the cloud are nearly depleted of gas. Therefore, the maximum mass that a protostar can reach by accretion is limited only by the amount of available gas.

14. Relative to the center of the protostar, does gravity more likely accelerate gas particles inward or outward, and does RP more likely accelerate gas particles inward or outward?
   - gravity: inward, inward
   - RP: inward, outward

15. Based on Scientist 2’s argument, do gas particles more likely accrete near the equator or near the poles of a protostar with a disk?
   - A. Near the equator, because the effect of RP is increased there.
   - B. Near the equator, because the effect of RP is reduced there.
   - C. Near the poles, because the effect of RP is increased there.
   - D. Near the poles, because the effect of RP is reduced there.
16. Detailed surveys of star clusters in and near the Milky Way have yielded no evidence of stellar mergers having occurred at any time during the galaxy’s history. These results are inconsistent with the argument(s) of which scientist(s)?
   F. Scientist 1 only
   G. Scientist 3 only
   H. Scientists 1 and 2 only
   J. Scientists 1 and 3 only

17. One of the most massive stars known is Eta Carinae, which has an approximate mass of 120 M☉. Based on the arguments of Scientists 1, 2, and 3, respectively, what is the minimum number of stars, each formed entirely by accretion, that would have been required to form Eta Carinae?
   Scientist 1  Scientist 2  Scientist 3
   A. 5 3 1
   B. 5 4 2
   C. 6 3 1
   D. 6 4 2

18. When the effect of RP overcomes that of gravity, a star is said to have “emerged from its envelope,” because that is the first time the star is directly observable from outside the cloud. An observation of which of the following stars emerging from its envelope would support Scientist 2’s argument but weaken Scientist 1’s argument?
   F. A 15 M☉ star
   G. A 20 M☉ star
   H. A 30 M☉ star
   J. A 50 M☉ star

19. Scientists 2 and 3 agree that a disk forms around a protostar as a result of the protostar’s:
   A. motion.
   B. emission of radiation.
   C. location within a star cluster.
   D. merger with another star.

20. Which of the scientists, if any, would be likely to agree that the Sun could have formed entirely by accretion?
   F. Scientist 1 only
   G. Scientist 3 only
   H. Scientists 1, 2, and 3
   J. None of the scientists
Passage IV

Two studies were done to examine how the proportion of vermicompost (feces from earthworms) in a particular potting soil affects the yield of each of 2 plant species: Solanum lycopersicum (a tomato plant) and Capsicum annuum (a pepper plant). The yield of a plant species is the mass of fruit produced per plant of the species.

Six different mixtures (Mixtures 1–6) were prepared according to the percents listed in Table 1.

<table>
<thead>
<tr>
<th>Mixture</th>
<th>Percent by volume of:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>vermicompost</td>
</tr>
<tr>
<td>1</td>
<td>0</td>
</tr>
<tr>
<td>2</td>
<td>20</td>
</tr>
<tr>
<td>3</td>
<td>40</td>
</tr>
<tr>
<td>4</td>
<td>60</td>
</tr>
<tr>
<td>5</td>
<td>80</td>
</tr>
<tr>
<td>6</td>
<td>100</td>
</tr>
</tbody>
</table>

Study 1

Equal amounts of Mixtures 1–6 were distributed among thirty-six 2 L pots in the following manner: 1.5 kg of Mixture 1 was put into each of 6 pots, 1.5 kg of Mixture 2 was put into each of 6 other pots, 1.5 kg of Mixture 3 was put into each of 6 other pots, and so on. Then, 3 S. lycopersicum seeds were added to each pot. For the next 158 days, all the pots received equal amounts of water and light. On Day 28 of the 158 days, all the seedlings that had emerged were removed from the pots with the exception of a single seedling in each pot. On Day 158, the yield of the remaining plant in each pot was measured. The average yield of the plants grown in each mixture was then calculated. The results are shown in Figure 1.

21. In both studies, as the percent by volume of vermicompost increased from 0% through 100%, the average yield:
A. decreased only.
B. increased only.
C. decreased, then increased.
D. increased, then decreased.

Study 2

The procedures of Study 1 were repeated, except that 5 C. annuum seeds instead of 3 S. lycopersicum seeds were added to each pot, the pots received water and light for 149 days instead of 158 days, seedling removal occurred on Day 42 of the 149 days, and plant yield was measured on Day 149. The results are shown in Figure 2.

22. In Study 1, which of the following mixtures was most likely intended to serve as a control for the effect of vermicompost on plant yield?
F. Mixture 1
G. Mixture 2
H. Mixture 4
J. Mixture 5

23. Suppose that in Study 1, average yield had been calculated in kilograms per plant (kg/plant) instead of g/plant. The average yield for Mixture 5 would have been:
A. 1.45 kg/plant.
B. 3.50 kg/plant.
C. 14.5 kg/plant.
D. 35.0 kg/plant.
24. Which of the factors listed below were the same in Study 2 as they were in Study 1?
   I. Number of pots used per mixture
   II. Length of time needed to perform the study
   III. Volume of each pot
   F. I and II only
   G. I and III only
   H. II and III only
   J. I, II, and III

25. Is the statement “Tomato plants require a lower proportion of vermicompost in the potting soil to achieve maximum yield than do pepper plants” consistent with the results of Studies 1 and 2?
   A. Yes; in Study 1, the greatest average yield was attained with Mixture 2, whereas in Study 2, the greatest average yield was attained with Mixture 3.
   B. Yes; in Study 1, the greatest average yield was attained with Mixture 3, whereas in Study 2, the greatest average yield was attained with Mixture 2.
   C. No; in Study 1, the greatest average yield was attained with Mixture 2, whereas in Study 2, the greatest average yield was attained with Mixture 3.
   D. No; in Study 1, the greatest average yield was attained with Mixture 3, whereas in Study 2, the greatest average yield was attained with Mixture 2.

26. In a 2 L pot, the presence of more than one plant can negatively affect the growth of all the plants in the pot, due to competition among the plants. What action was taken in the studies to prevent competition among the plants?
   F. Only one seed was planted per pot.
   G. Only one seedling was planted per pot.
   H. After an initial period of growth, all but one seed was removed from each pot.
   J. After an initial period of growth, all but one seedling was removed from each pot.

27. *S. lycopersicum* and *C. annuum* required water and light for the process represented by which of the following expressions?
   A. Water + light → glucose + oxygen + carbon dioxide
   B. Glucose + water + light → oxygen + carbon dioxide
   C. Oxygen + water + light → glucose + carbon dioxide
   D. Carbon dioxide + water + light → glucose + oxygen
Passage V

A cathode-ray tube (CRT) is a sealed, evacuated glass tube with a filament at one end and a fluorescent screen at the other end (see Figure 1).

When heated, the filament emits cathode rays that are accelerated by an electric potential, \( V \), toward a barrier having a pinhole. Beyond the barrier are 2 conducting plates, each of length \( L \), that have an electric field, \( E \), between them. (The direction of \( E \) can be upward or downward; in Figure 1, it is downward.) Any rays that pass through the pinhole travel through the field and strike the screen, producing a bright spot of visible light.

A group of students performed 3 studies on various CRTs, each of which had a ruler taped to the outer surface of the screen (see Figure 2) to measure a spot’s vertical location, \( y \) (in centimeters, cm).

Study 1

The students obtained a CRT having \( L = 2.5 \) cm. They set \( V \) to 1.0 kilovolt (kV), varied both the direction and the magnitude (in newtons per coulomb, N/C) of \( E \), and recorded the resulting values of \( y \) (see Table 1).

<table>
<thead>
<tr>
<th>Trial</th>
<th>direction*</th>
<th>magnitude (N/C)</th>
<th>( y ) (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>↑</td>
<td>( 1.0 \times 10^4 )</td>
<td>−3.2</td>
</tr>
<tr>
<td>2</td>
<td>↑</td>
<td>( 2.0 \times 10^4 )</td>
<td>−6.3</td>
</tr>
<tr>
<td>3</td>
<td>↑</td>
<td>( 3.0 \times 10^4 )</td>
<td>−9.5</td>
</tr>
<tr>
<td>4</td>
<td>↓</td>
<td>( 1.0 \times 10^4 )</td>
<td>3.2</td>
</tr>
<tr>
<td>5</td>
<td>↓</td>
<td>( 2.0 \times 10^4 )</td>
<td>6.3</td>
</tr>
<tr>
<td>6</td>
<td>↓</td>
<td>( 3.0 \times 10^4 )</td>
<td>9.5</td>
</tr>
</tbody>
</table>

*↑ = upward
↓ = downward

Study 2

Using the CRT from Study 1, the students set the magnitude of \( E \) to \( 1.0 \times 10^4 \) N/C, varied \( V \), and recorded the resulting values of \( y \) (see Table 2).

<table>
<thead>
<tr>
<th>Trial</th>
<th>( V ) (kV)</th>
<th>( y ) (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>7</td>
<td>0.5</td>
<td>6.3</td>
</tr>
<tr>
<td>8</td>
<td>1.0</td>
<td>3.2</td>
</tr>
<tr>
<td>9</td>
<td>1.5</td>
<td>2.1</td>
</tr>
<tr>
<td>10</td>
<td>2.0</td>
<td>1.6</td>
</tr>
<tr>
<td>11</td>
<td>2.5</td>
<td>1.3</td>
</tr>
</tbody>
</table>

Study 3

The students obtained various CRTs, each having a different \( L \). For each CRT, they set \( V \) to 1.0 kV, set the magnitude of \( E \) to \( 1.0 \times 10^4 \) N/C, and recorded the resulting value of \( y \) (see Table 3).

<table>
<thead>
<tr>
<th>Trial</th>
<th>( L ) (cm)</th>
<th>( y ) (cm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>12</td>
<td>1.5</td>
<td>−2.0</td>
</tr>
<tr>
<td>13</td>
<td>2.0</td>
<td>−2.6</td>
</tr>
<tr>
<td>14</td>
<td>2.5</td>
<td>−3.2</td>
</tr>
<tr>
<td>15</td>
<td>3.0</td>
<td>−3.8</td>
</tr>
<tr>
<td>16</td>
<td>3.5</td>
<td>−4.4</td>
</tr>
</tbody>
</table>
28. Studies 1 and 2 differed in which of the following ways? In Study 1, the students determined how the spot’s location varied with:
   F. electric potential, whereas in Study 2, they determined how the spot’s location varied with the magnitude and direction of the electric field.
   G. plate length, whereas in Study 2, they determined how the spot’s location varied with electric potential.
   H. the magnitude and direction of the electric field, whereas in Study 2, they determined how the spot’s location varied with electric potential.
   J. plate length, whereas in Study 2, they determined how the spot’s location varied with the magnitude and direction of the electric field.

29. Suppose that the students had performed a trial in Study 2 in which \( y \) was 2.6 cm. The value of \( V \) in this trial would most likely have been:
   A. less than 1.0 kV.
   B. between 1.0 kV and 1.5 kV.
   C. between 1.5 kV and 2.0 kV.
   D. greater than 2.0 kV.

30. Figure 2 could serve as an illustration of the result(s) of which trial(s)?
   F. Trial 1 only
   G. Trial 8 only
   H. Trials 1 and 4 only
   J. Trials 4 and 8 only

31. Based on the results of Study 1, in which direction did \( E \) most likely point in Study 2, and in which direction did \( E \) most likely point in Study 3?

<table>
<thead>
<tr>
<th>Study 2</th>
<th>Study 3</th>
</tr>
</thead>
<tbody>
<tr>
<td>A. ↑</td>
<td>↑</td>
</tr>
<tr>
<td>B. ↑</td>
<td>↓</td>
</tr>
<tr>
<td>C. ↓</td>
<td>↑</td>
</tr>
<tr>
<td>D. ↓</td>
<td>↓</td>
</tr>
</tbody>
</table>

32. Once a CRT is sealed, it cannot be reopened. However, because both \( V \) and \( E \) are controlled from the outside, a CRT can be used repeatedly under varying conditions. Based on the descriptions of Studies 1–3, what is the minimum number of different CRTs that the students required to complete the 3 studies?
   F. 1
   G. 5
   H. 11
   J. 16

33. Suppose that the students had performed a trial in which the cathode rays traveled all the way from the filament to the screen in a straight-line path, striking the screen at \( y = 0 \) cm. Based on the results of Studies 1 and 2, which of the following statements about \( V \) and the magnitude of \( E \) in this trial would have been true?
   A. \( V \) was zero but the magnitude of \( E \) was nonzero.
   B. \( V \) was nonzero but the magnitude of \( E \) was zero.
   C. Both \( V \) and the magnitude of \( E \) were zero.
   D. Both \( V \) and the magnitude of \( E \) were nonzero.

34. In a CRT, \( E \) is generated by building up equal and opposite electric charges on the 2 conducting plates. Suppose that cathode rays are negatively charged. If \( E \) is directed downward as shown in Figure 1, which conducting plate is more likely the negatively charged plate?
   F. The top plate, because charges of like sign are attracted to each other.
   G. The top plate, because charges of like sign are repelled from each other.
   H. The bottom plate, because charges of like sign are attracted to each other.
   J. The bottom plate, because charges of like sign are repelled from each other.
Passage VI

For gas atoms in a state of random motion, the mean free path, \( \lambda \), is the average distance a gas atom will travel between collisions with other gas atoms. This distance depends upon the diameter of the gas atom, \( d \), the volume of the gas, \( V \), and the number of atoms of the gas, \( N \). Table 1 lists the name, symbol, and value of \( d \) (in nanometers, nm) for each of 4 gases. Figure 1 shows, for each gas, at 293 kelvins (K), how \( \lambda \) (in nm) varies with \( V \) (in liters, L) in a sample with \( N = 6 \times 10^{23} \) atoms of the gas. Figure 2 shows, for each gas, at 293 K, how \( \lambda \) varies with \( N \) in a sample with \( V = 25 \text{ L} \).

Table 1

<table>
<thead>
<tr>
<th>Gas</th>
<th>Symbol</th>
<th>( d ) (nm)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Neon</td>
<td>Ne</td>
<td>0.076</td>
</tr>
<tr>
<td>Argon</td>
<td>Ar</td>
<td>0.142</td>
</tr>
<tr>
<td>Krypton</td>
<td>Kr</td>
<td>0.176</td>
</tr>
<tr>
<td>Xenon</td>
<td>Xe</td>
<td>0.216</td>
</tr>
</tbody>
</table>

35. According to Figure 2, what is the order of gas samples from shortest \( \lambda \) to longest \( \lambda \) for \( N = 15 \times 10^{23} \) atoms?

A. Ne, Ar, Kr, Xe  
B. Ne, Kr, Ar, Xe  
C. Xe, Ar, Kr, Ne  
D. Xe, Kr, Ar, Ne

36. According to Figure 2, doubling the Ne sample size from \( 6 \times 10^{23} \) atoms to \( 12 \times 10^{23} \) atoms effectively multiplies \( \lambda \) for Ne by a factor of:

F. \( \frac{1}{4} \)  
G. \( \frac{1}{2} \)  
H. 2  
J. 4

GO ON TO THE NEXT PAGE.
37. Consider 2 Kr samples at 293 K, each with $N = 6 \times 10^{23}$ atoms, but one with $V = 25$ L and the other with $V = 50$ L. Based on Figure 1, $\lambda$ for the 50 L sample would most likely be how many times as great as $\lambda$ for the 25 L sample?

A. $\frac{1}{4}$  
B. $\frac{1}{2}$  
C. 2  
D. 4

38. Based on Figure 1, for the Xe and Ar gas samples with $V = 20$ L, compared to $\lambda$ for Xe, approximately how much longer is $\lambda$ for Ar?

F. 50 nm  
G. 100 nm  
H. 150 nm  
J. 200 nm

39. The collision frequency is defined as the number of collisions between gas atoms per second. Consider the 5 L and 25 L Xe samples represented in Figure 1. Assuming the Xe atoms have the same average speed in both samples, in which sample would the collision frequency more likely be higher?

A. In the 5 L sample; Xe atoms in the 5 L sample travel, on average, shorter distances between collisions and therefore collide more often.  
B. In the 5 L sample; Xe atoms in the 5 L sample travel, on average, longer distances between collisions and therefore collide more often.  
C. In the 25 L sample; Xe atoms in the 25 L sample travel, on average, shorter distances between collisions and therefore collide more often.  
D. In the 25 L sample; Xe atoms in the 25 L sample travel, on average, longer distances between collisions and therefore collide more often.

40. For a particular sample of radon (Rn) gas in a 25 L container at 293 K, $\lambda$ is approximately 320 nm. If $d$ for Rn is 0.240 nm, then, based on Table 1 and Figure 2, approximately how many Rn atoms are most likely in this sample?

F. Less than $6 \times 10^{23}$  
G. Between $6 \times 10^{23}$ and $9 \times 10^{23}$  
H. Between $9 \times 10^{23}$ and $12 \times 10^{23}$  
J. More than $12 \times 10^{23}$
You may wish to photocopy these sample answer document pages to respond to the practice ACT Writing Test.

Begin WRITING TEST here.

If you need more space, please continue on the next page.
If you need more space, please continue on the next page.
STOP here with the Writing Test.
Practice Writing Test Prompt 1

Directions

This is a test of your writing skills. You will have forty (40) minutes to read the prompt, plan your response, and write an essay in English. Before you begin working, read all material in this test booklet carefully to understand exactly what you are being asked to do.

You will write your essay on the lined pages in the answer document provided. Your writing on those pages will be scored. You may use the unlined pages in this test booklet to plan your essay. Your work on these pages will not be scored.

Your essay will be evaluated based on the evidence it provides of your ability to:

- analyze and evaluate multiple perspectives on a complex issue
- state and develop your own perspective on the issue
- explain and support your ideas with logical reasoning and detailed examples
- clearly and logically organize your ideas in an essay
- effectively communicate your ideas in standard written English

Lay your pencil down immediately when time is called.

DO NOT OPEN THIS BOOKLET UNTIL TOLD TO DO SO.
Free Music

Free music is now available through many legal sources, from streaming services to online radio stations, making it largely unnecessary to purchase an album or even a single song. As sales figures continue to drop, some musicians, both high-profile and relatively unknown, have even quit trying to sell their music altogether, choosing instead to release new material for free online. Perhaps this trend is a matter of simple economics: cheap is good, but free is better. But it is worth considering whether our apparent unwillingness to spend money on music is an indication that its value in our lives is changing.

Read and carefully consider these perspectives. Each suggests a particular way of thinking about the changing value of music in our lives.

**Perspective One**

Digital technologies and the Internet have changed our relationship with music. It is so plentiful and readily available now that all value has been diluted.

**Perspective Two**

Music competes for our attention with many other kinds of inexpensive entertainment these days. We still value it, but we also have a lot of other ways to spend our money.

**Perspective Three**

With so many free sources, people are listening to more music and discovering more new musicians than ever before. Wide availability has only increased our appreciation of music.

**Essay Task**

Write a unified, coherent essay in which you evaluate multiple perspectives on the changing value of music in our lives. In your essay, be sure to:

- analyze and evaluate the perspectives given
- state and develop your own perspective on the issue
- explain the relationship between your perspective and those given

Your perspective may be in full agreement with any of the others, in partial agreement, or wholly different. Whatever the case, support your ideas with logical reasoning and detailed, persuasive examples.
Planning Your Essay

Your work on these prewriting pages will not be scored.

Use the space below and on the back cover to generate ideas and plan your essay. You may wish to consider the following as you think critically about the task:

Strengths and weaknesses of the three given perspectives
- What insights do they offer, and what do they fail to consider?
- Why might they be persuasive to others, or why might they fail to persuade?

Your own knowledge, experience, and values
- What is your perspective on this issue, and what are its strengths and weaknesses?
- How will you support your perspective in your essay?

If you need more space to plan, please continue on the back of this page.
Planning Your Essay

*Use this page to continue planning your essay. Your work on this page will not be scored.*
Scoring Your Practice Test

After taking your first ACT practice test, you are ready to score the test to see how you did overall. In this section, you learn how to determine your raw score, convert raw scores to scale scores, compute your Composite score, determine your estimated percentile ranks for each of your scale scores, and score your practice writing test.

When scoring each practice test and reviewing your scores, remember that your scores on the practice tests are only estimates of the scores that you will obtain on the ACT. If your score isn’t as high as you expected, it could mean a number of things. Maybe you need to review important content and skills. Maybe you should work a little faster when taking the test. Perhaps you simply weren’t doing your best work on the test. Or maybe you need to take more challenging courses to be better prepared. Keep in mind that a test score is just one indicator of your level of academic knowledge and skills. You know your own strengths and weaknesses better than anyone else, so keep them in mind as you evaluate your performance.

On each of the four multiple-choice tests (English, mathematics, reading, and science), the number of questions you answer correctly is called a raw score. To figure out your raw scores for the practice tests in this book count all your correct answers for each test using the scoring keys provided in the next section, “Scoring Your Multiple-Choice Practice Tests.” Then you can convert your raw scores into scale scores.

A scale score is a raw score that is converted to a scale score to enhance score interpretation and allow comparability across different forms. Scale scores are the scores that ACT reports to students, high schools, colleges, and scholarship agencies. One of the reasons ACT uses scale scores is to adjust for small differences among different forms of the ACT. After you’ve converted your raw scores for the practice tests to scale scores, you’ll want to convert your scale scores to percentile ranks. Percentile ranks, which are explained in the following pages, are useful for interpreting your scores relative to the scores of others who have taken the ACT.

If you took the optional practice writing test, the later section “Scoring Your Practice Writing Test Essay” includes a scoring rubric for evaluating your essay and estimating your writing test score. It is difficult to be objective about one’s own work, and you have not had the extensive training provided to actual readers of the writing test. However, it is to your advantage to read your own writing critically. Becoming your own editor helps you grow as a writer and as a reader, so it makes sense for you to evaluate your own practice essay. That having been said, it may also be helpful for you to give your practice essay to another reader to get another perspective: perhaps that of a classmate, a parent, or an English teacher, for example. To rate your essay, you and your reader should read the scoring rubric on pages 109–110 and the examples on pages 305–328, and then assign your practice essay a score of 1 (low) through 6 (high) in each of the four writing domains (ideas and analysis, development and support, organization, and language use).

Your writing test domain scores should be based on two ratings, so you may either multiply your own rating times two, or sum your rating and another reader’s rating to calculate your domain scores (2–12 for each domain). Your writing raw score is the sum of your domain scores.
Finally, convert your writing test score to percentile ranks using the procedures described. Percentile ranks enable you to compare your writing test score to those of others who have taken the writing test. **You can find the most current information on scoring the ACT writing test in the bonus online content.**

### Scoring Your Multiple-Choice Practice Tests

To score each of your multiple-choice practice tests, starting with the English test, follow these steps:

**STEP 1.** Write a “1” in the blank for each question that you answered correctly. An example is provided in the following box:

<table>
<thead>
<tr>
<th>Key</th>
<th>Your answer was</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. A</td>
<td>Incorrect</td>
</tr>
<tr>
<td>2. J</td>
<td>Correct</td>
</tr>
<tr>
<td>3. B</td>
<td>Correct</td>
</tr>
<tr>
<td>4. G</td>
<td>Incorrect</td>
</tr>
</tbody>
</table>

#### English Scoring Key - Practice Test 1

<table>
<thead>
<tr>
<th>Key</th>
<th>Key</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>2. F</td>
<td>27. D</td>
<td>52. J</td>
</tr>
<tr>
<td>5. B</td>
<td>30. F</td>
<td>55. B</td>
</tr>
<tr>
<td>7. C</td>
<td>32. F</td>
<td>57. C</td>
</tr>
<tr>
<td>9. C</td>
<td>34. F</td>
<td>59. C</td>
</tr>
<tr>
<td>10. G</td>
<td>35. D</td>
<td>60. F</td>
</tr>
<tr>
<td>17. A</td>
<td>42. J</td>
<td>67. A</td>
</tr>
<tr>
<td>18. G</td>
<td>43. C</td>
<td>68. H</td>
</tr>
<tr>
<td>20. F</td>
<td>45. C</td>
<td>70. J</td>
</tr>
<tr>
<td>23. D</td>
<td>48. F</td>
<td>73. D</td>
</tr>
</tbody>
</table>
STEP 2. Add the numbers you entered in step 1 and write this total in the following shaded box. This is your raw score.

Number Correct (Raw Score) for:
English test (75 questions) □□□□□□□□□□

STEP 3. Repeat steps 1 and 2 for the ACT mathematics, reading, and science tests using the scoring keys on the following pages.

Mathematics Scoring Key Practice Test 1

<table>
<thead>
<tr>
<th>Key</th>
<th>Key</th>
<th>Key</th>
</tr>
</thead>
<tbody>
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<td>2. G</td>
<td>22. K</td>
<td>42. J</td>
</tr>
<tr>
<td>5. B</td>
<td>25. D</td>
<td>45. A</td>
</tr>
<tr>
<td>7. E</td>
<td>27. C</td>
<td>47. E</td>
</tr>
<tr>
<td>14. F</td>
<td>34. F</td>
<td>54. G</td>
</tr>
<tr>
<td>15. B</td>
<td>35. B</td>
<td>55. A</td>
</tr>
<tr>
<td>17. E</td>
<td>37. A</td>
<td>57. A</td>
</tr>
<tr>
<td>20. G</td>
<td>40. F</td>
<td>60. K</td>
</tr>
</tbody>
</table>

Number Correct (Raw Score) for:
Math test (60 questions) □□□□□□□□□□
## Reading Scoring Key Practice Test 1

<table>
<thead>
<tr>
<th>Key</th>
<th>Key</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>5.</td>
<td>D</td>
<td>19.</td>
</tr>
<tr>
<td>13.</td>
<td>A</td>
<td>27.</td>
</tr>
</tbody>
</table>

Number Correct (Raw Score) for:
Reading test (40 questions)

## Science Scoring Key Practice Test 1

<table>
<thead>
<tr>
<th>Key</th>
<th>Key</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>13.</td>
<td>A</td>
<td>27.</td>
</tr>
</tbody>
</table>

Number Correct (Raw Score) for:
Science test (40 questions)
STEP 4. On each of the four tests, the total number of correct responses yields a raw score. Use the conversion table on the following page to convert your raw scores to scale scores. For each of the four tests, locate and circle your raw score or the range of raw scores that includes it in the conversion table. Then, read across to either outside column of the table and circle the scale score that corresponds to that raw score. As you determine your scale scores, enter them in the blanks provided below. The highest possible scale score for each test is 36. The lowest possible scale score for any of the four tests is 1.

Your Scale Scores

<table>
<thead>
<tr>
<th>English</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Mathematics</td>
<td></td>
</tr>
<tr>
<td>Reading</td>
<td></td>
</tr>
<tr>
<td>Science</td>
<td></td>
</tr>
<tr>
<td>Sum of Scores</td>
<td></td>
</tr>
<tr>
<td>Composite Score (sum ÷ 4)</td>
<td></td>
</tr>
</tbody>
</table>

STEP 5. Compute your Composite score by averaging the four scale scores. To do this, add your four scale scores and divide the sum by 4. If the resulting number ends in a fraction, round it off to the nearest whole number. (Round down any fraction less than one-half; round up any fraction that is one-half or more.) Enter this number in the appropriate blank below. This is your Composite score. The highest possible Composite score is 36. The lowest possible Composite score is 1.

Your Scale Scores

<table>
<thead>
<tr>
<th>English</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Mathematics</td>
<td></td>
</tr>
<tr>
<td>Reading</td>
<td></td>
</tr>
<tr>
<td>Science</td>
<td></td>
</tr>
<tr>
<td>Sum of Scores</td>
<td></td>
</tr>
<tr>
<td>Composite Score (sum ÷ 4)</td>
<td></td>
</tr>
</tbody>
</table>
### Scale Score Conversion Table: Practice Test 1

<table>
<thead>
<tr>
<th>Scale Score</th>
<th>Raw Score</th>
<th>Scale Score</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>English</td>
<td>Mathematics</td>
</tr>
<tr>
<td>36</td>
<td>74–75</td>
<td>57–60</td>
</tr>
<tr>
<td>35</td>
<td>71–73</td>
<td>54–56</td>
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<td>45–46</td>
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<td>27</td>
<td>60–61</td>
<td>43–44</td>
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<td>58–59</td>
<td>40–42</td>
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<td>24</td>
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</tr>
<tr>
<td>1</td>
<td>0–1</td>
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</tbody>
</table>

**STEP 6.** Use the table on page 107 to determine your estimated percentile ranks (percent at or below) for each of your scale scores. In the far left column of the table, circle your scale score for the English test (from page 105). Then read across to the percentile rank column for that test; circle or put a checkmark beside the corresponding percentile rank. Use the same procedure for the other three tests (from page 105). Using the right-hand column of scale scores for your science test and Composite scores may be easier. As you mark your percentile ranks, enter them in the blanks provided. You may also find it helpful to compare your performance with the national mean (average) score for each of the four tests and the Composite as shown at the bottom of the table.
### National Distributions of Cumulative Percents for ACT Test Scores

**ACT-Tested High School Graduates from 2013, 2014 and 2015**

<table>
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<tr>
<th>Score</th>
<th>ENGLISH</th>
<th>MATHEMATICS</th>
<th>READING</th>
<th>SCIENCE</th>
<th>COMPOSITE</th>
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**Mean** 20.3  20.9  21.3  20.8  21.0  
**S.D.** 6.6   5.3   6.4   5.4   5.4  

Note: These national norms are the source of U.S. Ranks, for multiple-choice tests, displayed on ACT reports during the 2015-2016 testing year. These norms with a sample size of 5,569,466, are based on 2013, 2014 and 2015 graduates.
Scoring Your Practice Writing Test Essay

To score your practice writing test essay, follow these steps:

**STEP 1.** Use the guidelines on the following scoring rubric to score your essay. Because many essays do not fit the exact description at each score point, read each description and try to determine which paragraph in the rubric best describes most of the characteristics of your essay.

You can find the most current information on scoring the ACT writing test in the bonus online content.
## The ACT Writing Test Scoring Rubric

<table>
<thead>
<tr>
<th>Score 6: Responses at this scorepoint demonstrate effective skill in writing an argumentative essay.</th>
<th>poorest Example</th>
<th>best Example</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Ideas and Analysis</strong></td>
<td>The writer generates an argument that critically engages with multiple perspectives on the given issue. The argument’s thesis reflects nuance and precision in thought and purpose. The argument establishes and employs an insightful context for analysis of the issue and its perspectives. The analysis examines implications, complexities and tensions, and/or underlying values and assumptions.</td>
<td>Development of ideas and support for claims deepen insight and broaden context. An integrated line of skilful reasoning and illustration effectively conveys the significance of the argument. Qualifications and complications enrich and bolster ideas and analysis.</td>
</tr>
<tr>
<td><strong>Development and Support</strong></td>
<td>Development of ideas and support for claims deepen insight and broaden context. An integrated line of skilful reasoning and illustration effectively conveys the significance of the argument. Qualifications and complications enrich and bolster ideas and analysis.</td>
<td>The response exhibits a productive organizational strategy. The response is mostly unified by a controlling idea or purpose, and a logical sequencing of ideas contributes to the effectiveness of the argument. Transitions between and within paragraphs consistently clarify the relationships among ideas.</td>
</tr>
<tr>
<td><strong>Organization</strong></td>
<td>The response exhibits a mostly unified, productive organizational strategy. The overall shape of the response reflects an emergent controlling idea or purpose. Ideas are logically grouped and sequenced. Transitions between and within paragraphs clarify the relationships among ideas.</td>
<td>The response exhibits a clear organizational strategy. The overall shape of the response reflects an emergent controlling idea or purpose. Ideas are logically grouped and sequenced. Transitions between and within paragraphs clarify the relationships among ideas.</td>
</tr>
<tr>
<td><strong>Language Use</strong></td>
<td>The writer’s use of language is basic and somewhat unclear. Word choice is general and occasionally imprecise. Sentence structures are usually clear but show little variety. Stylistic and register choices, including voice and tone, are not always appropriate for the rhetorical purpose. Distracting errors in grammar, usage, and mechanics may be present, but they generally do not impede understanding.</td>
<td>The use of language is skillful and precise. Sentence structures are consistently varied and clear. Stylistic and register choices, including voice and tone, are strategic and effective. While a few minor errors in grammar, usage, and mechanics may be present, they do not impede understanding.</td>
</tr>
</tbody>
</table>

You can find the most current information on scoring the ACT writing test in the bonus online content.
### The ACT Writing Test Scoring Rubric

<table>
<thead>
<tr>
<th>Score 2: Responses at this scorepoint demonstrate weak or inconsistent skill in writing an argumentative essay.</th>
<th>Ideas and Analysis</th>
<th>Development and Support</th>
<th>Organization</th>
<th>Language Use</th>
</tr>
</thead>
<tbody>
<tr>
<td>The writer generates an argument that weakly responds to multiple perspectives on the given issue. The argument’s thesis, if evident, reflects little clarity in thought and purpose. Attempts at analysis are incomplete, largely irrelevant, or consist primarily of restatement of the issue and its perspectives.</td>
<td>Development of ideas and support for claims are weak, confused, or disjointed. Reasoning and illustration are inadequate, illogical, or circular, and fail to fully clarify the argument.</td>
<td>The response exhibits a rudimentary organizational structure. Grouping of ideas is inconsistent and often unclear. Transitions between and within paragraphs are misleading or poorly formed.</td>
<td>The use of language is inconsistent and often unclear. Word choice is rudimentary and frequently imprecise. Sentence structures are sometimes unclear. Stylistic and register choices, including voice and tone, are inconsistent and are not always appropriate for the rhetorical purpose. Distracting errors in grammar, usage, and mechanics are present, and they sometimes impede understanding.</td>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>Score 1: Responses at this scorepoint demonstrate little or no skill in writing an argumentative essay.</th>
<th>Ideas and Analysis</th>
<th>Development and Support</th>
<th>Organization</th>
<th>Language Use</th>
</tr>
</thead>
<tbody>
<tr>
<td>The writer fails to generate an argument that responds intelligibly to the task. The writer’s intentions are difficult to discern. Attempts at analysis are unclear or irrelevant.</td>
<td>Ideas lack development, and claims lack support. Reasoning and illustration are unclear, incoherent, or largely absent.</td>
<td>The response does not exhibit an organizational structure. There is little grouping of ideas. When present, transitional devices fail to connect ideas.</td>
<td>The use of language fails to demonstrate skill in responding to the task. Word choice is imprecise and often difficult to comprehend. Sentence structures are often unclear. Stylistic and register choices are difficult to identify. Errors in grammar, usage, and mechanics are pervasive and often impede understanding.</td>
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</tbody>
</table>

**STEP 2.** Because your writing test domain scores are the sum of two readers’ ratings of your essay, multiply your own 1–6 rating from step 1 by 2. Or, have both you and someone else read and score your practice essay and add those ratings together. In either case, record the total in the blank in step 3.

**STEP 3.** Enter your writing test domain scores in the following box.

<table>
<thead>
<tr>
<th>Domain Score</th>
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<tbody>
<tr>
<td>Ideas and Analysis</td>
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<td>___________</td>
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<td>Development and Support</td>
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<tr>
<td>Language Use and Conventions</td>
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</tbody>
</table>

**STEP 4.** Enter the sum of the second-column scores here _______. This is your raw score (value between 8 and 48).

You can find the most current information on scoring the ACT writing test in the bonus online content.
**STEP 5.** Use the following table to find the scaled writing subject score that corresponds to your raw score.

## Scale Score Conversion Table: Writing Practice Test 1

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<th>Scale Score</th>
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</table>

**STEP 6.** Use the table on page 112 to determine your estimated percentile rank (percent at or below) for your writing test subscore. Circle your writing test subscore, this time using the column headed “Writing.” As you mark your percentile ranks, enter them in the blanks provided in the following table. You may also find it helpful to compare your performance with the national mean (average) score of the writing test subscore as shown at the bottom of the table on page 112.

You can find the most current information on scoring the ACT writing test in the bonus online content.
### National Distributions of Cumulative Percents for ACT
**STEM, ELA and Writing Test Scores beginning September 2015**

<table>
<thead>
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**Mean**  
21.1 | 19.4 | 17.2  
**S.D.**  
5.1  | 5.4  | 6.6  

Note: These national norms are the source of U.S. Ranks, for the STEM and ELA scores and for the writing test displayed on ACT reports for students who test beginning September 2015.

STEM norms with a sample size of 5,569,466, is based on 2013, 2014 and 2015 graduates.

ELA and writing norms are initially based on one special study.

Starting in September 2015, ACT has introduced enhancements to the ACT writing test. Key differences between the former and the enhanced designs can be found at:  
http://www.actstudent.org/writing/enhancements/

You can find the most current information on scoring the ACT writing test in the bonus online content.
Reviewing Explanatory Answers

After scoring your test, review the questions and answers to gain a better understanding of why each correct answer is correct and why the other choices for each question are wrong. We encourage you to review the explanatory answers for all questions, not just those you missed. As you read through the explanations, note any subject matter or concepts you don’t fully understand, such as subject-verb agreement on the English test or how to calculate the volume of three-dimensional objects on the mathematics test.

The following sections give the correct answers for each question along with an explanation of why each correct answer is correct, why each of the other choices is wrong, and (in some cases) insight into why certain wrong answers may have been tempting choices. For more guidance on how to identify subject areas or skills you may need to work on, turn to chapter 4.
Passage I

**Question 1. The best answer is C** because a comma is appropriate between the noun 1972 and the dependent, relative clause that begins with the word *when*.

**The best answer is NOT:**

A because the comma incorrectly separates the adverbial phrase “since 1972” from the main clause and the verb phrase it modifies, “has been studying.”

B because the phrase “since 1972” is essential to the meaning of the main clause (restrictive). Setting the phrase off with commas indicates the phrase is nonrestrictive, resulting in an ungrammatical sentence.

D because the context of the sentence requires the word *elephants* in the main clause to be plural and non-possessive, not plural possessive.

**Question 2. The best answer is F** because the choice correctly forms the adjective *now-famous* to modify “Amboseli National Park,” the compound noun that follows.

**The best answer is NOT:**

G because it incorrectly uses the adverb of time *then* rather than the conjunction *than* (used when making comparisons).

H because it incorrectly uses the adverb form *famously* to modify the noun that follows rather than the appropriate adjective form *famous*.

J because it incorrectly uses the adverb form *famously* to modify the noun that follows rather than the appropriate adjective form *famous*. 
Question 3. The best answer is B because the parenthetical information about the various threats to elephants’ survival interrupts the main clause and needs to be set off with appropriate punctuation (commas, parentheses, or em dashes). The parenthetical is introduced with an em dash, and therefore the parenthetical must end with an em dash.

The best answer is NOT:

A because the lack of punctuation creates a run-on sentence and does not appropriately set off the parenthetical information in the middle of the main clause.

C because a colon has to have an independent clause preceding it, and what comes before this colon is not a complete thought. The colon also incorrectly implies that what follows the colon defines what comes before it.

D because the parenthetical information about the various threats to elephants’ survival appears in the middle of the main clause and therefore needs to be set off with appropriate punctuation. The parenthetical is introduced with an em dash, so what follows the parenthetical must also be an em dash. This choice incorrectly uses a comma instead of a dash.

Question 4. The best answer is J because the preceding sentence mentions “human encroachment” as a threat to elephants, and inserting this sentence would add redundant information to the essay.

The best answer is NOT:

F because inserting this sentence would add redundant information, and the essay does not specify what factor determined Moss's interest in working with elephants.

G because inserting this sentence would add redundant information, and the focus of the rest of the essay is on elephants and learned behavior, not on the specific threat of humans to elephants.

H because the essay does mention the presence of humans in the lives of elephants in terms of the threat of humans to elephants' survival and in terms of Moss's study of elephants.

Question 5. The best answer is B because no punctuation is needed. The absence of punctuation creates a grammatical, clear, and understandable sentence.

The best answer is NOT:

A because the comma between the words intensive and field incorrectly separates the adjective from the noun it modifies. Furthermore, the comma between the words field and studies separates the two parts of the compound noun “field studies.”

C because the comma following the word studies incorrectly separates the subject of the main clause from its verb.

D because the comma between the words intensive and field incorrectly separates the adjective from the noun it modifies.
Question 6. The best answer is **G** because the phrase “for instance” offers the most logical transition from the claim about elephants and learned behavior at the end of the preceding paragraph to a specific example of learned behavior in elephants in this paragraph.

The best answer is **NOT**:

**F** because the word *however* indicates that the ideas in this paragraph will contrast with those from the preceding paragraph, which is not the case. Therefore, *however* does not offer a logical transition from the claim about elephants and learned behavior in the preceding paragraph to the example of learned behavior in elephants provided in this paragraph.

**H** because the phrase “as always” does not offer a logical transition from the claim about elephants and learned behavior in the preceding paragraph to an example of learned behavior in elephants in this paragraph.

**J** because the phrase “by now” does not offer a logical transition from the claim about elephants and learned behavior in the preceding paragraph to an example of learned behavior in elephants in this paragraph.

Question 7. The best answer is **C** because the gerund phrase “and sipping” maintains parallelism with the gerund *kneeling*, avoiding faulty and potentially confusing constructions within the prepositional phrase that begins with “by kneeling.”

The best answer is **NOT**:

**A** because the phrase “and it sipped” is not parallel with the gerund *kneeling*, resulting in a faulty construction. This phrase would also require a comma before the word *and*, as it would end the sentence with an independent clause.

**B** because the phrase “which it sips” incorrectly implies that the elephant is sipping the water’s edge rather than the water itself. The *which* phrase would also require a comma to precede it in order to be grammatically correct.

**D** because the phrase “that sips” is not parallel with the gerund *kneeling*. The phrase “that sips” also incorrectly implies that the water’s edge is sipping (a misplaced modifier).
**Question 8.** The best answer is G because the prepositional phrase that starts with “of pulling water” contains a compound object: “pulling and releasing.” The phrase “trunk and then” correctly joins the two objects with a conjunction and most clearly describes the elephant’s habit.

**The best answer is not:**

F because placing a period after the word *trunk* separates the compound object of the preposition and creates two sentence fragments.

H because the phrase “trunk then by” does not correctly join the compound object of the preposition and does not clearly explain the elephant’s habit.

J because the word *trunk* does not correctly join the compound object of the preposition and creates a run-on sentence.

**Question 9.** The best answer is C because “of witnessing” creates a prepositional phrase that most clearly and logically describes what the elephant has been doing for months.

**The best answer is not:**

A because the phrase “as if witnessing” results in a faulty construction and implies that the elephant’s observation was theoretical rather than actual.

B because the phrase “when witnessing” results in a faulty construction, and the combination of the adverbs *after* and *when* does not clearly explain what the elephant has spent months doing.

D because the phrase “then witness” results in a faulty construction and does not clearly describe what the elephant has spent months doing.

**Question 10.** The best answer is G because the phrase “in this regard” adds a prepositional phrase that creates a clear and complete sentence.

**The best answer is not:**

F because the phrase “in which this regard” is unnecessarily wordy, unclear, and creates a sentence fragment.

H because the referent for the phrase “ones that” is unclear, and its use creates a sentence fragment.

J because the word *which* creates a sentence fragment.
Question 11. The best answer is B because the phrase “a baby male” is the only choice that adds new and relevant information to the sentence.

The best answer is NOT:

A because the idea that Moss named the elephants in her observations is implicit in this paragraph and is not relevant to the focus of the sentence on the age of the elephants.

C because the phrase “an elephant” adds redundant information to the paragraph.

D because the phrase “the third” adds redundant information to the paragraph.

Question 12. The best answer is F because the phrase “he also grew” avoids an unnecessary tense shift within the sentence.

The best answer is NOT:

G because the phrase “he also will have grown” unnecessarily shifts the verb tense from simple past tense (overcame) to future perfect tense.

H because the phrase “he also had grown” unnecessarily shifts the verb tense from simple past tense (overcame) to past perfect tense.

J because the phrase “also growing” creates a sentence fragment and is not clearly connected to the main, independent clause.

Question 13. The best answer is D because this placement makes it clear why Echo needed to take special care of Ely and why Ely might signal distress.

The best answer is NOT:

A because this placement does not logically connect to the idea in the preceding sentence that Ely overcame his limitations. This placement also introduces a new idea at the end of a paragraph.

B because Ely has not yet been introduced in the paragraph, so placing the information about his deformed feet at the beginning of the paragraph does not make sense.

C because Ely is not introduced until sentence 4, so placing the information about his deformed feet before sentence 4 does not make sense.
Question 14. The best answer is J because all that is needed to complete the main clause of the sentence and make its meaning clear is the preposition to (connecting the phrase “an ever-expanding audience”).

The best answer is NOT:

F because this choice adds an unnecessary verb phrase “is provided,” which makes the structure of the sentence faulty and its meaning unclear.

G because this choice adds the unnecessary phrase “is given by her to,” which makes the structure of the sentence faulty and its meaning unclear.

H because this choice adds an unnecessary verb phrase “is reaching,” which makes the structure of the sentence faulty and its meaning unclear.

Question 15. The best answer is B because the essay does focus on Moss’s observations of specific learned behavior in elephants in Kenya.

The best answer is NOT:

A because the essay focuses on Moss’s observations of elephant behavior and not elephants’ ability to identify various family members.

C because the essay focuses on Moss’s observations of elephant behavior and not on how elephants have evolved differently throughout Africa.

D because the essay focuses on Moss’s observations of behavior in elephants in Kenya and not on elephants in zoos around the world.

Passage II

Question 16. The best answer is J because the phrase “Remnants of outdoor advertisements from a bygone era” functions as an appositive, providing more information about the compound noun “ghost signs.” This is an acceptable, grammatical inversion of the construction “They are called ‘ghost signs,’ remnants of outdoor advertisements from a bygone era.”

The best answer is NOT:

F because the phrase “Seeing remnants” is a misplaced modifier that incorrectly implies they (the ghost signs) are seeing remnants.

G because the phrase “The sight of remnants” is a misplaced modifier that incorrectly implies that ghost signs are the “sight of remnants,” not the remnants themselves.

H because the phrase “To see remnants” is a misplaced modifier that incorrectly implies that ghost signs are “to see remnants.”
Question 17. The best answer is A because the phrase “bygone era” in the sentence is sufficient to express the idea that ghost signs are remnants of outdoor advertisements from an earlier time.

The best answer is NOT:

B because the phrase “era that is no more” is redundant.
C because the phrase “era of another time” is redundant.
D because the phrase “era of times past” is redundant.

Question 18. The best answer is G because the examples of words found on ghost signs interrupts the main clause and must be set off by appropriate punctuation (commas, parentheses, or em dashes). This parenthetical information ends with an em dash and, therefore, must be introduced with an em dash as well.

The best answer is NOT:

F because the lack of punctuation creates a run-on sentence that does not appropriately set off the parenthetical examples.
H because the comma after remain does not appropriately set off the parenthetical examples (an em dash is required).
J because the colon after remain does not appropriately set off the parenthetical examples (an em dash is required).

Question 19. The best answer is B because the relative pronoun that is required to logically and grammatically link the clause that follows to the rest of the sentence.

The best answer is NOT:

A because the word should results in an illogical, faulty connection between the sentence's clauses.
C because adding the word they makes the final clause independent, resulting in a run-on sentence.
D because the phrase “should they” results in an illogical, faulty connection between the sentence's clauses.
Question 20. The best answer is F because no punctuation is necessary in order to connect compound direct object “products and businesses” to the rest of the sentence.

The best answer is NOT:

G because the comma following “products and businesses” incorrectly separates the main clause from the restrictive relative clause “that no longer exist.”

H because the comma following the word products separates the two objects in the compound direct object “products and businesses.”

J because the colon incorrectly implies that “businesses that no longer exist” is a definition of products.

Question 21. The best answer is B because the word instead is an interrupting aside that needs to be set off by commas. A comma also needs to come before the word with to separate the entire prepositional phrase “with, instead, their simple claims of complex colors” from the main clause.

The best answer is NOT:

A because the word instead is an interrupting aside that needs to be set off by commas, and this choice does not provide a comma directly before the word instead.

C because the word instead is an interrupting aside and needs to be set off by commas, and this choice does not provide a comma directly before the word instead. This choice also lacks a comma directly before the word with; this comma is required in order to correctly connect the prepositional phrase to the rest of the sentence.

D because both the word instead and the prepositional phrase that begins with the word with need to be set off by commas. This choice does not contain any punctuation.
**Question 22.** The best answer is H because this sentence is the most logical and grammatical choice, making it clear that the narrator started her collection one October as she was driving home from school.

The best answer is NOT:

F because this choice removes the subject I from the sentence, creating a misplaced modifier in which the participle phrase “Driving home from school one chilly October evening” modifies the noun phrase “my collection.”

G because this choice removes the subject I from the sentence, creating a dangling modifier in which the participle phrase “Driving home from school one chilly October evening” has no clear noun to modify. Therefore, it is possible to read this as the “beginning of my collection” was driving home.

J because the structure of this sentence is confusing and creates a misplaced modifier in which the participle phrase “driving home from school one chilly October evening” modifies “the start of my collection.” Furthermore, the clause “The start of my collection came to me” is unclear and implies that the collection was moving by itself.

**Question 23.** The best answer is D because the idea that the ad for Joe's Café was disappearing echoes the point the narrator made earlier in the essay that ghost signs are barely legible, faded, and pale.

The best answer is NOT:

A because the idea that the ad for Joe's Café was upright does not echo a point made earlier in the essay.

B because the idea that the narrator was not interested in the ad for Joe's Café is not supported by the rest of the essay (the narrator “collects” ghosts signs as a hobby).

C because the idea that the ad for Joe's Café might have been made of wood does not echo a point made earlier in the essay.
Question 24. The best answer is J because the phrase “setting sun illuminated” creates a logical and grammatical sentence.

The best answer is NOT:

F because the lack of a verb in the phrase “setting sun’s illumination of” results in an incomplete, illogical sentence.

G because the lack of a verb in the phrase “illuminating setting sun on” results in an incomplete, illogical sentence.

H because this choice creates a sentence that says “the sun illuminated the set on the yellowing plastic,” which is illogical.

Question 25. The best answer is B because “evidence of” is the correct, idiomatic phrase needed in order to make this sentence most understandable (“evidence of vandalism or of a hailstorm”).

The best answer is NOT:

A because the phrase “a clue to vandalism” is not idiomatic, and the preposition to is not parallel with the preposition of in “of a hailstorm.”

C because the adverb evidently results in a faulty construction when combined with the prepositional phrase “of a hailstorm.”

D because deleting the underlined portion leaves a structurally flawed, illogical sentence that reads “Maybe it was the small hole, vandalism or of a hailstorm.”

Question 26. The best answer is J because no transitional word or phrase is necessary in order to connect this sentence to the ideas in the rest of the paragraph.

The best answer is NOT:

F because the transitional word Instead implies that a contrast is being set up in this sentence. Rather, the sentence is building on the idea presented in the preceding sentence.

G because the transitional phrase “On the other hand” implies that a contrast is being set up in this sentence; instead, the sentence is building on the idea presented in the preceding sentence.

H because the transitional word Meanwhile incorrectly implies that the idea in this sentence is not directly connected to the idea presented in the preceding sentence.
Question 27. The best answer is D because given the context of the sentence, the adjective solo is the most logical and precise word to modify the noun trips.

The best answer is NOT:
A because the phrase “solitude trips” does not make sense given the context.
B because using the adverb solitarily to modify the noun trips is not logical or grammatical.
C because the phrase “solitaire trips” doesn’t make sense given the context.

Question 28. The best answer is H because the phrase “like the signs” is a nonrestrictive phrase in which the narrator compares herself to the signs. Setting off the phrase with commas prevents ambiguity when reading the sentence.

The best answer is NOT:
F because omitting the comma between the words I and like creates ambiguity and reads as though the narrator is about to describe something she likes, rather than setting up a comparison. The comma following the word signs also creates the fragment “am alone” at the end of the sentence.
G because setting off only the word like with commas creates a nonrestrictive element. If the word like were removed, the sentence would read “I the signs am alone,” indicating that like is essential to the meaning of the phrase and should not be set off by commas.
J because setting off only the words “the signs” with commas creates a nonrestrictive element. If the words “the signs” were removed, the sentence would read “I like am alone,” indicating that “the signs” is essential to the meaning of the entire phrase and should not be set off by commas.

Question 29. The best answer is A because the paragraph’s current placement makes the most logical sense within the narrative. The narrator first introduces signs, describes generally how her collection began, describes the specific instance that first drew her to ghost signs, and then concludes the essay by describing her hunts generally.

The best answer is NOT:
B because paragraph 1 is the best and clearest introduction of ghost signs. Describing how the narrator began collecting ghost signs (paragraph 2) before describing what they actually are does not make logical sense.
C because no logical transition exists between paragraph 1 and paragraph 3 if paragraph 2 were to be moved after paragraph 3. It also doesn’t make sense for the narrator to describe taking pictures of the ad for Joe’s Café in paragraph 3 before she introduces the idea that she uses photography to “collect” ghost signs.
D because paragraph 2 would not serve as a logical conclusion to the essay; it introduces the main focus of the essay.
Question 30. The best answer is F because the essay describes the narrator's hobby of photographing ghost signs and how her hobby got started after she saw the sign for Joe's Café.

The best answer is not:
G because the essay does not indicate that the narrator learned her hobby from a friend.
H because although the essay does use the terms lonely and forlorn to describe a particular sign, her description of her hobby is positive.
J because the essay describes only one hobby: collecting ghost signs in photographs.

Passage III

Question 31. The best answer is B because “a series of semitropical islands off the southeast coast of the United States” is an appositive phrase that further describes the Bahamas. This phrase is nonrestrictive and must be set off by commas. The verb are is also needed to avoid a sentence fragment.

The best answer is not:
A because the word which in this choice creates a sentence fragment. If the appositive (“a series of semitropical islands off the southeast coast of the United States”) were removed, the sentence would read “The Bahamas, which are home to some of the most unusual geological formations in the world: underwater caves known as blue holes.”
C because this choice removes the comma between the words States and are, which does not correctly set off the appositive from the main clause of the sentence.
D because this choice removes the verb are from the main clause, creating a sentence fragment.
Question 32. The best answer is F because this paragraph focuses on the formation of the caves, and this choice most logically introduces the topic by introducing a critical component of the formation: calcium carbonate. This choice is the only one to give us two pieces of essential information: that the Bahamas were formed from calcium carbonate and that calcium carbonate is a component of seawater.

The best answer is NOT:

G because the description of calcium carbonate is too general and is not specifically tied to the formation of the caves, which is the topic of the paragraph. Furthermore, the phrase “also found in seawater” does not connect to the preceding paragraph, since there is no mention of other components of seawater.

H because the idea that much of the land making up the Bahamas is still underwater is not immediately relevant to the topic of this paragraph, which is how the caves formed.

J because the idea that most types of limestone contain calcium carbonate is only loosely related to the focus of the paragraph and does not introduce the topic of cave formation.

Question 33. The best answer is A because the simple past tense built is consistent with the verb tense in the rest of the paragraph.

The best answer is NOT:

B because “are building” shifts the verb tense to present progressive tense, which is inconsistent with the verb tense in the rest of the paragraph.

C because “will build” shifts the verb tense to future tense, which is inconsistent with the verb tense in the rest of the paragraph.

D because build shifts the verb tense to simple present tense, which is inconsistent with the verb tense in the rest of the paragraph.

Question 34. The best answer is F because this choice presents the clearest, most concise, and most idiomatic way to say that the rainwater was buoyed by the seawater below.

The best answer is NOT:

G because this choice is unnecessarily wordy and illogical (it is not idiomatic to state that the rainwater was being buoyed because of the denser seawater below; the limestone was buoyed by the seawater).

H because the introduction of the pronoun-verb combination “it being” creates a sentence that is unnecessarily wordy and awkwardly constructed.

J because switching to the passive construction here is not only awkward but also results in an illogical sentence (the rainwater, trapped just below sea level, could not have buoyed the denser seawater below).
**Question 35.** The best answer is D because the word *either* in the sentence indicates that the brackish water is being compared to two things at the same time: rainwater and seawater. The omission of punctuation is appropriate and indicates that these two nouns are parallel elements in the construction “either rainwater or seawater.”

The best answer is NOT:

A because setting off the phrase “or seawater” with dashes separates the parallel elements (rainwater or seawater). Without further explanation, this separation is unnecessary and illogical.

B because setting off the phrase “or seawater” with commas separates the parallel elements (rainwater or seawater) and also incorrectly implies that seawater is acting as an appositive for rainwater.

C because placing a comma after rainwater incorrectly separates the parallel elements (rainwater or seawater).

**Question 36.** The best answer is H because the introductory adverb clause “As the limestone eroded” must be separated from the main clause (“caves formed”) by a comma.

The best answer is NOT:

F because the introductory adverb clause “As the limestone eroded” must be followed by a comma; the omission of punctuation creates ambiguity and results in a run-on sentence.

G because inserting a comma after the word *limestone* interrupts the introductory adverb clause “As the limestone eroded” and creates an incomplete thought. Moreover, *eroded* incorrectly refers to caves instead of limestone.

J because inserting a comma after the word *caves* incorrectly implies that the limestone eroded the caves and makes the meaning of the sentence ambiguous. The comma also leaves the verb *formed* without a subject.

**Question 37.** The best answer is B because this choice provides the most specific indication of time. Both “ice ages” and “temperate eras” speak to large swaths of time and indicate that a great deal of time passed during the cave-formation process.

The best answer is NOT:

A because “time periods in which the weather changed drastically” is vague and does not indicate a specific length of time. Weather can change drastically over short periods of time; therefore, “time periods” does not do enough to illustrate a specific length of time.

C because this choice is not as specific as B; “extended time” could be interpreted differently by different readers.

D because “As time passed” does not indicate a specific length of time.
**Question 38.** The best answer is J because the phrase “repeat at different depths” is the clearest and most concise choice in this context.

The best answer is NOT:

F because this choice is unnecessarily wordy and redundant. The preceding sentence already tells us that sea levels rose and fell by 100s of feet; “process to be a process” is also redundant.

G because “repeat again and again” and “various different” are both redundant.

H because “different depths that varied” is unnecessarily wordy and redundant.

**Question 39.** The best answer is C because the semicolon correctly separates the two independent clauses.

The best answer is NOT:

A because omitting punctuation between these two independent clauses creates a run-on sentence.

B because *that* doesn’t make sense in context and creates a run-on sentence.

D because inserting a comma after the word *caves,* without adding a coordinating conjunction, creates a comma splice.

**Question 40.** The best answer is H because the specific information about Dean’s Blue Hole as a popular cave-diving destination is not related to the focus of the paragraph, which is on cave formation in general.

The best answer is NOT:

F because the information about Dean’s Blue Hole is only tangentially related to the preceding sentence.

G because the sentence does not provide enough information about Dean’s Blue Hole to help the reader visualize this particular underwater cave. Even if the sentence did provide sufficient description, this information wouldn’t be relevant because it is not related to the paragraph’s focus on cave formation.

J because the sentence should not be added because the information about Dean’s Blue Hole isn’t related to the paragraph’s focus on cave formation, not because the sentence doesn’t provide an adequate description of Dean’s Blue Hole.
**Question 41.** The best answer is **B** because the noun *water* must be modified by the adjective *darker*, and the adjective *darker* should be modified by the adverb *strikingly*. This is the only choice that uses the correct adjective and adverb forms of these words.

The best answer is NOT:

**A** because the sentence is setting up a comparison between the appearance of the water of the blue hole and the water surrounding it; given this context, the correct adverb form to modify *darker* is *strikingly*.

**C** because the noun *water* must be modified by an adjective; this choice incorrectly modifies *water* with the adverb *darkly*.

**D** because the sentence sets up a comparison between the appearance of the water of the blue hole and the water surrounding it; therefore, the verb *striking* doesn’t make sense here. Furthermore, the noun *water* must be modified by an adjective; this choice incorrectly modifies *water* with the adverb *darkly*.

**Question 42.** The best answer is **J** because the pronoun *it* is appropriate given the context and agrees in number with its antecedent “a circular patch of water.”

The best answer is NOT:

**F** because the pronoun *them* does not agree in number with its singular antecedent “blue hole.”

**G** because the pronoun *these* does not agree in number with its singular antecedent “blue hole.”

**H** because the pronoun *one* is a confusing pronoun choice for the antecedent “a circular patch of water.” *One* implies that the focus is on a particular circular patch of water, whereas the sentence is describing a feature of blue holes in general.

**Question 43.** The best answer is **C** because the sentence presents a list of three findings of divers, the first of which is “remains of turtles and alligators now extinct on the island.”

The best answer is NOT:

**A** because adding a period between *alligators* and *Now* creates a sentence fragment and interrupts the list of the findings of divers.

**B** because adding a period between *now* and *Extinct* creates a sentence fragment and interrupts the list of the findings of divers.

**D** because adding a period between *extinct* and *On* creates a sentence fragment and interrupts the list of the findings of divers.
Question 44. The best answer is G because the essay tells us that the telltale sign of a blue hole is a “circular patch of water.” The word *dot* (a small round mark) indicates the circular shape of the blue holes and is the only choice that suggests a shape.

The best answer is **not**:

F because the phrase “can be sighted off” does not indicate shape in any way.

H because the phrase “darken parts of” speaks to color, not shape.

J because the phrase “appear in” does not indicate shape.

Question 45. The best answer is C because this placement most logically connects “these depths” in the added sentence to the first two sentences of paragraph 4 in which the depths of the water are described. The information about the well-preserved fossils and rock formations also helps introduce other discoveries made by divers in the caves.

The best answer is **not**:

A because the depths and exploration of the blue holes have not yet been introduced in paragraph 1, making this placement of the added sentence illogical.

B because this placement interrupts the description of cave formation in paragraph 2.

D because the added sentence does not logically introduce paragraph 5, which describes unexplored caves more generally. Moreover, the information about fossils and rock formations being well preserved should come before the list of examples in the previous sentence.

Passage IV

Question 46. The best answer is J because the phrase “defensive walls” is itself sufficient to express the original purpose of the ancient walls.

The best answer is **not**:

F because the word *protectively* is not needed here. The sentence’s idea—that the walls were defensive—would be clear simply with “walls intended to defend.”

G because the phrase “defensive walls for defending the city” is also redundant. Either “defensive walls” or “for defending the city” would be appropriate, not both.

H because the phrase “walls to provide defensive protection” is unnecessarily wordy; “defensive protection” is somewhat redundant.
Question 47. The best answer is C because the introductory adverb clause that starts with *Although* must be followed by a comma, and this choice correctly places a comma following the word *tall*.

**The best answer is NOT:**

A because the introductory adverb clause that starts with *Although* must be followed by a comma, and the omission of punctuation between *tall* and *they* creates a run-on sentence.

B because adding a period between *tall* and *They* creates a sentence fragment ("Although both were built as defensive walls and stood ten meters tall.").

D because a semicolon is used to separate two independent clauses, and placing a semicolon here would split a dependent clause ("Although both were built as defensive walls and stood ten meters tall") and an independent clause ("they were erected under different historical circumstances").

Question 48. The best answer is F because the word *It's* is correctly used in its contraction form to create a sentence that begins “It is thought that . . .”

**The best answer is NOT:**

G because this choice offers the possessive pronoun *its* rather than the contraction *it's*.

H because this choice also attempts a possessive pronoun. The use of the pronoun is incorrect, as is the placement of the apostrophe.

J because this choice places the possessive pronoun *its* into the sentence rather than the contraction *it's*.

Question 49. The best answer is A because the comma following “Aurelian Wall” correctly sets off the nonrestrictive appositive phrase “built in the late third century CE by the Roman Emperor Aurelian,” which further describes the Aurelian Wall.

**The best answer is NOT:**

B because adding the verb phrase “had been” creates a sentence with two predicates. In order to be grammatically correct, the sentence would have to read “the Aurelian Wall had been built in the late third century CE and was much sturdier than the older wall.”

C because the word *which* is unnecessary before the appositive “built in the late third century CE by the Roman Emperor Aurelian” and separates the appositive from its noun.

D because adding the verb *was* creates a sentence with two predicates and results in a run-on.
Question 50. The best answer is G because the phrase “much sturdier than” uses the correct comparative adjective much and the correct use of the subordinating conjunction than to compare the Aurelian Wall with the older wall.

The best answer is NOT:
F because the phrase “more sturdier” is an incorrect use of the comparative adjective more in combination with sturdier.

H because the phrase “more sturdier” is an incorrect use of the comparative adjective more in combination with sturdier. Furthermore, the subordinating conjunction than must be used to set up the comparison in the sentence, not the adverb then.

J because the subordinating conjunction than must be used to set up the comparison in the sentence, not the adverb then.

Question 51. The best answer is B because the meaning of the phrase “greatly expanded” is most clear in this case when it is placed directly before the noun it modifies: “city of Rome.” When we read “surrounded the greatly expanded city of Rome,” it is obvious that Rome itself, rather than the wall or the river, had expanded.

The best answer is NOT:
A because this placement of “greatly expanded” results in an unclear sentence; no noun directly precedes or follows the phrase. It sounds as if the wall itself has expanded, which doesn’t make sense.

C because the phrase “greatly expanded” does not make sense grammatically or logically when it follows directly after the noun Rome.

D because this placement of the phrase “greatly expanded” incorrectly indicates that it was the Tiber’s west bank that was greatly expanded, not the city of Rome.

Question 52. The best answer is J because no transition is needed between these two sentences, both of which describe the physical features of the Aurelian Wall.

The best answer is NOT:
F because the transitional phrase “in other words” implies that the ideas presented in this sentence are a restatement of the ideas in the preceding sentence, which isn’t the case.

G because Therefore implies a cause-effect relationship between this sentence and the preceding sentence, and there is no obvious cause-effect here.

H because Instead implies that a contrast is being made between this sentence and the preceding sentence, and there is no contrast being made between the physical features of the wall.
Question 53. The best answer is A because no punctuation is necessary within the phrase “Both the posterns and the towers.” The conjunction both at the beginning of the phrase indicates that the two things that follow equally served as defensive positions.

The best answer is not:

B because putting commas around the phrase “the posterns and the towers” incorrectly separates the conjunction both from the two nouns that follow. Placing commas around the phrase also signals that the phrase is nonrestrictive; in fact, the information is essential to understanding the sentence.

C because placing a comma after posterns incorrectly separates the two parallel nouns (“the posterns and the towers”).

D because placing a comma after the word towers incorrectly separates the subject of the sentence (“the posterns and towers”) from the verb (served).

Question 54. The best answer is G because this is the only choice that specifically indicates how the posterns and towers were used as defensive positions. They provided cover during an enemy attack.

The best answer is not:

F because the phrase “for protecting Rome” does not add any new information to the sentence, nor does it provide specific information about how the posterns and towers served as defensive positions.

H because the phrase does not add any new information about how the posterns and towers served as defensive positions; “to help Rome repel against enemy attacks” stops short of providing specific information. How did they help repel enemy attacks? That information can be found in G.

J because “by keeping Rome safe from invaders” does not add specific information about how the posterns and towers actually kept Rome safe from invaders. Again, see G.
**Question 55. The best answer is B** because the information about the Aurelian Wall continuing to dominate the Roman landscape most logically introduces the focus of paragraph 5 on what remains of the walls today. It also creates the best contrast between the well-preserved Aurelian Wall and the scant remains of the Servian Wall, a contrast demanded by the word *however*.

**The best answer is NOT:**

A because the information about the materials Romans used to build the Aurelian Wall does not logically introduce the focus of paragraph 5, which is on what remains of the walls today, and there is no clear connection between this information and the *however* in the next sentence.

C because there is no logical connection between the information about Emperor Aurelian and the information that follows in the paragraph.

D because the information about mounds of earth serving as protection prior to the construction of the walls is unrelated to the main focus of the essay and does not logically introduce the focus of paragraph 5, which is on what remains of the walls today.

**Question 56. The best answer is J** because the plural verb *remain* agrees in number with its plural subject *portions*. (The verb must agree with *portions*, not with *wall*.)

**The best answer is NOT:**

F because the singular verb *remains* does not agree in number with the plural subject *portions*.

G because the verb phrase “were remaining” shifts the verb tense in the sentence and is inconsistent with the verb tense in the rest of the paragraph.

H because the singular verb phrase “has remained” does not agree in number with the plural subject *portions*.

**Question 57. The best answer is C** because the information about architectural features of the Aurelian Wall is out of place and is unrelated to the discussion of the Servian Wall in the present day.

**The best answer is NOT:**

A because at this point the paragraph’s focus is on the Servian Wall in the present day; this sentence is neither related nor does it support the main idea.

B because the innovations and practicality of Roman engineers is irrelevant to the focus of the paragraph on the Servian Wall in the present day.

D because the level of detail is irrelevant; the sentence should not be added because it provides details that are unrelated to the topic at this point in the paragraph. Moreover, the level of detail itself is actually consistent with the level of detail in the rest of the essay.
Question 58. The best answer is **A** because “the future” provides the clearest and most concise description of the capital.

The best answer is **NOT**:

- **B** because “what was yet to be appointed to the designation of” is unnecessarily wordy and somewhat unclear.
- **C** because “what would in reality become the” is unnecessarily wordy; there is no reason to stress *reality* here at all.
- **D** because “a would-be but not yet” is exceedingly awkward phrasing. A clearer way to express the idea of “future” is simply to say “the future.”

Question 59. The best answer is **C** because the preservation of the remnants of the Servian Wall in a location that is commonplace and average, such as a fast-food restaurant, can be considered ironic given the prestige and distinction originally associated with the wall and the city in which it resided. Moreover, the idea of a centuries-old wall being preserved in a fast-food restaurant—where food is designed to be served and eaten quickly and which are often temporary themselves—might also be considered ironic.

The best answer is **NOT**:

- **A** because the detail that the importance of the wall is recognized by archaeologists simply builds on the idea about the prestige of the wall and Rome in the first part of the sentence. No irony is created with this choice.
- **B** because this idea builds on the idea about the prestige of the wall and Rome in the first part of the sentence. It makes sense that a wall that once protected the future capital of one of the ancient world’s most famous empires would be preserved as an important relic, and therefore no irony is created with this choice.
- **D** because “such varied locations” is vague in comparison to **C**, and the essay only provides one location before this point. Any resulting irony is unclear at best; the irony is best completed with “fast-food restaurant” in **C**.
Question 60. The best answer is F because the description of the walls as two concentric circles most logically connects to the general introduction of the walls in the first paragraph, in which the walls are described as surrounding the city and serving as protective barriers.

The best answer is NOT:

G because paragraph 2 only describes the construction of the Servian Wall, so the information about how the two walls look together does not logically fit here.

H because paragraph 3 only describes the construction of the Aurelian Wall, so the information about how the two walls look together does not logically fit here.

J because paragraph 4 continues the description of the Aurelian Wall, so the information about how the two walls look together does not logically fit here.

Passage V

Question 61. The best answer is C because the comma following the introductory adverb clause (“Before entering a British-run prison during the American Revolution”) is appropriate. Both the phrase “prisoner of war” and the name “James Forten” are restrictive in the sentence, so neither should be set off or interrupted by commas.

The best answer is NOT:

A because the name James Forten is restrictive (essential to the meaning of the sentence) and should not be set off by commas. Furthermore, a comma is required following the introductory adverb clause (“Before entering a British-run prison during the American Revolution”).

B because the comma following the name Forten incorrectly separates the subject of the sentence (James Forten) from its verb (said).

D because placing a comma after the word war separates the descriptor “prisoner of war” from the noun it modifies (James Forten), and eliminating the comma after the word Revolution introduces ambiguity (“American Revolution prisoner of war”).
Question 62. The best answer is G because this choice best introduces the focus of the paragraph, which is on the risks Forten faced by rejecting the British captor’s offer and choosing to stay in the United States.

   The best answer is NOT:

   F because the detail that Forten was one of many to serve in the American Revolution is unrelated to the main focus of the essay and does not introduce the focus of this paragraph, which is on the risks Forten faced by staying in the United States.

   H because this sentence is unrelated to the focus of the paragraph. The information in this sentence relates to the British captor’s offer instead of to the risk Forten took in refusing the offer; the focus of the paragraph is not on the offer but on the potential consequences for Forten in rejecting it.

   J because this information is both vague and out of place at this point in the essay, and this choice does not logically introduce the focus of the paragraph (Forten’s decision to stay in the United States and the risks he faced as a result).

Question 63. The best answer is C because the plural noun chances agrees in number with the plural verb were, and the choice correctly uses the preposition of in the idiomatic phrase “chances of surviving.”

   The best answer is NOT:

   A because the singular noun chance does not agree in number with the plural verb were.

   B because “chances to surviving” contains an incorrect use of the preposition to in the idiomatic phrase “chances of surviving.”

   D because the singular noun chance does not agree in number with the plural verb were.

Question 64. The best answer is F because a comma is required both following the dependent adverbial clause “if released at the war’s end or as part of an exchange” and following the noun he (to separate the noun from its appositive “a free black man”).

   The best answer is NOT:

   G because a semicolon should be used to separate two independent clauses; in this case, the semicolon after the word exchange separates a dependent and independent clause.

   H because a comma should be used following the dependent adverbial clause “if released at the war’s end or as part of an exchange,” not a dash. Furthermore, omitting a comma between the word he and the phrase “a free black man” does not set off the appositive from its noun.

   J because placing a period between the words exchange and he creates a sentence fragment.
Question 65. The best answer is B because the sentence demonstrates that Forten did make the right choice, despite the risks, and became successful as a result. Without this sentence, the essay lacks a clear transition to paragraph 3.

The best answer is NOT:
A because this sentence does not give any information about the tactics Forten used to survive imprisonment, and the essay has not yet described how he became a successful businessman.
C because this sentence does not compare or give any specifics about Forten's work as a businessman or abolitionist.
D because this sentence does not analyze or provide specific information about how Forten transitioned from a prisoner to a businessman and abolitionist.

Question 66. The best answer is F because the simple past tense rose is consistent with the verb tense in the rest of the paragraph.

The best answer is NOT:
G because arose is the wrong verb in context, and had arose is an incorrect formation (the correct past perfect form of arose is had arisen).
H because the shift to past perfect tense is inconsistent with the verb tense in the rest of the paragraph, and the correct past perfect tense form of the verb rise is had risen, not had rose.
J because the transitive verb raised is used incorrectly here since there is no direct object. Instead, the sentence calls for the intransitive verb rose.

Question 67. The best answer is A because the appositive phrase “white and black” further describes the workers. Because it is nonrestrictive, this phrase needs to be set off with commas.

The best answer is NOT:
B because the relative pronoun whom is used incorrectly here; whom is an object pronoun, but the sentence requires a subject pronoun (who).
C because an independent clause must precede a colon; in this choice, the colon is preceded by a dependent clause.
D because the appositive phrase “white and black” needs to be offset from its noun workers with commas; the omission of a comma following workers is incorrect.
**Question 68. The best answer is H** because the focus of the paragraph is on how Forten’s sailmaking business became a success; the information about his lost business records is unrelated to this focus.

**The best answer is NOT:**

F because the loss of Forten’s business records is not related to the success of his business; the sentence does not establish a correlation. The sentence is also unrelated to the paragraph’s focus on the success of Forten’s business.

G because the loss of Forten’s business records does not reveal specific information about how many workers Forten employed. The sentence does not provide evidence, nor is it related to the paragraph’s focus on the success of Forten’s business.

J because the sentence does not contradict the idea that Forten had high expectations for his workers; the information about the loss of business records is unrelated to Forten’s high expectations. Although the sentence should be deleted, the reason this choice offers for deleting it is inaccurate.

**Question 69. The best answer is D** because it is the most concise, least redundant choice. The phrase “premier sailmaker” by itself is sufficient to express the high regard people had for Forten’s sailmaking business.

**The best answer is NOT:**

A because “premier sailmaker in Philadelphia” is redundant; the essay has already mentioned what city Forten worked in.

B because foremost and leading are redundant, and “in his native Philadelphia” repeats information the essay has already provided.

C because “premier sailmaker in the city of Philadelphia” is unnecessarily wordy and unnecessarily repeats information about the city in which Forten works.
Question 70. The best answer is J because the paragraph provides two examples of Forten overcoming hardships in his business: the closing of the port of Philadelphia during the War of 1812 and changing demands in sail design, both of which he adapted to. Therefore, this choice most logically introduces the focus of this paragraph.

The best answer is NOT:

F because the information about Forten sustaining his business during wartime hardships and meeting changing demands, which is the focus of the paragraph, is not related to abolitionist causes, so this choice does not logically introduce this paragraph.

G because this choice repeats information about Forten's service during the Revolutionary War and is unrelated to the focus of the paragraph on Forten's ability to adapt to changing circumstances.

H because the information about Forten sustaining his business during wartime hardships and meeting changing demands, which is the focus of the paragraph, is not related to the information about Forten's donations to schools and hospitals. This choice does not logically introduce this paragraph.

Question 71. The best answer is A because the coordinate adjectives *smaller* and *quicker* both modify the noun *vessels*, and therefore a comma is needed to separate the two adjectives. The order of the adjectives could be swapped to say “quicker, smaller vessels,” and it would not change the meaning of the sentence. Likewise, the sentence could say “smaller and quicker” or “quicker and smaller.”

The best answer is NOT:

B because the coordinating conjunction *and* is incorrect when used with a comma between two coordinating adjectives (either a comma or the word *and* would be appropriate, not both), and the word *more* is incorrectly used with the comparative adjective *quicker*.

C because the word *more* is incorrectly used with the comparative adjective *quicker*.

D because a comma is needed to separate a pair of coordinate adjectives, or adjectives that both modify the same noun and not each other. In this case *smaller* and *quicker* both modify *vessels; smaller* does not modify *quicker*. 

Question 72. The best answer is J because the phrase “over half of his” is the clearest and most concise choice to express how much money Forten invested in abolitionist causes.

The best answer is NOT:

F because the phrase “over greater than half” is unnecessarily wordy; over and greater mean the same thing.

G because the phrase “over more than half” is unnecessarily wordy and redundant.

H because the phrase “more than over half” is redundant; either “more than half” or “over half” would have been acceptable, but not both.

Question 73. The best answer is D because it is the most logical and concise choice to conclude the essay.

The best answer is NOT:

A because the phrase “who served in this war” is redundant following the noun veteran.

B because the phrase “cultivating the sails of freedom” presents a vague and confusing metaphor (what exactly does “the sails of freedom” mean or refer to?), and the repetition of the word freedom in the sentence is a questionable stylistic choice.

C because “nurturing the road to reform” is a phrase that, like “cultivating the sails of freedom,” might sound good at first but actually presents a vague and confusing metaphor. “Nurturing the road” is not idiomatic and doesn’t make much sense in context.

Question 74. The best answer is J because the information about the articles Forten submitted under a pen name makes logical sense only if placed after the sentence that introduces his financing of the newspaper Liberator.

The best answer is NOT:

F because this sentence does not logically fit at this point in the essay; Forten has not yet been introduced or credited with the quotation in the first sentence. The information about his submission of articles under a pen name is also out of chronological order in the essay.

G because the information about his submission of articles under a pen name is not related to the focus of paragraph 3, which outlines how Forten got involved in the sailmaking business.

H because it does not make logical sense to describe how Forten submitted articles to a publication under a pen name before introducing the newspaper itself.
Question 75. The best answer is C because the focus of the essay is on Forten and the significant roles he played (patriot, businessman, abolitionist) and not on the more specific daily operations of his successful business.

The best answer is NOT:

A because the essay does not describe in detail the daily operations of a successful business. Although the essay does describe how Forten became a successful businessman and survived numerous challenges, the focus of the essay is on Forten’s significance in other aspects as well.

B because although the essay does, to a degree, indicate the historical significance of Forten’s business and the various ways it evolved, the main purpose of the essay is to describe Forten’s significance more generally.

D because the essay does not contrast Forten’s work as an abolitionist with his work as a sailmaker but instead shows how his success in business was beneficial to and worked in tandem with his work as an abolitionist.


**Mathematics • Practice Test 1 • Explanatory Answers**

**Question 1.** The correct answer is C. The correct approach for this problem is to first distribute \( a \) and then combine the two \( a \)-terms. Doing so, we get 
\[
4a - a^2 - 5a - 35 = -a^2 - a - 35.
\]
If you chose A, you may have thought that \( a \cdot a = a \) and did not get the \( a^2 \)-term when you distributed. If you chose B, you may have made the same error as above but also forgot to distribute \(-5\) over *both terms* of \( (a + 7) \). If you chose D, you may have incorrectly combined like terms by thinking 
\[
4a - a^2 - 5a = (4 - 1 - 5)a^3.
\]
Remember, you can only combine terms with identical variable parts.

**Question 2.** The correct answer is G. You can order the numbers by considering the decimal equivalent of \( \frac{1}{4} = 0.25 \) and writing each fraction in an equivalent form with 100 as the denominator: \( 0.2 = \frac{20}{100}, 0.03 = \frac{3}{100} \), and \( \frac{1}{4} = \frac{25}{100} \). The fractions can then be ordered based on the magnitude of the numerator: \( \frac{3}{100} < \frac{20}{100} < \frac{25}{100} \) or \( 0.03 < 0.2 < \frac{1}{4} \). If you chose F, you may have incorrectly used 2 < 3 < 4. If you chose H or J, you may not have considered that \( \frac{1}{4} = 0.25 \). If you chose K, you may have incorrectly given the order from greatest to least.

**Question 3.** The correct answer is C. Because \( x^2 + 4 = 29 \), you can solve the equation for \( x^2 \), \( x^2 + 4 = 29 \iff x^2 = 25 \). Substitute the value of \( x^2 \) into the expression \( x^2 - 4 \) to calculate the value the expression is equal to \( x^2 - 4 = 25 - 4 = 21 \).

If you chose A, you might have solved \( x^2 + 4 = 29 \) for the principal square root of \( x \), \( x^2 + 4 = 29 \iff x^2 = 25 \iff x = \pm 5 \) and neglected to evaluate the expression \( x^2 - 4 \). If you chose B, you might have incorrectly combined \( x^2 + 4 = 29 \) with \( x^2 - 4 \) and solved for \( x \), \( x^2 + 4 = 29 - 4 \iff x^2 = 29 - 4 \iff x^2 = 25 \iff x = \pm 5 \). If you chose D, you might have only solved \( x^2 + 4 = 29 \) for \( x^2 \), \( x^2 + 4 = 29 \iff x^2 = 25 \). If you chose E, you might have incorrectly manipulated \( x^2 + 4 = 29 \) and only solved for \( x^2 \), \( x^2 + 4 = 29 \iff x^2 = 25 + 4 \iff x^2 = 33 \).

**Question 4.** The correct answer is F. As shown in the following figure, the given vertices form a 5-unit-by-5-unit rectangle (or square), which has an area of \( 5 \times 5 = 25 \) square coordinate units. The portion of that square lying in Quadrant III is shown in the figure as the 2-unit-by-1-unit shaded rectangle, which has an area of \( 2 \times 1 = 2 \) square coordinate units. Therefore, the percent of the total area of the square lying in Quadrant III is 
\[
\frac{\text{the area of the shaded rectangle}}{\text{the area of the square}} \times 100\% = \frac{2}{25} \times 100\% = 8\%.
\]
Question 5. The correct answer is B. Assuming the cost increased *linearly* is equivalent to assuming the cost increased *at a constant rate*. Because the cost of the clothing increased from $620 to $1,000 in 10 years, the constant rate is equal to \( \frac{1,000 - 620}{10 \text{ years}} \), or $38 per year.

Therefore, the cost of the family's clothing in 1991 (6 years after 1985) is:

\[
620 + (6 \text{ years})(38 \text{ per year}) = 620 + 228 = 848.
\]

Question 6. The correct answer is K. You can let \( x \) represent the certain number so that \( \sqrt{x} = 9.2371 \) or \( x = 9.2371^2 \) after squaring both sides of the equation. Now, \( 9^2 < x < 9.5^2 \rightarrow 81 < x < 90.25 \) and \( 90.25 < 99 \), so \( x \) is between 81 and 99. If you chose F, you could have incorrectly thought that \( x^2 = 9.2371 \) and used the fact that \( 3^2 = 9 \) and \( 4^2 = 16 \).

If you chose G, you could have incorrectly thought that \( 2x = 9.2371 \) or \( x = \frac{9.2371}{2} \), which is between \( \frac{8}{2} = 4 \) and \( \frac{10}{2} = 5 \). If you chose H, you could have incorrectly thought that \( x = 9.2371 \), which is between 9 and 10. If you chose J, you could have incorrectly thought that \( \frac{9}{2} = 9.2371 \) or \( x = 2(9.2371) \), which is between \( 2(9) = 18 \) and \( 2(9.5) = 19 \).
Question 7. The correct answer is E. There are 10 – 2 = 8 pieces of candy that are NOT grape, and \( \frac{8}{10} = \frac{4}{5} \). If you chose A, you may have incorrectly found the probability that the candy randomly picked is either grape or not grape. If you chose B, you may have incorrectly found the probability of grape out of the four flavors. If you chose C, you may have incorrectly thought that the candy randomly picked is either grape or not grape, so there is a 50% chance of not grape. If you chose D, you may have incorrectly found the probability of not grape out of the four flavors.

Question 8. The correct answer is K. The coordinates of the midpoint, \((x_m, y_m)\), of a segment with endpoints \((x_1, y_1)\) and \((x_2, y_2)\) are \(\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)\). Substituting, we get

\[
1 = \frac{x_1 + (-3)}{2} \iff 2 = x_1 - 3 \iff x_1 = 5, \text{ and } 2 = \frac{y_1 + 4}{2} \iff y_1 = 0.
\]

Therefore the midpoint is \((5,0)\), K. An alternative approach to this problem would be to plot point B and the midpoint and then use the concept of displacement to find the coordinates of A. Because point B is 4 coordinate units left and 2 coordinate units up from the midpoint, point A must be 4 coordinate units right and 2 coordinate units down from the midpoint, (1,2). So, once again, we find the coordinates of point A to be \((1 + 4, 2 - 2) = (5,0)\). If you chose F, you may have used the correct midpoint formula but interchanged the coordinates of the midpoint and point B. If you chose G, you may have incorrectly written minus signs in the formula where there should be plus signs and used (1,2) and point B as the 2 endpoints. If you chose H, you found the midpoint of the segment with endpoints (1,2) and point B. If you chose J, you may have incorrectly written minus signs in the formula where there should be plus signs.

Question 9. The correct answer is B. Let \( x \) represent the number of customers Andrea’s company had 1 year ago. Paraphrasing, the 116 customers are 8 more than twice the number of customers the company had 1 year ago. Replacing the “are” with “=” and translating both halves of the sentence into symbols, we get \( 116 = 2x + 8 \). Solving this equation, we get \( x = 54 \), which is B. If you chose A, you may have added 8 to \( x \) rather than to \( 2x \), giving you the incorrect equation \( 116 = 2(x + 8) \). If you chose C, you may have subtracted 8 from \( 2x \) rather than adding it, giving you the incorrect equation \( 116 = 2x - 8 \). If you chose D, you may have subtracted 8 from \( x \) and then doubled that, obtaining the incorrect equation \( 116 = 2(x - 8) \). If you chose E, you may have written the incorrect equation \( 116 = x + 2(8) \). Please remember that “8 more than” means to add 8 to something. Add it to what? Add it to “twice the number of customers the company had 1 year ago,” which is \( 2x \).

Question 10. The correct answer is H. You can find the set amount per foot of fence by subtracting the $500 fee from the estimate given: $2,200.00 – $500.00 = $1,700 and dividing that result by 200 ft: \( \frac{1,700}{200} = \$8.50 \) per foot of fence. If you chose F, you may have incorrectly subtracted 200 from 2,200 and divided that result by 500. If you chose G, you may have incorrectly added 200 to 2,200 and divided that result by 500. If you chose J, you may have forgotten to subtract 500 from 2,200 before dividing by 200. If you chose K, you may have incorrectly used the sum of 500 and 2,200 divided by 200.
Question 11. The correct answer is C. You can solve this problem numerically by considering all the possible pairs of integer values representing the width and length of the room for which the area equals 180 $ft^2$. Then you can find the pair of values for which the perimeter equals 54 ft (that pair of values is 12 ft and 15 ft in the shaded region of the following table).

<table>
<thead>
<tr>
<th>Width (ft)</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>9</th>
<th>10</th>
<th>12</th>
</tr>
</thead>
<tbody>
<tr>
<td>Length (ft)</td>
<td>180</td>
<td>90</td>
<td>60</td>
<td>45</td>
<td>36</td>
<td>30</td>
<td>20</td>
<td>18</td>
<td>15</td>
</tr>
<tr>
<td>Area ($ft^2$)</td>
<td>180</td>
<td>180</td>
<td>180</td>
<td>180</td>
<td>180</td>
<td>180</td>
<td>180</td>
<td>180</td>
<td>180</td>
</tr>
<tr>
<td>Perimeter (ft)</td>
<td>362</td>
<td>184</td>
<td>126</td>
<td>98</td>
<td>82</td>
<td>72</td>
<td>58</td>
<td>56</td>
<td>54</td>
</tr>
</tbody>
</table>

You can also approach this problem analytically by solving the system of equations $2w + 2l = 54$ and $wl = 180$, which result from using the perimeter and the area formulas, respectively.

Notice that $2w + 2l = 54$ is equivalent to $w + l = 27$, and solving $wl = 180$ for $l$ gives $l = \frac{180}{w}$. Substituting this value for $l$, you obtain $w + \frac{180}{w} = 27$; multiplying both sides by $w$ and then subtracting $27w$ from both sides leads to $w^2 - 27w + 180 = 0$. Factoring the quadratic gives the equivalent equation $(w - 12)(w - 15) = 0$, with solutions $w = 12$ or $w = 15$; the corresponding solutions for $l$ are $\frac{180}{12} = 15$ and $\frac{180}{15} = 12$.

You may notice that the work involved in factoring is essentially the same work required in the numerical method, so the analytical method is a little less efficient. You may also notice that the system of equations is symmetric in $w$ and $l$, so that the solutions for either $w$ or $l$ give the dimensions of the living room.

Question 12. The correct answer is J. You can consider that $10.00 - 4.25 = 5.75$ and $\frac{5.75}{0.25} = 23$ quarters. If you chose F, you may have found the number of quarters in $25.00 and divided that number by 10. If you chose G, you may have incorrectly considered the number of quarters in $4.25 only. If you chose H, you may have incorrectly used the price of 25 candies at Carrie’s Chocolate Shop. If you chose K, you may have incorrectly divided the number of quarters in $25 by 10 and subtracted that result from the number of quarters in $10.00.

Question 13. The correct answer is B. The average price per candy is the total price divided by the number of candies. This is equal to $\frac{53.75}{20} = 2.6875$ or $2.69$ when rounded to the nearest $0.01. If you chose A, you may have incorrectly found the change in price from 5 candies to 20 candies and divided that result by 20. If you chose C, you may have incorrectly used the price of 20 candies at Carrie’s Chocolate Shop. If you chose D, you may have incorrectly multiplied the cost of 5 candies at Carrie’s Chocolate Shop by 4 and divided that result by 20. If you chose E, you may have incorrectly multiplied the cost of 5 candies at Tamika’s Treat Shop by 4 and divided that result by 20.
Question 14. The correct answer is F. You can verify that the relationship is linear by noting that each increase of 5 candies results in an increase of $1.00 in price so that the slope of the line is $m = \frac{1.00}{5} = 0.20$. The equation can then be written in the form $c = 0.20n + b$. You can solve for the value of $b$ by substituting any one of the $(n, c)$ ordered pairs for Carrie's Chocolate Shop into the equation. Using $(5, 1.50)$, we have $b = 1.50 - 0.20(5) = 0.50$. Therefore, the correct equation is $c = 0.20n + 0.50$. If you chose G, you may have incorrectly thought that the slope of the line would be $\frac{1.50}{5}$ and $b = 0$. If you chose H, you may have incorrectly found the slope to be the change in price at Tamika's Treat Shop relative to the change in price at Carrie's Chocolate Shop and the value of $b$ as the price for 5 candies at Carrie's Chocolate Shop. If you chose J, you may have incorrectly thought the $1.00 increase in price is because of an increase of 1 piece of candy and solved for $b$ using the equation $b = 1.50 - 5(1)$. If you chose K, you may have incorrectly found the slope by dividing the difference in price of 30 candies at the 2 shops by the difference in price of 25 candies at the 2 shops and using an ordered pair from Carrie's Chocolate Shop to find the value of $b$.

Question 15. The correct answer is B. To solve the quadratic equation $x^2 - 36x = 0$ for $x$, you would factor the left side to apply the zero product rule to $x(x - 36) = 0$. Thus, $x = 0$ or $x - 36 = 0$ implies $x = 0$ or 36. The solution given as an answer choice is 36.

If you chose C, you probably divided 36 by 2. If you chose D, you probably dropped the $x$ in the second term and solved $x^2 = 36$ for a positive value. If you chose E, you probably dropped the $x$ in the second term and solved $x^2 = 36$ for negative value because there was a negative sign in the original equation.

Question 16. The correct answer is J. Using the properties of supplementary angles, we find the measures of $\angle EDF = 180^\circ - 148^\circ = 32^\circ$ and $\angle EFD = 180^\circ - 140^\circ = 40^\circ$. Then, by the $180^\circ$ rule for triangles, the measure of $\angle DEF = 180^\circ - 32^\circ - 40^\circ = 108^\circ$. If you chose F, you may have forgotten to subtract the measures of $\angle EDF$ and $\angle EFD$ from $180^\circ$ ($180^\circ$ rule for triangles). If you chose G, you may have incorrectly subtracted $140^\circ$ from $148^\circ$ and added that result to $90^\circ$. If you chose H, you may have incorrectly subtracted $140^\circ$ rather than $148^\circ$ from $180^\circ$ for angle $\angle EDF$. If you chose K, you may have incorrectly subtracted $148^\circ$ rather than $140^\circ$ from $180^\circ$ for angle $\angle EFD$.

Question 17. The correct answer is E. Assume the base of the box is 9 inches by 9 inches. Because both dimensions are divisible by 3, 3 rows with 3 notepads in each row placed edge to edge will exactly cover the base. We can call this 1 layer. Because the box is 12 inches high, it will hold exactly 4 such layers. Therefore, 4 layers with 9 notepads in each layer will result in 36 notepads in the box, E. Because all 3 dimensions of the box are evenly divisible by the edge length of the cubical notepads, this can also be thought of as $\frac{9}{3} = 3$ notepads wide, $\frac{9}{3} = 3$ notepads long, and $\frac{12}{3} = 4$ notepads high, and $3 \times 3 \times 4 = 36$. If you chose A, you may have obtained 3 notepads long by 3 notepads wide by 4 notepads high but then added instead of multiplying. Because there will be no gaps or overlap of the notepads in the box, another method would be to divide the volume of the box by the volume of a single notepad. Using
the formula for the volume of rectangular prism, \( V = l \times w \times h \), we get \( \frac{\text{Volume of the box}}{\text{Volume of a notepad}} = \frac{9(9)(12)}{3(3)(3)} = 36. \) If you chose B, you may have been thinking this way but incorrectly used the area of \( \frac{1}{2} \) of the faces of the box instead of volume of the box. If you chose C, you may have thought the box could hold only one 3 notepads long by 4 notepads high layer, and you did not consider how many notepads wide it could hold. If you chose D, you may have been trying to divide the volume of the box by the volume of a single notepad, but you incorrectly found the volume of the box to be \( 2(9 \times 9 \times 12 + 9 \times 12) \), which is the surface area instead.

**Question 18. The correct answer is J.** Evaluate the function \( f \) for \( x = -4 \), \( f(-4) = -4(-4)^3 - 4(-4)^2 = -4(-64) - 4(16) = 256 - 64 = 192. \) If you chose F, you might have dropped the negative sign on the first 4 in the function: \( 4(-4)^3 - 4(-4)^2 \). If you chose G, you might have dropped the negative signs on both 4s in the function: \( 4(4)^3 - 4(4)^2 \). If you chose H, you might have dropped the negative on the first 4, evaluated the function at \( x = 4 \), and incorrectly calculated the exponents in the function: \( 4(4)^3 - 4(4)^2 \). If you chose K, you might have dropped the negative sign on the second 4 in the function: \( -4(-4)^3 + 4(-4)^2 \).

**Question 19. The correct answer is A.** Solving the first equation for \( x \) gives you \( x = 4 - 2y \). Plugging in the expression that \( x \) equals into the second equation gives you \( -2(4 - 2y) + y = 7 \). You can solve for \( y \) as follows \(-8 + 4y + y = 7 \Leftrightarrow -8 + 5y = 7 \Leftrightarrow 5y = 15 \Leftrightarrow y = 3 \). Now, take the value for \( y \) and plug it in for \( y \) in one of the original equations and solve for \( x \), \( x + 2(3) = 4 \Leftrightarrow x + 6 = 4 \Leftrightarrow x = -2 \). Therefore, \((-2, 3)\) is the solution for this system of equations.

If you chose B, you might have plugged \(-1\) in for \( x \) in the first equation and solved for \( y \) without checking to see if those values hold for the second equation, \(-1 + 2y = 4 \Leftrightarrow 2y = 5 \Leftrightarrow y = 2.5 \). If you chose C, you might have plugged 1 in for \( x \) in the first equation and solved for \( y \) without checking to see if those values hold for the second equation, \( 1 + 2y = 4 \Leftrightarrow 2y = 3 \Leftrightarrow y = 1.5 \). If you chose D, you might have plugged 1 in for \( y \) in the first equation and solved for \( x \) without checking to see if those values hold for the second equation, \( x + 2(1) = 4 \Leftrightarrow x + 2 = 4 \Leftrightarrow x = 2 \). If you chose E, you might have plugged 0 in for \( y \) in the first equation and solved for \( x \) without checking to see if those values hold for the second equation, \( x + 2(0) = 4 \Leftrightarrow x + 0 = 4 \Leftrightarrow x = 4 \).

**Question 20. The correct answer is G.** By definition, \( \log_3 36 \) is the power of \( x \) that it would take to be 36. That power is 2 from the right side of the equation. So, \( x^2 = 36 \). This equation is satisfied when \( x = 6 \).

The most common wrong answer is K, which is the solution to \( x \cdot 2 = 36 \).

**Question 21. The correct answer is C.** The area of a rectangle is given by \( \text{area} = \text{length} \times \text{width}, \) or \( A = lw \). The area of the picture before cutting is \( A = 7(5) = 35 \) square inches. The area enclosed by the frame is \( A = 6(4) = 24 \) square inches. Subtracting, we see \( 35 - 24 = 11 \) square inches must be cut off the picture to make it exactly
fit into the frame. That is C. If you chose A, you may have incorrectly thought that because the picture is 1 inch longer and 1 inch wider than the frame, a total of 2 inches must be cut off the picture. Please note that the problem asks for how much area must be cut off the picture. If you chose B, you may have incorrectly thought that because the picture is 1 inch longer and 1 inch wider than the frame, and the frame is 4 inches by 6 inches, the total area cut off must be 1(6) + 1(4) square inches. If you chose D, you may have incorrectly thought that because the picture is 1 inch longer and 1 inch wider than the frame, and the picture is 5 inches by 7 inches, the total area cut off must be 1(5) + 1(7) square inches. If you chose E, you may have incorrectly thought that because the picture is 1 inch longer and 1 inch wider than the frame, the amount of area that needs to cut off is 1 × 1 × the area of the frame.

**Question 22. The correct answer is K.** As the following diagrams show, there are many different arrangements of points that satisfy the conditions. But, in all of these, the order of points starting from point A is A, B, D, C.

Because D is between C and B distance CD is always shorter than distance BC. So, answer choice K is always true.

The other answer choices can each be true for particular arrangements of the points, but they can also each be false for particular arrangements. Line 1 shows that F is sometimes false, Line 2 that G is sometimes false, Line 3 that H is sometimes false, and Line 4 that J is sometimes false. If you got an incorrect answer, you probably did not consider enough cases.

**Question 23. The correct answer is E.** If you find which of the following integers could be y when the greatest common factor of \(x^2y^2\) and \(xy^3\) is 45, then you first recognize that the greatest common factor of \(x^2y^2\) and \(xy^3\) is \(xy^2\), which equals 45. Because x and y are both positive integers and 45 = \(3^25\), there are two possibilities for x, 5 or 45. If x is 45, then y is 1. If x is 5, then y = 3. Thus, 3 is the answer choice.

If you chose B, you probably found x rather than y. If you chose C, you probably found \(y^2\) rather than y. If you chose D, you probably found xy rather than y.
Question 24. The correct answer is G. The company’s testing was randomized because the 150 volunteers were chosen without bias. The testing was also an experiment because the results from a control group (the group that received the placebo) and a treatment group (the group that received the new medication) were compared. If you chose F, you might not have realized that a census is a survey of a population and does not involve testing medicine. If you chose H, you might not have realized that the experiment was randomized by the simulation described, which is similar to the randomized selection of a marble from a bag of marbles. If you chose J or K, you might not have realized that, for a sample survey, all the volunteers would have received the same survey or test—there would be no control group or treatment group.

Question 25. The correct answer is D. The two signs will flash at the same time when the elapsed time is a common multiple of the signs’ flash intervals, 4 seconds and 10 seconds. The least common multiple of 4 and 10 is 20, so the signs will flash at the same time after 20 seconds elapse.

If you chose A, you might have subtracted the 4-second flash interval from the 10-second flash interval \(10 - 4 = 6\). If you chose B, you might have divided the sum of the 4-second flash interval and the 10-second flash interval by 2, \(\frac{4 + 10}{2} = \frac{14}{2} = 7\). If you chose C, you might have added the 4-second flash interval to the 10-second flash interval. If you chose E, you might have multiplied the 4-second flash interval and the 10-second flash, \(4(10) = 40\).

Question 26. The correct answer is K. Please recall that \(|x|\) means the absolute value of \(x\) and, by definition, \(|x| = x\) if \(x \geq 0\) and \(|x| = -x\) if \(x < 0\). In any case, \(|x|\) is positive for all nonzero values of \(x\). Because the sum of 2 positive numbers is positive, \(|a| + |b| > 0\). Multiplying both sides of this inequality by \(-1\) and remembering to switch the direction of the inequality sign, we get \(-(|a| + |b|)) = -|a| - |b| < -0 = 0\). Therefore, the expression in K is always negative. We now show by example that the expressions in F, G, and J can be positive and that the expression in H is always positive. If you let \(a = b = -1\), then \(-a - b = -(1) - (-1) = 1 + 1 = 2\). Hence, the expression in G can be positive. If you let \(a = 2\) and \(b = 1\), then \(a - b = 2 - 1 = 1\), so the expression in F can be positive. Using those same two values for \(a\) and \(b\), \(|a| - |b| = |2| - |1| = 2 - 1 = 1\), so the expression in J can be positive. Finally, because the sum of two positive numbers is positive, \(|a| + |b|\) is positive, so the expression in H is always positive.

Question 27. The correct answer is C. You can sketch the graphs of the two conics to determine the number of points of intersection. The circle is centered at the origin and has a radius of 3. The vertex of the parabola is \((-3, -2)\), and passes through \((-2, -1)\) so that the parabola turns upward. The vertex of the parabola is at a distance of \(\sqrt{(-3)^2 + 2^2} = \sqrt{13}\) coordinate units from the origin and all points on the circle are at a distance of 3 coordinate units from the origin, so the vertex lies outside the circle. Thus, for \(x < -3\), the parabola will not intersect the circle in any points. For \(x > 3\), the parabola intersects the circle at two distinct points, one on the lower semicircle and one on the upper.
semicircle. If you chose A, you may have considered the portion of the parabola determined only by \( x < -3 \). If you chose B, you may have considered only where the parabola intersects the upper semicircle. If you chose D, you may have thought the parabola intersects the circle at the \( y \)-intercept of the lower semicircle and passed through the upper semicircle at two distinct points. If you chose E, you may have thought the vertex of the parabola lies below the \( y \)-intercept of the lower semicircle circle and thus intersects both the lower semicircle and the upper semicircle in two distinct points.

**Question 28. The correct answer is H.** Using \( \frac{as}{times} \) and \( is \) as equals, you can write \( 0.4(250) = 0.6x \) so that \( x = \frac{0.4(250)}{0.6} = 166\frac{2}{3} \). If you chose F, you may have incorrectly found 60% of 250. If you chose G, you may have incorrectly found 160% of 40% of 250. If you chose J, you may have incorrectly subtracted 40 from 250 and then added 60. If you chose K, you may have solved the incorrect equation, \( 0.6(250) = 0.4 \).

**Question 29. The correct answer is A.** We will write this inequality equivalently, with \( x \) on the left, in two steps. First, we add 6\( y \) to both sides and obtain \( -2x > 8y - 4 \). Then we divide both sides by \( -2 \), remembering to reverse the direction of the inequality sign when we do so. Doing this, we get the inequality \( x < -4y + 2 \), which is A. If you chose B, you probably forgot to reverse the direction of the inequality sign when you divided both sides by a negative number. If you chose C, you may have subtracted 6\( y \) from both sides instead of adding it in the first step. If you chose D, you may have obtained \( -2x > 8y - 4 \) but then missed the sign on \( y \) when you divided 8\( y \) by \(-2 \). If you chose E, you may have missed the sign on \( y \) when you divided 8\( y \) by \(-2 \) and also not reversed the direction of the inequality sign when you divided both sides by a negative number.

**Question 30. The correct answer is F.** You can use the identity \( \tan \alpha = \frac{\sin \alpha}{\cos \alpha} \) or \( \cos \alpha = \frac{\sin \alpha}{\tan \alpha} \) to find that \( \cos \alpha = \frac{40}{41} \). Alternatively, you can use the ratios \( \sin \alpha = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{40}{41} \), \( \tan \alpha = \frac{\text{opposite}}{\text{adjacent}} = \frac{40}{9} \), and \( \cos \alpha = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{9}{41} \). If you chose G, you may have incorrectly used \( \tan \alpha \). If you chose H, you may have incorrectly used \( \frac{1}{\tan \alpha} \). If you chose J or K, you may have attempted to calculate the length of the hypotenuse of the triangle using the given values.

**Question 31. The correct answer is B.** You can use the formula for the perimeter of a rectangle, \( P = 2(w + l) \) with \( P = 96 \), \( AB = w \), and \( BC = l \), to find that \( w + l = \frac{96}{2} = 48 \). Using this equation and the given ratio with \( k \) as the constant of proportionality, we have \( w = 3k \) and \( l = 5k \), so that the equation becomes \( 3k + 5k = 48 \) or \( 8k = 48 \). Solving for \( k \) gives \( k = 6 \) so that \( w = AB = 3(6) = 18 \) cm. If you chose A, you may have incorrectly thought that the length is given by the constant of proportionality. If you chose C, you may have incorrectly found \( BC \) rather than \( AB \). If you chose D, you may have incorrectly thought the perimeter is given by \( P = (w + l) \) and used this result to find \( AB \). If you chose E, you may have incorrectly thought the perimeter is given by \( P = (w + l) \) and used this result to find \( BC \).
**Question 32.** The correct answer is G. The area of a triangle is found by multiplying $\frac{1}{2}$ by the length of its altitude, $h$, and by the length of its base, $b$, $\frac{1}{2}hb$. For $\triangle ABC$, the length of the altitude is 8 inches and the length of the base is 16 inches. Therefore, the area of $\triangle ABC$ is 64 square inches, $\frac{1}{2}(8)(16) = \frac{1}{2}(128) = 64$. The area, in square inches, of a square with side length $x$ inches is $x^2$, $x^2 = 64 \iff x = \sqrt{64} \iff x = 8$. Thus the length of a side of the square is 8 inches.

If you chose F, H, J, or K, you might be misremembering the formulas for calculating the areas of a triangle and a square. If you chose F, you might have divided the sum of the lengths of the base and the altitude by 4, $(8 + 16) \div 4$. If you chose H, you might have divided the product of the length of the base and 3 by 4, $(16)(3) \div 4$. If you chose J, you might have correctly calculated the area of the triangle but then divided the area by 4 rather than calculating the square root, $\frac{1}{2}(8)(16) \div 4$. If you chose K, you might have divided the product of the lengths of the base and altitude by 4, $(8)(16) \div 4$.

**Question 33.** The correct answer is B. You can use the fact that $EFGH$ is a square so $HG = EF = 3.6$ meters, and $ABCD$ is a rectangle with $AD$ and $BC$ as opposing sides so $AD = BC = 12$ meters. The ratio of the length of $EH$ to the length of $AD$ is $\frac{3.6}{12} = 0.3$, so the length of $EH$ is $0.3(100)\% = 30\%$ percent of the length of $AD$. If you chose A, you may have incorrectly added the two lengths and written the result as a percent. If you chose C, you may have incorrectly used the ratio of the length of $EH$ to the length of $AB$. If you chose D, you may have incorrectly multiplied the two lengths and written the result as a percent.

**Question 34.** The correct answer is F. You can form a right triangle using $AD$ and $AJ$ as the legs and $JD$ as the hypotenuse. The length of $AD$ is 12 meters, and the length of $AJ$ is $\frac{10}{2} = 5$ meters. By the Pythagorean theorem, $AD = \sqrt{12^2 + 5^2} = 13$ meters. If you chose G, you may have incorrectly added the two lengths 12 meters and 3.6 meters. If you chose H, you may have incorrectly added the two lengths $\frac{10}{2} = 5$ meters and 12 meters. If you chose J, you may have incorrectly used 12 and 10 for the lengths of the two legs and then subtracted their squares instead of adding them when using the Pythagorean theorem. If you chose K, you may have incorrectly used 12 and 10 for the lengths of the two legs.

**Question 35.** The correct answer is B. Using the fact that the circumference of a circle is $\pi$ times the diameter of the circle, you can compute the length of arc $CD$ by finding $\frac{1}{2}$ of the circumference of the circle centered at $K$ with radius $CK = \frac{10}{2} = 5$ meters: $\frac{1}{2}(10\pi) = 5\pi$ meters. If you chose A, you may have incorrectly used the radius of the circle instead of its diameter in the formula for the circumference. If you chose C, you may have incorrectly attempted to use the formula for the area of the circle. If you chose D, you may have forgotten to divide the circumference by 2. If you chose E, you may have incorrectly used the area of the circle.
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**Question 36. The correct answer is H.** You can note that the y-coordinate of E is 12 because E lies on \( \overline{AB} \), and \( \overline{AB} \) lies on the line \( y = 12 \). Segment \( \overline{EH} \) is perpendicular to \( \overline{AB} \) and has length 3.6 coordinate units. Therefore, \( H \) has y-coordinate \( 12 - 3.6 = 8.4 \). If you chose F, you may have incorrectly used \( \frac{1}{2} \) of the length of \( \overline{EH} \). If you chose G, you may have incorrectly used the length of \( \overline{EH} \). If you chose J, you may have incorrectly used the length of \( \overline{AB} \). If you chose K, you may have incorrectly thought that \( H \) is on the line \( y = 12 \).

**Question 37. The correct answer is A.** The length can be found by finding the positive difference in the y-coordinate at \( C \), 4, and the y-coordinate of the point where the altitude intersects \( \overline{AB} \). All ordered pairs on \( \overline{AB} \) have y-coordinate 1, so the length of the altitude is \( 4 - 1 = 3 \) coordinate units. If you chose B, you may have incorrectly subtracted the x-coordinate at \( C \) from the x-coordinate at \( B \). If you chose C, you may have incorrectly used the length of \( \overline{AB} \). If you chose D, you may have incorrectly used the length of \( \overline{AC} \). If you chose E, you may have incorrectly used the midpoint of \( \overline{AB} \) and found the distance from this point to \( C \).

**Question 38. The correct answer is J.** The correct approach for this item is to substitute 2 for \( n \) in the formula \( P = \frac{3^n e^{-3}}{n!} \) and then evaluate. Substituting, we get \( P = \frac{3^2 e^{-3}}{2!} \). Because \( 3^2 = 9, 2! = 2, \) and \( e^{-3} = 0.05, \) we get \( P \approx \frac{9(0.05)}{2} = 0.225 \). The closest choice is J, 0.23. If you chose F, you may have forgotten to square the 3 when you evaluated. If you chose G, you may have thought \( 2! = 2^2 = 4 \). Remember, by definition, \( k! = 1 \times 2 \times 3 \times \cdots \times (k-1) \times k \). If you chose H, you may have substituted 1 for \( n \) in the formula and forgotten to square 3. Please note that the question asks for the probability that exactly 2 customers are in line, so \( n = 2 \). If you chose K, you may have thought \( 2! = 1 \). Please see the previously given definition of \( k! \).

**Question 39. The correct answer is B.** You can use the fact that the amplitude of a function of the form \( g(x) = A \cos(Bx + C) \) is \( |A| \). Alternatively, you can use the fact that \( -1 \leq \cos(3x + \pi) \leq 1 \) so that \( -\frac{1}{2} \leq \frac{1}{2} \cos(3x + \pi) \leq \frac{1}{2} \). The amplitude is then given by

\[
\frac{\text{maximum} - \text{minimum}}{2} = \frac{\frac{1}{2} - \left(-\frac{1}{2}\right)}{2} = \frac{1}{2}.
\]

If you chose A, perhaps you incorrectly thought the amplitude of \( g(x) = A \cos(Bx + C) \) is given by \( \frac{1}{\pi} \). If you chose C, you may have incorrectly thought the amplitude of \( g(x) = A \cos(Bx + C) \) is given by \( |AB| \). If you chose D, perhaps you incorrectly thought the amplitude of \( g(x) = A \cos(Bx + C) \) is given by \( \frac{1}{4} \). If you chose E, you may have incorrectly thought the amplitude of \( g(x) = A \cos(Bx + C) \) is given by \( |B| \).

**Question 40. The correct answer is F.** The Fundamental Counting Principle states that if event A can occur in \( m \) ways, and for each of these \( m \) ways event B can occur in \( n \) ways, there are exactly \( m \times n \) ways both events can occur together. In making a license plate for this state, we have to make six decisions. We have to choose a letter, another letter, another letter, a digit, another digit, and one more digit. There are 26 ways to choose a letter. Because
duplications are allowed, there are 26 ways to choose the second letter, and 26 ways to choose the third letter. Similarly, there are 10 ways to choose the first digit, 10 ways to choose the second digit, and, finally, 10 ways to choose the third digit. Using the Fundamental Counting Principle, there will then be \((26)(26)(26)(10)(10)(10) = 10^3 \cdot 26^3\) distinct license plates in this state. That is F. G would be the number of ways to choose a letter or a digit 3 times. If you chose H, you might not have remembered that \(k! = 1 \cdot 2 \cdot 3 \cdot \ldots \cdot k\). J would be the number of ways of choosing 1 out of 6 items 36 times. Many permutation problems have factorials in their solutions (K), but 26! would mean we are arranging all 26 letters of the alphabet without allowing duplications. Similarly, 10! would mean we are arranging all 10 digits without allowing duplications.

**Question 41. The correct answer is D.** The median of a data set is the middle term when the set is arranged in numerical order. The 20 quiz scores are placed in score intervals that are in numerical order. Because there are 20 quiz scores, the median of the scores will be between the 10th and 11th quiz scores. There are 9 quiz scores in the 76–80 score interval, which means the 10th and 11th quiz scores occur in the 81–85 score interval. Therefore, the median of the scores is contained in the 81–85 score interval.

If you chose A, you might have thought the median of the scores was contained in the highest score interval. If you chose B, you might have thought the median of the scores was contained in the interval with the lowest frequency of scores. If you chose C, you might have thought the median of the scores was the middle score interval. If you chose E, you might have thought the median of the scores was contained in the score interval with the highest frequency of scores.

**Question 42. The correct answer is J.** To find an equivalent expression for \(\frac{1}{(1+i)} - \frac{i}{(1+i)}\), you multiply and get \(\frac{1(1-i)}{(1+i)(1-i)} = \frac{1-i}{1-i^2} = \frac{1-i}{2}\).

If you chose G, you probably thought \(\frac{1}{1+i}\) was equivalent to \(1+i\) and canceled \((-i)\) in both places. If you chose H, you probably simplified \(1-i^2\) as 1 and got \(\frac{1}{1-i}\) or \(1-i\).

**Question 43. The correct answer is B.** For the temperature we are looking for, \(F = C = x\). Substituting \(x\) for both \(C\) and \(F\) into the given formula, we get \(x = \frac{9}{5}x + 32\). Multiplying both sides of this equation by \(5\), combining like terms, and solving for \(x\), we get \(5x = 9x + 160 \iff -4x = 160 \iff x = -40\), B. If you chose A, you may have incorrectly thought that \(\frac{9}{5}\) must be distributed over \(x + 32\). If you chose C, you may have incorrectly thought the respective freezing temperatures of water must give the desired value of \(x\). Because water freezes at 32°F, or 0°C, you may have concluded that \(x\) must be 32°F lower than the freezing temperature in degrees Celsius. If you chose D, you may have tried to solve the equation \(x = \frac{9}{5}x + 32\) by inspection and incorrectly thought that because there is an \(x\)-term on both sides, \(x = 0\) must be the solution. If you chose E, you may have incorrectly thought the desired value for \(x\) is the value of \(F\) when \(C = 0\).
**Question 44.** The correct answer is **G.** You can find the value closest to $k$ by considering that the ratio of $y$ to $x$ is approximately $k$, or $\frac{y}{x} = k$. As can be verified, you can choose any two of the $xy$-pairs to find the value among the choices closest to $k$. For example, $\frac{0.425}{8.50} = 0.05$. If you chose $F$ or $J$, you may have incorrectly found the difference in an $xy$-pair. If you chose $H$, you may have incorrectly multiplied an $xy$-pair. If you chose $K$, you may have incorrectly divided $x$ by $y$.

**Question 45.** The correct answer is **A.** The correct graphical model can be identified by considering the slope and the $y$-intercept of the graph of the equation $2x - 5y = -5$. Writing this equation in slope-intercept form, we get $y = \frac{2}{5}x + 1$. From this, we see the slope is $\frac{2}{5}$ and the $y$-intercept is 1. From the $y$-intercept alone, we can rule out C, D, and E because the $y$-intercepts of those graphs appear to be 0, 5, and 5, respectively. The graph in B appears to pass close to the point (2,6). Using that point and (0,1), along with slope in terms of the change in $y$ over the change in $x$, the slope of the graph in B is approximately $\frac{6-1}{2-0} = \frac{5}{2}$. However, the graph in A appears to pass close to the point (5,3). Again, using that point and (0,1), along with slope in terms of the change in $y$ over the change in $x$, the slope of the graph in A is approximately $\frac{3-1}{5-0} = \frac{2}{5}$. Because one of the graphs must be the correct model, it must be the graph in A.

**Question 46.** The correct answer is **J.** To figure out how many cups of flour Diana will use, you can set up a proportion (note: $1\frac{1}{2} = 1.5$, $2\frac{1}{2} = 2.5$, and $2\frac{3}{4} = 2.25$):

$$\frac{\text{teaspoons of yeast in the recipe}}{\text{cups of flour in the recipe}} = \frac{\text{teaspoons of yeast to be used}}{\text{cups of flour to be used (x)}}$$

$$\frac{1.5}{2.5} = \frac{2.25}{x} \iff 1.5x = 2.25(2.5) \iff 1.5x = 5.625 \iff x = 3.75.$$ Therefore, Diana will use $3\frac{3}{4}$ cups of flour.

If you chose F, you might have thought the difference between the amount of yeast the recipe calls for and the amount of yeast Diana will use should be multiplied by the amount of flour the recipe calls for, $(2\frac{1}{4} - 1\frac{1}{2})(2\frac{1}{4}) = (\frac{1}{4})(\frac{9}{4}) = \frac{9}{16}$. If you chose G, you might have thought the difference between the amount of yeast the recipe calls for and the amount of yeast Diana will use should be added to amount of flour the recipe calls for, $(2\frac{1}{4} - 1\frac{1}{2}) + 2\frac{1}{4} = \frac{3}{4} + 2\frac{1}{4} = 3\frac{1}{4}$. If you chose H, you might have thought the quotient of dividing the amount of yeast Diana will use by the amount of yeast the recipe calls for should be multiplied by 2 and added to $\frac{1}{4}$, $(2\frac{1}{4} + 1\frac{1}{2})(2) + \frac{1}{2} = (1\frac{1}{4})(2) + \frac{1}{2} = 3 + \frac{1}{2} = 3\frac{1}{2}$. If you chose K, you might have thought the quotient of dividing the amount of yeast Diana will use by the amount of yeast the recipe calls for should be added to the amount of flour the recipe calls for, $(2\frac{1}{4} + 1\frac{1}{2}) + 2\frac{1}{2} = 1\frac{1}{2} + 2\frac{1}{2} = 4$. 

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Question 47. The correct answer is E. There are two good approaches to this problem. We will show both. First, we factor the greatest common factor out of the numerator and then cancel factors of the numerator with identical factors of the denominator. Doing so, we get

\[
\frac{12x^6 - 9x^2}{3x^2} = \frac{3x^2(4x^4 - 3)}{3x^2} = \frac{3x^2}{3x^2} = 4x^4 - 3.
\]

A second approach is to use the property that states \( \frac{a+b}{c} = \frac{a}{c} + \frac{b}{c} \) and then reduce both rational expressions individually. Using this approach and remembering to subtract exponents when reducing a quotient of powers, we get

\[
\frac{12x^6 - 9x^2}{3x^2} = \frac{12x^6}{3x^2} - \frac{9x^2}{3x^2} = \frac{4x^4}{3} - \frac{3}{3} = \frac{4x^4 - 3}{3}.
\]

In either case, the correct answer is E.

If you chose A, you may have used the second approach shown previously but incorrectly divided the exponents rather than subtracting them. If you chose B, you may have used the second approach shown previously but incorrectly divided the exponents rather than subtracting them in the first term. If you chose C, you may have tried the first approach but incorrectly canceled the \( 3x^2 \) in the denominator with the identical factors of the first term in the numerator. Remember, you must factor the numerator first and then cancel identical factors. If you chose D, you may have used the second approach shown but incorrectly thought \( x^{4-2} = x^0 = 1 \). Remember, any nonzero value raised to the zero power is equal to 1.

Question 48. The correct answer is K. The dimensions of a matrix can be written as \( (r \times c) \), where \( r \) is the number of rows of the matrix and \( c \) is the number of columns of the matrix. To find the element in the \( i \)th row and the \( j \)th column of the product of two matrices, one must multiply the elements of the \( i \)th row of the matrix on the left with the corresponding elements in the \( j \)th column of the matrix on the right and then add those products together. For this reason, in order for the matrix product \( AB \) to be defined, the number of columns of matrix \( A \) must be equal to the number of rows of matrix \( B \). Another way of saying that is the product of an \( (r \times c) \)-matrix (on the left) and an \( (m \times n) \)-matrix (on the right) is defined if and only if \( c = m \). (Please remember that left and right are important here because matrix multiplication is not commutative.) The dimensions of \( W \) and \( X \) are \( (2 \times 2) \), the dimensions of \( Y \) are \( (2 \times 3) \), and the dimensions of \( Z \) are \( (3 \times 2) \). Because \( X \) is a \( (2 \times 2) \)-matrix and \( W \) is a \( (2 \times 2) \)-matrix, the matrix product \( WX \) is defined (J). Because \( X \) is a \( (2 \times 2) \)-matrix and \( Z \) is a \( (3 \times 2) \)-matrix, the matrix product \( XZ \) is undefined (K). Because \( W \) is a \( (2 \times 2) \)-matrix and \( X \) is a \( (2 \times 2) \)-matrix, the matrix product \( WX \) is defined (F). Because \( W \) is a \( (2 \times 2) \)-matrix and \( Y \) is a \( (2 \times 3) \)-matrix, the matrix product \( WY \) is defined (G). Because \( Y \) is a \( (2 \times 3) \)-matrix and \( Z \) is a \( (3 \times 2) \)-matrix, the matrix product \( YZ \) is defined (H). Therefore, we see that \( XZ \), K, is the only indicated matrix product that is undefined.
Question 49. The correct answer is A. All the parabolas open upward. This rules out answer choices D and E. All the parabolas have the same y-intercept, (0,1). This rules out answer choice C, which has y-intercept equal to n, which varies. The parabolas in the family go up more quickly as the value of n increases. This means the coefficient of x must get larger as n gets larger. That happens in A but not in B.

The most common incorrect answer is C. A graph of that family is shown in the following figure:

![Graph of parabolas](image)

Question 50. The correct answer is F. To find the minimum number of students in a class of 20 who play both guitar and piano when 8 play guitar and 9 play piano, you must look at the range for which the guitar and piano players may overlap. For instance, all 8 who play guitar could also play piano; that’s the maximum. The minimum would be the smallest overlap they can have. In this case, there are 20 total; the two groups could be disjoint because 9 + 8 or 17 is less than 20. Thus, the minimum is 0.

If you chose G, you probably found the difference between 9 and 8. If you chose H, you probably found the maximum rather than the minimum number. If you chose K, you probably added 9 and 8.

Question 51. The correct answer is B. The sum of any two different numbers between 1 and 18 must be between 3 and 35. The only perfect squares between 3 and 35 are 4, 9, 16, and 25. Therefore the sum of each of the nine pairs must be 4, 9, 16, or 25. So far, we know the possible pairs for 1 are 3, 8, or 15 and must consider each case.

Because 16, 17, and 18 are each greater than or equal to 16, we must pair them with a number so that the sum is 25. Therefore, 16 must be paired with 9, 17 with 8, and 18 with 7. After pairing these, we are left with 1 – 6 and 10 – 15.
We now must consider what happens if 1 is paired with 3 or with 15.

If 1 is paired with 3, then 15 would have to pair with 10, 2 would have to pair with 14, 11 with 5, and 12 with 4. We’d then be left with 13 and 6 which CANNOT be paired. For that reason 1 CANNOT be paired with 3. Thus 1 must be paired with 15.

When 1 is paired with 15, the pairs are as follows:

- $18 + 7 = 25$
- $17 + 6 = 25$
- $16 + 5 = 25$
- $15 + 1 = 16$
- $14 + 2 = 16$
- $13 + 3 = 16$
- $12 + 4 = 16$
- $11 + 5 = 16$
- $10 + 6 = 16$

If you chose A, you might have multiplied 1 and 16 rather than adding them together. If you chose C, you might have multiplied 1 and 9 and not considered that you need 9 pairs of numbers. If you chose D or E, you might not have considered that you need 9 pairs of numbers.

**Question 52. The correct answer is J.** Let $p =$ the number of pennies, $n =$ the number of nickels, $d =$ the number of dimes, and $q =$ the number of quarters. Each of these variables can be expressed in terms of a common variable—in this case, $p$.

Lucky had $p$ pennies, so the value of the pennies was $p$ cents. Because she had twice as many nickels as pennies, $n = 2p$, and the value of the nickels was $5(2p)$ cents. She had 1 fewer dime than nickels, so $d = n - 1 = 2p - 1$, and the value of the dimes was $10(2p - 1)$ cents. Finally, she had 1 more quarter than nickels, so $q = n + 1 = 2p + 1$, and the value of the quarters was $25(2p + 1)$ cents.

Because the total value of the coins is $8.25, or 825 cents, $p$ satisfies the following equation:

$$p + 5(2p) + 10(2p - 1) + 25(2p + 1) = 825$$

Multiplying out each factor on the left-hand side and collecting like terms, you can see that $81p + 15 = 825$, so $81p = 810$. Therefore, $p = 10$ and $q = 2p + 1 = 2(10) + 1 = 21$ quarters.
Question 53. The correct answer is C. Solve for $x$:

$$10^{\frac{2x-1}{x}} = 1$$

$$\Leftrightarrow \log\left(10^{\frac{2x-1}{x}}\right) = \log1$$

$$\Leftrightarrow \frac{2x-1}{x} = 0$$

$$\Leftrightarrow x\left(\frac{2x-1}{x}\right) = 0 \cdot x$$

$$\Leftrightarrow 2x - 1 = 0$$

$$\Leftrightarrow 2x = 1$$

$$\Leftrightarrow x = \frac{1}{2}$$

If you chose A, B, D, or E, you might have performed an incorrect algebraic manipulation and neglected to test your calculated value of $x$ in the equation to see if it held.

For A, you might have correctly manipulated the expression except for incorrectly keeping the negative on the 1:

$$10^{\frac{2x-1}{x}} = 1$$

$$\Leftrightarrow \log\left(10^{\frac{2x-1}{x}}\right) = \log1$$

$$\Leftrightarrow \frac{2x-1}{x} = 0$$

$$\Leftrightarrow x\left(\frac{2x-1}{x}\right) = 0 \cdot x$$

$$\Leftrightarrow 2x - 1 = 0$$

$$\Leftrightarrow 2x = -1$$
For B, you might have incorrectly tried to solve the exponential equation by multiplying both sides by 10 rather than taking the log of both sides:

$$10^{\left( \frac{2x-1}{x} \right)} = 1$$

$$\iff 10^{\left( \frac{2x-1}{x} \right)} = 1 \cdot 10$$

$$\iff \frac{2x-1}{x} = 10$$

For D, you might have incorrectly tried to solve the exponential equation by dividing both sides by 10 rather than taking the log of both sides:

$$10^{\left( \frac{2x-1}{x} \right)} = 1$$

$$\iff 10^{\left( \frac{2x-1}{x} \right)} = 1 + 10$$

$$\iff \frac{2x-1}{x} = \frac{1}{10}$$

For E, you might have incorrectly thought log1 = 1 rather than 0:

$$10^{\left( \frac{2x-1}{x} \right)} = 1$$

$$\iff \log \left( 10^{\left( \frac{2x-1}{x} \right)} \right) = \log 1$$

$$\iff \frac{2x-1}{x} = 1$$
Question 54. The correct answer is G. According to the table, 90 people play an instrument but only 50 of those 90 people like to read. Therefore, the desired probability is \( \frac{50}{90} = \frac{5}{9} \).

If you chose F, you calculated the probability that a person randomly selected out of the total people surveyed both likes to read and plays a musical instrument, \( \frac{50}{250} \), rather than the probability that a person randomly selected out of the total people that play an instrument likes to read. If you chose H, you calculated the probability that a person randomly selected out of the total people that like to read plays a musical instrument, \( \frac{50}{110} \), rather than the probability that a person randomly selected out of the total people that play an instrument likes to read. If you chose J, you calculated the probability that a person randomly selected out of the total people surveyed plays a musical instrument, \( \frac{90}{250} \), rather than the probability that a person randomly selected out of the total people that play an instrument likes to read. If you chose K, you calculated the probability that a person randomly selected out of the total people surveyed likes to read, \( \frac{110}{250} \), rather than the probability that a person randomly selected out of the total people that play an instrument likes to read.

Question 55. The correct answer is A. Mario will travel a distance equal to 1 circumference of the wheel for each complete revolution of the wheel. So first, we must find the circumference of Mario’s wheel. The formula for the circumference of a circle is \( C = \pi D \), where \( D \) is the diameter of the circle. Hence, \( C = 26\pi \) inches. Using unit multipliers to find Mario’s speed in feet per second, we get \( \left( \frac{200 \text{ ft}}{1 \text{ min}} \right) \left( \frac{1 \text{ min}}{60 \text{ sec}} \right) \left( \frac{26\pi \text{ in}}{1 \text{ ft}} \right) \left( \frac{1 \text{ ft}}{12 \text{ in}} \right) \left( \frac{1 \text{ sec}}{1 \text{ min}} \right) \left( \frac{1 \text{ min}}{60 \text{ sec}} \right) = \frac{65\pi \text{ ft}}{9 \text{ sec}} \). Therefore, the correct answer is A. If you chose B, you may have used the radius rather than the diameter when you found the circumference. If you chose C, you may have had an extra factor of 2 in the formula for circumference. If you chose D, you may have used the formula for area of a circle rather than the formula for circumference. If you chose E, you may have used the formula for area of a circle with an incorrect value for the radius rather than the formula for circumference.

Question 56. The correct answer is K. You can use properties of exponents and the fact that for \( b > 0, b \neq 1, b^x = b^y \rightarrow x = y \) to solve for the value of \( \frac{j}{k} \). Because \( (\sqrt{3})^{\frac{1}{2}} = (3^\frac{1}{2})^{\frac{1}{2}} = 3^{\frac{1}{4}} \) and \( 27^k = (3^3)^k = 3^{3k} \), you can rewrite the equation as \( 3^j = 3^{3k} \rightarrow \frac{1}{2} = 3k \) so that \( \frac{j}{k} = 3(2) = 6 \). If you chose F, you may have incorrectly thought that \( (\sqrt{3})^{\frac{1}{2}} = 3^{\frac{1}{2}} \) and \( 27^k = 3^k \) and solved \( 2j = k \). If you chose G, you may have incorrectly thought that \( (\sqrt{3})^{\frac{1}{2}} = 3^{\frac{1}{2}} \) and \( 27^k = 3^k \) and solved \( 2j = 3k \). If you chose H, you may have ignored \( \sqrt{3} \) to get \( 3^j = 3^{3k} \) and solved \( j = 3k \). If you chose J, you may have incorrectly written \( 27^k \) as \( 3^{2k} \) and solved \( \frac{j}{k} = 2k \).
Question 57. The correct answer is A. \(\frac{3}{4} + d, \frac{3}{4} + 2d, \frac{3}{4} + 3d, \frac{3}{4} + 4d, \frac{3}{4} + 5d, \frac{3}{4} + 6d\). The median of these is the middle term, \(\frac{3}{4} + 3d\). The mean is the sum of all the terms divided by 7. We can quickly find the sum of these terms using the formula \(S_n = \frac{n(a_1 + a_n)}{2}\) where \(a_1\) is the first term, \(a_n\) is the \(n\)th term, and \(n\) is the number of terms. The sum is thus:

\[
S_7 = \frac{7(\frac{3}{4} + d) + 7(\frac{3}{4} + 2d) + 7(\frac{3}{4} + 3d) + 7(\frac{3}{4} + 4d) + 7(\frac{3}{4} + 5d) + 7(\frac{3}{4} + 6d)}{2} = 7(\frac{3}{4} + 3d).
\]

Now that you have the sum, you can divide it by 7 to get the mean of the 7 terms, \(\frac{7(\frac{3}{4} + 3d)}{7} = \frac{3}{4} + 3d\). Because the mean and the median are both \(\frac{3}{4} + 3d\), their difference is 0.

If you chose B, you might have selected the first term of the sequence. If you chose C, you might have taken the reciprocal of the first term. If you chose D, you might have thought the mean of the 7 terms was 4 and the median of the 7 terms was 7, \(7 - 4 = 3\). If you chose E, you might have thought the mean of the 7 terms was 3 and the median of the 7 terms was 7, \(7 - 3 = 4\).

Question 58. The correct answer is F. Arc length can be thought of as a fractional part of the circumference. That fraction is given by \(\frac{\theta}{360}\), where \(\theta\) is the measure of the central angle, in degrees, intercepting the desired arc. So first we must find the measure of \(\angle D\). Using the sine ratio, we see \(\sin \angle D = \frac{1}{4}\), making the measure of \(\angle D\) equal to \((\sin^{-1}(\frac{1}{4}))\)^°. The circumference of the circle is \(2\pi r = 2\pi(4) = 8\pi\) cm. Therefore, the length of \(\overline{AC}\) is \(\frac{\sin^{-1}(\frac{1}{4})}{360} \times (8\pi)\). Reducing \(\frac{8}{360}\), we get \(\frac{\pi}{45}(\sin^{-1}(\frac{1}{4}))\), which is F. If you chose G, you may have incorrectly thought that the cosine ratio, not the sine ratio, is given by the length of the opposite leg over the length of the hypotenuse. If you chose H, you may have incorrectly used the formula for the area of the circle rather than the formula for the circumference of the circle. If you chose J, you may have made both of the described errors. If you chose K, you may have incorrectly thought that the tangent ratio, not the sine ratio, is given by the length of the opposite leg over the length of the hypotenuse and also incorrectly used the formula for the area of the circle rather than the formula for the circumference of the circle.
**Question 59. The correct answer is C.** The area of the triangle can be found by using the given formula, \( \frac{1}{2}ab \sin C \). Since only one angle measure is given in the triangle, use that for \( C \) in the formula: \( \frac{1}{2}(8.0)(4.0) \sin 30^\circ \). The length of the side opposite from angle \( C \), the 30° angle, is 5.0 cm and must correspond to side \( c \). That means that the other side lengths, 8.0 cm and 4.0 cm, correspond to sides \( a \) and \( b \) and can be plugged into the formula: \( \frac{1}{2}(8.0)(4.0)\left( \frac{1}{2} \right) \), which results in 8 cm², the area of the triangle. If you chose A, you may have incorrectly thought the area of the triangle was equal to 8.0(sin 30°). If you chose B, you may have used the given formula but incorrectly used 4.0 and 5.0 for the side lengths of \( a \) and \( b \) rather than 4.0 and 8.0. If you chose D, you may have incorrectly thought the given triangle was a right triangle and calculated the area using \( \frac{1}{2}(5.0)(4.0) \), or you may have used the given formula but incorrectly used 5.0 and 8.0 for the side lengths of \( a \) and \( b \) rather than 4.0 and 8.0. If you chose E, you may have incorrectly used the cosine of 30° rather than the sine of 30°.

**Question 60. The correct answer is K.** The expected value of a random variable is its theoretical long-run average value. We find this by

\[
E(X) \equiv \sum_{x_i} x_i P(X = x_i) = \frac{1}{6}(0) + \frac{1}{12}(1) + \frac{1}{4}(2) + \frac{1}{12}(3) + \frac{1}{12}(4) + 0(5) + \frac{1}{3}(6).
\]

You may have gotten F if you did \( \frac{1}{6} + \frac{1}{12} + \frac{1}{4} + \frac{1}{12} + \frac{1}{12} + \frac{1}{3} \div 6 \). You may have gotten G if you recorded the last entry in the table. You may have gotten H if you did \( \frac{1}{6} + \frac{1}{12} + \frac{1}{4} + \frac{1}{12} + \frac{1}{12} + 0 + \frac{1}{3} \). You may have gotten J if you did \( \frac{1}{3} \).
Passage I

**Question 1. The best answer is B** because the story is narrated by Nidali, who, in telling the story of how she came to get her name, offers perceived insights into her parents’ thoughts and actions from a time she was too young to remember. First-person narration can be seen by the use of *I* throughout the passage.

**The best answer is NOT:**

A because even though the story is in first person, it is not about events that happened before the narrator was born; the events are the very story of the narrator being born.

C because although the story does address the thoughts and actions of several characters, those thoughts and actions are filtered through Nidali’s perspective; an omniscient third-person narrator would be wholly outside the story.

D because the story is told from the perspective of *I* and *me* and *my*, indicating that this story is told by Nidali herself rather than from a third-person narrator.

**Question 2. The best answer is J** because Nidali describes how easily her father ignored the tradition of naming a child after the grandfather: “It was an onus he brushed off his then-solid shoulders unceremoniously” (lines 19–20). This implies Baba made this decision quite nonchalantly and without giving it a great deal of thought, brushing it off just as one would a piece of lint or dandruff.

**The best answer is NOT:**

F because while Baba was casual about disregarding this tradition, the grandfather “angrily” penned a letter to Nidali’s father when he found out what had happened (lines 22–24); the grandfather was clearly upset that the tradition wasn’t honored.

G because the lint and dandruff were explicitly called “analogies” (line 21), provided by the grandfather to describe how easily the father ignored tradition; they were not literal.

H because the lint and dandruff were not evidence of the importance of family naming traditions but rather of the ease with which the father ignored those traditions. We know the importance of this tradition from lines 15–19: “Baba, whose name is Waheed and who was known during his childhood as Said, was the only son of the family, so the onus of renaming a son after my grandfather fell squarely upon his shoulders.”
Question 3. The best answer is A because when Mama found out about the baby’s name, even though she’d just given birth, she immediately “got out of bed and walked us to the elevator, the entire time ignoring my baba” (lines 49–50). Baba was yelling at Mama, encouraging her not to be rash, stressing that Nidali was a beautiful name. Mama’s immediate action, combined with Baba’s pleading, suggests her obvious disapproval. However, even though she disapproved of the name, she soon let it go; the narrator says, “Mama must not have fought long” (line 54) because she realized she couldn’t change the name without having to go to a place full of death certificates. Moreover, the narrator kept the name Nidali, which means Mama eventually accepted the name.

The best answer is NOT:

B because although Mama’s reaction to the name (as described above) could be interpreted to contain at least some “annoyance,” she is clearly more disapproving than annoyed. Furthermore, there is no evidence in the story to suggest that she is ever amused by the situation.

C because Mama is never shown to be embarrassed, and her secondary feeling about the name is resignation, not outrage. If she were outraged, it’s fair to assume she would not have given up the fight, and Nidali’s name may have actually been changed.

D because even if it could be said that Mama was “shocked” by the baby’s name, that shock could not be said to turn into resentment; rather, the fact Mama stops fighting about it and lets the baby keep the name makes clear that she is resigned to the name, not resentful about it.

Question 4. The best answer is G because the scene in the seventh paragraph (lines 54–68) did not really occur; it is a fictitious scene the narrator imagines could have happened had Mama pursued her quest to change the name. The narrator sets up the imagined scene by using “who knows” in the first line of the paragraph. She also repeatedly uses “maybe” to imagine the way events might have unfolded.

The best answer is NOT:

F because even though Baba is said to be a purveyor of exaggerated tales, this paragraph is the narrator’s imagining of a scene, not Baba’s telling of a story.

H because this paragraph is not told from Mama’s point of view but rather comes from the perspective of Nidali, the narrator.

J because this paragraph is not a memory at all; it is a scenario that could have happened, as evidenced by the narrator’s use of “who knows” and “maybe.” The narrator could not have remembered events immediately following her own birth, and she is more concerned with the personalities of Baba and Mama than with her own.
Question 5. The best answer is D because although lines 48–53 reveal that Mama is unhappy with the baby’s new name, the next paragraph states that Mama “must not have fought long.” The paragraph imagines everything Mama might have done if she had fought the name, including taking a trip to the clerk’s office, and the narrator concludes that the trip didn’t happen “because I still have my name” (lines 67–68). It is clear that if Mama had actually gone to the clerk’s office, the narrator’s name would have been changed.

The best answer is NOT:

A because Baba never wanted to change the name he had given the baby. That can be seen clearly in lines 51–52, when he pleads with the disapproving mother: “Nidali is a beautiful name, so unique, come on Ruz, don’t be so rash…”

B because it is not a winter storm but summer heat that Nidali imagined might be problematic: Mama “shuddered at the thought of taking me, a newborn, through the heat” (lines 62–63).

C because the story never states or implies anything about how easily Mama might or might not change her mind.

Question 6. The best answer is H because there is an earlier reference to “these stories,” where Nidali says of her father, “I knew he must have embellished. Baba liked to do that: tell stories that were impossible but true all at once, especially if those stories made him look like a rock star” (71–74).

The best answer is NOT:

F because there are no “conflicting” stories about the origins of Nidali’s name; there is simply one story about where her name came from, even if that might be an elaborate or embellished story.

G because the “notebooks and poetry” mentioned in the story are what Baba would have written had he still been a writer, but their subject is not explained in this story; it’s impossible to tell whether they would have been filled with sadness or not.

J because the narrator’s account of her family’s time in Boston isn’t necessarily sad, whereas lines 71–78 make it clear that Baba places his sadness in the stories he tells, and those stories are his famously embellished ones.
**Question 7. The best answer is C** because the narrator says the fact that her father was an architect instead of a writer was “a reality that filled him with great sadness” (lines 77–78); in addition, the narrator notes that the fact the house was filled with toys and dirty socks instead of a piano was something that caused her mother, a musician, “great sadness” (line 86).

*The best answer is NOT:*

A because the passage gives no indication that either feels particular pride in their professional lives. Baba is sad that he is a writer instead of an architect, and Mama is sad that she is a musician “who no longer played music” (lines 81–82).

B because although Baba and Mama are clearly sad about their professional lives, the passage does not link that sadness to anxiety in any way.

D because lines 77–78 and 85–86 make it clear the parents each feel sadness over their professional lives, and sadness does not suggest contentment.

**Question 8. The best answer is F** because the narrator states that Mama is “the most superstitious of all humans (even more than Baba, and to that she’ll attest)” (lines 60–62).

*The best answer is NOT:*

G because lines 60–62 make clear that Mama was more superstitious than Baba.

H because the narrator states that Mama is “the most superstitious of all humans,” which indicates she is more superstitious than Nidali herself.

J because the narrator states that Mama is “the most superstitious of all humans,” which indicates she is more superstitious than Rhonda.

**Question 9. The best answer is D** because the narrator states that “Mama liked to expose him when he told such stories; she was his paparazzo, his story-cop” (lines 79–80). As a story-cop, Mama would be paying attention to the accuracy of details and correcting Baba.

*The best answer is NOT:*

A because by calling Mama a “story-cop,” Nidali is implying that Mama was actively involved in pointing out Baba’s mistruths, not that she was bored by his stories. There is nothing in the passage to indicate that she either yawns or rolls her eyes.

B because Mama couldn’t “expose” Baba or serve as his “story-cop” if she were ignoring him.

C because there is nothing in the passage to suggest Mama participates in Baba’s exaggerations and embellishments; as a “story-cop,” she does the opposite.
Question 10. The best answer is F because in the last paragraph, we see a contrast between home and school: “I knew from the beginning that home meant embellishing, and that’s why I loved school. Teachers were there; they taught us facts based on reality” (lines 87–89).

The best answer is NOT:

G because when the narrator describes Mama as the “true rock star,” it is not to draw a distinction between Mama’s musical skills and Baba’s; instead, the narrator is asserting that although Baba liked to tell stories that made him feel like a rock star, Mama was actually an accomplished musician. The passage makes no claims about Baba being an amateur musician.

H because it inverts what makes Baba happy and sad. Lines 77–78 say he feels a “great sadness” that he is now an architect instead of a writer, not the other way around.

J because it is not text-based; the story never discusses what is required to either write or make music.

Passage II

Question 11. The best answer is D because the entire second paragraph of the passage (lines 8–24) provides examples of all the different laws that were passed to limit automobile use, including those in San Francisco. In addition, lines 4–5 state that “consumers were staying away from the ‘devilish contraptions’ in droves.” All this indicates a great deal of displeasure regarding automobiles and very little support for them.

The best answer is NOT:

A because cars were not affordable at all; lines 25–27 actually state that “the asking price for the cheapest automobile amounted to twice the $500 annual salary of the average citizen.”

B because the passage doesn’t make this assertion. In fact, the passage states that cars were banned from “all tourist areas, effectively exiling them from the city” (lines 23–24).

C because passage A does not detail any public-relations efforts. (Public-relations efforts regarding the Edsel are detailed in passage B.)
Question 12. The best answer is G because lines 12–13 state that “incensed local lawmakers responded with monuments to legislative creativity”: these “monuments” were elaborate legislation, not actual statues or buildings constructed to commemorate something.

The best answer is NOT:

F because the “puddles” mentioned in line 11 are actual puddles cars were getting stuck in.

H because the “bells” mentioned in line 18 were real bells that rang as a warning to alert passersby to the arrival of automobiles.

J because the “hills” cited in line 39 are actual inclines automobiles were having a hard time climbing, not figurative hills the cars were unable to overcome.

Question 13. The best answer is A because the word accessories appears in front of a list of car parts that includes such things as bumpers and headlights, parts most consumers would deem essential. The cheapest automobiles were just four wheels, a body, and an engine; everything else was sold separately—including those parts most people would view as essential.

The best answer is NOT:

B because although the previous paragraph mentions legislation, this paragraph is primarily concerned with a different obstacle: price. The point is that even essential car parts cost extra; there is no indication that the word accessories appeared in legal documents.

C because the passage makes it clear that essentials were deliberately labeled as accessories, which drove up the price for the average citizen. There is no suggestion that those citizens misunderstood these essential car parts to be accessories.

D because none of the car parts listed would be considered a luxury feature. The point is that even the most basic automobiles were prohibitively expensive.
Question 14. The best answer is H because the passage indicates that Ford Motor Company put a lot into the Edsel (18 varieties and a great deal of advertising hype), and lines 70–73 indicate how spectacularly the car failed. “On September 4, 1957, proclaimed by Ford as E-Day, nearly 3 million Americans flocked to showrooms to see the Edsel. Unfortunately, very few of them bought the Edsel.” This indicates the failure happened on a huge scale, while the fact that Ford “pulled the plug” (line 91) on the Edsel after only a few years indicates the failure happened quickly.

The best answer is NOT:

F because only 3 years occurred between the launch of the Edsel and when Ford “pulled the plug” (line 91), which wasn't gradual but quick; in addition, the failure of the Edsel was big news, not something that went unnoticed.

G because the car didn't sell well initially. Lines 87–89 state that Ford predicted 200,000 car sales but only managed 63,110.

J because it is not text-based; the passage does not discuss other automakers.

Question 15. The best answer is D because launching “not one, not two, but 18 varieties of Edsel” (line 44) implies that one or two models might have been reasonable, but eighteen is extreme. Such grandiosity reflects the story of the Edsel overall.

The best answer is NOT:

A because these lines contain no information about any car other than the Edsel.

B because the passage does not reveal any “obligation” on the part of Ford executives to involve consumers; had they done so, perhaps those executives would have found out earlier just how unpopular the new design would be.

C because neither these lines nor the passage as a whole focus on the thoughts of the typical consumer; they focus instead on the thoughts and plans of Ford planners and designers.
Question 16. The best answer is G because lines 84–85 state, “The Edsel was an upscale car launched a couple months after a stock market plunge.” It is clear that the stock market plunge happened before E-Day and the car sales that followed.

The best answer is NOT:

F because E-Day was the day the Edsel was launched. According to lines 84–85, the car was launched after a stock market plunge.

H because the sales numbers of 45,000 and 2,846 happened in the second and third years of the Edsel’s existence, which obviously happened after its launch on E-Day and the preceding stock market plunge.

J because as in H, the sales numbers of 45,000 and 2,846 happened in the second and third years of the Edsel’s existence, which obviously happened after its launch on E-Day and the preceding stock market plunge.

Question 17. The best answer is C because the passage indicates that the Edsel was an “upscale car” (line 84) launched during a recession. The passage goes on to say that “sales of all premium cars plummeted” (lines 85–86) after the stock market plunge led to a recession, with the implication being that upscale and premium cars belonged to the same category and didn’t sell well when much of the country was cutting back on luxuries.

The best answer is NOT:

A because the term premium is not being used to discuss the value of the Edsel today but how the car was marketed at the time of its launch.

B because the word premium was not invented by the makers of Edsel but was used to denote a general class of car, similar to luxury.

D because there is no indication in the passage that this term was used sarcastically by Edsel owners. People did joke that Edsel stood for “Every day something else leaks” (lines 81–82), so it is not unreasonable to think they might have scoffed at the term premium. But there is no specific textual support for D.
Question 18. The best answer is F because passage A focuses on automobiles in San Francisco at the turn of the twentieth century, and passage B focuses on the history of the Ford Edsel, which debuted and died around 1960. Both happened a considerable time ago.

The best answer is NOT:

G because neither passage reveals anything about the author’s experience; both are written in the third person and virtually nothing is known about the writers or their professional backgrounds.

H because neither passage makes an assertion about the automobile’s overall functionality. Passage A focuses on the problems with the first cars in San Francisco, and passage B focuses on the great failure of the Ford Edsel, but neither passage implies cars have contributed little worthwhile throughout their existence.

J because passage A does discuss traffic and road conditions in San Francisco around 1903, but passage B makes no mention of those things in its look at the Ford Edsel.

Question 19. The best answer is A because in passage A, lines 12–13 mention that “incensed local lawmakers responded with monuments to legislative creativity” and the rest of the paragraph highlights various laws passed to deal with the early days of automobiles. Passage B, however, does not address legislation at all.

The best answer is NOT:

B because both passages do discuss the feelings of the general public, including passage A’s emphasis on the antipathy evoked by the first automobiles in San Francisco and passage B’s discussion of the Edsel’s unpopularity with consumers.

C because economics are mentioned in both passages, including the cost of cars in passage A (lines 25–27) and the “stock market plunge” in line 85 of passage B.

D because passage B cites industry experts regarding the problems with the Ford Edsel, but passage A has no such quotations.
**Question 20.** The best answer is G because lines 65–68 state, “The Edsel PR team touted the glories of the cars, but wouldn’t let anybody see them. When they finally released a photo, it turned out to be a picture of . . . the Edsel’s hood ornament.” This illustrates how the Ford people used just a single detail in their marketing. A comparable example would be a picture of a gleaming headlight or a polished door handle.

**The best answer is NOT:**

F because Ford actually showed almost nothing of the car in advertisements, and their ads certainly would not have drawn attention to a potential problem with the car. The cars in Passage A had problems getting up the steep Nineteenth Avenue, a detail that publicity experts likely would have wanted to keep hidden.

H because as stated, Ford’s marketing for the Edsel consisted of talking up the car but actually showing very little of it. Showing the meticulousness of the assembly line would reveal too much of the car.

J because even if it seems an intelligent way to market the cars in passage A, such positive marketing was not evidenced in passage B. The lines cited above indicate the Edsel was marketed based on a single detail and an air of mystery; pictures of an attractive young couple out for a ride would run counter to that “mystery.”

**Passage III**

**Question 21.** The best answer is C because this passage explores Homer’s development as an artist and the various influences on his work, such as the time he spent in Paris ("the artist spent 10 months in the city, which later proved to have a profound effect on his art” (lines 11–13)) and his time in Tynemouth ("he found the subject matter that would inspire him most” (lines 26–27)).

**The best answer is NOT:**

A because the passage is not focused on a single painting. A few paintings are mentioned as illustrations of Homer’s influences, but the passage as a whole is a broader look at Homer’s work.

B because although the passage discusses the effect nature had on Homer’s work, it never discusses an overall relationship between nature and the fine arts. This choice is too broad and leaves out Homer entirely.

D because the passage does not describe “artists” in the plural at all; it focuses exclusively on Homer.
Question 22. The best answer is G because the passage states that Homer “found the subject matter that would inspire him most” in 1881, when he spent the summer in a coastal town and “became enthralled by the dramas of the people who make their living from the ocean” (see lines 25–44). He then spent the last twenty-five years of his life in Maine, where “the sea outside his window now inspired the artist to create what came to be known as his greatest paintings” (lines 68–70). It is clear that the sea and the people working on the sea most interested Homer later in his life.

The best answer is NOT:

F because it was in the 1870s that Homer was painting “his genre subjects: tourist scenes, schoolchildren, and farm life” (lines 24–25). Later in his life, beginning with his move to Tynemouth in 1881, Homer became more interested in the lives of people working on the ocean.

H because Homer might have painted something like this earlier in his career, before the sea became his primary focus.

J because after 1881 Homer became more interested in the lives of people working on the ocean; he might have painted a tourist scene like this earlier in his career.

Question 23. The best answer is A because lines 20–22 state that after Homer returned from Paris, “the weakness of earlier compositions is replaced by a boldness and lucidity in which simple shapes are massed into powerful designs.”

The best answer is NOT:

B because the passage never discusses Homer’s shapes as being particularly “sharp” or “rounded.”

C because the passage does not indicate a shift from dark shapes to light shapes; the passage discusses Homer’s themes as being “dark” but not his shapes.

D because Homer’s later work is described as frequently having “a stark and melancholy atmosphere” (line 9), but his shapes are not described thus, and his earlier works are never described as particularly “uplifting.”
Question 24. The best answer is J because regarding what Homer found in Tynemouth, lines 46–49 state that “the dynamic and dangerous relationship between human activity and natural forces exposed in this setting would occupy Homer for many years to come.” This makes clear that Homer would care about this subject for a long time, which can also be seen in the fact he moved to a similar area in Maine when he returned to the United States.

The best answer is not:

F because the passage explicitly states that Homer would focus on these things “for many years to come” (lines 48–49).

G because the passage makes it clear that Homer’s time in Tynemouth influenced the work he did for the rest of his life.

H because even if Homer did feel a fascination for what he found at Tynemouth for “a long time,” the passage never mentions whether Homer returned there.

Question 25. The best answer is B because lines 39–46 explain that what “enthralled” Homer in Tynemouth was “the fisherman’s wives staring out to sea as they wait for their men, the launch of the lifeboat to rescue sailors from a foundering ship, the agonizingly fragile fishing boats being tossed on angry waves.” Those scenes featuring the interplay between the sea and the lives of fishermen and their families thus became the inspiration for his works.

The best answer is not:

A because though lines 30–33 state that Homer may have gone to Tynemouth to look for the sorts of tourists and bathers he’d successfully painted back in New Jersey, the rest of the paragraph makes it clear that he ultimately was inspired by something else in Tynemouth.

C because Homer’s time in Tynemouth had little to do with farmers but a great deal to do with fisherman.

D because in Tynemouth, Homer was said to have found a “dynamic and dangerous” (line 46) relationship between humans and the sea, not anything particularly “soothing.”
Question 26. The best answer is F because it’s clear that Homer enjoyed some success before moving to Tynemouth (for example, his work had already been displayed in Paris at the Great Exposition in 1867), but what he found there obviously became the foundation for the rest of his career. “Here at last was a subject matter that matched the artist’s deepest feelings” (lines 44–46). It was this subject matter that most moved him and led to his greatest success.

The best answer is NOT:

G because the passage never discusses Homer’s feelings about his work being displayed in Paris.

H because Homer’s visiting the Caribbean later in life is mentioned as being evidence that he continued to travel; along with the information about his family, this is meant to show that Homer was not a recluse. The passage does not mention what effect, if any, the Caribbean might have had on his work.

J because the passage suggests that Homer never got over his sense of melancholy about the world; as lines 8–9 state, even his later work was “imbued with a stark and melancholy atmosphere.”

Question 27. The best answer is B because lines 17–22 state that Homer’s viewing of Japanese art in Paris had an immediate effect on him. When he returned to the United States, the “weakness of earlier compositions [was] replaced by a boldness and lucidity . . .”

The best answer is NOT:

A because lines 17–22 indicate the changes Homer made were dramatic, not subtle.

C because lines 17–22 indicate the changes Homer made were dramatic and immediate, not imperceptible.

D because though Homer’s work got stronger after Paris, his subject matter didn’t change until he went to Tynemouth (lines 23–27).

Question 28. The best answer is F because lines 68–70 state that “the sea outside his window now inspired the artist to create what came to be known as his greatest paintings,” with the remainder of the final paragraph emphasizing this acme in Homer’s career, which occurred when he was living on the Maine coast.

The best answer is NOT:

G because the last paragraph focuses not on the grandeur of humans but the grandeur of nature, what lines 85–86 describe as “haunting evocations of the eternal power of the ocean.”

H because the paragraph does not specifically discuss the best way to paint water. It is instead a broader look at the culmination of Homer’s influences and skills.

J because the effect these paintings had on the author is not clear; the passage does not include the thoughts or feelings of the author.
Question 29. The best answer is D because lines 30–33 state that, regarding Homer’s decision to go to Tynemouth, “It is possible that he was searching for a town filled with the type of tourists and bathers that made his paintings of the Jersey shore successful back home.”

The best answer is NOT:

A because there is no indication in the passage that Homer was “returning” to Tynemouth at all; it’s not clear from the passage whether he’d ever been there. The passage does not specify what inspired Homer to become a painter in the first place.

B because it is not text-based. The passage makes no mention of “distractions” Homer faced in Paris.

C because lines 30–33 make clear that in Tynemouth Homer was looking for a place similar to the Jersey shore, not that he needed a break from it.

Question 30. The best answer is J because lines 66–67 are explicit about what could irk Homer when he was painting: “he could be extremely short-tempered when interrupted.”

The best answer is NOT:

F because lines 66–67 clearly state that Homer could get annoyed if he was interrupted, but the passage says nothing about him being bothered by how well his paintings were or were not selling.

G because it is inconsistent with the passage to imply Homer would be upset by storms; storms at sea were the very subjects he came to love painting. Moreover, there is no evidence in the passage that Homer painted outside.

H because it is inconsistent with the passage to imply Homer would be upset by the rough sea; it was one of the subjects he loved painting later in life.

Passage IV

Question 31. The best answer is B because the first paragraph describes the discovery of planets in general, while the second paragraph switches focus to scientists’ search for “a hint of the familiar: planets resembling Earth” (lines 18–19). This is the focus of the rest of the passage.

The best answer is NOT:

A because the passage does not actually “raise the question” about whether exoplanets exist. The second sentence clearly explains that they do: “To date, astronomers have identified more than 370 ‘exoplanets’” (lines 4–5).

C because though the passage describes the search for planets, no such definition of the term planets is provided, and no distinction is made between planets in Earth’s solar system and more distant planets that might be familiar only to astronomers.

D because the passage doesn’t really refer to mythology at all, beyond a passing mention of Icarus.
Question 32. The best answer is G because the passage is peppered with figurative language. For example, lines 23–27 state, “To see a planet as small and dim as ours amid the glare of its star is like trying to see a firefly in a fireworks display; to detect its gravitational influence on the star is like listening for a cricket in a tornado.”

The best answer is NOT:

F because there are no rhetorical questions in the passage.

H because no such excerpts are found in the passage.

G because none of these excerpts are found in the passage either.

Question 33. The best answer is D because the first paragraph mentions a number of such worlds, including “an Icarus-like ‘hot Saturn’” (lines 6–7) whose year is only three days long and the many “floaters” (line 17) that languish in space. It is amid this exotica, these planets so unlike our own, that scientists search for “the familiar: planets resembling Earth” (line 19).

The best answer is NOT:

A because the term *exotica* is part of the larger phrase “amid such exotica” in line 18, thus referring back to the worlds mentioned in the first paragraph. At this point, there has been no discussion of the technology used to identify these planets.

B because the planets mentioned in the first paragraph (the “exotica”) orbit stars “other than the sun” (lines 5–6). These are planets outside our solar system.

C because there are no such overblown claims in this passage; although the passage makes statements about distant worlds that could be considered strange or unusual, nothing in the passage indicates those claims are exaggerated or untrue.

Question 34. The best answer is J because the second paragraph makes clear just how difficult it would be to find a planet like Earth, equating that task to seeing a “firefly in a fireworks display” (line 25) or hearing a “cricket in a tornado” (lines 26–27). Although the remainder of the passages focuses on those efforts, this paragraph emphasizes just how difficult the task itself is.

The best answer is NOT:

F because there is no evidence in the second paragraph to support the idea that scientists were disappointed by recently discovered exoplanets.

G because the paragraph doesn’t actually mention exoplanets that were once thought to be stars at the center of solar systems.

H because there is no evidence in the second paragraph to support a claim about such a discovery; in fact, it is reasonable to infer the opposite from this paragraph because planets resembling Earth are so difficult to detect.
**Question 35.** The best answer is B because lines 33–37 state, “Most of the others [exoplanets] have been detected by using the spectroscopic Doppler technique, in which starlight is analyzed for evidence that the star is being tugged ever so slightly back and forth by the gravitational pull of its planets.”

The best answer is NOT:

A because lines 33–37 make it clear that it is “gravitational pull” that the Doppler technique detects, not light intensity.

C because lines 33–37 make it clear that the Doppler technique detects gravitational pull, not rotational speed.

D because lines 33–37 make it clear that the Doppler technique detects gravitational pull, rather than directly measuring the distance between an exoplanet and its former sun.

**Question 36.** The best answer is J because according to lines 74–76, “Kepler scientists won’t announce the presence of a planet until they have seen it transit at least three times,” meaning confirmation doesn’t occur until they’ve seen the slight dimming three times.

The best answer is NOT:

F because lines 62–63 state that “Kepler is essentially just a big digital camera,” and lines 65–66 say that the camera works by “capturing the light of more than 100,000 stars in a single patch of sky.” This makes clear that Kepler focuses on light, not on water in any form.

G because the Kepler does not look for uninterrupted light; it instead looks for interrupted light, including “the slight dimming that could signal the transit of a planet” (lines 69–70).

H because the passage indicates scientists will announce the presence of a planet when they see it transit at least three times, “a wait that may be only a few days or weeks” (line 76).

**Question 37.** The best answer is C because lines 31–33 explicitly answer this question: “Only 11 exoplanets, all of them big and bright and conveniently far away from their stars, have as yet had their pictures taken.”

The best answer is NOT:

A because lines 4–5 say that 370 exoplanets have been “identified,” but lines 31–33 make it clear that only eleven have been photographed.

B because 95 is the number in the passage associated with the capabilities of the Kepler camera; it has nothing to do with the number of exoplanets that have been photographed.

D because lines 31–33 clearly state that eleven exoplanets have been photographed.
Question 38. **The best answer is F** because lines 64–67 explain that the Kepler “makes wide-field pictures every 30 minutes, capturing the light of more than 100,000 stars in a single patch of sky between the bright stars Deneb and Vega.”

**The best answer is NOT:**

G because the Kepler doesn’t determine the distance between an exoplanet and its stars, just the possible existence of such an exoplanet by any “slight dimming” (line 69) of light in space.

H because it is not text-based. The passage mentions the “hot Jupiter” (line 10) that is 150 light years from Earth but never uses that distance in any discussion of the Kepler.

J because the passage discusses the Kepler’s ability to detect the possible presence of exoplanets through pictures that reveal a slight dimming of light in space; there is no indication that the Kepler can identify the presence of water on the surface of these planets.

Question 39. **The best answer is A** because lines 64–67 explain that the Kepler “makes wide-field pictures every 30 minutes, capturing the light of more than 100,000 stars in a single patch of sky between the bright stars Deneb and Vega,” marking these stars as the edges of the examined area.

**The best answer is NOT:**

B because Deneb and Vega are identified as stars, not planets. The figure 70% relates to the exoplanets discovered by the French COROT satellite (“seven transiting exoplanets, one of which is only 70% larger than Earth”).

C because lines 64–67 are explicit that Deneb and Vega are stars in space, not scientists.

D because there is no indication in the passage that Deneb and Vega are “former” stars.

Question 40. **The best answer is H** because lines 78–80 state, “By combining Kepler results with Doppler observations, astronomers expect to determine the diameters and masses of transiting planets.”

**The best answer is NOT:**

F because lines 78–80 are explicit that it is “diameters and masses” those combined technologies can find, not the length of its year.

G because lines 78–80 are explicit that it is “diameters and masses” those combined technologies can find, not the distance from its sun.

J because lines 78–80 are explicit that it is “diameters and masses” those combined technologies can find, not its distance from Earth.
Passage I

1. **The best answer is A.** According to the passage, the percent relative reflectance shown in Figure 2 is based on a comparison to a standard with 100% reflectance. The higher the percent reflectance, the brighter the soil. According to Figure 2, the highest average percent relative reflectance was 70% measured at an inland distance of 0 km. In other words, this measurement was made at the coastal site, so A is correct. **B** is incorrect; 50 km inland the percent reflectance was less than 25%. **C** is incorrect; 100 km inland the percent reflectance was near 0%. **D** is incorrect; 150 km inland the percent reflectance was close to 10%.

2. **The best answer is H.** According to Figure 1, the average relative brightness of the dorsal stripe was 0.25 at an inland distance of approximately 60 km. **F** is incorrect; 20 km inland the brightness was greater than 0.75. **G** is incorrect; 40 km inland the brightness was greater than 0.75. **H** is correct; 60 km inland the brightness was 0.25. **J** is incorrect; 80 km inland the brightness was less than 0.25.

3. **The best answer is C.** According to Figure 1, on the graph representing the brightness of the fur on the rostrum, the line is steepest between inland distances of 50 km and 65 km, indicating that this is where there was the greatest change in the average relative brightness of the fur on the rostrum. **A** is incorrect; between 0 km and 25 km inland, the brightness decreased by a little less than 0.25. **B** is incorrect; between 25 km and 50 km inland, the brightness decreased by less than 0.25. **C** is correct; between 50 km and 75 km inland, the brightness decreased by approximately 0.50. **D** is incorrect; between 100 km and 125 km inland, the brightness increased very slightly.

4. **The best answer is J.** According to Figure 1, 150 km inland the average relative brightness of the ventrum fur was 0 whereas at the coastal site it was 1.00. The fur was brighter at the coastal site than 150 km inland. The fur was darker 150 km inland. **F** and **G** are incorrect; the fur was darker 150 km inland. **H** is incorrect; the relative brightness 150 km inland was less. **J** is correct.

5. **The best answer is B.** In order to answer this item, the examinee must know that natural selection is the survival and reproduction of organisms because of environmental forces that result in favorable adaptations. If the fur pigmentation matches the soil, then it will increase the chances of the mouse’s survival, and it will be more likely to pass these traits on to its offspring. **A** is incorrect; the mouse will be more likely to pass its fur pigmentation traits to its offspring. **B** is correct. **C and D** are incorrect; the mouse would be less likely to be found by a predator.

6. **The best answer is J.** According to Figure 2, the standard had 100% reflectance. Because the soil at the coastal site had an average percent relative reflectance of 70%, the soil was darker than the standard. **F and G** are incorrect; the surface soil at the coastal site was darker than the standard. **H** is incorrect; the average percent relative reflectance of the soil at the coastal site was 70%. **J** is correct.
Passage II

7. The best answer is B. According to Table 1, in Experiment 1, as the reaction time increased, the CNF also increased. When the reaction time was 10 min, the CNF was 6 mg/kg, and when the reaction time was 3 days, the CNF was 39 mg/kg. If a reaction time of 2 days had been tested, then the CNF would most likely have been between 6 mg/kg and 39 mg/kg. A is incorrect; the CNF would have been greater than 6 mg/kg. B is correct. C and D are incorrect; the CNF would have been less than 39 mg/kg.

8. The best answer is F. According to Table 1, the lowest concentration of dissolved nickel in the filtrate was found in Trial 1 (CNF = 6 mg/kg). In Trial 1, the reaction time was 10 min and the standard filtration method was used. F is correct. G is incorrect; a CNF of 42 mg/kg was measured when the reaction time was 7 days and the standard filtration method was used. H is incorrect; a CNF of 58 mg/kg was measured when the reaction time was 10 min and the vacuum filtration method was used. J is incorrect; a CNF of 73 mg/kg was measured when the reaction time was 7 days and the vacuum filtration method was used.

9. The best answer is C. In order to answer this item, the examinee must know that applying a vacuum will increase the net force on the mixture in the funnel. The net force exerted on the mixture was greater in Trial 6 than in Trial 3, because the vacuum filtration technique was used in Trial 6. A and B are incorrect; the net force exerted on the mixture in the funnel was most likely less in Trial 3. C is correct. D is incorrect; the filtration apparatus was connected to a vacuum pump in Trial 6.

10. The best answer is G. According to the passage, the solutions were mixed, the mixture was stirred, the solid was recovered by filtration, and then the CNF was measured. F is incorrect; measuring the CNF was the last step. G is correct. H and J are incorrect; mixing the solutions was the first step.

11. The best answer is D. According to Table 1, when the reaction time was 3 days and vacuum filtration was used, the CNF was 69 mg/kg (Trial 5). When the reaction time was 10 min and vacuum filtration was used, the CNF was 58 mg/kg (Trial 4). The data do support the student’s prediction that the CNF will be greater for 3 days and vacuum filtration than for 10 min and vacuum filtration. A and B are incorrect; the data do support the student’s prediction. C is incorrect; Trials 1 and 2 both involved standard filtration, not vacuum filtration. D is correct.

12. The best answer is G. According to the passage, only Trials 1, 2, and 3 used standard filtration. In Trial 2, the reaction time was 3 days, and in Trial 3, the reaction time was 7 days. The reaction time for Trial 1 was only 10 min. F is incorrect; in both Trials 2 and 3 the solid was recovered by standard filtration after a reaction time of at least 3 days. G is correct. H and J are incorrect; in only 2 trials was the solid recovered by standard filtration after a reaction time of at least 3 days.
13. **The best answer is A.** In order to answer this item, the examinee must recognize that the stoichiometry of the balanced chemical equation shows that 2 hydroxide ions are needed to produce 1 formula unit of the monohydrate. If 6 hydroxide ions are used, then 3 formula units of the monohydrate will be produced. **A** is correct. **B, C, and D** are incorrect; there is a 2:1 ratio between hydroxide and the product. If 6 hydroxide ions are used, then 3 monohydrates will be produced.

**Passage III**

14. **The best answer is G.** According to the passage, the protostar’s gravitational field attracts gas. This indicates that gravity accelerates gas particles inward, toward the center of the protostar. The passage also states that RP causes gas to be pushed away. This indicates that RP will accelerate gas particles outward, relative to the center of the protostar. **F** is incorrect; RP will accelerate gas particles outward. **G** is correct. **H** is incorrect; gravity will accelerate particles inward, and RP will accelerate particles outward. **J** is incorrect; gravity will accelerate particles inward.

15. **The best answer is B.** According to Scientist 2, a disk of gas that forms at the protostar’s equator reduces the effect of RP in that plane, allowing gas to accrete. This gas will therefore accrete near the equator. **A** is incorrect; the effect of RP is decreased there. **B** is correct. **C and D** are incorrect; the gas particles will likely accrete near the equator.

16. **The best answer is H.** According to the passage, Scientist 1 and Scientist 2 both think that stellar mergers are likely and use these to explain how certain size protostars form. Scientist 3 claims that stellar mergers are very unlikely. The lack of evidence of stellar mergers is most inconsistent with the arguments of Scientists 1 and 2. **F** is incorrect; the information is also inconsistent with the argument of Scientist 2. **G** is incorrect; the information is consistent with the argument of Scientist 3. **H** is correct. **J** is incorrect; the information is also inconsistent with the argument of Scientist 2 and is consistent with the argument of Scientist 3.

17. **The best answer is C.** According to the passage, Scientist 1 states that the maximum mass of a star formed by accretion is 20 M☉. It would take six of these stars to make Eta Carinae. Scientist 2 states that the maximum mass of a star formed by accretion is 40 M☉. It would take three of these stars to make Eta Carinae. Scientist 3 states that the maximum size is limited only by the amount of gas available; therefore, Eta Carinae could have been formed entirely by accretion. **A and B** are incorrect; Scientist 1 would say that 5 stars would merge to form a star with a maximum mass of only 5 × 20 M☉ = 100 M☉. **C** is correct. Scientist 1 would say that 6 stars would merge to form a star with a maximum mass of 6 × 20 M☉ = 120 M☉. Scientist 2 would say that 3 stars would merge to form a star with a maximum mass of 3 × 40 M☉ = 120 M☉. Scientist 3 would say that 1 star could form Eta Carinae if there was enough gas available. **D** is incorrect; Scientist 2 would say that the minimum number of stars that could merge to form Eta Carinae is 3.
18. The best answer is H. According to the passage, Scientist 1 states that the most massive star that can form from accretion would have a mass of 20 $M_S$. Scientist 2 states that the most massive star that can form from accretion would have a mass of 40 $M_S$. A star with a mass that is greater than 20 $M_S$ but less than or equal to 40 $M_S$ would support Scientist 2’s argument, but weaken Scientist 1’s argument. F and G are incorrect; observations of these stars would not weaken the arguments of either Scientist 1 or Scientist 2. H is correct. J is incorrect; an observation of this star would weaken the arguments of both Scientist 1 and Scientist 2.

19. The best answer is A. According to the passage, both Scientists 2 and 3 agree that a disk of gas forms because the protostar rotates about its axis. A is correct; the protostar’s motion (rotation) is responsible for the formation of the disk. B is incorrect; the emission of radiation does not cause the formation of the disk. C is incorrect; the location within a star cluster might affect the likelihood of a stellar merger but will not cause the formation of the disk. D is incorrect; a stellar merger will create a more massive star but is not responsible for the formation of the disk.

20. The best answer is H. According to the passage, 1 $M_S$ is the mass of the Sun. Scientist 1 states that the maximum mass of a star formed by accretion is 20 $M_S$. Scientist 2 states that the maximum mass of a star formed by accretion is 40 $M_S$. Scientist 3 claims that the maximum mass of a star depends on the amount of available gas. All three scientists would agree that a star with a mass of 1 $M_S$ could form entirely by accretion, assuming enough gas is present to form the sun. F, G, and J are incorrect; all three scientists would agree. H is correct.

Passage IV

21. The best answer is D. According to Figure 1, as the percent vermicompost increased, the average yield for *S. lycopersicum* increased and then decreased. Figure 2 shows that as the percent vermicompost increased, the average yield for *C. annuum* also increased and then decreased. A, B, and C are incorrect; the yield for both increased and then decreased. D is correct.

22. The best answer is F. According to Table 1, Mixture 1 had 0% compost. This mixture would serve as a control so that the scientists could determine the effect that vermicompost had on the yield. F is correct. G is incorrect; Mixture 2 was 20% vermicompost and would not serve as the control. H is incorrect; Mixture 4 was 60% vermicompost and would not serve as the control. J is incorrect; Mixture 5 was 80% vermicompost and would not serve as the control.

23. The best answer is B. In order to answer this item, the examinee must know how to convert units. According to Figure 1, in Study 1, the average yield for Mixture 5 was 3,500 g/plant. This is equal to $3,500 \text{ g/plant} \times \frac{1 \text{ kg}}{1,000 \text{ g}} = 3.5 \text{ kg/plant}$. A, C, and D are incorrect; B is correct.
24. **The best answer is G.** According to the passage, both studies used thirty-six 2 L pots. The type and number of seeds used in each study was different, and the amounts of time that the plants were allowed to grow were different. The number of pots used per mixture and the volume of each pot were the same in both studies. 
   
   F, H, and J are incorrect; the length of time needed to perform Study 1 was 158 days, and the length of time needed to perform Study 2 was 149 days. 
   
   G is correct; the number of pots used per mixture and the volume of each pot were the same in both studies.

25. **The best answer is A.** According to Figure 1, *S. lycopersicum*, a tomato plant, had its greatest average yield in Mixture 2, which was 20% vermicompost. According to Figure 2, *C. annuum*, a pepper plant, had its greatest average yield in Mixture 3, which was 40% vermicompost. The statement is consistent with the results of the studies. 
   
   A is correct. 
   
   B is incorrect; in Study 1 the greatest average yield was attained with Mixture 2. 
   
   C and D are incorrect; the statement is consistent with the results of Studies 1 and 2.

26. **The best answer is J.** According to the passage, in Study 1, after 28 days all the seedlings except 1 were removed from each pot. In Study 2, the seedlings were removed after 42 days. 
   
   F is incorrect; more than one seed was planted per pot in both studies. 
   
   G is incorrect; the seedlings were not planted. 
   
   H is incorrect; all but one seedling was removed from each pot. 
   
   J is correct.

27. **The best answer is D.** In order to answer this item, the examinee must know the overall chemical reaction for photosynthesis. Carbon dioxide, water, and sunlight are used to produce oxygen and glucose. 
   
   A is incorrect; carbon dioxide is a reactant. 
   
   B is incorrect; glucose is a product. 
   
   C is incorrect; oxygen is a product. 
   
   D is correct.

**Passage V**

28. **The best answer is H.** According to the passage, in Study 1, the students varied the direction and magnitude of E (the electric field). In Study 2, the students varied V (electric potential). 
   
   F is incorrect; electric potential was varied in Study 2. 
   
   G is incorrect; plate length was varied in Study 3. 
   
   H is correct. 
   
   J is incorrect; plate length was varied in Study 3.

29. **The best answer is B.** According to Table 2, as V increased, y decreased. When 
   
   \[ y = 3.2 \text{ cm}, \quad V = 1.0 \text{ kV} \]  
   
   and when 
   
   \[ y = 2.1 \text{ cm}, \quad V = 1.5 \text{ kV} \] 
   
   It follows that if 
   
   \[ y = 2.6 \text{ cm}, \quad V = \text{no value} \] 
   
   then V would have some value between 1.0 kV and 1.5 kV. 
   
   A is incorrect; V would have been greater than 1.0 kV. 
   
   B is correct. 
   
   C and D are incorrect; V would have been less than 1.5 kV.

30. **The best answer is J.** In Figure 2, the spot was located at approximately +3 cm. 
   
   According to Tables 1 and 2, the trials with spots in this position were Trial 4 and Trial 8 (both at +3.2 cm). 
   
   F is incorrect; \( y = -3.2 \text{ cm} \) in Trial 1. 
   
   G is incorrect; Trial 4 also had \( y = +3.2 \text{ cm} \). 
   
   H is incorrect; \( y = -3.2 \text{ cm} \) in Trial 1. 
   
   J is correct.
31. The best answer is C. According to Table 1, when $E$ had an upward direction, $y$ was negative; when $E$ had a downward direction, $y$ was positive. Table 2 shows that in Study 2, $y$ was positive, indicating that $E$ had a downward direction. Table 3 shows that in study 3, $y$ was negative, indicating that $E$ had an upward direction. A, B, and D are incorrect; $E$ most likely pointed downward in Study 2 and upward in Study 3. C is correct.

32. The best answer is G. According to the passage, in Studies 1 and 2 only, $V$ and $E$ were varied and therefore one CRT with $L = 2.5$ cm could be used. In Study 3, $L$ was varied, including one trial with $L = 2.5$ cm. Because five different $L$ values were tested and because $L$ cannot be varied from outside the tube, five different CRTs must have been used. F, H, and J are incorrect; a minimum of five CRTs were required. G is correct.

33. The best answer is B. According to the results of Study 1, as the magnitude of $E$ increased, the farther the spot was from $y = 0$ cm. According to the results of Study 2, as $V$ increased, $y$ decreased. In order to have $y = 0$ cm, $V$ should be nonzero and the magnitude of $E$ should be zero. A is incorrect; $V$ should be nonzero. B is correct. C is incorrect; $V$ should be nonzero. D is incorrect; the magnitude of $E$ should be zero.

34. The best answer is J. In order to answer this item, the examinee should know that charges of like sign repel each other and charges of opposite sign attract each other. According to Figure 1, the cathode ray is deflected upward (toward the top plate and away from the bottom plate). Because like charges repel one another and because the cathode ray is negatively charged, the bottom plate must be negatively charged. F and G are incorrect; the cathode ray is deflected toward the top plate and therefore the top plate must be positively charged. H is incorrect; charges of like sign repel one another. J is correct.

Passage VI

35. The best answer is D. According to Figure 2, when $N = 15 \times 10^{23}$ atoms, Xe had the shortest $\lambda$, followed by Kr, Ar, and Ne. A and B are incorrect; Ne had the longest $\lambda$. C is incorrect; Kr had the second shortest $\lambda$. D is correct.

36. The best answer is G. According to Figure 2, when $N$ for Ne was equal to $6 \times 10^{23}$ atoms, $\lambda = 1,600$ nm and when $N$ for Ne was equal to $12 \times 10^{23}$ atoms, $\lambda = 800$ nm. When the Ne sample size doubled, $\lambda$ was reduced by half. F, H, and J are incorrect; $\lambda$ was multiplied by $\frac{1}{2}$. G is correct.

37. The best answer is C. According to Figure 1, as $V$ increases, $\lambda$ also increases. When $V = 5$ L, $\lambda$ was approximately 50 nm and when $V = 10$ L, $\lambda$ was approximately 100 nm. Based on this trend, if $V$ is doubled from 25 L to 50 L, then $\lambda$ should also double. A and B are incorrect; $\lambda$ for the 50 L sample should be greater than $\lambda$ for the 25 L sample. C is correct. D is incorrect; $\lambda$ only increases by 2 times when $V$ is doubled.
38. **The best answer is J.** According to Figure 1, when $V = 20 \text{ L}$, $\lambda$ for Xe is approximately 175 nm and $\lambda$ for Ar is approximately 375 nm. Thus, $\lambda$ for Ar is approximately 200 nm longer than $\lambda$ for Xe. F, G, and H are incorrect; the difference is closest to 200 nm. J is correct.

39. **The best answer is A.** If the atoms have the same average speed, then the sample with the shortest $\lambda$ (distance between collisions) will have the highest collision frequency. Figure 1 shows that Xe atoms in the 5 L sample have a shorter $\lambda$ than atoms in the 25 L sample. A is correct; the atoms in the 5 L sample travel a shorter distance between collisions. B is incorrect; the atoms in the 5 L sample travel a shorter distance between collisions. C and D are incorrect; the atoms in the 25 L sample would have a lower collision frequency.

40. **The best answer is F.** According to Figure 2, for any given $\lambda$, the lower the value of $d$, the greater the value of $N$. When $\lambda = 320 \text{ nm}$ for Xe, there are fewer than $6 \times 10^{23}$ atoms of Xe present. Because $d$ for Rn is greater than that for Xe, it follows that there are also fewer than $6 \times 10^{23}$ atoms of Rn present. F is correct. G, H, and J are incorrect; there will be fewer than $6 \times 10^{23}$ atoms of Rn present.
Chapter 4: Identifying Areas for Improvement

Your practice test scores alone provide very little insight into what you need to do to improve your score. For example, you may have missed a certain math question because you haven’t yet taken trigonometry or because you misread the question or the answer choices or because you were anxious about finishing the test on time.

When evaluating your performance on any of the practice tests in this book or elsewhere, examine not only whether you answered a question correctly or incorrectly but also why you answered it correctly or incorrectly. Recognizing why you chose the correct or incorrect answer sheds light on what you need to do to improve your score on future practice tests and on the ACT. Perhaps you need to review certain subjects, take a particular course, develop a better sense of how much time to spend on each question, or read questions and answer choices more carefully.

In this chapter, we offer guidance on how to evaluate your performance on ACT practice test 1 in order to identify subject areas and test-taking strategies and skills that you may need to work on. Take a similar approach to evaluate your performance on subsequent practice tests.
Reviewing Your Overall Performance

After you have determined your scores, consider the following questions as you evaluate how you did on the practice tests. Keep in mind that many of these questions require you to make judgment calls based on what you were thinking or the steps you took to decide on the answer choice you selected. The answer explanations in chapter 4 may help you make these determinations, but ultimately you are the only one who can determine why or how you chose the correct or incorrect answer.

Did you run out of time before you completed a test?
If so, read the sections in this book on pacing yourself. See chapter 2 for general advice that applies to all tests, and see chapters 5 through 9 for advice specific to each test. Perhaps you need to adjust the way you use your time in responding to the questions. Remember, there is no penalty for guessing, so try to answer all questions, even if you have to make an educated guess.

Did you spend too much time trying to understand the directions to the tests?
The directions in the practice test are the same directions that will appear in your test booklet on test day. Make sure you understand them now, so you won’t have to spend too much time reading them when you take the test.

Did you rush through the test and make mistakes?
People tend to make mistakes when they are in a hurry. If you had plenty of time remaining at the end of the test but made mistakes, you probably hurried through the test and made errors such as these:

- Misreading a passage
- Misreading a question
- Not reading or considering all answer choices
- Selecting a response that was an incomplete answer
- Selecting an answer that did not directly respond to the question

Did a particular type of question confuse you?
Use the explanatory answers following each practice test to help you identify any mistakes you may have made regarding certain question types or answer choices. The explanatory answers can help you understand why you may have chosen the incorrect answer and avoid making that same mistake again.

Highlighting Strengths and Areas for Improvement on the English Test
The process of scoring your English practice test and reviewing the answer explanations should reveal the reason you chose the correct or incorrect answer for each question. If you
struggled to answer questions on the test because you have not yet acquired certain English language knowledge and skills. Review the questions and your answers closely to determine more specifically what you need to work on.

The English test requires knowledge and skills in several areas. The best way to raise your score is to improve your English language skills, which you can accomplish in the following ways:

- Take an English composition course. Such a course will help you write more clearly, logically, and concisely while developing a better understanding of English punctuation, grammar, and usage conventions.
- Practice your writing skills in other courses. In most courses, including English literature, social studies, speech, and perhaps even science, you have opportunities to practice your writing skills and receive feedback.
- Read well-written publications in the form of books, magazine articles, and online content from reputable sources—material that has been professionally edited. As you read, pay attention to punctuation, grammar, usage, sentence structure, writing strategy, organization, and style to see how a variety of writers express themselves while adhering to the same conventions.
- Practice writing and having your writing edited by an English teacher or someone else who is qualified to provide feedback.

**Test-Taking Skills**

A low test score does not necessarily mean that you lack the English language knowledge and skills required to do well on the test. It may indicate that you rushed through the test and made mistakes, spent too much time on certain questions that you didn't finish, or committed some other test-taking error(s). As you evaluate your answers to determine why you missed certain questions, consider your test-taking strategies and skills. Place a checkmark next to each of the following common test-taking errors you think you need to work on eliminating:

**Worked too slowly:** You may need to improve your reading speed and comprehension or try answering the easy questions first and then returning to the harder questions if time remains.

**Rushed through the test:** If you finished with plenty of time remaining but made mistakes, you may need to spend more time reading and understanding the passages, reading the questions, or carefully considering all of the answer choices.

**Misread passages:** If you missed questions because of misreading or misinterpreting passages, work on your reading comprehension. Try reading more carefully and rereading when you do not fully understand a passage.

**Misread questions:** Every question points to the correct answer, so read questions carefully and make sure you understand what a question is asking before you choose your answer.
Did not consider all answer choices: If you tend to select the first answer choice that seems to be correct, try considering all answer choices before making your final selection. A good way to double-check an answer is to find reasons to eliminate the other three choices.

Did not consider the writing style: The entire passage conveys the author’s overall writing style, which you may need to consider when answering certain style-related questions.

Did not consider a question’s context: Writing strategy and organization questions often require consideration of surrounding text. You may need to skim the passage first before answering these questions or read one or two sentences before or after the sentence in question.

Did not account for a word’s connotations: Many words have a denotation (a literal meaning or dictionary definition) and a connotation (a thought or emotion that the word evokes from the reader or listener). To answer some usage questions, you must consider what the word means in the context in which it is used.

Did not connect an underlined portion of text with its corresponding question: The underline portion of the text and the corresponding question work together to point to the correct answer choice, so be sure to consider them both when selecting your answer.

Overlooked differences in the answer choices: Answer choices may differ so subtly that you overlook the differences, so be sure to recognize what’s different about each choice before selecting your answer.

Chose an answer that introduced a new error: Some answer choices correct the error in the underlined text but introduce a new error. Do not fall for this common trap.

Did not choose the best answer: Two or more answers may be correct, but the English test requires that you choose the best answer. Again, consider all answer choices before selecting an answer.

Did not reread the sentence using the selected answer: A great way to double-check an answer is to insert it in place of the underlined text and then reread the sentence to make sure it makes sense.

Missed a two-part question: With a two-part question, each of the answer choices typically starts with “yes” or “no” followed by a reason, so you must determine first whether the answer is yes or no and then why. Carefully compare and consider the reasons before making your selection.

Did not consider interrelated questions: A question may be easier to answer after you have answered the next question, so consider skipping back to a question if you feel that answering the current question has given you new insight.

See chapter 5 for in-depth coverage of test-taking strategies and skills that may help to raise your English test score.
Highlighting Strengths and Areas for Improvement on the Mathematics Test

The process of scoring your mathematics practice test and reviewing the answer explanations should reveal your strengths and any areas for improvement. You may discover that you are a whiz at algebra and geometry but are in dire need of a refresher course in trigonometry. Or, you may find that your math knowledge and skills are sound in all areas but you need to work on test-taking strategies to ensure that your test results accurately reflect your knowledge and skills.

Use the checklists in the following sections to flag subject areas and test-taking skills you may need to focus on.

Math Subject Areas

If you struggled to answer questions on the test because you have not yet acquired the requisite math language knowledge and skills, review the questions and your answers closely to determine more specifically what you need to work on.

Your performance on the ACT mathematics test may be affected by your ability to handle certain types of questions. For example, you may breeze through straightforward, basic math questions but get tripped up by word problems. As you evaluate your performance on mathematics practice test 1, try to identify the types of questions you struggle with most:

- **Basic math**: These questions are straightforward with very little text. You just need to do the math.
- **Basic math in settings**: These are word problems that challenge your ability to translate the problem into one or more mathematical equations and then solve those equations.
- **Very challenging math problems**: These can be basic math or basic math in settings questions that challenge your ability to reason mathematically and perhaps draw from your knowledge of more than one math subject area to solve them. In addition to the differences in how math problems are presented, you may encounter questions sets—two or more sequential math problems related to the same information.

Test-Taking Errors

Incorrect or unanswered questions on the practice test may be less of a reflection of your math knowledge and skills and more a reflection of your test-taking strategies and skills. As you review your scores and answers, try to determine whether you committed any of the following common test-taking errors:

- **Worked too slowly**: If you answered questions correctly but your score suffered from unanswered questions because you ran out of time, you may simply need more practice to improve your speed.
- **Rushed through the test**: If you finished with plenty of time remaining but made mistakes, you may need to spend more time reading and understanding the questions and doing the math before selecting an answer.
Got stuck on a very challenging question: Answering the easy questions first and then returning to the harder questions later may help you address this issue.

Misread the question: The question contains all information you need to answer it. Misreading the question may cause you to extract and use the wrong information in your calculations or calculate an answer for something other than what the question directed.

Overlooked information in the answer choices: Answer choices often provide clues as to what form the answer is in. A glance at the answer choices can often clarify what the question is asking for.

Overlooked or misinterpreted information in an image: Many math questions include an image, table, or graph that provides key information. Misreading an image will lead you to select the wrong answer choice.

Did not use logic to solve a problem: Math questions, especially the very challenging ones, often test your ability to reason through problems.

Not doing the math: Although you are not required to show your work on the test, consider writing out your calculations to double-check your reasoning and avoid mental errors. Also, when a question includes an image, consider writing any dimensions provided in the question on to the image so that the image contains all of the measurements you have to work with.

Not double-checking your answers: For many questions, you can insert the answer you think is correct into the equation provided and do the math to double-check the answer choice. Take the opportunity to double-check answers when given the opportunity.

For math test strategies and tips, turn to chapter 6.

Highlighting Strengths and Areas for Improvement on the Reading Test

The process of scoring the reading practice test and reviewing the answer explanations should reveal the reason you chose the correct or incorrect answer for each question. Reasons for choosing wrong answers or struggling with certain questions can be classified in three categories:

Subject matter
The type of passage—prose fiction, humanities, social studies, or science—may affect your ability to read and comprehend the passage and answer questions about it. For example, you may have no trouble answering questions about fact-based passages in social studies and science but struggle reading and understanding prose fiction.

Reading skills
The reading test is designed to evaluate numerous skills, including the ability to identify details in the text, draw generalizations about those details, and understand the meaning of
a word or phrase based on how it is used in a sentence. In addition, each passage challenges you to read quickly and with understanding.

**Test-taking strategies and skills**

Not reading the entire passage, misreading the question or answer choices, and not verifying an answer choice with the passage can all lead to careless mistakes.

Use the checklists in the following sections to flag the types of reading passages, reading skills, and test-taking strategies and skills you may need to focus on.

**Types of Reading Passages**

Your ability to comprehend reading passages and answer questions about them may vary based on the type of passage. For example, if you are accustomed to reading science books and articles, you are probably familiar with many of the concepts and vocabulary in the science passages on the test; therefore, you might expect to have no trouble reading, comprehending, and answering questions about such passages. However, if you have read very little fiction, you may find it challenging to identify the plot (sequence of events), draw conclusions about characters, or sense the mood that a passage is intended to evoke. In short, you may struggle more with certain types of reading passages than with others.

As you score your reading test and review the answer explanations, use the following checklist to flag any types of reading passages you found particularly challenging (the passage type is indicated at the beginning of each passage on the test):

**Prose fiction**: Passages from short stories or novels

**Social studies**: Passages that cover topics such as anthropology, archaeology, biography, business, economics, education, geography, history, political science, psychology, and sociology

**Humanities**: Articles about topics including architecture, art, dance, ethics, film, language, literary criticism, memoir, music, personal essays, philosophy, radio, television, and theater

**Natural science**: Passages related to subjects such as anatomy, astronomy, biology, botany, chemistry, ecology, geology, medicine, meteorology, microbiology, natural history, physiology, physics, technology, and zoology

**Reading Skills Tested**

The ability to read, comprehend, and answer questions about passages involves numerous skills. Questions on the test are written specifically to evaluate these skills. As you review the answer explanations, place a checkmark next to any of the following skills you think you need to develop more fully:

**Identify and interpret details**: Nearly all questions require an ability to identify and interpret details from the passage that supports whichever answer choice you select. Many questions specifically state, “According to the passage, …” This skill is essential for performing well on the reading test.
Identifying Areas for Improvement

Determine the main idea of a paragraph(s) or passage: A few questions may require an ability to recognize the general meaning or point of one or more paragraphs.

Understand comparative relationships (comparison and contrast): Questions may ask about comparisons and contrasts made in the passage.

Understand cause-effect relationships: Some reading passages explore cause-effect relationships. Others are accompanied by questions that more subtly test your ability to identify cause-effect relationships.

Make generalizations: To answer many reading questions, you must be able to draw conclusions from or make generalizations about details provided in the passage.

Determine the meaning of words or phrases from context: You are likely to encounter several questions on the ACT reading test that challenge you to determine the meaning of a word or phrase based on the context in which it is used.

Understand sequences of events: A few reading test questions may require an ability to read and comprehend a series of events.

Draw conclusions about the author’s voice and method: You may be asked to get into the mind of the author and figure out what his or her attitude, purpose, or method is.

For more about reading skills tested, including examples of the types of questions used to evaluate these skills, turn to chapter 7.

Test-Taking Errors

Even if your reading speed and comprehension are solid, you may miss questions by committing one or more of the following common test-taking errors. Place a checkmark next to each error you think you may be susceptible to making:

Read too slowly or too quickly: By reading too slowly, you may not have sufficient time to read all passages and answer all questions. However, reading too quickly may result in errors or having to return to a passage several times to locate the evidence needed to decide which answer choice is correct.

Did not read the entire passage: Skim-reading a passage is useful for understanding what a passage is about, but it often results in overlooking the details required to answer specific questions. Read the entire passage word-for-word.

Misread the question: Questions, especially those that contain the word NOT, can be tricky. Make sure you understand what a question is asking as you evaluate the various answer choices.

Misread or overlooked an answer choice: Misreading an answer choice or not considering all answer choices can result in mistakes. Consider all answer choices and read them carefully.
Did not verify an answer choice with the passage: If time allows, try to verify every answer choice by locating details in the passage that support it. Use the same technique to rule out other answer choices when necessary.

For additional reading test strategies and tips, turn to chapter 7.

Highlighting Strengths and Areas for Improvement on the Science Test

The process of scoring the science practice test and reviewing the answer explanations should reveal the reason you chose the correct or incorrect answer for each question. Reasons for choosing wrong answers or struggling with certain questions can be classified into three categories:

Subject matter
The science test does not require in-depth knowledge of biology, chemistry, earth science, space science, or physics. Nor does it require you to memorize formulas or solve complex math problems. However, questions are presented in the context of these subject areas, and you may need some knowledge of scientific terms or concepts to answer some of the questions.

Question type
Science test questions are presented in three different formats: data representation (graphs, tables, illustrations); research summaries (from experiments); and conflicting viewpoints (alternative theories and hypotheses). You may struggle more with one type of question than with the others.

Test-taking strategies and skills
The science test evaluates your ability to extract and use information presented in a variety of formats to solve problems and answer questions. Even if you are highly skilled and knowledgeable in all science subject areas, your score will suffer if you make careless mistakes or are so careful that you run out of time before answering all of the questions.

Use the checklists in the following sections to flag the subject areas, question types, and test-taking strategies and skills you may need to focus on.

Subject Matter
You may benefit from identifying subject areas in which you struggle. Use the following checklist to flag subject matter you may need to review:

Biology: Cell biology, botany, zoology, microbiology, ecology, genetics, and evolution

Chemistry: Properties of matter, acids and bases, kinetics and equilibria, thermo-chemistry, organic chemistry, biochemistry, and nuclear chemistry

Earth science: Geology, meteorology, oceanography, and environmental science

Physics: Mechanics, thermodynamics, electromagnetism, fluids, solids, and optics

Space science: Formerly known as astronomy
Types of Science Questions
As you review answer explanations and evaluate your performance on the science test, check to see whether you had more trouble with certain types of science questions than with others. Place a checkmark next to any question types that you found particularly challenging:

Data representation requires you to understand, evaluate, and interpret information presented in graphs, tables, and illustrations.

Research summary requires you to understand, analyze, and evaluate the design, execution, and results of one or more experiments.

Conflicting viewpoints requires you to compare and evaluate alternative theories, hypotheses, or viewpoints on a specific observable phenomenon.

For more about these different question types and guidance on how to approach them effectively, turn to chapter 8.

Common Science Test-Taking Errors
As mentioned previously, the science test does not require in-depth scientific knowledge. It relies more on your ability to understand and identify detailed information presented in a variety of formats—text, graphs, tables, and diagrams. If your science test score is lower than you had hoped, you may have committed one or more test-taking errors. Place a checkmark next to each of the following test-taking errors that you think you need to work on avoiding:

Worked too slowly: If time expired before you had a chance to answer all 40 questions, you need to pick up the pace.

Worked too quickly: If you finished with plenty of time remaining but made mistakes, you need to practice slowing down and reading the science passages, questions, and answer choices more carefully.

Misread or misinterpreted text: If you missed questions because you misread a passage, question, or answer choice, check this box.

Misread or misinterpreted a graph or table: Graphs, tables, and images contain much of the information required to answer the science test questions.

Misread or misinterpreted a research summary: You may need to develop a better understanding of the scientific method for designing and conducting experiments.

Did not use reason effectively to find the answer: Most of the questions on the science test challenge your ability to think and reason. If you struggled to understand questions, check this box. You may be able to improve your score by adopting a problem-solving strategy that steps you through the question, as discussed in chapter 8.

For science test-taking strategies that will help you avoid these common mistakes and others, turn to chapter 8.
Highlighting Strengths and Areas for Improvement on the Writing Test

The optional writing test is designed to evaluate your ability to write at a level expected of students entering first-year college English composition courses. A solid essay demonstrates your ability to analyze and evaluate multiple perspectives on a complex issue, to state and develop your own perspective on the issue, to explain and support your ideas with logical reasoning and detailed examples, to clearly and logically organize your ideas, and to effectively communicate your ideas in standard written English.

After scoring your writing practice test, use the checklists in the following sections to highlight writing skills you may need to develop more fully and to avoid errors related to writing strategy and process.

Writing Skills Tested

As you evaluate your writing practice test, consider not only your scores but also, more importantly, which skills contributed to your scores. You may be able to improve your scores significantly by more fully developing only one or two of the following skills. Place a checkmark next to each skill you think you need to work on:

- **Analyze and evaluate multiple perspectives on a complex issue**: If you had trouble analyzing the relationship between your perspective and at least one other perspective, practice writing counterarguments. Pick a debatable issue and choose a stance. Now, imagine what someone who disagrees with you might say, and practice writing paragraphs that first present the other person’s side of the issue. Then offer your response. Next, imagine a perspective that is in general agreement with yours but differs in some important ways. How do you respond to this perspective? As you think and write, ask yourself: What accounts for the similarities and differences among your perspective and others you can imagine? Where are the strengths and weaknesses in these other perspectives, and where are the strengths and weaknesses in your own? Most importantly, ask yourself how engaging with another view—whether it generally agrees or disagrees with your own—can help you advance an argument. Considering these questions as you practice can help you learn to analyze and engage with different perspectives.

- **State and develop your own perspective on the issue**: If your essay did not establish a clear perspective, practice formulating thesis statements. Whenever you write an essay, practice stating your thesis in the first few sentences of the essay. By presenting your perspective in the introduction, you not only state your main idea clearly but also give your essay a focal point.

- **Explain and support your ideas with logical reasoning and detailed examples**: Failure to support your assertions can result in a lower score. Remember that every claim you make should be backed up with good supporting evidence. As you explain the reasoning behind your argument, remember that logical fallacies, including overgeneralization and moral equivalence (associating minor offenses with moral atrocities), can weaken your ideas.
Clearly and logically organize your ideas in an essay: An essay should flow directly from point A to point B and not circle back or wander off track. (Prewriting, discussed in the next section, can help ensure that your essay is well organized.)

Effectively communicate your ideas in standard written English: Here is where your mastery of punctuation, grammar, usage, sentence structure, and style apply.

You can develop all of these skills in high school English classes and other classes that require you to write essays and where you receive feedback that targets these skills. For more about improving your writing test score, along with sample essays that demonstrate the differences between high-scoring and lower-scoring essays, turn to chapter 9.

Writing Strategy or Process Errors

When scoring an essay, the focus is on the product, but the score may be a reflection of the process used to produce that essay. For example, prewriting (planning) can help you think of good ideas, ensure that your ideas are presented logically, and remind you to provide evidence to support your ideas. After scoring your practice essay, think back to when you wrote the essay and place a checkmark next to any of these writing strategy or process errors you may have committed:

Poor pacing: Writing too quickly may result in careless errors, whereas writing too slowly results in an incomplete essay or insufficient time to review and correct errors.

Insufficient prewriting (planning): It is hard to write an effective essay if you don’t have much to say. If you had trouble generating critical ideas, consider using the guided prewriting section found in the test booklet. The questions presented in this section are intended to help you produce a perspective and analyze its relationships with other points of view. They are also useful as you think about how you will support your ideas. It can also be difficult to organize your ideas as you write. You may instead consider using the prewriting space to write an outline. You do not need a detailed outline, but starting with a thesis and mapping a structure to support it can help you define the logic of your argument before you begin to write it.

Not reviewing or editing: If you completed your essay with time to spare, did not review or edit it, and lost points because of grammar, usage, sentence structure, or style errors, check this box. And next time you write an essay, be sure to read and edit it as time allows.

Insufficient practice: Producing well-written essays requires practice and feedback, which you often receive only in a formal English composition course. The practice writing tests in this book provide additional opportunities, but we strongly recommend that you have your practice writing tests evaluated by a qualified third party—perhaps an English teacher or a fellow student who is a strong writer.

For additional tips on improving your writing test score, turn to chapter 9.
Part Three: Improving Your Score

In This Part
This part features various ways to improve your scores on the English, mathematics, reading, science, and optional writing tests. Here, you get a preview of the types of questions you can expect on each test, along with test-taking strategies and skills that apply specifically to each test:

**English:** Find out more about test content, look at sample questions, and develop strategies for choosing the best answer.

**Mathematics:** Learn about the subject areas covered on the test, the types of math problems you will encounter, and strategies for improving your speed and accuracy in answering questions.

**Reading:** Discover the types of reading passages you will encounter on the test, the types of questions you will need to answer, and strategies for improving your reading speed and comprehension.

**Science:** Identify the areas of science covered on the test, the types of questions you will encounter, and test-taking strategies and skills for extracting information from passages and using it to reason your way to the correct answers.

**Writing:** Check out a sample writing prompt, find out what the people scoring your essay will be looking for, read sample scored essays from poor to excellent, and pick up a few strategies that may help to raise your writing score.
On the ACT English test, you have 45 minutes to read five passages, or essays, and answer 75 multiple-choice questions about them—an average of 15 questions per essay. The essays on the English test cover a variety of subjects; the sample passages that follow this discussion range from a personal essay about the different ways of figuring one's age to an informative essay about the legal history of school dress codes.

**Content of the ACT English Test**

The ACT English test is designed to measure your ability to accomplish the wide variety of decisions involved in revising and editing a given piece of writing. An important part of revision and editing decisions is a good understanding of the conventions of standard written English. You may not always use standard written English in casual writing (for instance, when you are e-mailing a friend) or in conversation. In casual writing or conversation, we often use slang expressions that have special meanings with friends our own age or in our part of the country. Because slang can become outdated (does anybody say *groovy* anymore?) and regional terms might not be familiar to students everywhere (Do you and your friends say *soda* or *soft drink* or *pop*?), this test emphasizes the standard written English that is taught in schools around the country.
Questions on the English test include the following:

- **Usage/Mechanics** (punctuation, grammar and usage, sentence structure)
- **Rhetorical Skills** (writing strategy, organization, style)

You’ll receive a score for all 75 questions. If you choose to take the Writing test, you will also receive an English Language Arts (ELA) score.

You will **not** be tested on spelling, vocabulary, or on rote recall of the rules of grammar. Grammar and usage are tested only within the context of the essay, not by questions such as “Must an appositive always be set off by commas?” Likewise, you won’t be tested directly on your vocabulary, although the better your vocabulary is, the better equipped you’ll be to comprehend the reading passages and answer questions that involve choosing the most appropriate word.

The English test doesn’t require you to memorize what you read. The questions and essays are side-by-side for easy reference. This is **not** a memorization test.

The questions discussed on the following pages are taken from the sample passages and questions that follow on pages 221–227. If you prefer, you can work through the sample passages and questions before you read the rest of this discussion. However, to better understand the English test, you may want to first read the discussion, then work through the sample passages and questions.

**Types of Questions on the ACT English Test**

Many questions refer to an underlined portion of the essay. You must decide on the best alternative for that underlined portion. Usually, your options include NO CHANGE, which means that the essay is best as it’s written. Sometimes, you’ll also have the option of deleting the underlined portion. For example, the following question (from Sample Passage II on pages 223–225) offers you the option of removing the word to from the sentence.

<table>
<thead>
<tr>
<th>Otherwise, this difference points</th>
<th>22. F. NO CHANGE</th>
</tr>
</thead>
<tbody>
<tr>
<td>to significant underlying cultural values</td>
<td>G. on</td>
</tr>
<tr>
<td></td>
<td>H. at</td>
</tr>
<tr>
<td></td>
<td>J. OMIT the underlined portion.</td>
</tr>
</tbody>
</table>

In this example, the best answer is not to delete the underlined portion but to leave it as it is (F).

Other questions on the English test may ask about a section of the essay or an aspect of the essay as a whole. For example, in the following question (from Sample Passage I on pages 221–223), you’re given a sentence to be added to the essay, then you’re asked to decide the most logical place in the essay to add that sentence.
15. Upon reviewing this essay and finding that some information has been left out, the writer composes the following sentence incorporating that information:

> Those same German influences helped spawn a similar musical form in northern Mexico known as *norteño*.

The sentence would most logically be placed after the last sentence in Paragraph:

A. 1.
B. 2.
C. 3.
D. 4.

In this example, the best answer is C, because paragraph 3 focuses on the European musical influences on the O'odham people of Arizona, and the last sentence of the paragraph specifically refers to the musical influences of German immigrants.

Let's look at some additional examples of the kinds of questions you're likely to find on the ACT English test. If you want to know what an individual question looks like in the context of the passage in which it appears, turn to the pages indicated. You can also use those sample passages and questions for practice, either before or after reading this discussion.

**Usage/Mechanics**

Usage/mechanics questions focus on the conventions of punctuation, grammar and usage, and sentence structure and formation.

Punctuation questions involve identifying and correcting the following misplaced, missing, or unnecessary punctuation marks:

- Commas
- Apostrophes
- Colons, semicolons, and dashes
- Periods, question marks, and exclamation points

These questions address not only the rules of punctuation but also the use of punctuation to express ideas clearly. For example, you should be prepared to show how punctuation can be used to indicate possession or to set off a parenthetical element.
In many punctuation questions, the words in every choice will be identical, but the commas or other punctuation will vary. It's important to read the choices carefully in order to notice the presence or absence of commas, semicolons, colons, periods, and other punctuation. The following example of a punctuation question comes from Sample Passage I on pages 221–223.

Around this time the polka music and button accordion played by German immigrant railroad workers; left their mark on waila.

14. F. NO CHANGE
   G. workers
   H. workers:
   J. workers,

It may help you to read through this sentence without paying attention to the punctuation so you can identify its grammatical construction. The subject of this sentence is “the polka music and button accordion.” What follows that subject might seem like the predicate verb of the sentence, but it’s not. The phrase “played by German immigrant railroad workers” is a participle phrase (a phrase formed with the past participle “played”). This participle phrase functions as an adjective because it modifies the nouns it follows (“the polka music and button accordion”).

After the participle phrase is the predicate verb of the main clause, “left.” Then comes a phrase that explains what was left (the direct object “their mark”) and a prepositional phrase that explains where it was left (“on waila”).

Now we can deal with the question about what kind of punctuation should follow that participle phrase. Sometimes, these phrases are set off from the main clause with commas to indicate that the phrase is parenthetical or provides information not essential to the meaning of the sentence. That’s not the case here for two reasons. First, there’s no comma at the beginning of the participle phrase. Second, the phrase is essential to the sentence; the sentence is not referring to just any polka music and button accordion but to the music and accordion played by those German immigrant railroad workers (presumably, not while they were working on the railroad).

Ignoring the participle phrase for a minute, we need to ask ourselves what kind of punctuation we would usually place between the subject “the polka music and button accordion” and the predicate “left.” Our answer should be no punctuation at all, making G the best answer. Of course, you could answer this question without this rather tedious analysis of the parts of the sentence. You might simply decide that because the sentence contains no other punctuation, you would never insert a single punctuation mark between the subject and the predicate of the main clause. Or you might just plug in each of the four punctuation choices—semicolon, no punctuation, colon, comma—and choose the one that looks or sounds best to you.

**Grammar and usage** questions involve choosing the best word or words in a sentence based on grammar and usage conventions. Some examples of poor and better phrases are given in the following.
• Grammatical agreement
  (Subject and verb)
  “The owner of the bicycles are going to sell them.”
  should be:
  “The owner of the bicycles is going to sell them.”
  * * *

(Pronoun and antecedent)
“Susan and Mary left her briefcases in the office.”
should be:
“Susan and Mary left their briefcases in the office.”
  * * *

(Adjectives and adverbs with corresponding nouns and verbs)
“Danielle spread frosting liberal on the cat.”
should be:
“Danielle spread frosting liberally on the cat.”

• Verb forms
“Fritz had just began to toast Lydia’s marshmallows when the rabbits stampeded.”
should be:
“Fritz had just begun to toast Lydia’s marshmallows when the rabbits stampeded.”

• Pronoun forms and cases
“Seymour and Svetlana annoyed there parents all the time.”
should be:
“Seymour and Svetlana annoyed their parents all the time.”
  * * *

“After the incident with the peanut butter, the zebra and me were never invited back.”
should be:
“After the incident with the peanut butter, the zebra and I were never invited back.”

• Comparative and superlative modifiers
“My goldfish is more smarter than your brother.”
should be:
“My goldfish is smarter than your brother.”
  * * *
“Your brother, however, has the cuter aardvark that I’ve ever seen.”

should be:
“Your brother, however, has the cutest aardvark that I’ve ever seen.”

• Idioms

“The definition of a word can be looked down in the dictionary.”

should be:
“The definition of a word can be looked up in the dictionary.”

Questions dealing with pronouns often have to do with using the proper form and case of the pronoun. Sometimes they address a pronoun’s agreement with its antecedent, or referent. In such cases, consider the entire sentence, and sometimes the preceding sentence, to make sure you know what the antecedent is. Consider the following question (from Sample Passage I on pages 221–223).

Here, the possessive pronoun in question refers back to the subject of the main clause (“they”), which in turn refers back to the subject of the introductory subordinate clause (“the dancers”). Thus, the best answer is the third-person plural possessive pronoun (“their,” A). Choice B might seem like a possibility because they’re sounds like their (that is, they’re homonyms). However, they’re is a contraction for they are. We can rule out C and D because of the pronoun-antecedent agreement problem and also because it’s is not a possessive pronoun but a contraction for it is, and its’ is not even a word.

Sentence structure questions involve the effective formation of sentences, including dealing with relationships between and among clauses, placement of modifiers, and shifts in construction. Following are some examples:

• Subordinate or dependent clauses and participle phrases

“These hamsters are excellent pets because providing hours of cheap entertainment.”

This sentence could be rewritten as:

“These hamsters are excellent pets providing hours of cheap entertainment.”
(participle phrase)

It could also be revised as:

“These hamsters are excellent pets because they provide hours of cheap entertainment.”
(subordinate/dependent clause)
• Run-on or fused sentences
  “We discovered that the entire family had been devoured by anteaters it was horrible.”
  This sentence should actually be two:
  “We discovered that the entire family had been devoured by anteaters. It was horrible.”

• Comma splices
  “The anteaters had terrible manners, they just ate and ran.”
  This sentence could be rewritten as:
  “The anteaters had terrible manners. They just ate and ran.”
  Because a semicolon can serve as a “soft” period, the sentence could also be rewritten as:
  “The anteaters had terrible manners; they just ate and ran.”

• Sentence fragments
  “When he found scorpions in his socks.”
  This needs a subject to let us know who “he” is and what he did:
  “Julio didn’t lose his temper when he found scorpions in his socks.”

• Misplaced modifiers
  “Snarling and snapping, Juanita attempted to control her pet turtle.”
  Unless Juanita was doing the snarling and snapping, the sentence should be rewritten:
  “Snarling and snapping, the pet turtle resisted Juanita’s attempt to control it.” It could also be rewritten this way:
  “Juanita attempted to control her pet turtle, which snarled and snapped.”

• Shifts in verb tense or voice
  “We sat down to the table to eat, but before we began, John says grace.”
  This should be rewritten as:
  “We sat down to the table to eat, but before we began, John said grace.”

• Shifts in pronoun person or number
  “Hamsters should work at the most efficient pace that one can.”
  This should be rewritten as:
  “Hamsters should work at the most efficient pace that they can.”
Many questions about sentence structure and formation will ask you about how clauses and phrases are linked. This means that you may have to consider punctuation or the lack of punctuation, which can create problems such as comma splices, run-on sentences, or sentence fragments. You also may have to consider various words that can be used to link clauses and phrases: conjunctions such as and, but, because, and when, and pronouns such as who, whose, which, and that. The following question (from Sample Passage I on pages 221–223) is a good example of a sentence structure question.

<table>
<thead>
<tr>
<th>It is a social music that performed at weddings, birthday parties, and feasts.</th>
</tr>
</thead>
<tbody>
<tr>
<td>4. F. NO CHANGE</td>
</tr>
<tr>
<td>5. G. music in which it is performed</td>
</tr>
<tr>
<td>6. H. music, performing</td>
</tr>
<tr>
<td>7. J. music, performed</td>
</tr>
</tbody>
</table>

What would be the best way to link the clause “It is a social music” and the phrase “performed [or performing] at weddings, birthday parties, and feasts”? Relative pronouns such as that and which stand in for the noun that the relative clause modifies. (They relate the clause to the noun.) One way to try out choices such as F and G is to replace the relative pronoun with the noun and then decide if the resulting statement makes sense:

Social music performed at weddings, birthday parties, and feasts. (F)

This does not make sense. Musicians perform, but the music itself does not. Music is performed.

In social music it is performed at weddings, birthday parties, and feasts. (G)

This also seems nonsensical. What does it refer to—social music?

The other two choices offer a different approach to connecting information in a sentence. The phrases “performing at weddings, birthday parties, and feasts” (H) and “performed at weddings, birthday parties, and feasts” (J) are participle phrases. Similar to adjective clauses, these phrases modify a noun. We can rule out H for the same reason that we rejected F: it doesn’t make sense to think of “social music” as “performing.” However, it sounds fine to refer to “social music” as “performed” (J).

Rhetorical Skills

Rhetorical skills questions focus on writing strategy, organization, and style.

Writing strategy questions focus on the choices made and strategies used by a writer in the act of composing or revising an essay. These questions may ask you to make decisions concerning the appropriateness of a sentence or essay in relation to purpose, audience, unity, or focus, or the effect of adding, revising, or deleting supporting material.

The following question (from Sample Passage I on pages 221–223) is a fairly typical example of the kinds of writing decisions that strategy questions ask you to make.
In the early 1900s the O’odham became acquainted with marching bands and woodwind instruments (which explains the presence of saxophones in waila).

13. Given that all of the choices are true, which one is most relevant to the focus of this paragraph?

A. NO CHANGE
B. (although fiddles were once widely used in waila bands).
C. (even though they’re now often constructed of metal).
D. (which are frequently found in jazz bands also).

It’s important to read these questions carefully and, sometimes, to reread the essay or parts of the essay. This question is fairly clear-cut, but it does suggest that you need a pretty good sense of what paragraph 3 is about. A quick review of the paragraph indicates that it is focused on how the O’odham and their music were influenced by the musical styles and instrumentation of the European immigrants they encountered.

Which of these parenthetical statements is most relevant to that focus? Choice D, which states that woodwind instruments are frequently found in jazz bands, is not. Likewise, choice C, which indicates that woodwind instruments are now often constructed of metal, strays from the paragraph’s topic. Choice B, which points out that fiddles were once widely used in waila bands, is getting closer, but this too seems a diversion, unconnected to the other information in this paragraph. Guitars, woodwinds, and button accordions are mentioned but not fiddles or violins.

Choice A, however, provides an appropriate and relevant elaboration. It draws the connection between the O’odhams’ introduction to marching bands and woodwinds in the early 1900s and the eventual inclusion of saxophones in a typical waila band.

Organization questions deal with the order and coherence of ideas in an essay and the effective choice of opening, transitional, and closing statements. For example, you may be asked about the organization of ideas (the most logical order for sentences within a paragraph or paragraphs within an essay) or about the most logical transitional phrase or statement.

The following question (from Sample Passage II on pages 223–225) is a good example of the kind of organization question you might encounter.
Today, after many birthdays and New Year’s Days, I now find meaningful the difference I once found confusing. Otherwise, this difference points to significant underlying cultural values. 21. A. NO CHANGE  
B. Though,  
C. In fact,  
D. Then,

The choices in this question are sometimes referred to as conjunctive adverbs or transitional words or phrases because their main job is to connect or link the statement in one sentence with the statement in a preceding sentence. These are often little words—so, thus, soon, yet, also—that do a lot of work to make an essay logical.

In order to answer such questions correctly, it helps to think about the logical relationship between the sentences, as well as the logical relationships expressed by the choices. The main statement of the opening sentence of this paragraph is “I now find meaningful the difference [in computing one's age] I once found confusing.” The second sentence states, “This difference points to significant underlying cultural values.” The writer then goes on to explain those cultural values.

Which of these four choices enables readers to move most easily from the opening sentence into the rest of this paragraph? Choice A suggests that the second statement contrasts with the first statement. A typical dictionary definition for Otherwise is “in different circumstances.” Similarly, choice B, Though, suggests that the statement to follow is contrary to or in opposition to the preceding statement. Neither of those adverbs works well here. Nor does Then (choice D), which usually expresses a time relationship—meaning “next” or “soon after in time.”

The best choice here is C. The phrase “In fact” is often used to introduce a statement that builds on the preceding statement. We can pare down these opening sentences to their bare essentials to show that the phrase works well here: “I now find the difference in computing one's age meaningful. In fact, the difference points to important cultural values about life experience and longevity.”

Style questions involve effective word choices in terms of writing style, tone, clarity, and economy. Sometimes, a phrase or sentence that isn't technically ungrammatical is nevertheless confusing because it's poorly written. Sometimes, a word or phrase clashes with the tone of the essay. Good writing also involves eliminating ambiguous pronoun references, excessively wordy or redundant material, and vague or awkward expressions.

Similar to most writing strategy and organization questions, style questions require a general understanding of the essay as a whole. The following style question (from Sample Passage III on pages 225–227) focuses on the issues of economy and consistency of tone.
The school board members believed that wearing “play clothes” to school made the students inefficient toward their 32 school work, while more formal attire established a positive educational climate.

You will be better able to recognize the appropriateness of choice J if you know that lax means “lacking necessary strictness, severity, or precision” and indifferent means “lacking interest, enthusiasm, or concern.” These terms touch on two related but distinct concerns—academic laziness and apathy. One could imagine school board members using these very words in their meetings. And the words are consistent with the overall style and tone of this straightforward, informative essay about a legal case.

Choices G and H are fairly easy to rule out if you think about the generally formal tone of the essay. It’s not that one should never use slang phrases such as “bored to tears” or “blow off” in one’s writing; it’s just that this particular essay is not the place to use them. When we consider that this statement is describing the school board members’ belief, these phrases are even more inappropriate.

It seems more in character for school board members to be concerned about student inefficiency, but F is a weak choice because the phrase “inefficient toward their school work” sounds odd or awkward. Perhaps it’s the preposition that trips us up. The word toward works fine in J when describing attitudes (“lax,” “indifferent”) toward school work, but the word inefficient is describing an ability or skill.

The questions provided here are a small sample of the kinds of questions that might be on the test. The previous question, for example, is only one kind of style question; it doesn’t cover all the territory of style that might be addressed on the test. The sample passages and questions at the end of this section have all the examples referred to in this chapter as they would appear in a test. These sample passages and questions and the later practice tests will provide you with a thorough understanding of the ACT English test.

**Strategies for Taking the ACT English Test**

**Pace Yourself**

The ACT English test contains 75 questions to be completed in 45 minutes, which works out to exactly 36 seconds per question. Spending 1½ minutes skimming through each essay leaves you about 30 seconds to respond to each question. If you spend less time than that on each question, you can use the remaining time allowed for this test to review your work and to return to the questions that were
most difficult for you. Another way to think of it is that you have 45 minutes to read and answer the questions for five essays, giving you a maximum of 9 minutes for each essay and its questions.

**Be Aware of the Writing Style Used in the Essay**

The five essays cover a variety of topics and are written in a variety of styles. It’s important that you take into account the writing style used in each essay as you respond to the questions.

Some of the essays will be anecdotes or narratives written from an informal, first-person point of view. Others will be more formal essays, scholarly or informative in nature, often written in the third person. Some questions will ask you to choose the best answer based not on its grammatical correctness but on its consistency with the style and tone of the essay as a whole. For example, an expression that’s too breezy for an essay on the life of President Herbert Hoover might be just right for a personal narrative about a writer’s attempt at learning to skateboard.

**Consider a Question’s Context before Choosing an Answer**

Some people find it helpful to skim an essay and its questions before trying to answer those questions. Having a general sense of the essay in mind before you begin to answer questions involving writing strategy or style can help. If you encounter questions about the order of sentences within a paragraph, or the order of paragraphs within an essay, or where to add a sentence in an essay, you may want to answer those questions first to make sure that the major elements of the essay are arranged logically. Understanding the order of the passage may make it easier for you to answer some of the other questions.

As you’re answering each question, be sure to read at least a sentence or two beyond the sentence containing the portion being questioned. You may need to read even more than that to understand what the writer is trying to say.

**Be Aware of the Connotations of Words**

Vocabulary isn’t tested in an isolated way on the ACT English test. Nevertheless, a good vocabulary and an awareness of not only the dictionary definitions of words but also the connotations (feelings and associations) suggested by those words will help you do well on the test.

The following question (from Sample Passage II on pages 223–225) asks you to think about how certain words and their connotations can function in terms of the rest of the essay.
Many people might be surprised to learn that the American way of computing a person’s age differs from the traditional Korean way. In Korean tradition, a person is considered to be already one year old at the time of his or her birth.

As a child growing up in two cultures, I found this contest a bit confusing.  

16. F. NO CHANGE  
G. change  
H. dispute  
J. difference  

Which word best captures or summarizes what has been described in the preceding paragraph? The word contest (F) doesn’t seem right because it suggests a competition between opposing sides or teams. In a similar vein, the word dispute (H) doesn’t fit here because it generally refers to a verbal debate or argument. The word change (G) is a little off because it expresses the idea of transformation, making something or someone different, which doesn’t accurately summarize that opening paragraph. The word difference (J), however, seems just right. It echoes the verb in the first sentence of the preceding paragraph, but more important, it accurately reflects the writer’s perspective up to this point in the essay that the American way and the Korean way of computing a person’s age are not competing or arguing with each other. They are simply unlike each other (and because of that mismatch, a bit confusing).

In questions such as this one, you have to focus on what the words mean and what associations the words have for the typical reader.

**Look for a Stated Question**

Before responding to a question identified by an underlined portion, check for a stated question preceding the options. If there is one, it will provide you with some guidelines for deciding on the best choice. Some questions will ask you to choose the alternative to the underlined portion that is NOT or LEAST acceptable. Here’s an example from Sample Passage I on pages 221–223.
For these types of questions, look closely at the underlined portion, because the question has told you that it is acceptable. Likewise, three of the alternative choices are acceptable. The best answer, in this case, is the one that is not acceptable. In the underlined portion, a dash is used between two independent clauses: “The music is mainly instrumental” and “the bands generally consist of guitar, bass guitar, saxophones, accordion, and drums.” The dash is sometimes thought of as a less formal type of punctuation, but it can work quite well to provide emphasis or to signal that an explanation will follow.

Placing a period (C) or a semicolon (D) between these two independent clauses would also be acceptable. Likewise, choice A is acceptable because it too places a semicolon between the two clauses, using the phrase “in general” rather than the adverb “generally.” Choice B is not acceptable and is, therefore, the best answer. A comma is not usually a strong enough punctuation mark between two independent clauses not joined by a conjunction. Notice that this sentence has other commas, used to distinguish nouns in a series. How would a reader know that the comma between the clauses is a much stronger break than those other commas?

Whether a stated question is presented or not, you should carefully examine what is underlined in the essay. Consider the features of writing that are included in the underlined portion. The options for each question will contain changes in one or more aspects of writing.

**Note the Differences in the Answer Choices**

Many of the questions that refer to underlined portions will involve more than one aspect of writing. Examine each choice and note how it differs from the others. Consider all the features of writing that are included in each option.

**Avoid Making New Mistakes**

Beware of correcting mistakes in the essay and, in your haste, picking a response that creates a new mistake. Be observant, especially in questions where the responses have similar wording. One comma or apostrophe can make all the difference, as the following question (from Sample Passage III on pages 225–227) illustrates.
Perhaps you took only a moment to reject choice A because of the unnecessary comma between the noun *review* and the prepositional phrase “of students’ rights.” And if you were able to make that call, you may have ruled out choice B for the same reason. It is probably more difficult to recognize that the comma between the noun *rights* and the conjunction *and* (D) is unnecessary and misleading. Because you were thinking about how the underlined portion should be punctuated, you may also have wondered about the plural apostrophe in the word *students’* but then realize that the apostrophe is in the same place in all four choices. (The best answer is C.)

**Determine the Best Answer**

There are at least two approaches you can take to determine the best answer to a question about an underlined portion. One approach is to reread the sentence or sentences containing the underlined portion, substitute each of the answer choices in turn, and decide which is best. Another approach is to decide how the underlined portion might best be phrased and then look for your phrasing among the choices offered. If the underlined portion is correct as it is, select the NO CHANGE option.

If you can’t decide which option is best, you may want to mark the question in your test booklet so you can return to it later. Remember: you’re not penalized for guessing, so after you’ve eliminated as many options as you can, take your best guess.

**Reread the Sentence Using Your Selected Answer**

After you have selected the answer you feel is best, reread the corresponding sentence or sentences in the essay, substituting the answer you’ve selected for the underlined portion or for the boxed numeral. Sometimes an answer that sounds fine out of context doesn’t fit within the sentence or essay. Be sure to keep in mind both the punctuation marks and words in each possible response; sometimes just the omission of a comma can make an important difference.

**Watch for Questions about the Entire Essay or a Section of the Essay**

Some questions ask about a section of the essay. They are identified by a question number in a box at the appropriate point in the essay, rather than by an underlined portion. Here’s an example from Sample Passage II on pages 223–225.
Perhaps the celebration of New Year’s Day in Korean culture is heightened because it is thought of as everyone’s birthday party.  

20. Upon reviewing this paragraph, the writer considers deleting the preceding sentence. If the writer were to delete the sentence, the paragraph would primarily lose:

F. a comment on the added significance of the Korean New Year celebration.
G. a repetitive reminder of what happens every birthday.
H. a defense of the case for celebrating every birthday.
J. an illustration of the Korean counting system.

This question asks you to think about the role this sentence plays in terms of the paragraph as a whole. If the sentence were deleted, the paragraph would lose the elaboration on the point that Korean tradition indicates that everyone becomes a year older on New Year’s Day, regardless of when they were actually born. Without the sentence, the point about the “added significance of the Korean New Year celebration” (F) would have been unstated.

Some other questions ask about an aspect of the essay as a whole. These are placed at the end of the essay, following boxed instructions like these:

Question 15 asks about the preceding passage as a whole.

You may want to read any questions that ask about the essay as a whole first so you can keep them in mind while you’re reading through the essay. For questions about a section of the essay or the essay as a whole, you must decide the best answer on the basis of the particular writing or revision problem presented in the question.

Be Careful with Two-Part Questions

Some questions require extra thought because you must decide not only which option is best but also which supporting reason for an option is most appropriate or convincing. The following question occurs at the end of Sample Passage III on pages 225–227. Each option begins with either a yes or no response, followed by a supporting reason for that response.
45. Suppose the writer’s goal had been to write a brief persuasive essay urging students to exercise their constitutional rights. Would this essay fulfill that goal?

A. Yes, because the essay focuses on how Kevin encouraged other students to exercise their constitutional rights.

B. Yes, because the essay focuses on various types of clothing historically worn by students as a freedom of expression.

C. No, because the essay suggests that the right to wear blue jeans was not a substantial constitutional right in the 1970s.

D. No, because the essay objectively reports on one case of a student exercising a particular constitutional right.

Once you decide whether the essay would or would not fulfill the writer’s goal, as described in the question, you need to decide which reason or explanation provides the most appropriate support for the answer and is most accurate in terms of the essay. Sometimes, the supporting reason does not accurately reflect the essay (the explanations in B and C, for example). Sometimes, the reason accurately reflects the essay but doesn’t logically support the answer to the question. And sometimes, the reason might logically support the question (that is, the writer’s goal) but that reason overstates the focus of the essay. It may be fair to say that Kevin Bannister’s case led to a review of student rights, but this essay does not at any point describe Kevin encouraging other students to exercise their rights, as A states. The best answer is D: this essay is more an objective reporting on a legal case about student rights (and that case’s historical significance) than it is a persuasive argument or call to students to exercise those rights.

Watch for Interrelated Questions

As pointed out previously, you’ll sometimes find that the best way to answer questions about a passage is not necessarily in their numbered order. Occasionally, answering a question after you’ve answered the one that follows it is easier. Or you might find two questions about different elements of the same sentence, in which case considering them both together may be helpful.

In the following example (from Sample Passage III on pages 225–227), considering questions 40 and 41 together may be helpful, because they’re contained in the same sentence. First, answer the question that seems easier to you. Once you’ve solved that problem in the sentence, turn to the other question.
Questions 40 and 41 deal with different kinds of writing problems. Question 40 is about choosing the most logical transitional word, and question 41 is about the correct use in this sentence of the gerund (a verb form with an -ing ending that’s used as a noun). You might find that answering question 41 helps you to figure out the answer to question 40. The best answer to question 41 is C—the noun phrase “wearing jeans” works as the subject of the dependent clause “wearing jeans would actually impair the learning process of Kevin or of his fellow classmates.” Try penciling in your answer choice for 41 (that is, edit the essay) so that you can more easily read the sentence while responding to question 40. Does this approach make it easier for you to decide that the most logical answer to question 40 is J (“however”)?

* * *

Remember that this section is only an overview of the English test. Directly or indirectly, a question may test you in more than one of the areas mentioned, so do not become overly concerned with categorizing a question before you answer it. And, although awareness of the types of questions can help you be a more critical and strategic test-taker, just remember: the type of question you’re answering isn’t important. Most important, focus on what the question asks and do your best to pick the best answer based on evidence provided in the passage.
SAMPLE PASSAGE I

The Music of the O’odham

[1]

For some people, traditional American Indian music is associated and connected with high penetrating vocals accompanied by a steady drumbeat. In tribal communities in the southwestern United States, however, one is likely to hear something similar to the polka-influenced dance music of northern Mexico. The music is called “waila.” Among the O’odham tribes of Arizona, waila has been popular for more than a century. The music is mainly instrumental—the bands generally consist of guitar, bass, guitar, saxophones, accordion, and drums.

[2]

Unlike some traditional tribal music, waila does not serve a religious or spiritual purpose. It is a social music that performed at weddings, birthday parties, and feasts. The word itself comes from the Spanish word for dance, baile. Cheek to cheek, the dance is performed to the relaxed two-step tempo, and the bands often play long past midnight. As the dancers step to the music, they were also stepping in time to a sound that

1. A. NO CHANGE
   B. connected by some of them
   C. linked by association
   D. associated

2. F. NO CHANGE
   G. popular, one might say, for
   H. really quite popular for
   J. popular for the duration of

3. Which of the following alternatives to the underlined portion would NOT be acceptable?
   A. instrumental; in general, the bands
   B. instrumental, the bands generally
   C. instrumental. The bands generally
   D. instrumental; the bands generally

4. F. NO CHANGE
   G. music in which it is performed
   H. music, performing
   J. music, performed

5. A. NO CHANGE
   B. word, itself,
   C. word, itself
   D. word itself,

6. F. NO CHANGE
   G. Couples dance cheek to cheek to the relaxed two-step tempo,
   H. A relaxed two-step tempo, the couples dance cheek to cheek,
   J. Cheek to cheek, the two-step tempo relaxes dancing couples,

7. A. NO CHANGE
   B. play long, past,
   C. play, long past,
   D. play, long past

8. F. NO CHANGE
   G. are also stepping
   H. have also stepped
   J. will also step
embodies their unique history and suggests the influence of outside cultures on their music.

The O’odham in the 1700s first encountered the guitars of Spanish missionaries. In the 1850s the O’odham have borrowed from the waltzes and mazurkas of people of European descent on their way to California.

In the early 1900s the O’odham became acquainted with marching bands and woodwind instruments (which explains the presence of saxophones in waila). Around this time the polka music and button accordion played by German immigrant railroad workers; left their mark on waila.

9. A. NO CHANGE
   B. they’re
   C. it’s
   D. its’

10. At this point, the writer is considering adding the following true statement:
     The agricultural practices of the O’odham are similar to those of the Maya.
     Should the writer make this addition here?
     F. Yes, because the sentence establishes that the O’odham often borrowed ideas from other groups.
     G. Yes, because the sentence provides important information about the O’odham people.
     H. No, because the sentence is not supported by evidence of a connection between the O’odham and the Maya.
     J. No, because the sentence distracts from the paragraph’s focus on waila’s uses and influences.

11. All of the following would be acceptable placements for the underlined portion EXCEPT:
     A. where it is now.
     B. at the beginning of the sentence (revising the capitalization accordingly).
     C. after the word guitars.
     D. after the word missionaries (ending the sentence with a period).

12. F. NO CHANGE
    G. have been borrowing
    H. were borrowed
    J. borrowed

13. Given that all of the choices are true, which one is most relevant to the focus of this paragraph?
    A. NO CHANGE
    B. (although fiddles were once widely used in waila bands).
    C. (even though they’re now often constructed of metal).
    D. (which are frequently found in jazz bands also).

14. F. NO CHANGE
    G. workers
    H. workers:
    J. workers,
It should be no surprise that musicians these days are adding touches of rock, country, and reggae to wail. Some listeners fear that an American musical form may soon be lost. But the O’odham are playing waila with as much energy and devotion as ever. A unique blend of traditions, waila will probably continue changing for as long as the O’odham use it to express their own sense of harmony and tempo.

SAMPLE PASSAGE II

How Old Am I?

Many people might be surprised to learn that the American way of computing a person’s age differs from the traditional Korean way. In Korean tradition, a person is considered to be already one year old at the time of his or her birth.

As a child growing up in two cultures, I found this contest a bit confusing. When I was in the fifth grade, was I ten or eleven years old? To add to the confusion, every New Year’s Day a person according to this Korean counting system, becomes a year older, regardless of his or her actual birthday.

Birthdays are important throughout the world. A person who is sixteen years old on his or her birthday in March would become seventeen years old on the following New Year’s Day, even though he or she isn’t expected to turn seventeen (in “American” years) until that next birthday in March. Perhaps the celebration of New Year’s Day in Korean culture is heightened because it is thought of as

Question 15 asks about the preceding passage as a whole.

15. Upon reviewing this essay and finding that some information has been left out, the writer composes the following sentence incorporating that information:

Those same German influences helped spawn a similar musical form in northern Mexico known as norteño.

This sentence would most logically be placed after the last sentence in Paragraph:

A. 1.
B. 2.
C. 3.
D. 4.

16. F. NO CHANGE
G. change
H. dispute
J. difference

17. A. NO CHANGE
B. person,
C. person;
D. person who,

18. F. NO CHANGE
G. Most cultures celebrate birthdays.
H. Birthdays focus attention on a culture’s youth.
J. OMIT the underlined portion.

19. A. NO CHANGE
B. raised
C. lifted
D. lighted
everyone’s birthday party.

Today, after many birthdays and New Year’s Days, I now find meaningful the difference I once found confusing. Otherwise, this difference points to significant underlying cultural values. The practice of advancing a person’s age seems to me to reflect the value a society places on life experience and longevity. Their idea was demonstrated often when my elderly relatives, who took pride in reminding younger folk of their “Korean age.” With great enthusiasm, they added on a year every New Year’s Day. By contrast American society has often been described as one that values the vibrant energy of youth over the wisdom and experience gained with age. After a certain age, many Americans I know would balk, refuse, and hesitate at the idea of adding a year or two to what they regard as their actual age.

20. Upon reviewing this paragraph, the writer considers deleting the preceding sentence. If the writer were to delete the sentence, the paragraph would primarily lose:
   F. a comment on the added significance of the Korean New Year celebration.
   G. a repetitive reminder of what happens every birthday.
   H. a defense of the case for celebrating every birthday.
   J. an illustration of the Korean counting system.

21. A. NO CHANGE
   B. Though,
   C. In fact,
   D. Then,

22. F. NO CHANGE
   G. on
   H. at
   J. OMIT the underlined portion.

23. A. NO CHANGE
   B. persons’ age
   C. persons age
   D. person’s age,

24. F. NO CHANGE
   G. One’s
   H. Its
   J. This

25. A. NO CHANGE
   B. by
   C. while
   D. as if

26. Which choice would most clearly communicate the elderly relatives’ positive attitude toward this practice?
   F. NO CHANGE
   G. Duplicating an accepted practice,
   H. Living with two birthdays themselves,
   J. Obligingly,

27. A. NO CHANGE
   B. whose
   C. this
   D. whom

28. If the writer were to delete the phrases “the vibrant energy of” and “the wisdom and experience gained with” from the preceding sentence, the sentence would primarily lose:
   F. its personal and reflective tone.
   G. an element of humor.
   H. details that illustrate the contrast.
   J. the preference expressed by the writer.

29. A. NO CHANGE
   B. balk and hesitate
   C. refuse and balk
   D. balk
Even something as visibly simple or natural as computing a person’s age can prove to be not so clear-cut. Traditions like celebrating birthdays reveal how deeply we are affected by the culture we live in.

**SAMPLE PASSAGE III**

**Wearing Jeans in School**

In 1970, the school board in Pittsfield, New Hampshire, approved a dress code that prohibited students from wearing certain types of clothing. The school board members believed that wearing “play clothes” to school made the students inefficient toward their school work, while more formal attire established a positive educational climate. When twelve-year-old Kevin Bannister wore a pair of blue jeans to school, he was sent home for violating the dress code.

Kevin and his parents believed that his constitutional rights had been violated. The United States District Court of New Hampshire agreed to hear Kevin’s case. His claim was based on the notion of personal liberty—the right of every individual to the control of his or her own

30. F. NO CHANGE
   G. apparently
   H. entirely
   J. fully

31. Given that all of the choices are true, which one would best illustrate the term dress code as it is used in this sentence?
   A. NO CHANGE
   B. clothing that was inappropriate.
   C. clothing, including sandals, bell-bottom pants, and “dungarees” (blue jeans).
   D. clothing that is permitted in some schools today.

32. F. NO CHANGE
   G. lazy and bored to tears with
   H. blow off
   J. lax and indifferent toward

33. Given that all of the choices are true, which one would most effectively introduce the main idea of this paragraph?
   A. NO CHANGE
   B. The principal said dungarees and blue jeans were the same thing, so Kevin should have known better.
   C. If Kevin’s jeans had been dirty and torn, the principal might have been justified in expelling him.
   D. These events occurred in a time of social unrest, and emotions were running high.

34. F. NO CHANGE
   G. Court of New Hampshire
   H. Court of New Hampshire
   J. Court of New Hampshire,
person—protected by the Constitution’s Fourteenth Amendment. The court agreed with Kevin that a person’s right for wearing clothing of his or her own choosing is, in fact, protected by the Fourteenth Amendment.

The court noted, however that restrictions may be justified in some circumstances, such as in the school setting. So did Kevin have a right to wear blue jeans to school? The court determined that the school board had failed to show that wearing jeans actually inhibited the educational process, which is guided by authority figures.

Furthermore, the board offered no evidence to back up it’s claim that such clothing created a negative educational environment. Certainly the school board would be justified in prohibiting students from wearing clothing that was unsanitary, revealing, or obscene. The court remained unconvinced, therefore, that when wearing jeans would actually impair the learning process of Kevin or of his fellow classmates.

Kevin Bannister’s case was significant in that it was the first in the United States to address clothing prohibitions of a school dress code. His challenge

35. A. NO CHANGE
   B. of wearing
   C. to wear
   D. wearing

36. F. NO CHANGE
   G. court noted, however,
   H. court, noted however,
   J. court noted however,

37. A. NO CHANGE
   B. process, which has undergone changes since the 1970s.
   C. process, a process we all know well.
   D. process.

38. F. NO CHANGE
   G. they’re
   H. its
   J. ones

39. A. NO CHANGE
   B. where
   C. which
   D. in which

40. F. NO CHANGE
   G. thus,
   H. moreover,
   J. however,

41. A. NO CHANGE
   B. by wearing
   C. wearing
   D. having worn

42. Which choice would most effectively open this paragraph and convey the importance of this case?
   F. NO CHANGE
   G. Therefore, Kevin’s case reminds us that you should stand up for your rights, no matter how old you are.
   H. The case for personal liberty means the right to speak up must be taken seriously by the courts.
   J. All in all, clothing is an important part of our identity.
initiated a review of students’ rights and administrative responsibility in public education.

43. A. NO CHANGE
   B. review, of students’ rights.
   C. review of students’ rights
   D. review of students’ rights,

44. F. NO CHANGE
   G. on
   H. with
   J. about

Question 45 asks about the preceding passage as a whole.

45. Suppose the writer’s goal had been to write a brief persuasive essay urging students to exercise their constitutional rights. Would this essay fulfill that goal?
   A. Yes, because the essay focuses on how Kevin encouraged other students to exercise their constitutional rights.
   B. Yes, because the essay focuses on various types of clothing historically worn by students as a freedom of expression.
   C. No, because the essay suggests that the right to wear blue jeans was not a substantial constitutional right in the 1970s.
   D. No, because the essay objectively reports on one case of a student exercising a particular constitutional right.
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<td>5.</td>
<td>A</td>
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<td>J</td>
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<td>29.</td>
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<td>44.</td>
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<td>15.</td>
<td>C</td>
<td>30.</td>
<td>G</td>
<td>45.</td>
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Chapter 6: Improving Your Math Score

The ACT mathematics test asks you to answer 60 multiple-choice questions in 60 minutes. The questions are designed to measure your mathematical achievement—the knowledge, skills, and reasoning techniques that are taught in high school mathematics courses and are prerequisites for college mathematics courses. Therefore, the questions cover a wide variety of concepts, techniques, and procedures. Naturally, some questions will require computation, but you are allowed to use a calculator on the mathematics test. You’ll need to understand basic mathematical terminology and to recall some basic mathematical principles and formulas. However, the questions on the test are designed to emphasize your ability to reason mathematically, not to focus on your computation ability or your ability to recall definitions, theorems, or formulas.
Content of the ACT Mathematics Test
The ACT mathematics test questions are drawn from several areas, which are explained later in this section. These content topics represent areas of mathematics commonly taught by the end of grade 11 that are important to success in entry-level college mathematics courses:

- Pre-algebra
- Elementary algebra
- Intermediate algebra
- Coordinate geometry
- Plane geometry
- Trigonometry

You will receive a score for all 60 questions.

**Pre-algebra** questions involve solving problems using the mathematics that you probably learned before you took your first math course in high school. Questions involve operations such as using whole numbers, fractions, decimals, and integers; numbers raised to positive integer powers and square roots of numbers; ratio, proportion, and percent; multiples and factors of integers; absolute value; ordering numbers from least to greatest or greatest to least; simple linear equations with one variable; simple probability and counting the number of ways something can happen; representing and interpreting data in charts, tables, and graphs; and simple descriptive statistics including mean, median, and mode.

**Elementary algebra** questions evaluate understanding and skills such as using variables to express relationships, substituting the value of a variable in an expression, performing basic operations on polynomials, factoring polynomials, solving simple quadratic equations (the kind that can be solved by factoring), solving linear inequalities with one variable, and applying properties of integer exponents and square roots.

**Intermediate algebra** questions ask you to apply your knowledge, skills, and reasoning ability to solve problems that involve more advanced topics of algebra such as the quadratic formula, radical and rational expressions, inequalities and absolute value equations, sequences, systems of equations, quadratic inequalities, functions, matrices, roots of polynomials, and complex numbers.

**Coordinate geometry** questions deal with the real number line and the standard \((x, y)\) coordinate plane. They involve number line graphs as well as graphs of points, lines, polynomials, circles, and other curves in the standard \((x, y)\) coordinate plane. They also involve relationships between equations and graphs; slope, parallel and perpendicular lines; distance; midpoints; transformations; and conics.
**Plane geometry** questions test your grasp of topics that are usually part of high school geometry, though some topics are introduced in earlier course work. Included are the properties and relations of plane figures (triangles, rectangles, parallelograms, trapezoids, and circles); angles, parallel lines, and perpendicular lines; translations, rotations, and reflections; simple three-dimensional geometry; and measurement concepts such as perimeter, area, and volume. Justification, proof techniques, and logical conclusions are a part of this area.

**Trigonometry** questions cover topics such as the trigonometric ratios defined for right triangles; the values, properties, and graphs of the trigonometric functions; trigonometric identities; trigonometric equations; and modeling with trigonometric functions.

### Types of Questions on the ACT Mathematics Test

The questions on the ACT mathematics test differ in terms of content and complexity. The rest of this section gives you examples of questions—of various types and complexities from all content areas. All of the questions used in the examples are from actual ACT mathematics tests that have been taken by students from across the country. A solution strategy is given for each question. As you read and work through each example, please keep in mind that the strategy given is just one way to solve the problem. Other strategies may work even better for you.

#### Basic Math Problems

The type of question you’re probably the most familiar with (and probably find the easiest) is the stripped-down, bare-bones, basic math problem. Problems of this type are simple and straightforward. They test readily identifiable skills in the content areas, usually have very few words and no extra information, ask the very question you’d expect them to ask, and usually have a numeric answer.

Question 1 is a good example of a basic math problem from pre-algebra.

<table>
<thead>
<tr>
<th>1. What is 4% of 1,100?</th>
</tr>
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<tr>
<td>A. 4</td>
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<tr>
<td>B. 4.4</td>
</tr>
<tr>
<td>C. 40</td>
</tr>
<tr>
<td>D. 44</td>
</tr>
<tr>
<td>E. 440</td>
</tr>
</tbody>
</table>

This problem has very few words, asks a direct question, and has a numeric answer. The solution is simple: convert 4% to a decimal and multiply by 1,100 to get (0.04)(1,100) = 44, choice D. You probably wouldn’t need your calculator on this problem, but remember that you may use it if you wish. If you chose answer B or E, you may have used rules about moving decimal points and moved the wrong number of places.
Question 2 is a basic elementary algebra problem.

2. For all $x$, $(x + 4)(x - 5) =$ ?

F. $x^2 - 20$
G. $x^2 - x - 20$
H. $2x - 1$
J. $2x^2 - 1$
K. $2x^2 - x + 20$

You should know what to do to answer the question the instant you read the problem—use the distributive property (FOIL—first, outside, inside, last) and get $x(x - 5) + 4(x - 5) = x^2 - 5x + 4x + 4(-5) = x^2 - x - 20$, choice G. On this problem, you probably wouldn't use your calculator. If you chose F, you probably just multiplied the first terms and the last terms. Check your answer by substituting a number (try 6) into the original expression and into your answer. If the results are not equal, then the expressions cannot be equivalent.

Question 3 is an example of a basic problem from intermediate algebra.

3. If $x + y = 1$, and $x - y = 1$, then $y =$ ?

A. $-1$
B. $0$
C. $\frac{1}{2}$
D. $1$
E. $2$

This problem gives you a system of linear equations with unknowns $x$ and $y$ and asks for the value of $y$. You might be able to solve this problem intuitively—the only number that can be added to and subtracted from another number and give the same result for the problem ($x + y$ and $x - y$ both give 1) is 0, so $y$ must be 0, choice B. Or, you could use algebra and reason that, because $x + y$ and $x - y$ both equal 1, they equal each other, and $x + y - x - y$ gives $2y = 0$, so $y = 0$. Although some calculators have graphing or matrix functions for solving problems of this type, using a calculator on this problem would probably take most students longer than solving it with one of the strategies given here. If you chose answer D, you probably found the value of $x$ rather than the value of $y$. 
Question 4 is an example of a basic problem in coordinate geometry.

4. What is the slope of the line containing the points (-2,7) and (3,-3)?

F. 4
G. 1/4
H. 0
J. -1/2
K. -2

This problem has a few more words than some of the other examples of basic problems you’ve seen so far, but the most important word is slope. Seeing that you are given two points, you would probably think of the formula that defines the slope of a line through two points:

\[
\frac{y_1 - y_2}{x_1 - x_2}
\]

Applying the formula gives \(7 - (-3)/-2 -3 = 10/-5 = -2\), choice K. If you chose answer J, you probably got the expression for slope upside down. The change in \(y\) goes on top.

You may also encounter basic plane geometry problems on the ACT mathematics test. Question 5 is a good example.

5. If the measure of an angle is \(37\frac{1}{2}\)°, what is the measure of its supplement, shown in the figure below?

\[
\text{?} \quad 37\frac{1}{2}°
\]

A. 52\frac{1}{2}°
B. 62\frac{1}{2}°
C. 127\frac{1}{2}°
D. 142\frac{1}{2}°
E. Cannot be determined from the given information
Similar to many geometry problems, this problem has a figure. The figure tells you what you are given (an angle of 37½°) and what you’re asked to find (its supplement, marked by “?”). You need not mark anything on the figure, because all the important information is already there. If you know that the sum of the measure of an angle and the measure of its supplement equals 180°, a simple subtraction gives the correct answer (180° – 37½° = 142½°), choice D. If you chose A, you found the complement, not the supplement.

A word of caution is in order here. You probably noticed that “Cannot be determined from the given information” is one of the options for question 5. Statistics gathered over the years for the ACT mathematics test show that many students choose “Cannot be determined from the given information” even when the answer can be determined. You should not think that whenever “Cannot be determined from the given information” is an option, it is automatically the correct answer. It isn’t, as question 5 demonstrates. Later in this section is a question for which the correct answer is “Cannot be determined from the given information.” Be sure to think carefully about problems with this answer choice.

You’ll also find basic trigonometry problems, such as question 6, on the ACT mathematics test.

6. What is the sine of ∠A in the triangle below?

![Image of a triangle with sides labeled 6, 10, and 8, and angles labeled C and A.]

- F. 0.30
- G. 0.50
- H. 0.60
- J. 0.75
- K. 0.80

This question asks you to find the sine of ∠A in the triangle shown in the figure. If you have studied trigonometry, you’ve seen questions similar to this before. The lengths of all three sides of the triangle are given on the figure, even though only two are actually needed for finding sin ∠A. The extra information is there not to confuse you but rather to test your ability to sort out the information you need from the information you are given. Picking 6 (the length of the side opposite ∠A) and 10 (the length of the hypotenuse) and forming the ratio gives the correct answer, 0.60, choice H. The cosine and the tangent of ∠A are also present in the answer choices. In order to do well on problems such as this one, you need to be able to tell which trigonometric function is which.
Basic Math Problems in Settings

Basic math problems in settings are what people often call word problems or story problems. They typically describe situations from everyday life in which you need to apply mathematics in order to answer a real-life question. The major difference between this type of problem and the basic math problems that you’ve seen in the examples so far is that the problem isn’t set up for you—you have to set it up yourself. Most people find this to be the most difficult part of word problems. The key steps are reading the problem carefully, deciding what you’re trying to find, sorting out what you really need from what’s given, and then devising a strategy for finding the answer. Once the problem is set up, finding the answer is not much different from solving a basic math problem.

You can find basic math problems in settings in all of the content areas. Question 7 is an example from pre-algebra.

7. What is the total cost of 2.5 pounds of bananas at $0.34 per pound and 2.5 pounds of tomatoes at $0.66 per pound?
   A. $1.00
   B. $2.40
   C. $2.50
   D. $3.50
   E. $5.00

Here, you’re asked to find the total cost of some bananas and tomatoes. The important information is that the total cost includes 2.5 pounds of bananas at $0.34 per pound and 2.5 pounds of tomatoes at $0.66 per pound. A straightforward solution strategy would be to multiply to find the cost of the bananas and the cost of the tomatoes and then add to find the total cost. Now, the problem you’re left with is very basic—calculating $2.5(0.34) + 2.5(0.66)$. Using your calculator might save time and avoid computation errors, but if you see that $2.5(0.34) + 2.5(0.66) = 2.5 (0.34 + 0.66) = 2.5(1.00) = 2.50$, answer C, you might be able to do the computation more quickly in your head.

Basic elementary algebra problems also can be in settings. Question 8 is an example.

8. The relationship between temperature expressed in degrees Fahrenheit (F) and degrees Celsius (C) is given by the formula

   \[ F = \frac{9}{5} C + 32 \]

   If the temperature is 14 degrees Fahrenheit, what is it in degrees Celsius?
   F. -10°
   G. -12°
   H. -14°
   J. -16°
   K. -18°
In this problem, you’re given a relationship (in the form of an equation) between temperatures expressed in degrees Fahrenheit (\(F\)) and degrees Celsius (\(C\)). You’re also given a temperature of 14 degrees Fahrenheit and asked what the corresponding temperature would be in degrees Celsius. Your strategy would probably be to substitute 14 into the equation in place of the variable \(F\). This leaves you with a basic algebra problem—solving the equation \(14 = \frac{9}{5} C + 32\) for \(C\). Before going on to the next problem, checking your answer would probably be a good idea. If you chose \(-10^\circ\) (answer choice \(F\)), substitute \(-10\) for \(C\), multiply by \(9/5\), and add 32 to see if the result is \(14\)°F and confirm that your answer choice was indeed correct. Checking doesn’t take long, and you might catch an error.

Question 9 is an example of an intermediate algebra problem in a setting.

After reading the problem, you know that it is about travel and that the basic formula “distance equals the rate multiplied by the time” \((D = rt)\) or one of its variations \(r = \frac{D}{t}\) or \(t = \frac{D}{r}\) will probably be useful. For travel problems, a table is often an efficient way to organize the information. Because the problem asks for Amy’s usual speed (rate), it would probably be wise to let the variable \(r\) represent her usual speed in miles per hour (mph). You might organize your table like this:

<table>
<thead>
<tr>
<th>Distance (miles)</th>
<th>Rate (mph)</th>
<th>Time (hours)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Usual trip</td>
<td>200</td>
<td>(r)</td>
</tr>
<tr>
<td>Time (\frac{200}{r})</td>
<td></td>
<td></td>
</tr>
<tr>
<td>This trip</td>
<td>200</td>
<td>(r + 10)</td>
</tr>
<tr>
<td>Time (\frac{200}{r+10})</td>
<td></td>
<td></td>
</tr>
</tbody>
</table>

Then, because the time for this trip \(\frac{200}{r+10}\) is 1 hour less than the time for the usual trip \(\frac{200}{r}\), solving \(\frac{200}{r+10} = \frac{200}{r}\) \(-1\) will give the answer. Solving this equation is a matter of using routine algebra skills and procedures. The solution, \(r = 40\), choice \(C\), answers the question, “What is her usual driving speed?” A quick check shows that driving 200 miles at 40 mph takes 5 hours and
that driving 200 miles at 50 mph (which is 10 mph faster) takes 4 hours (which is 1 hour less). This quick check should convince you that your answer is correct.

Coordinate geometry problems can be in settings, too. Question 10 is an example.

10. A map is laid out in the standard \((x,y)\) coordinate plane. How long, in units, is an airplane’s path on the map as the airplane flies along a straight line from City A located at \((20,14)\) to City B located at \((5,10)\)?

- F. \(\sqrt{1,201}\)
- G. \(\sqrt{241}\)
- H. \(\sqrt{209}\)
- J. 7
- K. \(\sqrt{19}\)

In this problem, you’re told that you will be working with the standard \((x,y)\) coordinate plane and that you will need to find a distance. The distance formula should immediately come to mind. All you need is two points, and those are given. The problem now becomes a basic math problem—applying the distance formula:

\[
\sqrt{(x_1-x_2)^2+(y_1-y_2)^2} = \sqrt{(20-5)^2+(14-10)^2} = \sqrt{241} (G).
\]

Your calculator might be useful in finding \((20 – 5)^2 + (14 – 10)^2\), but you should not press the square root key because most of the answer choices are in radical form.

A geometry problem in a setting is illustrated by question 11.

11. A person 2 meters tall casts a shadow 3 meters long. At the same time, a telephone pole casts a shadow 12 meters long. How many meters tall is the pole?

- A. 4
- B. 6
- C. 8
- D. 11
- E. 18

Question 11 has no figure, which is sometimes the case with geometry problems. It might be wise to draw your own figure and label it with the appropriate numbers from the problem. “A person 2 meters tall casts a shadow 3 meters long” is a pretty good clue that you should draw a right triangle with the vertical leg labeled 2 and the horizontal leg labeled 3. And, “a telephone pole casts a shadow 12 meters long” suggests that you should draw another right triangle with the horizontal leg labeled 12. Finding the height of the pole amounts to finding the length of the other leg of your second triangle, which you would label with a variable, say \(h\). Your figure would be similar to this:
The triangles are similar (they’re both right triangles and the angle that the sun’s rays make with the ground is the same for both because the shadows were measured at the same time), so finding the height of the pole amounts to setting up and solving a proportion between corresponding sides of the triangles—a basic math problem. Your proportion might be \( \frac{3}{12} = \frac{2}{h} \). Cross multiply—that is, multiply the numerator of each (or one) side by the denominator of the other side—to get \( 3h = 24 \), and solve to get \( h = 8 \), choice C. Because the numbers are quite simple to work with, you probably wouldn’t use your calculator on this problem.

Last (but not least) of the basic math questions, question 12 shows an example of a trigonometry problem in a setting.

12. The hiking path to the top of a mountain makes, at the steepest place, an angle of 20° with the horizontal, and it maintains this constant slope for 500 meters, as illustrated below. Which of the following is the closest approximation to the change in elevation, in meters, over this 500-meter section?

(Note: You may use the following values, which are correct to 2 decimal places:
\( \cos 20° \approx 0.94; \sin 20° \approx 0.34; \tan 20° \approx 0.36 \)

This problem has a figure, and the figure is labeled with all the necessary information, including a question mark to tell you what you need to find. To set up the problem, you need to decide which of the trigonometric ratios involves the hypotenuse and the side opposite the given angle of a right triangle. Once you decide that the sine ratio is appropriate, you have only a basic trigonometry problem to solve: \( \sin 20° = \frac{h}{500} \), or \( 500 \sin 20° = h \). Then, using the approximation for \( \sin 20° \) given in the note, calculate \( h = 500(0.34) = 170 \), choice G. You may want to use your...
calculator to avoid computation errors. If you chose K, then you probably used the value for cosine rather than sine. Answer H comes from using tangent rather than sine.

**Very Challenging Problems**

The ACT mathematics test emphasizes reasoning ability, so it naturally has problems that can be very challenging. Because these problems are designed to test your understanding of mathematical concepts and your ability to pull together what you have learned in your math classes, they will probably be unlike problems you usually see. Some will be in settings, and some won’t. Some will have figures, and some won’t. Some will have extra information that you should ignore, and some won’t have enough information, so the correct answer will be “Cannot be determined from the given information.” Some will have numeric answers, some will have answers that are expressions or equations that you have to set up, and some will have answers that are statements for you to interpret and judge. On some questions your calculator will be helpful, and on others it will be better not to use it. All of the questions will share one important characteristic, however—they will challenge you to think hard and plan a strategy before you start to solve them.

These challenging problems come from all content areas. Question 13 is one such pre-algebra problem.

<table>
<thead>
<tr>
<th>13. If $537^{102}$ were calculated, it would have 279 digits. What would the digit farthest to the right be (the ones digit)?</th>
</tr>
</thead>
<tbody>
<tr>
<td>A. 1</td>
</tr>
<tr>
<td>B. 3</td>
</tr>
<tr>
<td>C. 4</td>
</tr>
<tr>
<td>D. 7</td>
</tr>
<tr>
<td>E. 9</td>
</tr>
</tbody>
</table>

You certainly wouldn’t want to calculate $537^{102}$ by hand, and your calculator doesn’t display enough digits for you to be able to read off the ones digit for this very large number, so you have to figure out another way to see the ones digit. A good place to start might be to look at the ones digit for powers of 7 because 7 is the ones digit of 537. Maybe there will be a pattern: $7^0 = 1, 7^1 = 7, 7^2 = 49, 7^3 = 343, 7^4 = 2401, 7^5 = 16,807, 7^6 = 117,649, 7^7 = 823,543$. It looks like the pattern of the ones digits is 1, 7, 9, 3, 1, 7, 9, 3, …, with the sequence of these 4 digits repeating over and over. Now, if you can decide where in this pattern the ones digit of $537^{102}$ falls, you’ll have the problem solved. You might organize a chart like this:

<table>
<thead>
<tr>
<th>Ones digit</th>
<th>1</th>
<th>7</th>
<th>9</th>
<th>3</th>
</tr>
</thead>
<tbody>
<tr>
<td>Power of 7</td>
<td>0</td>
<td>1</td>
<td>2</td>
<td>3</td>
</tr>
<tr>
<td></td>
<td>4</td>
<td>5</td>
<td>6</td>
<td>7</td>
</tr>
</tbody>
</table>
The next row would read “8 9 10 11” to show that the ones digits of $7^8$, $7^9$, $7^{10}$, and $7^{11}$, respectively, are 1, 7, 9, and 3. You could continue the chart row after row until you got up to 102, but that would take a lot of time. Instead, think about where 102 would fall. The numbers in the first column are the multiples of 4, so 100 would fall there because it is a multiple of 4. Then 101 would be in the second column, and 102 would fall in the third column. Therefore, the ones digit of $537^{102}$ is 9, choice E.

Question 14 is an elementary algebra problem designed to challenge your ability to think mathematically and use what you’ve learned.

### Question 14: If $a < -1$, which of the following best describes a general relationship between $a^3$ and $a^2$?

- **F.** $a^3 > a^2$
- **G.** $a^3 < a^2$
- **H.** $a^3 = a^2$
- **J.** $a^3 = -a^2$
- **K.** $a^3 = \frac{1}{a^2}$

Here you are told that $a < -1$. Then you are asked for the relationship between $a^3$ and $a^2$. By stopping to think for a moment before trying to manipulate the given inequality or experimenting with numbers plugged into the answer choices, you might realize that if $a < -1$, then $a$ is a negative number, so its cube is a negative number. Squaring a negative number, however, gives a positive number. Every negative number is less than every positive number, so the correct relationship between $a^3$ and $a^2$ is $a^3 < a^2$, choice G. Of course, there are other ways to approach the problem.

For a very challenging intermediate algebra problem, look at question 15.

### Question 15: If $\left(\frac{4}{5}\right)^n = \sqrt{\left(\frac{5}{4}\right)^3}$, then $n =$?

- **A.** $-\frac{3}{2}$
- **B.** $-1$
- **C.** $-\frac{2}{3}$
- **D.** $\frac{2}{3}$
- **E.** $\frac{3}{2}$
In this problem, you’re asked to find the value of a variable, but the variable is in the exponent. After some thought you might decide to try to rewrite \( \sqrt{\left(\frac{5}{4}\right)^3} \) so that it is \( \frac{5}{4} \) raised to a power. You should remember that the square root is the same as the \( \frac{1}{2} \) power, so, after using some properties of exponents, \( \sqrt{\left(\frac{5}{4}\right)^3} = \left(\left(\frac{5}{4}\right)^{\frac{1}{2}}\right)^3 = \left(\frac{5}{4}\right)^{\frac{3}{2}} \). Now at least the left side and the right side of the equation have the same form, but the bases of the two expressions aren’t the same—they’re reciprocals. In thinking about the connection between reciprocals and exponents, it is good to realize that taking the opposite of the exponent (that is, making it have the opposite sign) will flip the base, because \( a^{-k} = \frac{1}{a^k} \). That means \( \left(\frac{5}{4}\right)^{\frac{3}{2}} = \left(\frac{4}{5}\right)^{-\frac{3}{2}} \). So now, with \( \left(\frac{4}{5}\right)^{\frac{3}{2}} = \left(\frac{4}{5}\right)^{\frac{1}{2}} \), \( n = -\frac{3}{2} \), choice A.

Coordinate geometry problems can also be very challenging. Question 16 is an example.

**16.** In the standard \((x, y)\) coordinate plane, the triangle with vertices at \((0,0)\), \((0,k)\), and \((2,m)\), where \(m\) is constant, changes shape as \(k\) changes. What happens to the triangle’s area, expressed in square coordinate units, as \(k\) increases starting from 2?

- **F.** The area increases as \(k\) increases.
- **G.** The area decreases as \(k\) increases.
- **H.** The area always equals 2.
- **J.** The area always equals \(m\).
- **K.** The area always equals \(2m\).

This problem might seem confusing at first because it contains two different variables and no figure to clarify. You’re told that \(m\) is a constant but \(k\) changes. So, to get started, you could pick a value for \(m\), say \(m = 1\). Then, at least you can start sketching a figure. The point \((0,k)\) is on the \(y\)-axis and \(k\) increases starting with 2, so you could start by drawing a figure similar to this:

You can see the triangle that the problem mentions. If you think of the line segment from \((0,0)\) to \((0,k)\) as the base and the line segment from \((2,1)\) to \((0,1)\) as the height, you can see that as \(k\) increases, the base of the triangle gets longer but the height remains the same. From geometry, you know that the area of a triangle is given by \( \frac{1}{2} \) (base)(height). Therefore, the area will increase as the base gets longer. So, the area will increase as \(k\) increases, choice F. You should be able to
reason that for any value of $m$, the result would have been the same, and you can feel confident that the correct answer is the first answer choice.

Question 17 is an example of a very challenging geometry problem.

17. In the figure below, $\overline{AB} \cong \overline{AC}$ and $\overline{BC}$ is 10 units long. What is the area, in square inches, of $\triangle ABC$?

A. 12.5
B. 25
C. $25\sqrt{2}$
D. 50
E. Cannot be determined from the given information

This problem has a figure, but none of the information given is marked on the figure. A wise move is to mark the figure yourself to indicate which sides are congruent and which side is 10 units long. You need to find the area of $\triangle ABC$, and you know that the base $\overline{BC}$ is 10 units long. You need the measure of the height $\overline{AD}$ before you can apply the formula for the area of a triangle. You might ask yourself, “Is there any way to get the height?” If you were given the measure of one of the angles or the measure of one of the congruent sides, you might be able to find the height, but no other information is given. With a little more thought, you should realize that the height can be any positive number because there are infinitely many isosceles triangles with bases 10 units long. You conclude that not enough information is given to solve this problem, and the correct answer choice is E: “Cannot be determined from the given information.”

This is the example that was mentioned earlier when “Cannot be determined from the given information” is the correct answer. Remember not to jump to a hasty conclusion when “Cannot be determined from the given information” is an answer choice. Sometimes it is the right answer, but sometimes it isn’t.

Very challenging problems can be in settings, too. Question 18 is an example from pre-algebra.
18. A bag of pennies could be divided among 6 children, or 7 children, or 8 children, with each getting the same number, and with 1 penny left over in each case. What is the smallest number of pennies that could be in the bag?

F. 22
G. 43
H. 57
J. 169
K. 337

In this problem, whenever the pennies in the bag (which contains an unknown number of pennies) are divided evenly among 6 children, 7 children, or 8 children, 1 penny is always left over. This means that if you take the extra penny out of the bag, then the number of pennies left in the bag will be divisible (with no remainder) by 6, 7, and 8. You should ask yourself, “What is the smallest number that is divisible by 6, 7, and 8?” In mathematical terminology, you’re looking for the least common multiple of 6, 7, and 8. One way to find the least common multiple is to use the prime factorizations of the three numbers and to find the product of the highest power of each prime that occurs in one or more of the three numbers. This process will yield $2^3 \cdot 3 \cdot 7 = 168$. (As a check: $168 \div 6 = 28$, $168 \div 7 = 24$, and $168 \div 8 = 21$.) But wait! You’re not quite finished. Remember to add back in the penny that you took out of the bag originally to make the divisions come out even. Thus, your answer is 169, choice J.

Question 19 is an example of an elementary algebra word problem that is very challenging.

19. There are $n$ students in a class. If, among those students, $p\%$ play at least 1 musical instrument, which of the following general expressions represents the number of students who play NO musical instrument?

A. $np$
B. $.01np$
C. $\frac{(100 - p)n}{100}$
D. $\frac{(1 - p)n}{.01}$
E. $100(1 - p)n$

This is an example of a problem that has a mathematical expression as its answer. Finding an expression to answer a question usually makes you think more than finding a numerical answer because the variables require you to think abstractly. In this problem, you are told that out of a class of $n$ students, $p\%$ play 1 or more musical instruments. Finding the percent of students who play no musical instrument is simple: $(100 - p)\%$. To find the number of students who play no musical instrument, you’d probably want to convert $(100 - p)\%$ to a decimal and multiply by $n$. If $100 - p$ were a number you’d automatically move the decimal point two places to the left. But,
because there's no decimal point to move in $100 - p$, you have to think about what you need to do to convert $(100 - p)\%$ to a decimal. Moving the decimal point two places to the left is the same as dividing by 100, so $(100 - p)\%$ as a decimal is $\frac{100 - P}{100}$, and the number of students who play no musical instrument is $\frac{(100 - p)n}{100}$, choice C.

Question 20 is an example of a very challenging coordinate geometry problem in a setting.

20. Starting at her doorstep, Ramona walked down the sidewalk at 1.5 feet per second for 4 seconds. Then she stopped for 4 seconds, realizing that she had forgotten something. Next she returned to her doorstep along the same route at 1.5 feet per second. The graph of Ramona’s distance ($d$) from her doorstep as a function of time ($t$) would most resemble which of the following?

F. $d$

J. $d$

G. $d$

K. $d$

H. $d$
This problem is different from any of the problems you’ve seen so far because its answer is a graph. And, instead of giving you an equation and asking you to identify the equation's graph, this problem describes a situation and asks you to decide which graph represents the situation. You need to think about what the description of each of Ramona’s activities says in terms of distance as a function of time and what each activity would translate into graphically. For example, at first, Ramona walked at a constant rate down the sidewalk. Therefore, she moved farther away from her doorstep as time elapsed, and her distance from her doorstep increased at a constant rate as time increased. So, the first part of the graph should be a line segment with a positive slope. Unfortunately, all five graphs start out this way, so none of the options can be eliminated at this point. The next thing Ramona did was stop for 4 seconds. If she stood still, her distance from her doorstep would not change even though time was still elapsing. This part of the graph should then reflect a constant value for \( d \) as time increases. It should be a horizontal line segment. This information allows you to eliminate options F, G, and K, because they do not have a horizontal line segment. Ramona’s next activity helps you decide between H and J. Ramona walked back home at the same rate along the same route as before. On her way back home, her distance from her doorstep decreased at a constant rate as elapsed time increased. This would be graphed as a line segment with a negative slope, and therefore J is the correct graph.

Another word problem that challenges you to think mathematically is question 21.

21. An object detected on radar is 5 miles to the east, 4 miles to the north, and 1 mile above the tracking station. Among the following, which is the closest approximation to the distance, in miles, that the object is from the tracking station?

- A. 6.5
- B. 7.2
- C. 8.3
- D. 9.0
- E. 10.0

This problem is about computing a distance, but it’s a distance in three-dimensional space without a picture to help you. For this problem, drawing a sketch of the situation might help. Your sketch might be a “box” such as this:
You need to find the length of the diagonal from the lower left corner of the front of the box to the top right corner of the back of the box. This is the hypotenuse of a right triangle (ΔOBT on the figure redrawn in the following) that has its right angle at B. One leg of this triangle has length 1, but the other leg is BT, and you don't know the length of BT.

A closer look shows that BT is the hypotenuse of ΔTAB, which has its right angle at A and legs that measure 5 and 4. Using the Pythagorean theorem gives $BT = \sqrt{5^2 + 4^2} = \sqrt{41}$.

Now you can use the Pythagorean theorem again to get $OT = \sqrt{BT^2 + OB^2} = \sqrt{(\sqrt{41})^2 + 1^2} = \sqrt{42}$ which is about 6.5, choice A.

**Question Sets**

The mathematics test generally contains sets of questions that all relate to the same information. Questions 22–24 illustrate a question set that relates to information from a paragraph and a graph. The mathematics test typically contains two question sets with two to four questions per set.
Use the following information to answer questions 22–24.

At both Quick Car Rental and Speedy Car Rental, the cost, in dollars, of renting a full-size car depends on a fixed daily rental fee and a fixed charge per mile that the car is driven. However, the daily rental fee and the charge per mile are not the same for the 2 companies. In the graph below, line $Q$ represents the total cost for Quick Car Rental and line $S$ represents the total cost for Speedy Car Rental.

22. Robert plans to rent a full-size car for 1 day and drive only 50 miles. If his only consideration is to incur the least cost, which company should he choose?

F. Quick Car Rental, because the cost is $5.00 less.
G. Quick Car Rental, because the cost is $15.00 less.
H. Either company, because the costs are equal.
J. Speedy Car Rental, because the cost is $5.00 less.
K. Speedy Car Rental, because the cost is $15.00 less.
23. If you rent a full-size car from Quick Car Rental for 1 day, how much more would the total rental cost be if you drove the car 78 miles than if you drove it 77 miles?
   A. $0.10
   B. $0.15
   C. $0.20
   D. $0.40
   E. $0.55

24. What would be the total cost of renting a full-size car from Speedy Car Rental for 1 day and driving the car 150 miles?
   F. $60
   G. $75
   H. $85
   J. $90
   K. $120

Once you’ve looked at the information given for a group of questions, you can use the same sorts of strategies to answer the questions that you would use on any question on the ACT mathematics test. Question 22 requires you to read the graph and compare the costs of renting a car from the 2 companies, assuming that the car is going to be driven 50 miles. From the graph, the cost for Speedy Car Rental appears to be about $40, and the cost of Quick Car Rental appears to be about $35. These points are marked on the graph that is redrawn in the following.

So Robert will incur the least cost if he rents from Quick Car Rental because that cost is $5 less, choice F.
Question 23 requires you to determine how much more Robert would pay if he rented a car from Quick Car Rental and drove 78 miles than if he drove 77 miles. Using mathematical concepts might be a better approach than trying to read the graph, because you might not be able to read the graph accurately enough. You know from coordinate geometry that, in the standard \((x,y)\) coordinate plane, the slope of a line gives the rate of change in \(y\) per unit change in \(x\), which is exactly what you want to find in this problem—how much the cost at Quick Car Rental changes when the car is driven 1 more mile.

The formula to determine the slope of a line is \(m = \frac{(y_2 - y_1)}{(x_2 - x_1)}\), where \(m\) is the slope, \((x_1,y_1)\) are the coordinates of one point, and \((x_2,y_2)\) are the coordinates of the other. Two points that are easy to read accurately off the graph are \((0,15)\) and \((50,35)\), labeled on the redrawn following graph. Plug the coordinates into the equation to get \(m = \frac{(35 - 15)}{(50 - 0)} = \frac{20}{50} = 0.4\) mile. So, the difference for driving 78 miles instead of 77 miles (that is, for driving 1 more mile) is \$0.40, choice D.

In question 24, you are asked for the cost of renting a car from Speedy Car Rental and driving it 150 miles. You can’t simply read the cost off the graph, because 150 isn’t on the graph, but you can find an equation of the line for Speedy Car Rental and then plug 150 into the equation. Recall that a line is determined by any two points on the line, call them \((x_1,y_1)\) and \((x_2,y_2)\), and that one way of finding an equation of the line is by first finding slope with \(m = \frac{y_2 - y_1}{x_2 - x_1}\) and then using the two-point form of the equation of a line, \((y - y_1) = m(x - x_1)\). Here, you can use two points that are easy to read off the graph for Speedy Car Rental, such as \((0,30)\) and \((100,50)\), shown on the redrawn graph on the next page. The slope through any two points on this line is \(m = \frac{50 - 30}{100 - 0} = \frac{20}{100} = 0.2\), and the equation \((y - 30) = 0.2(x - 0)\) fits all of the points.
on the line. This equation can be rewritten as \((y - 30) = 0.2x\). So, when \(x = 150\), that means 
\((y - 30) = 0.2(150)\) and then \(y - 30 = 30\) and then \(y = 60\). The cost is $60, choice F.

As you have seen in the sample questions in this section, the mathematics test includes many 
types of questions. Some will be easy for you, and some will be hard. They all will require you to 
demonstrate as much as possible about what you know and can do in mathematics.
Strategies for Taking the ACT Mathematics Test

**Pace Yourself**
You have 60 minutes to answer 60 questions, which gives you an average of 1 minute per problem. Some problems will take you less than 1 minute, and some will take you more. Don’t spend too much time on any one question. You should keep a close eye on your watch to make sure you work at a pace that will enable you to finish the test in the 60 minutes allotted. When determining your pace, be aware that the questions are arranged approximately in order of difficulty: easier questions first and hardest last.

**Answer All Questions**
Answer all questions even if you have no idea how to solve some of them. If you’re stumped and have time, eliminate as many of the options as you can and then guess from among the remaining choices. If time is running out and you don’t have time to eliminate any of the options, guess anyway. Even a wild guess has a 20% chance of being correct, but a blank has no chance of being correct. Remember, your score is based solely on the number of questions you answer correctly—there is no penalty for guessing and no penalty for wrong answers. Scores are most comparable if everyone answers every question.
**Answer All the Easy Questions First, Then Go Back to Answer the Hard Ones**

Easy and hard are relative terms. What might be easy for one student might be hard for another. You know which math topics are easy for you and which are hard. Answer all the questions that are easy for you and then go back to the hard ones. Remember that you don't get more points for answering hard questions. All questions, no matter how easy or hard, count equally toward your mathematics total score. If you don't see a way to solve a problem, or if the method you're using seems to be taking a lot of time, take your best guess (as explained in the previous section) or skip the question and move on to questions that you can answer more easily. If you skip the question, don't forget to mark in the test booklet (never on the answer document) all those questions that you skip so that you can easily return to them later.

**Note:** In some circumstances you are not permitted to write in your test booklet. In those circumstances, you’ll be given scratch paper, and you can use it to jot down the numbers of the questions you skip.

**Read Each Problem Carefully**

Read carefully enough so you know what you’re trying to find before you start looking for it and so you know what you have to work with to help you find it. Remember that questions may contain extraneous details you will need to ignore or insufficient information to solve the problem. Think twice before choosing “Cannot be determined from the given information,” because test-takers often choose this option when the answer, in fact, can be determined from the information given. Make sure you are not overlooking a key piece of information provided or an alternate strategy for solving the problem.

**Look for Information in the Answer Choices**

Sometimes looking at the answer choices provides valuable information about the form of the answer. For example, you might be able to judge whether your answer should be left in radical form or converted to a decimal approximation, whether your polynomial answer should be left in factored form or multiplied out, or whether you should spend time reducing a probability to lowest terms. For some problems, you have to analyze the options as part of your solution strategy. For example, when a question asks, “Which of the following statements is true?” and the statements are the five options, you probably need to examine each option in turn. Sometimes, using the options gives you an alternate way to solve a problem. For example, suppose you’re trying to solve a quadratic equation and you can’t get the quadratic expression to factor and can’t remember the quadratic formula. You might be able to get the correct answer by substituting the options, in turn, into the equation until one works. This strategy should be used very sparingly, however, because it can be more time-consuming than other strategies.
Use Illustrations Wisely and Whenever You Can

The old saying “A picture is worth a thousand words” holds true on the mathematics test:

- Refer to illustrations whenever they are provided.
- If no illustration is provided and one might be useful, draw your own illustration in the test booklet. This can be especially helpful in solving word problems.
- Transfer information from the question to the illustration, if you think it might be helpful. For example, you might write dimensions on the figure that are given in the question but aren’t shown on the figure or that you calculate in the process of solving the problem, or you might add marks to show congruences or draw auxiliary lines such as perpendiculars and diagonals.

Note: In some circumstances you are not permitted to write in your test booklet. In those circumstances, you’ll be given scratch paper to use.

Use Your Calculator Wisely

Each problem on the mathematics test can be solved in a reasonable amount of time without a calculator. A calculator is most helpful if you are very familiar with the one you bring to the test and you use it wisely during the test. Experimenting with the capabilities of a new calculator during the testing session or using a calculator in situations when a non-calculator approach would be better can cost you precious time. Bring the calculator that you are most familiar with—the one you use in your math classes or at home—but make sure it is an ACT-permitted calculator (visit www.actstudent.org for details). Don’t worry that other students have more sophisticated calculators than yours; the type of calculator that students use should not make a difference in their scores. Use your calculator wisely; remember that a non-calculator strategy is often better than a calculator strategy. And don’t believe everything your calculator tells you. Make sure the numbers it gives you are reasonable and make sense.

Think!

Your head is by far a more powerful and efficient problem-solving tool than a pencil or a calculator. Think before you plunge in and begin working on a problem. Don’t panic if you suddenly can’t remember a formula or all of the steps of a procedure you’ve been taught. You can often find another way to do a problem that will work just as well. For example, you don’t have to write and solve an equation for every algebra word problem. You might be able to reason through such a problem and get the correct answer without an equation. Sometimes the best option is to let your common sense about numbers take over.
Show Your Work
You have certainly heard this before—probably in every math class you’ve ever taken. Of course, you’re not going to have time during the test to write down every step for every problem the way you might on a homework assignment, but writing down at least some of what you are thinking and doing as you solve a problem will be worth the time it takes. If you’re using a calculator, you can write down the numbers that you plug into it and the intermediate results it gives you, to keep a running record of what you did. If you don’t write anything down and your answer for a problem doesn’t match any of the answer choices, your only alternative is to start over. But, if you have at least something written down, you may be able to go back over your work and find your mistake. Also, if you have time at the end of the test to go back and check your answers, having something written down will enable you to check your work more quickly.

Check Your Answers
Before you leave a question, make sure your answer makes sense. Don’t believe everything your calculator tells you; make sure that the answer your calculator displays makes sense to you and that your answer actually answers the question. For example, if a problem about oranges and apples asks for the number of apples, make sure your answer doesn’t give the number of oranges, or if a problem asks for the altitude of a triangle, make sure your answer isn’t the hypotenuse. Remember, if you have time remaining after answering all of the questions, use it wisely and go back and check your work. That’s a skill that will help you in college and career, too.
Chapter 7: Improving Your Reading Score

Designed to measure your reading speed and comprehension, the ACT reading test comprises several reading passages, each of which is followed by 10 multiple-choice questions, for a total of 40 questions. You are given 35 minutes to complete the test. The passages on the reading test come from published materials, such as books and magazines, written at a level that a first-year college student can expect to read for a class.

Content of the ACT Reading Test
The ACT reading test may contain passages from each of the following categories:

- **Prose fiction** (passages from short stories or novels)
- **Humanities** (architecture, art, dance, ethics, film, language, literary criticism, memoir, music, personal essays, philosophy, radio, television, theater)
- **Social studies** (anthropology, archaeology, biography, business, economics, education, geography, history, political science, psychology, sociology)
You’ll have 35 minutes to read the reading test’s passages and answer the 40 multiple-choice questions. That’s not a lot of time, but it’s more than you might think. Once you’ve read through this section, you’ll have a better idea of what the reading test is all about and what you need to do in order to perform well on it. Your reading test score will tell you how you did on all 40 questions of the reading test.

The reading test evaluates your ability to understand the passages that appear on the test. It does not test your ability to remember relevant facts from outside the passage. You don’t need to be knowledgeable about the subject area that a passage covers in order to do well on the questions, but you do need to read attentively and to think carefully about what you read. The passages may deal with familiar or unfamiliar subjects. It doesn’t matter though; the passages contain all the information you need to answer the questions.

Types of Passages on the ACT Reading Test

Just as going to see the latest action movie is different from watching a wildlife special on public television, reading a novel or short story is a different experience from reading a scientific article. As you read the different passages on the reading test, you may find it helpful to keep their essential differences in mind.

Prose Fiction

Prose fiction passages generally include a narration of events and revelation of character. Think about how you read fiction. What do you look for? Do you read fiction hoping to find facts or to be entertained and enlightened? Although we learn a great deal when we read fiction, most of us read for the story—to “find out what happens”—or because we’re interested in the characters. The questions on prose fiction passages ask about the kinds of things you pay attention to when you read a short story or novel—plot, characters, and mood, among other things.

As you read a prose fiction passage, don’t just note events. Try to be aware of the passage’s mood or tone, the relationships of the characters, and the emotion implied by what the characters say as well as how they say it. An author often uses dialogue not only to explain a situation to a reader but also to reveal character. Refer to the sample passages on pages 271 and 272 for examples of prose fiction passages.

Humanities

Humanities passages describe or analyze ideas or works of art. Although some humanities passages taken from memoirs or personal essays may seem a bit like prose fiction passages, there is one important difference: the memoirs and personal essays are written as fact, whereas prose fiction is imagined.
Humanities passages present information, but you’ll also need to pay attention to the author and his or her point of view. Sometimes, a question will ask you to project the author’s likely response to a hypothetical argument or situation based on what the passage tells you about the author’s opinions and what the language implies.

These passages might have characters, but they’re not characters like those in a short story. Rather, they’re historical figures or contemporary people—people who have actually lived. In these passages, the kinds of relationships you’ll be asked to infer or identify are those among events, ideas, people, trends, or modes of thought. Refer to the sample passage on page 275 for an example of a humanities passage.

**Social Studies**

Social studies passages typically present information gathered by research. A social studies passage might be about Japanese history or political action committees or a psychological experiment. You’ll find names, dates, and concepts in these passages. You’ll also need to pay close attention to what name goes with what concept in a discussion of political systems and to keep track of who said what in a passage discussing different views of a constitutional amendment. Watch for cause-effect relationships, comparisons, and sequences of events. Pay careful attention to the specifics, especially the way in which they help you shape an idea of the passage’s subject. Refer to the sample passages on pages 273 and 274 for examples of social studies passages.

**Natural Sciences**

The natural sciences passage typically presents a science topic and an explanation of the topic’s significance. It requires a different sort of analysis than a prose fiction passage. For instance, in a natural sciences passage, the author is typically concerned with the relationships between natural phenomena, not the relationships between characters. As with social studies passages, you should pay special attention to cause-effect relationships, comparisons, and sequences of events. Keep track of any specific laws, rules, and theories mentioned, but don’t try to memorize them.

Many of the reading test’s nonfiction passages, especially natural sciences passages, will include some specialized or technical language. Don’t let new words throw you. If knowing the meaning of a word is necessary to answer a question, the passage will provide clues to the word’s meaning. Do your best to figure out the meaning from the context, and then go on. Don’t devote extra time to a single word unless it comes up later in one of the questions. Refer to the sample passages on pages 276 and 277 for examples of natural sciences passages.

**Types of Questions on the ACT Reading Test**

On the reading test, the questions typically fall into one of two basic categories: referring and reasoning. Referring questions ask you to find or use information that is clearly stated in the passage. Reasoning questions ask you to do more: they ask you to take information that’s either stated or implied in the passage and use it to answer more complex questions.
You shouldn't worry about these categories while you're taking the reading test. It's most important that you focus on the questions themselves and on what they ask you about a given passage. Because each passage is different, the kinds of questions will vary from passage to passage. Still, there are some general types of questions you're likely to encounter. Most questions will ask you to do one of the following:

- Identify and interpret details
- Determine the main idea of a paragraph, paragraphs, or a passage
- Understand comparative relationships (comparisons and contrasts)
- Understand cause-effect relationships
- Make generalizations
- Determine the meaning of words from context
- Understand sequences of events
- Draw conclusions about the author's voice and method

Sometimes, the reading test contains other types of questions, but don't worry. Just make sure you read each passage and its questions carefully. You'll find that the information you need to determine the best answer for a question is always available in the passage. Questions that illustrate each of the most common types of questions on the reading test follow.

**Representative ACT Reading Test Questions**

**Details.** Some test questions ask you to pick out a detail from a passage. A detail can be something as seemingly simple as a characteristic of a person, place, or thing, or a particular date. Other questions of this type require you to do a bit more interpreting of minor or subtly stated details, as in the following example, based on a social studies passage on Eleanor Roosevelt (ER), which is found on page 273:

1. The passage states that ER believed the relationship between a people and their government should be:
   A. begun and carried out as if it were an isolated, individualist adventure.
   B. formed and modeled by the White House.
   C. based on organized, widespread citizen participation.
   D. controlled through radio broadcasts and formal channels.

You'll have to look around the passage for the information you need—not unusual for this kind of question. According to the author, ER's "abiding conviction . . . was that nothing good would happen to promote the people's interest unless the people themselves organized to demand government responses" (lines 55–58). Because ER felt "a people's movement required active citizen participation" (lines 58–59), it's clear that C is the best answer. A, B, and D violate the
spirit of the quoted lines: ER wanted collective action and active citizen participation, not isolated individualism (A), White House domination (B), or control through radio broadcasts and formal channels (D).

Questions about details sometimes ask you to find the one detail that does not support a particular point. Such questions are usually signaled by words such as NOT and EXCEPT. Pay careful attention to these questions. When you answer them, remember that the usual question format is being reversed. Here’s an example of this kind of reverse question, based on a prose fiction passage about a girl and her friend Eugene (page 271):

2. Which of the following questions is NOT answered by information in the passage?
   F. Has the narrator ever walked around inside Eugene's house?
   G. What hobby or interest do Eugene and the narrator share?
   H. What makes Eugene's house different from other houses on the block?
   J. What careers other than teaching has the narrator considered pursuing?

Three of the questions presented in the answer choices are answered by the passage, and the fourth one—the one you’re looking for—isn’t. Of the four, the only question not answered by the passage is J: we never learn what other careers besides teaching the narrator has considered pursuing. All three of the other questions are answered in the passage. We learn from lines 81–82 that although the narrator has watched the house “for so many years,” she only dreams about going inside, ruling out F. We know from lines 39–40 and lines 63–66 that Eugene and the narrator are both interested in books, so G is out. According to the narrator, Eugene's house is “the only house on the block that had a yard and trees” (lines 5–6), so H, too, is incorrect.

Detail questions aren’t the only kind of question that can make use of the reverse format. Don’t worry, though—just watch for words such as NOT and EXCEPT in questions, and you’ll be fine.

**Main Ideas.** To answer this kind of question, you need to be able to determine the focus of a passage or of a paragraph or paragraphs in a passage. You shouldn’t count on finding this information summed up in the first paragraph of a passage or in the first sentence of a paragraph. You may have been advised to make the first sentence of each paragraph the topic sentence in your own writing, but not every writer does that. You’ll need to figure out what the author’s main point is in one or more paragraphs or in an entire passage by reading the paragraph(s) or passage carefully.

Main idea questions can be fairly straightforward. The following question, based on a social studies passage about the development of perceptual abilities (page 274), is pretty direct:

3. The main point of the passage is that:
   A. during the first four to seven months of life, babies learn at an accelerated pace.
   B. organisms deprived of critical life experiences may or may not develop normal sensory performance.
   C. the development of perceptual abilities is the result of the interaction between nature and experience.
   D. research concerned with physical skills and abilities adds little to our knowledge of the growth of the mind.
The idea that the interaction between nature and experience shapes the development of perceptual abilities (C) is the clear focus of the entire passage. In the first paragraph, the author states that “the ancient central question of psychology” is “how much is due to nature and how much to nurture (or, in developmental terms, to maturation and to learning)” (lines 5–8). The second through eighth paragraphs (lines 9–85) describe research designed to help answer this question as it relates to the development of perceptual abilities in children. The last paragraph sums up the passage by saying that this research helps us “catch the first glimpse of how mind is constructed out of matter by experience” (lines 88–89). Though in lines 50–53 the author describes the rapid development of infants between four and seven months old, this is only a minor part of the passage, so A is incorrect. The seventh paragraph (lines 61–73) does mention that organisms can be permanently harmed if they miss critical life experiences, but this, also, isn’t the main point of the passage, making B incorrect. Choice D is just plain wrong: the whole passage deals with how research on physical skills and abilities has added to our knowledge of the growth of the mind.

As that example shows, you may have to rule out answer choices that either are supporting (rather than main) ideas or simply misstate what the passage says. Both types of wrong answers appear in this next example, based on the natural sciences passage about lightning and fire (page 276):

4. One of the main points of the third paragraph (lines 41–61) is that:

   F. Arizona researchers record tree mortality by volume.
   G. tree mortality rates fail to capture the true extent of lightning-inflicted damage.
   H. ponderosa pine trees are resistant to secondary diseases.
   J. pine tree forests draw fewer lightning strikes than many other habitat types in Arizona.

Choice G is the best answer here. Tree mortality rates “describe only direct injury” to trees (line 56), but lightning can also kill trees indirectly by making them vulnerable to insects, wind, and mistletoe and by causing fires. Although F is true, according to lines 54–56, the fact that Arizona researchers record tree mortality by volume is a minor point. The paragraph never claims that ponderosa pine trees are resistant to secondary diseases or that pine tree forests draw fewer lightning strikes than do many other habitat types in Arizona, so both H and J are incorrect.

Some questions for prose fiction or humanities passages will use phrases such as main conflict or main theme instead of main idea, but you should approach the questions in the same way as you would other main idea questions. Here’s an example based on a prose fiction passage about a young woman, Cally Roy (page 272):

5. The main conflict in this passage could best be described as the:

   A. tension between the narrator’s mother and Frank.
   B. hostility expressed between the narrator and her mother.
   C. narrator’s efforts to break her ties to her mother and grandmothers.
   D. narrator’s internal struggle to connect with her past and find her future.
You have to read the whole passage carefully to sort out what the main conflict is because there’s at least some truth to all of the answer choices. Choice D turns out to be the best of the four choices because the main conflict is within the narrator herself. She journeys away from home and “into the city’s bloody heart” (lines 18–19), she wonders “about the meaning of [her] spirit name” (line 22), she feels out of place in her too-big “Frankenstein body” (line 76), and she ends the passage torn between her “city corner” and her life “back home” (lines 82–83). The narrator says her mother loves Frank “too much to live with” him (lines 36–37) and also that Frank “can’t drag himself away from the magnetic field of mother’s voice” (lines 68–69), but the tension between the narrator’s mother and Frank isn’t the main conflict of the passage, making A wrong. There could be some hostility between the narrator and her mother because the narrator doesn’t seem to want to go to the tribal college like her mother wants her to (see lines 79–82), but the narrator also wants to “curl next to her and be a small girl again” (lines 74–75), so mother-daughter hostility isn’t the main conflict, either, ruling out B. Choice C misses the mark because although the narrator has left her home and her mother, her grandmothers are only briefly talked about in the passage (see lines 24–33), so the main conflict can’t revolve around them.

**Comparative Relationships.** You’re likely to find questions asking you to make comparisons and contrasts in passages that contain a lot of information or that feature multiple characters or points of view. This kind of test question can make you process a lot of information—you may be asked to weigh one concept against another and identify a significant difference between the two. But comparison and contrast questions aren’t always overly complicated. In the following example, based on a humanities passage about the nature of work (page 275), the comparison is directly made in a few lines in the passage:

6. According to the author, the significant difference between a bread-maker and a bread pan is that only one:
   
   F. was used by previous generations.
   
   G. came on the market in recent years.
   
   H. goes in the oven when the dough is prepared.
   
   J. diminishes the human role in making bread.

Lines 1–3 state, “The difference between a machine and a tool—between a bread-maker and a bread pan—is that a tool extends human skills, a machine replaces them.” Thus, J is the best answer. None of the other three answer choices is mentioned in the passage: the author never claims that the significant difference between a bread-maker and a bread pan is that one was used by previous generations (F), came on the market in recent years (G), or goes in the oven when the dough is prepared (H).

Not all comparative relationships questions are this direct, however. This next example, based on the same passage, shows that this type of question can get more complicated, especially when the question is in the reverse format discussed in the Details section:
The information needed to answer this question is in the first paragraph: once the narrator lost her indis, she says, she “began to wander from home, first in my thoughts, then my feet took after” (lines 11–13). Choice G is therefore the best answer. Choice F is pretty much the opposite of the truth, in the sense that the narrator decided to leave home. Although the narrator claims she “remember[s] every detail” of her indis (line 5), this isn’t because she lost it but because “the turtle hung near my crib, then off my belt, and was my very first play toy” (lines 5–7). So H can’t be the best answer. Choice J is incorrect because the narrator never really implies that losing her indis has caused her to fight with her family. Although her mother was “in a panic” (line 27) over the narrator’s decision to leave, this seems more out of concern for the narrator than the result of a fight.
Following is an example of a somewhat more complex cause-effect question, this time based on the natural sciences passage on lightning and fire:

9. The third paragraph (lines 41–61) suggests that if lightning did not fix atmospheric nitrogen, then:
   A. rain could not fall to Earth, leaving nitrogen in the atmosphere.
   B. less nitrogen would be found on Earth.
   C. electrical current could not be conducted by air.
   D. lightning bolts would strike the earth with less frequency.

Although the question lets you know to look in the third paragraph, the wording of that paragraph is subtle and requires close reading. The relevant information is in lines 45–46: “Lightning helps to fix atmospheric nitrogen into a form that rain can bring to Earth.” This matches nicely with B, which says that less nitrogen would be found on Earth. Although nitrogen would remain in the atmosphere if lightning didn’t fix it, the paragraph never suggests that rain wouldn’t fall to Earth, making A tempting but wrong. The paragraph doesn’t suggest that if lightning didn’t fix atmospheric nitrogen, electrical current couldn’t be conducted by air or that lightning bolts would strike the earth with less frequency, making C and D incorrect.

**Generalizations.** This type of question usually asks you to take a lot of information—sometimes the whole passage—and boil it down into a more concise form. A generalization question may involve interpreting mood, tone, or character, or it may ask you to make some kind of general observation or draw a conclusion about the nature of an argument the author is making. The following example, based on the social studies passage about Eleanor Roosevelt, focuses on personality or character:

10. As she is revealed in the passage, ER is best described as:
   F. socially controversial but quietly cooperative.
   G. politically courageous and socially concerned.
   H. morally strong and deeply traditional.
   J. personally driven but calmly moderate.

This question requires you to sum up the complex personality of Eleanor Roosevelt in just a few short words. The best answer is G, because examples of ER being politically courageous and socially concerned are found throughout the passage. The fourth paragraph (lines 20–25), for instance, reveals that as First Lady, “she upset race traditions, championed a New Deal for women, and on certain issues actually ran a parallel administration” to the one her husband, Franklin Delano Roosevelt, ran as president of the United States. Although ER “is the most controversial First Lady in United States history” (lines 1–2) and though she believed in collective action and “united democratic movements for change” (lines 61–62), it would be wrong to say, as F does, that “socially controversial but quietly cooperative” is the best description of ER. The passage implies that there was very little quiet about ER. She clearly wasn’t deeply traditional, so H is out. Similar to F, choice J is tempting because it’s in some ways true but, again, not the best description of ER. Although she was personally driven and supported the idea of a “middle
way” (line 54) between fascism and communism, J wrongly states that ER was calmly moderate. She was, in fact, someone who challenged long-held traditions and created great controversy by doing so.

**Meanings of Words.** Questions about meanings of words ask you to determine from context what a particular word, phrase, or statement most nearly means. In some cases, the word or words will probably be unfamiliar to you, but even when familiar words are tested, you’ll have to look at the context in which they appear to determine the closest synonym or paraphrase. Sometimes, looking at a single sentence of the passage is enough to figure this out, but other times, you’ll have to look at sentences before or after the given word, phrase, or statement in order to determine the closest meaning.

Many meanings-of-words questions will focus on a single word or a short phrase. The answer choices will include synonyms for the word or phrase that you might find in a dictionary or thesaurus, but only one of the choices will truly reflect how the word or phrase is used in this particular case. Look at the following example, based on the natural sciences passage about lightning and fire:

11. The process of “electrocution” mentioned in line 62 most nearly refers to:
   
   A. the ignition of rotten wood and pine needles.
   B. accidental death by electrical current.
   C. a lightning strike of a tree.
   D. the scorching of plants by lightning.

If you merely looked at the question without looking at the passage, B might be an attractive choice because this is how the word *electrocution* is often used in everyday life. But B makes little sense in the context of the fourth paragraph (lines 62–70), which discusses how lightning scorches plants, so the best answer is D. Scorching isn’t the same thing as igniting, and the paragraph doesn’t mention rotten wood or pine needles, so A is incorrect. Choice C isn’t the best answer, either, because lines 64–65 state that the process of “electrocution” isn’t “limited to trees.”

Sometimes meanings-of-words questions will ask you to paraphrase an entire statement, as in the following example, taken from the prose fiction passage about a girl and her friend Eugene:

12. When the narrator says, “I begin to think of the present more than of the future” (lines 80–81), she most likely means that meeting Eugene led her to:
   
   F. shift some of her attention away from her career plans and onto the developing friendship.
   G. think more about her own work interests than about the career her parents thought she should pursue.
   H. put off her plans of returning to Puerto Rico or a visit in favor of continuing to prepare for college.
   J. want to spend more time with him instead of helping her parents plan a vacation to Puerto Rico.
All of the answer choices describe possible shifts from the future to the present, but only one, F, fits the context of the passage. Although in the sixth paragraph (lines 67–79) the narrator discusses her parents’ dreams and her own plans to go to college and become a teacher (“the future”), the last paragraph shows the narrator shifting some of her attention to her friendship with Eugene (“the present”). She wants to go into Eugene’s house and sit at the kitchen table with him “like two adults” (lines 85–86). Choice G is wrong because she’s shifting attention away from her work interests and because we don’t know what career her parents thought she should pursue. Choice H, too, is incorrect: the narrator doesn’t say she’s had plans to return to Puerto Rico, and she’s thinking less, not more, about preparing for college. Although the narrator does want to spend more time with Eugene, she hasn’t been helping her parents plan a vacation to Puerto Rico—the sixth paragraph only says that her parents would like to retire there someday—so J is incorrect.

Sequence of Events. In some passages, the order, or sequence, in which events happen is important. Sequence-of-events questions ask you to determine when, for example, a character in a prose fiction passage did something or to figure out the order in which the researchers described in a natural sciences passage performed certain steps in a biology experiment.

Speaking of natural sciences, the following question, based on a passage about the small-comet theory (page 277), requires a fairly straightforward ordering of events:

13. According to the passage, the research that led to the development of the small-comet theory began with a project originally intended to study:
   - A. the electrical activity accompanying sunspots.
   - B. water entering Earth’s upper atmosphere.
   - C. static in satellite transmissions.
   - D. specks in satellite images.

The author indicates that Frank and Sigwarth were analyzing “photos of the electrical phenomena that accompany sunspots” when “they noted dark specks appearing in several images from NASA’s Dynamics Explorer 1 satellite” (lines 46–48). These specks started Frank and Sigwarth toward their small-comet theory, as the rest of the passage reveals. Thus, A is the best answer. The other answer choices are related to Frank and Sigwarth’s research, but none of them names the original study. Lines 55–58 show that B is incorrect: the two scientists decided that water was entering Earth’s upper atmosphere in the form of small comets only after they’d examined photos of the electrical phenomena accompanying sunspots. The author says that static in the satellite transmission was the first hypothesis Frank and Sigwarth came up with to explain the dark specks (lines 49–50), but the photos in which the specks appeared were originally taken to study sunspot-related activity, so C is incorrect. Choice D is likewise incorrect because the specks Frank and Sigwarth found were in photos originally taken as part of a study of sunspot-related activity.
The social studies passage on the development of perceptual abilities is challenging in part because you have to keep clear in your mind when certain abilities develop in infants. The following question, based on that passage, deals with that very point:

14. It is reasonable to infer from the passage that one-month-old babies will demonstrate which of the following skills?
   
   F. Noticing the difference between a pale yellow rattle and a bright yellow rattle
   G. Recognizing each of their older brothers and sisters as individuals
   H. Glancing from their father’s face to their mother’s face and back to their father again
   J. Following a wooden butterfly on a slow-moving mobile hanging above their bed

What makes this question harder is that the examples provided in the answer choices aren’t specifically found in the passage. You have to infer from the information given in the passage which of the four answer choices is most likely, given the age of the child. In this case, the best answer is J. Lines 39–40 state that “during the first month [infants] begin to track slowly moving objects.” It’s reasonable to infer from this that a one-month-old baby would be able to follow a wooden butterfly on a slow-moving mobile hanging above his or her head. Choices F, G, and H are perceptual abilities that develop later. The ability to “differentiate among hues and levels of brightness” (lines 42–43) doesn’t begin to develop until “the second month” (lines 40–41), meaning a one-month-old is unlikely to be able to note the difference between a pale yellow rattle and a bright yellow rattle (F). The ability to “glance from one object to another, and distinguish among family members” (lines 44–45) doesn’t emerge until three months, so a one-month-old couldn’t recognize each of his or her older siblings as individuals (G) or glance from father to mother and back again (H).

**Author’s Voice and Method.** Finally, some questions deal with the author’s voice and method. *Voice* relates to such things as the author’s style, attitude, and point of view, whereas *method* focuses on the craft of writing—the main purpose of a passage, what role parts of a passage (such as a paragraph) play in the whole work, and so on.

A couple of examples should help clear up what this category is about. The first, taken from the social studies passage on Eleanor Roosevelt, asks you to consider what hypothetical statement the author would most likely agree with:

15. According to the last paragraph, which of the following statements would the author most likely make with regard to ER’s vision and ideals?
   
   A. ER considered politics a game and played only when she knew she could win.
   B. ER worked with agitators and remained dedicated to the pursuit of justice and peace in victory and defeat.
   C. ER placed herself in the position of president, making decisions that determined White House policy.
   D. ER saw herself as the country’s role model and personally responsible for bringing about change.

All of the ideas in B—though not quite in those words—can be found in the last paragraph: ER “brought her network of agitators and activists into the White House” (lines 90–91), “worked with movements for justice and peace” (lines 87–88), and “never considered a political setback a
permanent defeat” (lines 91–92). Choice A is incorrect because although ER “enjoyed the game” (line 93), she saw defeat as only temporary, meaning she stuck with politics, win or lose. Choice C goes well beyond what the last paragraph (or the rest of the passage, for that matter) says about ER. She never placed herself in the position of the president, even if, as the author pointed out earlier, “ER made decisions and engineered policy” (line 25) in some areas. Choice D is incorrect for the same kind of reason: neither the last paragraph nor the passage as a whole states that ER made decisions and engineered policy” (line 25) in some areas. Choice E is incorrect because a contrast is made between the two sets of parents.

A second example, based on the prose fiction passage about a girl and her friend Eugene, deals with the contribution two paragraphs make to the story:

16. In terms of developing the narrative, the last two paragraphs (lines 67–87) primarily serve to:
   
   F. provide background details about the narrator and her family in order to highlight the narrator's unique and shifting perspective.
   
   G. describe the narrator's family in order to establish a contrast between her parents and Eugene's parents.
   
   H. portray the narrator's family in order to show how her friendship with Eugene affected the various members of her family.
   
   J. depict the hopes and dreams of the narrator's parents in order to show how her parents' aspirations changed over time.

To answer this question correctly, consider not only what the last two paragraphs of the passage say but also their role in advancing the story. Choice F is the best answer here. We learn in the sixth paragraph (lines 67–79) about how the parents’ dreams and the narrator’s plans (going to college and becoming a teacher) differ, suggesting she has a unique perspective. The last paragraph emphasizes how the narrator's perspective has shifted from focusing on “the future” to focusing on “the present.” Choice F is easier to see when you consider the place of the last two paragraphs in the whole passage; lines 67–87 help shift the focus from the narrator’s meetings with Eugene to her reflection on how her friendship with Eugene has changed her life. Choice G is incorrect because although the second paragraph (lines 27–42) describes Eugene's parents and the sixth paragraph describes the narrator's parents, no direct contrast is made between the two sets of parents. The passage also contains no indication that the narrator's friendship with Eugene affects her family at all (or that they even know about it), making H a poor option. Choice J is wrong because the only discussion of the narrator's parents’ aspirations is in the sixth paragraph, and nothing suggests that these aspirations changed over time.
Answer Key for Reading Test Sample Questions

5. D  11. D

Strategies for Taking the ACT Reading Test

Performance on the ACT reading test relies not only on reading speed and comprehension but also on test-taking strategies and skills. The following sections describe strategies and skills specifically for improving your ACT reading test score.

Pace Yourself

Before you read the first passage of the reading test, you may want to take a quick look through the entire reading test. If you choose to do this, flip through the pages and look at each of the passages and their questions. (Note that the passages begin on the pages to your left, and the questions follow.) You don't need to memorize anything—you can look at any of the reading test passages and questions during the time allotted for that test.

Some readers find that looking quickly at the questions first gives them a better idea of what to look for as they're reading the passage. If you're a slow reader, though, this may not be a good strategy. If you do decide to preview the questions, don't spend too much time on them—just scan for a few key words or ideas that you can watch for when you read the passage. To see what approach works best for you, you might want to try alternating between previewing the questions and not previewing the questions as you work through the practice tests in this book. Remember that when you take the ACT for real, a clock will be running. Plan your approach for the reading test before you take the actual ACT.

Use the Time Allotted

You have 35 minutes to read four passages and answer 40 questions. You'll want to pace yourself so you don't spend too much time on any one passage or question. If you take 2 to 3 minutes to read each passage, you'll have about 35 seconds to answer each question associated with the passage. Some of the questions will take less time, which will allow you more time for the more challenging ones.
Because time is limited, you should be very careful in deciding whether to skip more difficult questions. If you skip the difficult questions from the first passage until you work through the entire reading test, for example, you may find that you’ve forgotten so much of the first passage that you have to reread it before you can answer the questions that puzzled you the first time through. It will probably work better for you to think of the test as four 8-minute, 30-second units and to try to complete all the questions for a passage within its allotted time. Answer all the questions; you’re not penalized for guessing.

**Think of an Overall Strategy That Works for You**

Are you the kind of person who likes to get the big picture first, then carefully go over your work? Do you like to answer the questions you’re sure of right away and then go back and puzzle out the tougher ones? Or are you something of a perfectionist? (Do you find it hard to concentrate on a question until you know you got the one before it right?) There isn’t any right way or wrong way to approach the reading test—just make sure the way you choose is the way that works best for you.

**Keep the Passage as a Whole in Mind**

Your initial look at the whole reading test should give you some ideas about how to approach each passage. Notice the subject heading and short paragraph before each passage. These “advance organizers” tell you the subject matter of the passage, where the passage comes from, who wrote it, and sometimes a little information about the passage. Occasionally, an advance organizer will define a difficult word, explain a concept, or provide background information. Reading the advance organizers carefully should help you be more prepared as you approach each passage.

Always remember that the reading test asks you to refer and reason on the basis of the passage. You may know a lot about the subject of some of the passages you read, but try not to let what you already know influence the way you answer the questions, because the author’s perspective may differ from yours. There’s a reason why many questions begin with “According to the passage” or “It can reasonably be inferred from the passage.” If you read and understand the passage well, your reasoning ability will help you to figure out the correct answer. During the reading test, you can refer back to the passages as often as you like.

**Find a Strategy for Approaching Each Question**

First, read each question carefully so you know what it asks. Look for the best answer, but read and consider all the options, even though you may feel you’ve identified the best one. Ask yourself whether you can justify your choice as the best answer.

Some people find it useful to answer the easy questions first and skip the difficult ones (being careful, of course, to mark the answer document correctly and to mark in the test booklet the questions they skipped). Then they go back and consider the difficult questions. When you’re
working on a test question and aren't certain about the answer, try to eliminate choices you're sure are incorrect. If you can rule out a couple of choices, you'll improve your chances of selecting the correct answer. Keep referring back to the passage for information.

**Reading Strategies Summary**

The sample passages used as examples in this section can be found on the following pages. They come from ACTs that thousands of students have already taken. Remember, the passages in this section don't represent every type you're likely to see, but they should give you a good idea of the kinds of questions you'll encounter when you take the ACT reading test. For a more complete picture of what the ACT reading test will look like, five complete reading tests are included in the five practice ACTs in chapters 3 and 10. And remember that the best way to do well on the ACT reading test is to have a solid understanding of each passage—so read quickly but carefully.
Sample Passage I

PROSE FICTION: This passage is adapted from the short story “American History” by Judith Ortiz-Cofer (c)1992 by Judith Ortiz-Cofer. The story appeared in the anthology Iguana Dreams: New Latino Fiction.

There was only one source of beauty and light for me my ninth grade year. The only thing I had anticipated at the start of the semester. That was seeing Eugene. In August, Eugene and his family had moved into the only house on the block that had a yard and trees. I could see his place from my bedroom window in El Building. In fact, if I sat on the fire escape I was literally suspended above Eugene’s backyard. It was my favorite spot to read my library books in the summer.

Until that August the house had been occupied by an old couple. Over the years I had become part of their family, without their knowing it, of course. I had a view of their kitchen and their backyard, and though I could not hear what they said, I knew when they were arguing, when one of them was sick, and many other things. I knew all this by watching them at mealtimes. I could see their kitchen table, the sink, and the stove. During good times, he sat at the table and read his newspapers while she fixed the meals. If they argued, he would leave and the old woman would sit and stare at nothing for a long time. When one of them was sick, the other would come and get things from the kitchen and carry them out on a tray. The old man had died in June. The house had stood empty for weeks. I had had to resist the temptation to climb down into the yard and water the flowers the old lady had taken such good care of.

By the time Eugene’s family moved in, the yard was a tangled mass of weeds. The father had spent several days mowing, and when he finished, from where I sat, I didn’t see the red, yellow, and purple clusters that meant flowers to me. I didn’t see this family sit down at the kitchen table together. It was just the mother, a red-headed tall woman who wore a white uniform; the father was gone before I got up in the morning and was never there at dinner time. I only saw him on weekends when they sometimes sat on lawn-chairs under the oak tree, each hidden behind a section of the newspaper; and there was Eugene. He was tall and blond, and he wore glasses. I liked him right away because he sat at the kitchen table and read books for hours. That summer, before we had even spoken one word to each other, I kept him company on my fire escape.

Once school started I looked for him in all my classes, but P. S. 13 was a huge place and it took me days and many discreet questions to discover Eugene. After much maneuvering I managed “to run into him” in the hallway where his locker was—on the other side of the building from mine—and in study hall at the library where he first seemed to notice me, but did not speak; and finally, on the way home after school one day when I decided to approach him directly, though my stomach was doing somersaults.

I was ready for rejection, snobbery, the worst. But when I came up to him and blurted out: “You’re

55 Eugene. Right?” he smiled, pushed his glasses up on his nose, and nodded. I saw then that he was blushing deeply. Eugene liked me, but he was shy. I did most of the talking that day. He nodded and smiled a lot. In the weeks that followed, we walked home together. He would linger at the corner of El Building for a few minutes then walk down to his house.

I did not tell Eugene that I could see inside his kitchen from my bedroom. I felt dishonest, but I liked my secret sharing of his evenings, especially now that I knew what he was reading since we chose our books together at the school library.

I also knew my mother was unhappy in Paterson, New Jersey, but my father had a good job at the blue-jeans factory in Passaic and soon, he kept assuring us, we would be moving to our own house there. I had learned to listen to my parents’ dreams, which were spoken in Spanish, as fairy tales, like the stories about life in Puerto Rico before I was born. I had been to the island once as a little girl. We had not been back there since then, though my parents talked constantly about buying a house on the beach someday, retiring on the island—that was a common topic among the residents of El Building. As for me, I was going to go to college and become a teacher.

80 But after meeting Eugene I began to think of the present more than of the future. What I wanted now was to enter that house I had watched for so many years. I wanted to see the other rooms where the old people had lived, and where the boy spent his time. Most of all, I wanted to sit at the kitchen table with Eugene like two adults, like the old man and his wife had done, maybe drink some coffee and talk about books.
Sample Passage II

PROSE FICTION: This passage is adapted from The Antelope Wife by Louise Erdrich (©1996 by Louise Erdrich).

My mother sewed my birth cord, with dry sage and sweet grass, into a turtle holder of soft white buckskin. She bade that little turtle using precious old cobalts and yellows and Cheyenne pinks and greens in a careful design. I remember every detail of it, me, because the turtle hung near my crib, then off my belt, and was my very first play toy. I was supposed to have it on me all my life, bury it with me on reservation land, but one day I came in from playing and my indi was gone.

I thought nothing of it, at first and for many years, but slowly over time the absence . . . it will tell. I began to wander from home, first in my thoughts, then my feet took after, so at last at the age of eighteen, I walked the road that led from the front of our place to the wider spaces and then the country beyond that, where that one road widened into two lanes, then four, then six, past the farms and service islands, into the dead wall of the suburbs and still past that, finally, into the city’s bloody heart.

My name is Cally Roy, Ozhawashkwamashkodayway is what the spirits call me. All my life so far I’ve wondered about the meaning of my spirit name but nobody’s told it, seen it, got ahold of my history flying past. Mama has asked, she has offered tobacco, even blankets, but my grandmas Mrs. Zosie Roy and Mary Shawano only nod at her, holding their tongues as they let their eyes wander. In a panic, once I knew I was setting out, not staying home, Mama tried to call up my grandmas and ask if I could live at their apartment in the city. But once they get down to the city, it turns out they never stop moving. They are out, and out again. Impossible to track down. It’s true, they are extremely busy women.

So my mom sends me to Frank.

Frank Shawano. Famous Indian bakery chef. My Mama’s eternal darling, the man she loves too much to live with.

I’m weary and dirty and sore when I get to Frank’s bakery shop, but right away, walking in and the bell dinging with a cheerful alertness, I smell those good bakery smells of yeasty bread and airy sugar. Behind the counter, lemony light falls on Frank. He is big, strong, pale brown like a loaf of light rye left to rise underneath a towel. His voice is muffled and weak, like it is squeezed out of the clogged end of a pastry tube. He greets me with gentle pleasure.

“Just as I’m closing.” His smile is very quiet. He cleans his hands on a towel and beckons me into the back of the bakery shop, between swinging steel doors.

I remember him as a funny man, teasing and playing games and rolling his eyes at us, making his pink sugar-cookie dogs bark and elephants trumpet. But now he is serious, and frowns slightly as I follow him up the back stairs and into the big top-floor apartment with the creaky floors, the groaning pipes, odd windows that view the yard. My little back room, no bigger than a closet, overlooks this space.

I’m so beat, though, I just want to crawl into my corner and sleep.

“Not too small, this place?” He sounds anxious.

I shake my head. The room seems okay, the mattress on the floor, the blankets, and the shelves for my things.

“Call your mom?” Frank gives orders in the form of a question. He acts all purposeful, as though he is going back downstairs to close up the store, but as I dial the number on the kitchen wall phone he lingers. He can’t drag himself away from the magnetic field of my mother’s voice, muffled, far off, but on the other end of the receiver. He stands in the doorway with that same towel he brought from downstairs, folding and refolding it in his hands.

“Mama,” I say, and her voice on the phone suddenly hurts. I want to curl next to her and be a small girl again. My body feels too big, electric, like a Frankenstein body enclosing a tiny child’s soul.

We laugh at some corny joke and Frank darts a glance at me, then stares at his feet and frowns. Reading between my Mama’s pauses on the phone, I know she is hoping I’ll miss the real land, and her, come back and resume my brilliant future at the tribal college. In spite of how I want to curl up in my city corner, I picture everything back home. On the wall of my room up north, there hang a bundle of sage and Grandma Roy’s singing drum. On the opposite wall, I taped up posters and photos. Ever since I was little, I slept with a worn bear and a new brown dog. And my real dog, too, curled at my feet sometimes, if Mama didn’t catch us. I never liked dolls. I made good scores in math. I get to missing my room and my dog and I lose track of Mama’s voice.

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Sample Passage III

SOCIAL STUDIES: This passage is adapted from volume 2 of Blanche Wiesen Cook’s biography Eleanor Roosevelt ©1999 by Blanche Wiesen Cook.

Eleanor Roosevelt [ER] is the most controversial First Lady in United States history. Her journey to greatness, her voyage out beyond the confines of good wife and devoted mother, involved determination and amazing courage. It also involved one of history’s most unique partnerships. Franklin Delano Roosevelt [FDR] admired his wife, appreciated her strengths, and depended on her integrity.

However, ER and FDR had different priorities, occasionally competing goals; and often disagreed. In the White House they ran two distinct and separate courts.

By 1933 [her first year as First Lady], ER was an accomplished woman who had achieved several of her life’s goals. With her partners, ER was a businesswoman who co-owned the Val-Kill crafts factory, a political leader who edited and copublished the Women’s Democratic News, and an educator who co-owned and taught at a New York school for girls.

As First Lady, Eleanor Roosevelt did things that had never been done before. She upset race traditions, championed a New Deal for women, and on certain issues actually ran a parallel administration. On housing and the creation of model communities, for example, ER made decisions and engineered policy.

At the center of a network of influential women who ran the Women’s Committee of the Democratic Party led by Molly Dewson, ER worked closely with the women who had dominated the nation’s social reform struggles for decades. With FDR’s election, the goals of the great progressive pioneers, Jane Addams, Florence Kelley, and Lillian Wald, were at last at the forefront of the country’s agenda. ER’s mentors since 1903, they had battled on the margins of national politics since the 1880s for public health, universal education, community centers, sanitation programs, and government responsibility for the welfare of the nation’s poor and neglected people.

Now their views were brought directly into the White House. ER lobbied for them personally with her new administrative allies, in countless auditoriums, as a radio broadcaster, and in monthly, weekly, and, by 1936, daily columns. Called “Eleanor Everywhere,” she was interested in everyone.

Every life was sacred and worthy, to be improved by education, employment, health care, and affordable housing. Her goal was simple, a life of dignity and decency for all. She was uninterested in complex theories, and demanded action for betterment. She feared violent revolution, but was not afraid of socialism—and she courted radicals.

As fascism and communism triumphed in Europe and Asia, ER and FDR were certain that there was a middle way, what ER called an American “revolution without bloodshed.” Her abiding conviction, however, was that nothing good would happen to promote the people’s interest unless the people themselves organized to demand government responses. A people’s movement required active citizen participation, and ER’s self-appointed task was to agitate and inspire community action, encourage united democratic movements for change.

Between 1933 and 1938, while the Depression raged and the New Deal unfolded, ER worked with the popular front. She called for alliances of activists to fight poverty and racism at home, and to oppose isolationism internationally.

Active with the women’s peace movement, ER spoke regularly at meetings of the Women’s International League for Peace and Freedom, and the Conference on the Cause and Cure of War. She departed, however, from pacifist and isolationist positions and encouraged military preparedness, collective security, and ever-widening alliances.

Between 1933 and 1938 ER published countless articles and six books. She wrote in part for herself, to clear her mind and focus her thoughts. But she also wrote to disagree with her husband. From that time to this, no other First Lady has actually rushed for her pen to jab her husband’s public decisions. But ER did so routinely, including in her 1938 essay This Troubled World, which was a point-by-point rejection of FDR’s major international decisions.

To contemplate ER’s life of example and responsibility is to forestall gloom. She understood, above all, that politics is not an isolated individualist adventure. She sought alliances, created community, worked with movements for justice and peace. Against great odds, and under terrific pressure, she refused to withdraw from controversy. She brought her network of agitators and activists into the White House, and never considered a political setback a permanent defeat. She enjoyed the game, and weathered the abuse.
Sample Passage IV

SOCIAL STUDIES: This passage is adapted from Morton Hunt’s The Story of Psychology (©1993 by Morton Hunt). In the passage, the term maturation refers to the process of growth and development, and the term perceptual ability refers to the capacity to recognize something through the senses (sight, smell, touch, etc.).

Much maturation research is concerned with physical skills and physical attributes, and adds little to our knowledge of the growth of the mind. But research on the development of perceptual abilities begins to provide solid factual answers to the ancient central question of psychology: How much is due to nature and how much to nurture (or, in developmental terms, to maturation and to learning)?

The work has been focused on early infancy, when perceptual abilities evolve rapidly; its aim is to discover when each new ability first appears, the assumption being that at its first appearance, the new ability arises not from learning but from maturation of the optic nervous structures and especially of that part of the brain cortex where visual signals are received and interpreted.

Much has been learned by simply watching infants. What, exactly, do very young infants see? Since we cannot ask them what they see, how can we find out?

In 1961, the psychologist Robert Fantz devised an ingenious method of doing so. He designed a stand in which, on the bottom level, the baby lies on her back, looking up. A few feet above it is a display area where the experimenter puts two large cards, each containing a design—a white circle, a yellow circle, a bull’s-eye, a simple sketch of a face. The researcher, peering down through a tiny peephole, can watch the movement of the baby’s eyes and time how long they are directed at one or the other of each pair of patterns. Fantz found that at two months babies looked twice as long at a bull’s-eye as at a circle of solid color, and twice as long at a sketch of a face as at a bull’s-eye. Evidently, even a two-month-old can distinguish major differences and direct her gaze toward what she finds more interesting.

Using this technique, developmental psychologists have learned a great deal about what infants see and when they begin to see it. In the first week infants distinguish light and dark patterns; during the first month they begin to track slowly moving objects; by the second month they begin to have depth perception, coordinate the movement of the eyes, and differentiate among hues and levels of brightness; by three months they can glance from one object to another, and can distinguish among family members; by four months they focus at varying distances, make increasingly fine distinctions, and begin to recognize the meaning of what they see (they look longer at a normal sketch of a face than at one in which the features have been scrambled); and from four to seven months they achieve stereopsis, recognize that a shape held at different angles is still the same shape, and gain near-adult ability to focus at varying distances.

Exactly how maturation and experience interact in the brain tissues to produce such developmental changes is becoming clear from neuroscience research. Microscopic examination of the brains of infants shows that as the brain triples in size during the first two years of life, a profusion of dendrites (branches) grow from its neurons and make contact with one another.

By the time a human is twelve, the brain has an estimated hundred trillion synapses (connections between nerve cells). Those connections are the wiring plan that establishes the brain’s capabilities. Some of the synaptic connections are made automatically by chemical guidance, but others are made by the stimulus of experience during the period of rapid dendrite growth. Lacking such stimulus, the dendrites wither away without forming the needed synapses. Mice reared in the dark develop fewer dendritic spines and synaptic connections in the visual cortex than mice reared in the light, and even when exposed to light never attain normal vision.

Why should nature have done that? Why should perceptual development be possible only at a critical period and not later? It does not make evolutionary sense for the organism to be permanently impaired in sensory performance just because it fails to have the proper experiences at specific times in its development. But some brain researchers say that there is an offsetting advantage: the essential experiences are almost always available at the right time, and they fine-tune the brain structure so as to provide far more specific perceptual powers than could result from genetic control of synapse formation.

With that, the vague old terms nature and nurture take on precise new meaning. Now, after so many centuries of speculation, we catch the first glimpse of how mind is constructed out of matter by experience.
Sample Passage V

**HUMANITIES:** This passage is adapted from the essay “Faith and Work” by Scott Russell Sanders (©1995 by Scott Russell Sanders).

The difference between a machine and a tool—between a bread-maker and a bread pan—is that a tool extends human skills, a machine replaces them. When the freedom and craft have been squeezed out of work it becomes toil, without mystery or meaning, and that is why many people hate their jobs. You can measure the drudgery of a job by the number of layers of supervision required to keep the wheels spinning or the cash registers ringing. Toil drains us; but good work may renew us, by giving expression to our powers.

A generation or two ago it would have seemed less strange to relish hard work. My grandparents might smile at the laziness of Tom Sawyer, who fooled others into doing his chores, but they would remind you that Tom was a child. Grown-ups do their chores, unless they are idlers, good-for-nothings, ne’er-do-wells. Grown-ups look after their own needs, provide for their families, help their neighbors, do something useful. So my grandparents taught by word and example. Any job worth doing is worth doing right, they used to say. To try sliding by with the least effort, my grandparents believed, was to be guilty of a sin called sloth.

I knew this cluster of values by experience long before I heard it referred to as the work ethic, a phrase that has lost its edge from tumbling over the lips of too many cynical bosses and politicians. Whatever happened to the work ethic? laments the manager who wishes to squeeze more profit from his employees. Whatever happened to the work ethic? groans the official who wants to shrink the welfare rolls. As I understand it, a regard for the necessity and virtue of work has nothing to do with productivity or taxes, and everything to do with fulfilling one’s humanity. As I have seen it embodied in the lives not only of grandparents but of parents and neighbors and friends, this ethic arises from a belief that the creation is a sacred gift, and that by working we express our gratitude and celebrate our powers. To honor that gift, we should live simply, honestly, conservingly, saving money and patching clothes and fixing what breaks, sharing what we have.

Those values are under assault every minute of the day in a consumer economy—from advertising, from the glittering goodies in stores, from the luxurious imagery of television, magazines, and films, and from a philosophy that views the universe not as a gift to be honored but as a warehouse to be ransacked. If money is meaning, if winning the lottery or beating the stock market defines success, if the goal of life is easy sensation, then why lift a finger so long as you can force someone or something else to do it for you?

I can think of many reasons to lift a finger, among them the delight in exercising skill, in sharing labor with companions, in planning a task and carrying it through, in bringing some benefit to the world. But the chief reason for relishing work is that it allows us to practice our faith, whatever that faith may be. The Buddha advised his followers to seek right livelihood, to provide for their needs in a modest and responsible manner, with respect for other creatures, in harmony with the way of things. We show our understanding of the way of things by the quality of our work, whether or not we have heard the Buddha’s teachings. The old theological debate as to whether salvation is to be gained by works or by faith begins from a false dichotomy. Faith concerns our sense of what is real, what is valuable, what is holy; work is how we act out that faith.

The Shakers condensed their faith into the maxim, “Hands to work, hearts to God.” Anyone who has looked at their furniture or buildings can sense the clarity of their vision. “One feels that for the Shaker craftsmen,” Thomas Merton observed, “love of God and love of truth in one’s own work came to the same thing, and that work itself was a prayer, a communion with the inmost spiritual reality of things and so with God.” Mother Ann Lee, who launched the Shaker movement, counseled her followers to “Do all your work as if you had a thousand years to live, and as you would if you knew you must die tomorrow.”

If the purpose of life is not to acquire but to inquire, to seek understanding, to discover all we can about ourselves and the universe, to commune with the source of things, then we should care less about what we earn—money, prestige, salvation—and more about what we learn. In light of all we have to learn, the difference between dying tomorrow and a hundred years from tomorrow is not very great.
Sample Passage VI


Lightning affects electrical equilibrium on the earth. Air is a poor conductor, but some electricity constantly leaks to the atmosphere, creating an electrical potential. Electricity moves back according to the gradient [change in potential with distance]. During a thunderstorm, the gradient becomes very steep, and the electrical potential discharges as lightning. The discharge may move between any oppositely charged regions—from cloud to earth, from earth to cloud, or from cloud to cloud. It was calculated as early as 1887 that the earth would lose almost all its charge in less than an hour unless the supply were replenished; that is, on a global scale, lightning will discharge to the earth every hour a quantity of electricity equal to the earth’s entire charge. Thunderstorms are thus an electromagnetic as well as a thermodynamic necessity. It has been reckoned that the earth experiences some 1,800 storms per hour, or 44,000 per day. Collectively, these storms produce 100 cloud-to-ground discharges per second, or better than 8 million per day globally. And these estimates are probably low. The total energy in lightning bolts varies greatly, but about 250 kilowatt hours of electricity are packed into each stroke. Almost 75 percent of this total energy is lost to heat during discharge.

Two types of discharge patterns are commonly identified: the cold stroke, whose main return [ground-to-cloud] stroke is of intense current but of short duration, and the hot stroke, involving lesser currents of longer duration. Cold lightning, with its high voltage, generally has mechanical or explosive effects; hot lightning is more apt to start fires. Studies in the Northern Rockies suggest that about one stroke in 25 has the electrical characteristics needed to start a fire. Whether it does or not depends strongly on the object it strikes, the fuel properties of the object, and the local weather. Ignition requires both heat and kindling. Lightning supplies the one with its current and occasionally finds the other among the fine fuels of rotten wood, needles, grass, or dustlike debris blown from a tree by the explosive shock of the bolt itself.

The consequences of lightning are complex. Any natural force of this magnitude will influence the biological no less than the geophysical environment, and the secondary effects of lightning are significant to life. Lightning helps to fix atmospheric nitrogen into a form that rain can bring to earth. In areas of heavy thunderstorm activity, lightning can function as a major predator on trees, either through direct injury or by physiological damage. In the ponderosa pine forests of Arizona, for example, one forester has estimated that lightning mortality runs between 0.7 and 1.0 percent per year. Other researchers have placed mortality as high as 25–33 percent. For southern pines, the figure may be even steeper. A study in Arkansas calculated that 70 percent of mortality, by volume, was due to lightning. These figures describe only direct injury, primarily the mechanical destruction of branches and bole; the other major causes of mortality— insects, wind, and mistletoe—are likely secondary effects brought about in trees weakened by lightning. All of these effects, in turn, may be camouflaged by fire induced by lightning.

The process of “electrocution” is increasingly recognized. Lightning scorch areas of between 0.25 and 25 acres have been identified. Nor is the process limited to trees: it has been documented for grasses, tomatoes, potatoes, cabbages, tea, and other crops. Long attributed to inscrutable “die-offs” or to infestation by insects or diseases (often a secondary effect), such sites are now recognized worldwide as a product of physiologic trauma caused by lightning.

The most spectacular product of lightning is fire. Except in tropical rain forests and on ice-mantled land masses, lightning fire has occurred in every terrestrial environment on the globe, contributing to a natural mosaic of vegetation types. Even in tropical landscapes lightning bombardment by itself may frequently be severe enough to produce a mosaic pattern similar to that resulting from lightning fire. Lightning fires have ignited desert grasslands, tundra, chaparral, swamplands, marshes, grasslands, and, of course, forests. Though the intensity and frequency of these fires vary by region, their existence is undeniable.
Sample Passage VII

NATURAL SCIENCE: This passage is adapted from “Publish and Punish: Science’s Snowball Effect” by Jon Van (©1997 by The Chicago Tribune Company).

It’s a scientific finding so fundamental that it certainly will make the history books and maybe snag a Nobel Prize if it pans out, but the notion that cosmic snowballs are constantly pelting Earth is something Louis Frank just as soon would have ducked.

Frank is the University of Iowa physicist whose research led him to declare more than a decade ago that Earth is being bombarded by hundreds of house-sized comets day after day that rain water on our planet and are the reason we have oceans. That weather report caused the widely respected scientist to acquire a certain reputation among his colleagues as a bit unstable, an otherwise estimable fellow whose hard work may have pushed him over the edge.

Frank and his associate, John Sigwarth, probably went a way toward salvaging their reputations when they presented new evidence that leaves little doubt Earth is indeed being bombarded by something in a manner consistent with Frank’s small-comet theory. Rather than gloating or anticipating glory, Frank seemed relieved that part of a long ordeal was ending. “I knew we’d be in for it when we first put forth the small-comet theory,” Frank conceded, “but I was naive about just how bad it would be. We were outvoted by about 10,000 to 1 by our colleagues. I thought it would have been more like 1,000 to 1.”

To the non-scientist this may seem a bit strange. After all, the point of science is to discover information and insights about how nature works. Shouldn’t every scientist be eager to overturn existing ideas and replace them with his or her own? In theory, that is the case, but in practice, scientists are almost as loath to embrace radically new ideas as the rest of us.

“Being a scientist puts you into a constant schizophrenic existence,” contends Richard Zare, chairman of the National Science Board. “You have to believe and yet question beliefs at the same time. If you are a complete cynic and believe nothing, you do nothing and get nowhere, but if you believe too much, you fool yourself.”

It was in the early 1980s when the small-comet theory started to haunt Frank and Sigwarth, who was Frank’s graduate student studying charged particles called plasmas, which erupt from the sun and cause the aurora borealis (northern lights). As they analyzed photos of the electrical phenomena that accompany sunspots, they noted dark specks appearing in several images from NASA’s Dynamics Explorer 1 satellite. They assumed these were caused by static in the transmission.

After a while their curiosity about the dark spots grew into a preoccupation, then bordered on obsession. Try as they did, the scientists couldn’t find any plausible explanation of the pattern of dark spots that appeared on their images. The notion that the equipment was picking up small amounts of water entering Earth’s upper atmosphere kept presenting itself as the most likely answer.

Based on their images, the Iowa scientists estimated 20 comets an hour—each about 30 feet or so across and carrying 100 tons of water—were bombarding the Earth. At that rate, they would produce water vapor that would add about an inch of water to the planet every 10,000 years, Frank concluded. That may not seem like much, but when talking about a planet billions of years old, it adds up.

Such intimate interaction between Earth and space suggests a fundamentally different picture of human evolution—which depends on water—than is commonly presented by scientists. Frank had great difficulty getting his ideas into a physics journal 11 years ago and was almost booted from the room when he presented his theory at scientific meetings. Despite the derision, colleagues continued to respect Frank’s mainstream work on electrically charged particles in space and the imaging cameras he designed that were taken aboard recent NASA spacecraft to explore Earth’s polar regions.

Unbeknown to most, in addition to gathering information on the northern lights, Frank and Sigwarth designed the equipment to be able to snatch better views of any small comets the spacecraft might happen upon. It was those images from the latest flights that caused even harsh critics of the small-comet theory to concede that some water-bearing objects appear to be entering Earth’s atmosphere with regularity.

To be sure, it has not been proved that they are comets, let alone that they have anything to do with the oceans. But Frank’s evidence opens the matter up to study. Had he been a researcher of lesser standing, his theory probably would have died long ago.
Chapter 8: Improving Your Science Score

The ACT science test asks you to answer 40 multiple-choice questions in 35 minutes. The questions measure the interpretation, analysis, evaluation, and problem-solving skills associated with science. The science test is made up of several passages, each of which is followed by multiple-choice questions.

Content of the ACT Science Test

The content areas of the ACT science test parallel the content of courses commonly taught in grades 7 through 12 and in entry-level college courses. Passages on the test represent the following content areas (examples of subjects included in each content area are given in parentheses):

- **Biology** (botany, cell biology, ecology, evolution, genetics, microbiology, zoology)
- **Chemistry** (acids and bases, biochemistry, kinetics and equilibria, nuclear chemistry, organic chemistry, properties of matter, thermo-chemistry)
• **Earth/Space Sciences** (astronomy, environmental science, geology, meteorology, oceanography)

• **Physics** (electromagnetism, fluids, mechanics, optics, thermodynamics, solids)

You do not need advanced knowledge in these subjects, but you will need some knowledge specific to these subjects—scientific terms or concepts—to answer some of the questions. The test assumes that students are in the process of taking the core science course of study (three years or more) that will prepare them for college-level work and have completed two years of introductory high school science course work.

The passages of the science test are concise and clear; you should have no trouble reading them. The test emphasizes application of scientific reasoning skills rather than recall of scientific content, reading ability, or math skills, but you may need to make minimal arithmetic computations in order to answer some questions. The use of calculators is not permitted on the science test but should also not be needed.

**Format of the ACT Science Test**

The scientific information presented in each passage of the ACT science test is conveyed in one of three different formats:

- The **Data Representation** format requires you to understand, evaluate, and interpret information presented in graphic or tabular form.

- The **Research Summaries** format requires you to understand, evaluate, analyze, and interpret the design, execution, and results of one or more experiments.

- The **Conflicting Viewpoints** format requires you to evaluate several alternative theories, hypotheses, or viewpoints on a specific observable phenomenon.

Turn to chapter 1 to find out the approximate proportion of the ACT science test devoted to each of these three different passage formats.

You’ll find examples of the kinds of passages that you’re likely to find in each of the formats in the pages that follow.

The sample ACT science test passages and questions in this section are representative of those you’ll encounter in the actual ACT. The following chart illustrates the content area, format, and topic covered by each sample passage given in the remainder of this section:

<table>
<thead>
<tr>
<th>Passage</th>
<th>Content area</th>
<th>Format</th>
<th>Topic of passage</th>
</tr>
</thead>
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<td>I</td>
<td>Chemistry</td>
<td>Data Representation</td>
<td>Calorimetry</td>
</tr>
<tr>
<td>II</td>
<td>Physics</td>
<td>Research Summaries</td>
<td>Illuminance</td>
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<tr>
<td>III</td>
<td>Biology</td>
<td>Conflicting Viewpoints</td>
<td>Conjugation</td>
</tr>
</tbody>
</table>
Data Representation Format

This type of format presents scientific information in charts, tables, graphs, and diagrams similar to those found in science journals and texts. Examples of tables used in an actual Data Representation passage administered to students are found in Sample Passage I that follows.

The questions you'll find in the Data Representation format ask you to interpret charts and tables, read graphs, evaluate scatterplots, and analyze information presented in diagrams. There are five sample questions presented with the sample Data Representation passage.
Sample Passage I

A bomb calorimeter is used to determine the amount of heat released when a substance is burned in oxygen (Figure 1). The heat, measured in kilojoules (kJ), is calculated from the change in temperature of the water in the bomb calorimeter. Table 1 shows the amounts of heat released when different foods were burned in a bomb calorimeter. Table 2 shows the amounts of heat released when different amounts of sucrose (table sugar) were burned. Table 3 shows the amounts of heat released when various chemical compounds were burned.

![Figure 1]

Table 1

<table>
<thead>
<tr>
<th>Food</th>
<th>Mass (g)</th>
<th>Change in water temperature (°C)</th>
<th>Heat released (kJ)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bread</td>
<td>1.0</td>
<td>8.3</td>
<td>10.0</td>
</tr>
<tr>
<td>Cheese</td>
<td>1.0</td>
<td>14.1</td>
<td>17.0</td>
</tr>
<tr>
<td>Egg</td>
<td>1.0</td>
<td>5.6</td>
<td>6.7</td>
</tr>
<tr>
<td>Potato</td>
<td>1.0</td>
<td>2.7</td>
<td>3.2</td>
</tr>
</tbody>
</table>

Table 1 adapted from American Chemical Society, ChemCom: Chemistry in the Community. ©1993 by American Chemical Society.

Table 2

<table>
<thead>
<tr>
<th>Amount of sucrose (g)</th>
<th>Heat released (kJ)</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.1</td>
<td>1.6</td>
</tr>
<tr>
<td>0.5</td>
<td>8.0</td>
</tr>
<tr>
<td>1.0</td>
<td>16.0</td>
</tr>
<tr>
<td>2.0</td>
<td>32.1</td>
</tr>
<tr>
<td>4.0</td>
<td>64.0</td>
</tr>
</tbody>
</table>

Table 3

<table>
<thead>
<tr>
<th>Chemical compound</th>
<th>Molecular formula</th>
<th>Mass (g)</th>
<th>Heat released (kJ)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Methanol</td>
<td>CH₃OH</td>
<td>0.5</td>
<td>11.4</td>
</tr>
<tr>
<td>Ethanol</td>
<td>C₂H₅OH</td>
<td>0.5</td>
<td>14.9</td>
</tr>
<tr>
<td>Benzene</td>
<td>C₆H₆</td>
<td>0.5</td>
<td>21.0</td>
</tr>
<tr>
<td>Octane</td>
<td>C₈H₁₈</td>
<td>0.5</td>
<td>23.9</td>
</tr>
</tbody>
</table>

I. According to Tables 1 and 2, as the mass of successive sucrose samples increased, the change in the water temperature produced when the sample was burned most likely:

A. increased only,
B. decreased only,
C. increased, then decreased,
D. remained the same.
2. Which of the following graphs best illustrates the relationship between the heat released by the foods listed in Table 1 and the change in water temperature?

F. 

![Graph F]

G. 

![Graph G]

H. 

![Graph H]

J. 

![Graph J]

3. Based on the data in Table 2, one can conclude that when the mass of sucrose is decreased by one-half, the amount of heat released when it is burned in a bomb calorimeter will:
   A. increase by one-half.
   B. decrease by one-half.
   C. increase by one-fourth.
   D. decrease by one-fourth.

4. Which of the following lists the foods from Tables 1 and 2 in increasing order of the amount of heat released per gram of food?
   F. Potato, egg, bread, sucrose, cheese
   G. Sucrose, cheese, bread, egg, potato
   H. Bread, cheese, egg, potato, sucrose
   J. Sucrose, potato, egg, bread, cheese

5. Based on the information in Tables 1 and 2, the heat released from the burning of 5.0 g of potato in a bomb calorimeter would most likely be closest to which of the following?
   A. 5 kJ
   B. 10 kJ
   C. 15 kJ
   D. 20 kJ

Discussion of Sample Passage I (Data Representation)

According to this Data Representation passage, the amount of heat generated when a material is burned in oxygen can be determined using a bomb calorimeter. The bomb calorimeter has an outer shell made of an insulating material. Inside this shell is a bomb (steel casing) immersed in a fixed amount of water. When a material is burned inside the bomb, the water absorbs heat generated by the combustion, causing the temperature of the water to increase. The amount of the increase in water temperature depends on the amount of heat absorbed by the water. So, if we measure the increase in water temperature, we can calculate the amount of heat released when a material is burned inside the bomb.

Note that the passage contains three tables. Table 1 lists the temperature change of the water and the amount of heat generated when 1 g of each of four foods is burned in the calorimeter. Table 2 lists the amounts of heat released when various quantities of the sugar sucrose are burned. Table 3 lists several chemical compounds and their chemical formulas, as well as the amount of heat released for each compound when 0.5 g of the compound is burned in the calorimeter.
1. According to Tables 1 and 2, as the mass of successive sucrose samples increased, the change in the water temperature produced when the sample was burned most likely:
   A. increased only.
   B. decreased only.
   C. increased, then decreased.
   D. remained the same.

Question 1 asks you to determine how the change in water temperature varied as the amount of sucrose burned increased, based on the data in Tables 1 and 2. Notice that the change in water temperature and the amount of heat released are listed in Table 1 for each material burned. In Table 2, the amount of sucrose burned and the amount of heat released are listed, but the change in water temperature is not listed. Let us assume that the relationship between the amount of heat released and the change in water temperature for sucrose is the same as the relationship between the amount of heat released and the change in water temperature for the materials listed in Table 1. According to Table 2, as the amount of sucrose burned increased, the amount of heat released steadily increased. According to Table 1, as the amount of heat released increased, the magnitude of the change in water temperature steadily increased. Therefore, as the amount of sucrose burned increased, the magnitude of the change in the water temperature steadily increased. The best answer is A.

2. Which of the following graphs best illustrates the relationship between the heat released by the foods listed in Table 1 and the change in water temperature?

<p>| | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>F.</td>
<td>H.</td>
</tr>
<tr>
<td>G.</td>
<td>J.</td>
</tr>
</tbody>
</table>

Question 2 asks you to choose a graph that best illustrates the relationship between the amount of heat released and the change in water temperature for the four substances listed in Table 1. According to the data in Table 1, as the change in water temperature increased, the amount of
heat released steadily increased. No data in Table 1 supports the conclusion that as the change in water temperature increased the amount of heat released decreased or remained constant. Therefore, G is the best answer.

3. Based on the data in Table 2, one can conclude that when the mass of sucrose is decreased by one-half, the amount of heat released when it is burned in a bomb calorimeter will:
   A. increase by one-half.
   B. decrease by one-half.
   C. increase by one-fourth.
   D. decrease by one-fourth.

Question 3 asks you to predict, based on the data in Table 2, the fractional change in the amount of heat released by sucrose when the amount of sucrose burned is decreased by half. An examination of the data in Table 2 shows that when the amount of sucrose burned was decreased by half, the amount of heat released decreased by half. For example, when the amount of sucrose burned was decreased from 4.0 g to 2.0 g, the amount of heat released decreased from 64.0 kJ to 32.1 kJ; that is, the amount of heat released also decreased by half. (The amount of heat released actually decreased by 31.9 kJ, which is not exactly half of 64.0 kJ, but the 0.1 kJ difference between 31.9 kJ and 32.0 kJ can be attributed to limitations in the precision of the measurements [the amount of heat released is rounded off to the nearest 0.1 kJ] and can be ignored.) The amount of heat released was also decreased by half when the amount of sucrose burned was decreased from 2.0 g to 1.0 g and again when the amount of sucrose burned was decreased from 1.0 g to 0.5 g. Therefore, one can conclude that when the amount of sucrose burned is decreased by half, the amount of heat released during the burning of sucrose is decreased by half, so B is the best answer.

4. Which of the following lists the foods from Tables 1 and 2 in increasing order of the amount of heat released per gram of food?
   F. Potato, egg, bread, sucrose, cheese
   G. Sucrose, cheese, bread, egg, potato
   H. Bread, cheese, egg, potato, sucrose
   J. Sucrose, potato, egg, bread, cheese

Question 4 asks you to list the foods from Tables 1 and 2 in increasing order, from the food that releases the least amount of heat per gram of food to the food that releases the greatest amount of heat per gram of food. According to Table 1, the amount of heat released was determined for 1 g samples of each of the foods listed. Therefore, the amount of heat listed in Table 1 for each food item is the amount of heat released per gram of food. In Table 2, the amount of heat released is given for various masses of sucrose. To get the amount of heat released per gram of sucrose we can divide the amount of heat released by the mass of sucrose that was burned. However, an easier method is to notice that a trial was conducted using 1.0 g of sucrose, and during that trial, the amount of heat released was 16.0 kJ. Therefore, the amount of heat released per g of sucrose was 16.0 kJ/g. An inspection of the heat released by the combustion of the foods in Table 1 shows
that the potato sample released the least amount of heat (3.2 kJ/g), followed by the egg sample (6.7 kJ/g), the bread sample (10.0 kJ/g), and the cheese sample (17.0 kJ/g). The amount of heat per g released by sucrose, 16.0 kJ/g, places sucrose between the cheese sample and the bread sample. Therefore, the correct order is potato, egg, bread, sucrose, cheese. The best answer is F.

5. Based on the information in Tables 1 and 2, the heat released from the burning of 5.0 g of potato in a bomb calorimeter would be closest to which of the following?

<table>
<thead>
<tr>
<th>Option</th>
<th>Heat Released (kJ)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A.</td>
<td>5</td>
</tr>
<tr>
<td>B.</td>
<td>10</td>
</tr>
<tr>
<td>C.</td>
<td>15</td>
</tr>
<tr>
<td>D.</td>
<td>20</td>
</tr>
</tbody>
</table>

Question 5 asks you to use Tables 1 and 2 to estimate the amount of heat released when 5.0 g of potato is burned. Notice that Table 1 provides you with the amount of heat released (3.2 kJ) when 1.0 g of potato is burned. You might guess that burning 5.0 g of potato in the calorimeter would cause the release of five times the amount of heat released when 1.0 g of potato is burned. Do you have any evidence to support this guess? Table 1 only lists the amount of heat released when 1.0 g of potato is burned. Table 2 provides the amount of heat released from various amounts of sucrose, but not potatoes. In the absence of information to the contrary, you can assume that the relationship between the amount of potato burned and the amount of heat released is similar to the relationship between the amount of sucrose burned and the amount of heat released. According to Table 2, the heat released in kJ equals 16 times the mass of sucrose burned in grams. Note that this relationship holds whether 0.1 g of sucrose is burned or 4.0 g of sucrose is burned. For example, if 0.1 g of sucrose is burned, 0.1 g × 16 kJ released per g of sucrose = 1.6 kJ of heat released. If 4.0 g of sucrose is burned, 4.0 g × 16 kJ released per g of sucrose = 64 kJ of heat released. This relationship is a linear relationship. If the relationship between the amount of potato burned and the amount of heat released is also linear, then burning five times the amount of potato will release five times the amount of heat. Because 3.2 kJ of heat was released when 1.0 g of potato was burned, 5 × 3.2 kJ = 16 kJ will be released when 5.0 g of potato is burned. The answer closest to 16 kJ is 15 kJ, choice C.

Research Summaries Format

This type of format provides descriptions of one or more related experiments or studies similar to those conducted by researchers or science students. The descriptions typically include the design, procedures, and results of the experiments or studies. The results are often depicted in graphs or tables. Sample Passage II provides an example of the Research Summaries format that shows the results of two different experiments with light bulbs. The questions you’ll find in the Research Summaries format ask you to understand, evaluate, and interpret the design and procedures of the experiments or studies and to analyze the results. There are five sample questions presented with this sample Research Summaries passage.
Sample Passage II

A student studied illumination using the following equipment:

- 6 identical light bulbs (Bulbs A–F)
- Fixture 1, light fixture for Bulbs A–E
- Fixture 2, light fixture for Bulb F
- 2 identical paraffin blocks
- A sheet of aluminum foil having the same length and width as a paraffin block
- A meterstick

Light could pass through each paraffin block, and each block glowed when light passed through it. The aluminum foil was placed between the 2 blocks. The light fixtures, light bulbs, blocks, foil, and the meterstick were arranged as shown in Figure 1.

In the following experiments, the base of Fixture 2 was always 0.200 m from the aluminum foil, and L was the distance from the base of Fixture 1 to the aluminum foil. The distance between adjacent bulbs in Fixture 1 was the same for all of the bulbs.

Bulb F was always lit.

Experiment 1

The student turned the room lights off, lit Bulb A, and varied L until the 2 blocks looked equally bright. This process was repeated using Bulbs B–E. The results are shown in Table 1.

<table>
<thead>
<tr>
<th>Table 1</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bulb lit</td>
</tr>
<tr>
<td>(in addition to Bulb F)</td>
</tr>
<tr>
<td>A</td>
</tr>
<tr>
<td>B</td>
</tr>
<tr>
<td>C</td>
</tr>
<tr>
<td>D</td>
</tr>
<tr>
<td>E</td>
</tr>
</tbody>
</table>

Experiment 2

The procedure from Experiment 1 was repeated using various combinations of Bulbs A–E. The results are shown in Table 2.

<table>
<thead>
<tr>
<th>Table 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>Bulbs lit</td>
</tr>
<tr>
<td>(in addition to Bulb F)</td>
</tr>
<tr>
<td>A and B</td>
</tr>
<tr>
<td>A, B, and C</td>
</tr>
<tr>
<td>A, B, C, and D</td>
</tr>
<tr>
<td>A, B, C, D, and E</td>
</tr>
</tbody>
</table>
Discussion of Sample Passage II (Research Summaries)

This Research Summaries passage describes two experiments in which a student uses two identical paraffin blocks to compare the brightness of the light from one source (Fixture 1) with the brightness of the light from another source (Fixture 2). Fixture 1 contains five light bulbs, Bulbs A through E, and Fixture 2 contains only one light bulb, Bulb F (see Figure 1 in the passage). The two paraffin blocks are set between the fixtures. The two blocks are separated by a sheet of aluminum foil, so that the block on the left is illuminated only by bulbs in Fixture 1, and the block on the right is illuminated only by Bulb F in Fixture 2. The distance, \(L\), between Fixture 1 and the aluminum foil can be varied, but the distance between Fixture 2 and the foil, 0.200 m, is fixed.

In Experiment 1, one bulb at a time is lit in Fixture 1, and Bulb F is lit in Fixture 2. For each combination of lit bulbs, \(L\) is varied until the two blocks glow equally brightly. This value of \(L\) is recorded in Table 1 along with the combination of lit bulbs used to obtain this value of \(L\). In Experiment 2, two or more bulbs at a time are lit in Fixture 1, and Bulb F is lit in Fixture 2. For each combination of lit bulbs, \(L\) is varied until the two blocks glow equally brightly. This value of \(L\) is recorded in Table 2 along with the combination of lit bulbs.

6. Which of the following best explains why the student turned off the room lights?
   - F. To ensure that only the light from Bulbs A–F illuminated the 2 paraffin blocks
   - G. To ensure that light from outside the room illuminated the 2 paraffin blocks unequally
   - H. To keep the 2 paraffin blocks from casting shadows, because shadows would make the meterstick harder to read
   - J. To keep the 2 light fixtures from casting shadows, because shadows would make the meterstick harder to read

Question 6 asks you why the student turned off the room lights before measuring \(L\). Recall that the student was to compare the brightness of the light produced by Fixture 1 to the brightness of the light produced by Fixture 2 under a variety of conditions. The presence of light sources other than Fixtures 1 and 2 could have introduced error into the measurements of \(L\) by making one fixture or the other seem brighter than it really was. The overhead lights were turned off so that all of the light on the blocks came from the light bulbs in Fixtures 1 and 2. Thus, F is the best answer.

7. During Experiment 2, suppose the student replaced Fixture 1 with a new fixture. The new fixture held 6 light bulbs, each bulb identical to Bulb F. When all 6 bulbs in the new fixture were lit and the paraffin blocks looked equally bright, \(L\) would probably have been closest to:
   - A. 0.262 m.
   - B. 0.331 m.
   - C. 0.415 m.
   - D. 0.490 m.
Question 7 proposes that Fixture 1 be replaced by a different fixture holding six light bulbs instead of five. Each of the light bulbs in the new fixture is identical to Bulb F. The question asks you to estimate \( L \) for the case that all six light bulbs in the new fixture, as well as Bulb F, are lit. According to Table 2, as the number of lit bulbs in Fixture 1 increased from two to five, \( L \) increased. So if the new fixture is used, increasing the number of lit bulbs from five to six, one would expect \( L \) to be greater than the value of \( L \) given in Table 2 for five lit bulbs in Fixture 1, 0.446 m. Only D contains a value for \( L \) exceeding 0.446 m, so D is the best answer.

8. The main purpose of Experiment 1 was to:
   - F. calibrate the meterstick.
   - G. determine the relationship between \( L \) and the number of lit bulbs.
   - H. determine if \( L \) depended on a lit bulb’s position in Fixture 1.
   - J. find the brightness of Bulb F.

Question 8 asks you to determine the main purpose of Experiment 1. In Experiment 1, one bulb at a time was lit in Fixture 1, but the location of the lit bulb in Fixture 1 was varied. Thus, the main purpose of Experiment 1 must have been to determine the effect, if any, that the location of the lit bulb had on the value of \( L \). Only H states that the purpose of Experiment 1 was to determine if the position of the lit bulb within Fixture 1 affected \( L \), so H must be the best answer.

9. Suppose that all of the light bulbs in Fixture 1 were replaced with a single bulb. Based on Experiments 1 and 2, if the 2 paraffin blocks looked equally bright when Fixture 2 was 0.200 m from the aluminum foil and \( L = 0.446 \) m, the brightness of the new light bulb was most likely:
   - A. \( \frac{1}{6} \) the brightness of one of the original bulbs.
   - B. \( \frac{1}{5} \) the brightness of one of the original bulbs.
   - C. 5 times the brightness of one of the original bulbs.
   - D. 6 times the brightness of one of the original bulbs.

Question 9 proposes that the five light bulbs in Fixture 1 be replaced with a single light bulb, and that when the new bulb and Bulb F are lit, for the two blocks to glow equally brightly, \( L \) must equal 0.446 m. You are asked to compare the brightness of the new bulb to the brightness of one of the original bulbs in Fixture 1. According to Table 2, the two paraffin blocks glowed equally brightly when all five bulbs in Fixture 1 were lit and \( L = 0.446 \) m, the same as the \( L \) obtained with the new bulb. Thus, the brightness of the new bulb would have to equal the sum of the brightness of the five original bulbs. Because each of the five original bulbs had the same brightness, the new bulb would have to be five times as bright as one of the original bulbs. Only C is consistent with this conclusion, so the best answer is C.
10. In Experiment 2, suppose the student had replaced Bulb F with a much brighter light bulb, Bulb G. Compared to \( L \) when Bulb F was used, \( L \) when Bulb G was used would have been:

- **F.** greater for every combination of lit bulbs.
- **G.** smaller for every combination of lit bulbs.
- **H.** smaller when Bulbs A–E were simultaneously lit and greater when other combinations of light bulbs were lit.
- **J.** greater when both Bulbs A and B were simultaneously lit and smaller when other combinations of light bulbs were lit.

Question 10 proposes that in Experiment 2, Bulb F be replaced by a much brighter bulb, Bulb G. For each combination of lit bulbs in Fixture 1 and Bulb G lit in Fixture 2, when the two paraffin blocks are equally bright, how would the value of \( L \) compare to that obtained when Bulb F was used in Fixture 2? Because Bulb G is brighter than Bulb F and would be the same distance (0.200 m) away from the aluminum foil as Bulb F, the paraffin block closer to Bulb G would glow more brightly than it glowed when Bulb F was used. Thus, for each combination of lit bulbs in Fixture 1, to make the two blocks glow with equal brightness, Fixture 1 would have to be closer to the blocks than when Bulb F was used. That is, when Bulb G was used, \( L \) for each combination of lit bulbs in Fixture 1 would have to be less than when Bulb F was used for the two blocks to glow with equal brightness. Only choice **G** is consistent with this conclusion. The best answer is **G**.

**Conflicting Viewpoints Format**

This type of format provides several alternative theories, hypotheses, or viewpoints on a specific observable phenomenon. These conflicting viewpoints are based on differing premises or on incomplete data and are inconsistent with one another. Sample Passage III, a biology passage on gene replication, is an example of the Conflicting Viewpoints format. Notice that this passage presents the theories of four different students.

The questions you’ll find in the Conflicting Viewpoints format ask you to understand, analyze, evaluate, and compare several competing theories, hypotheses, or viewpoints. Five sample questions are presented with this sample Conflicting Viewpoints passage.
Sample Passage III

Many bacteria contain plasmids (small, circular DNA molecules). Plasmids can be transferred from 1 bacterium to another. For this to occur, the plasmid replicates (produces a linear copy of itself). The relative position of the genes is the same on the original plasmid and on the linear copy, except that the 2 ends of the linear copy do not immediately connect.

While replication is occurring, 1 end of the linear copy leaves the donor bacterium and enters the recipient bacterium. Thus, the order in which the genes are replicated is the same as the order in which they are transferred. Unless this process is interrupted, the entire plasmid is transferred, and its 2 ends connect in the recipient bacterium.

Four students studied the way in which 6 genes (F, X, R, S, A, and G) on a specific plasmid were donated by a type of bacterium (see the figure). The students determined that the entire plasmid is transferred in 90 min and that the rate of transfer is constant. They also determined that the genes are evenly spaced around the plasmid, so 1 gene is transferred every 15 min. They disagreed, however, about the order in which the genes are replicated and thus transferred. Four models are presented.

**Student 1**
Replication always begins between Gene F and Gene X. Gene X is replicated first and Gene F is replicated last.

**Student 2**
Replication always begins between Gene F and Gene X. However, the direction of replication varies. If Gene F is replicated first, Gene X is replicated last. Conversely, if Gene X is replicated first, Gene F is replicated last.

**Student 3**
Replication can begin between any 2 genes. Replication then proceeds around the plasmid in a clockwise direction (with respect to the figure). Thus, if Gene S is replicated first, Gene A is replicated second, and Gene R is replicated last.

**Student 4**
Replication can begin between any 2 genes. Likewise, replication can proceed in either direction. So the order of replication varies.

11. Based on the information presented, if the transfer of the linear copy was interrupted 50 min after transfer began, how many complete genes would have been transferred to the recipient bacterium?
A. 2
B. 3
C. 4
D. 5

12. Based on the model presented by Student 3, if all 6 genes are replicated and the first gene replicated is Gene G, the third gene replicated would be:
F. Gene F
G. Gene A
H. Gene S
J. Gene X

13. Which students believe that any of the 6 genes on the plasmid can be the first gene transferred to a recipient bacterium?
A. Students 2 and 3
B. Students 2 and 4
C. Students 3 and 4
D. Students 2, 3, and 4

14. Suppose that Student 2’s model is correct and that the transfer of genes between 2 bacteria was interrupted after 30 min. Under these conditions, which of the following genes would definitely NOT be transferred from the donor bacterium to the recipient bacterium?
F. Gene A
G. Gene R
H. Gene G
J. Gene X

15. Suppose that the transfer of genes between 2 bacteria was interrupted, that the last gene transferred was Gene A, and that no incomplete copies of a gene were transferred. Based on this information, Student 1 would say that transfer was most likely interrupted how many minutes after the transfer began?
A. 15
B. 30
C. 45
D. 60
Discussion of Sample Passage III (Conflicting Viewpoints)

According to this Conflicting Viewpoints passage, plasmids (small DNA molecules, each molecule consisting of genes arranged in a circle) are found in bacteria. While a plasmid is replicating (producing an identical copy of itself) in one bacterium, the gene copies are being transferred to a second bacterium, the recipient bacterium, eventually forming a complete copy of the plasmid in the recipient bacterium.

Notice the diagram of a plasmid in the passage. The plasmid in the diagram contains six genes. The passage tells us that when the plasmid replicates, it produces a linear copy of itself; that is, the six genes in the copy are arranged in the same order as in the original plasmid, but the genes in the copy are first arranged in a row rather than in a circle. The plasmid copies one gene at a time, and, according to the passage, the gene copies are transferred to the recipient bacterium one at a time in the order in which the copies are produced. For example, if the plasmid copies Gene F, followed by Gene X, Gene F will be transferred to the recipient bacterium first, followed by Gene X. Once all of the genes of the original plasmid have been copied and transferred to a recipient bacterium, the two ends of the linear plasmid copy connect to each other, forming a circle just like the one in the passage.

Four students agree that the rate of gene transfer between bacteria is constant and occurs at the rate of one gene every 15 minutes, so a complete plasmid is transferred between the bacteria in $6 \times 15 = 90$ minutes. However, the identity of the first gene to be replicated and the direction (clockwise or counterclockwise around the circle) in which replication proceeds are subjects of disagreement among the four students.

- According to Student 1, Gene X is always replicated and transferred first, and Gene F is always replicated and transferred last. That is, replication always starts with Gene X and proceeds in a clockwise direction around the plasmid.
- According to Student 2, replication always begins with either Gene F or Gene X. If Gene F is first, then Gene X is last; that is, if replication begins with Gene F, then replication proceeds in a counterclockwise direction around the plasmid. If Gene X is first, then Gene F is last; that is, if replication begins with Gene X, then replication proceeds in a clockwise direction around the plasmid.
- According to Student 3, replication can start with any gene but always proceeds in a clockwise direction around the plasmid.
- According to Student 4, replication can start with any gene and can proceed in either direction around the plasmid.
11. Based on the information presented, if the transfer of the linear copy was interrupted 50 min after transfer began, how many complete genes would have been transferred to the recipient bacterium?

A. 2
B. 3
C. 4
D. 5

Question 11 asks you to predict how many complete genes would have been transferred to the recipient bacterium if gene transfer had been interrupted 50 minutes after transfer had begun. According to the passage, one gene was transferred every 15 minutes. Therefore, three genes would have been transferred in $3 \times 15 = 45$ minutes. A partial gene transfer would have occurred in the remaining 5 minutes, but the question asks about complete gene transfers, so you can ignore the partial gene transfer. The answer is three genes. Therefore, the best choice is B.

12. Based on the model presented by Student 3, if all 6 genes are replicated and the first gene replicated is Gene G, the third gene replicated would be:

F. Gene F.
G. Gene A.
H. Gene S.
J. Gene X.

Question 12 asks you to suppose that all six genes in a plasmid are replicated and that Gene G is the first gene replicated. You are asked to predict the third gene replicated, assuming that Student 3’s model is correct. According to Student 3’s model, replication can start with any gene but always proceeds around the plasmid in a clockwise direction. Therefore, starting with Gene G and proceeding in a clockwise direction, Gene F would be the second gene replicated and Gene X would be the third gene replicated. The best answer is J.

13. Which students believe that any of the 6 genes on the plasmid can be the first gene transferred to a recipient bacterium?

A. Students 2 and 3
B. Students 2 and 4
C. Students 3 and 4
D. Students 2, 3, and 4

Question 13 asks which students believe that any of the six genes on the plasmid can be the first gene transferred to a recipient bacterium. According to the passage, the order in which genes are transferred is the same as the order in which genes are replicated. Student 1 asserts that replication always begins with Gene X, so Student 1 would disagree with the statement that any of the six genes on the plasmid can be the first gene transferred. Student 2 asserts that replication
always begins with either Gene X or Gene F, so Student 2 would disagree with the statement that any of the six genes on the plasmid can be the first gene transferred.

According to Students 3 and 4, replication can begin between any two genes on the plasmid, so they agree that any of the six genes on the plasmid can be the first gene transferred to a recipient bacterium. Because only Students 3 and 4 agree that any gene on the plasmid can be the first gene transferred, the best answer is C.

14. Suppose that Student 2’s model is correct and that the transfer of genes between 2 bacteria was interrupted after 30 min. Under these conditions, which of the following genes would definitely NOT be transferred from the donor bacterium to the recipient bacterium?

- F. Gene A
- G. Gene R
- H. Gene G
- J. Gene X

Question 14 asks you to suppose that the transfer of genes between two bacteria was interrupted 30 minutes after the transfer began. You are asked to select from among a list of genes (A, R, G, and X) the gene that could NOT have been transferred to the recipient bacterium within the allotted 30 minutes, assuming that Student 2’s model is correct. According to the passage, one complete gene transfer occurs every 15 minutes. Therefore, two complete gene transfers would have occurred after $2 \times 15 = 30$ minutes. Based on Student 2’s model, gene transfer can start with Gene X and proceed around the plasmid in a clockwise direction, or transfer can start with Gene F and proceed around the plasmid in a counterclockwise direction. If transfer had started with Gene X, Gene R would have been the second gene transferred. If transfer had started with Gene F, Gene G would have been the second gene transferred. Therefore, we conclude Genes X, R, F, and G could have been transferred. The only gene in the list that could not have been transferred is Gene A. Based on Student 2’s model, if Gene X had been the first gene transferred, then $4 \times 15 = 60$ minutes would have been required for Gene A to be transferred, because Gene A is the fourth gene in the clockwise direction from Gene X. If Gene F had been the first gene transferred, $3 \times 15 = 45$ minutes would have been required for Gene A to be transferred, because Gene A is the third gene in the counterclockwise direction from Gene F. The best answer is F.

15. Suppose that the transfer of genes between 2 bacteria was interrupted, that the last gene transferred was Gene A, and that no incomplete copies of a gene were transferred. Based on this information, Student 1 would say that transfer was most likely interrupted how many minutes after the transfer began?

- A. 15
- B. 30
- C. 45
- D. 60

Question 15 asks you to suppose that the transfer of genes between two bacteria was interrupted after the transfer of Gene A had been completed, and that no incomplete transfer of a gene occurred
after the transfer of Gene A. You are asked to determine the number of minutes between the time that gene transfer began and the time at which gene transfer was interrupted, assuming that Student 1’s model is correct. According to Student 1, Gene X is always transferred first, and Gene F is always transferred last. That is, transfer always starts with Gene X and proceeds in a clockwise direction around the plasmid. If we count genes in the clockwise direction, starting with Gene X, we find that Gene A is the fourth gene, so Gene A would have been the fourth gene transferred. According to the passage, each complete transfer of a gene requires 15 minutes. Thus, the number of minutes between the time at which the transfer of Gene X began and the time at which the transfer of Gene A was completed would have been $4 \times 15 = 60$ minutes. The best answer is D.

<table>
<thead>
<tr>
<th>Answer Key for Science Test Sample Questions</th>
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**Strategies for Taking the ACT Science Test**

Performance on the ACT science test relies mainly on the ability to understand and process scientific information presented in various formats but can also be affected by problem-solving strategies and skills. The following sections describe strategies and skills specifically for improving your ACT science score.

**Develop a Problem-Solving Method**

Because you have only a limited time in which to take the science test, you may find it helpful to work out a general problem-solving method that you can use for all or most of the questions. The method described here is certainly not the only way to solve the problems, but it is one that works for most science problems. Whether you see a way to adapt this method, or you work out your own approach, use the method that works best for you.

One approach to solving problems is to break the process into a series of smaller steps, such as these:

1. Restate the problem in your own words.
2. Decide what information is needed to solve the problem.
3. Extract the needed information from the passage. Information may include data, concepts, or even conclusions you’ve been able to draw from the information provided.
4. Consider any additional scientific knowledge (terms or concepts) you may have.
5. Organize the information and use reason to arrive at the answer.
6. Compare your answer to the answer choices and choose the option you think is correct.

**Take Notes**

As you read a question, take notes in the test booklet or on scratch paper to record what the question is asking and what information you have at your disposal to answer the question. (In some circumstances you are not permitted to write in your test booklet. In those circumstances, you’ll be given scratch paper to use.) Sometimes, the process of writing down or reviewing notes reveals the answer or helps you develop an effective approach to finding the answer.

**Pace Yourself**

Remember, you have 35 minutes to read several passages and their accompanying questions (40 questions altogether). That’s about 5 minutes for each passage and the accompanying questions. You can think of it as 40 questions in 35 minutes, or a little less than a minute per question. If you’re like most people, you’ll find some of the passages more familiar and probably easier than some of the others, so it’s a good idea to try to work fast enough to allow yourself time to come back to any questions you have trouble answering the first time.

**Practice Interpreting Graphs, Tables, and Diagrams**

Much of the information you need to answer the science test questions is presented graphically in the form of graphs, tables, and diagrams. Practice interpreting tables and different types of graphs, including pie charts, line charts, bar or column charts, and scatter charts, especially those included in science articles. Examine graphs and tables closely until you understand the data and can pick out specific pieces of data.

**Tip:** Pay attention to any and all text in graphs, tables, or diagrams, because any of this text is likely present to serve as instruction for how to interpret the data:

**Graphs**

Read the axis labels and the labels for any lines (curves) present. Typically, the $y$-axis indicates what is being measured (the dependent variable) and the $x$-axis most often indicates what is being manipulated (the independent variable). Some graphs may have a legend (labeled *Key*) that identifies line styles and the quantities they represent. Graphs may also have notes at the bottom of the graph to supply additional information.

**Tables**

Look at the column and row headings, which will identify quantities and their units of measure. Often (but not always) manipulated variables (independent variables) will be on the left side of the graph and the measured quantity (the dependent variable) will be to the right of the graph. Some tables will have notes at the bottom that provide vital information for interpreting the data.
Diagrams

Diagrams often contain labeled parts and could represent everything from a food web to a laboratory setup or show the cross-section of an object, such as the layers of Earth or of Earth’s atmosphere. Diagrams generally contain more text than numbers. Look for a title (above the diagram) or a caption (below the diagram) and for labels on the diagram itself. The diagram may not have a title, but parts of it may be labeled, as in a diagram of a laboratory setup that sheds light on how an experiment works.

Give yourself some time to figure out what the graph, table, or diagram is showing you in general. You can always look at these graphic representations more closely when answering questions, but having a general idea of what they show may shed light on what the questions are asking.

*Make the Most of the Information in Graphs*

Graphs illustrate data in ways that can be very useful if you follow a few rules. First, it’s important to identify what is being displayed in the graph (e.g., mass, volume, velocity). What unit or units of measurement is (are) used (e.g., grams, liters, kilometers per hour)? Graphs usually have axis labels that provide this information and some will have a key or legend or other short explanation of the information presented. Many graphs consist of two axes (horizontal and vertical), both of which will be labeled, and some may have dual axes with more than one curve. Remember, the first thing to find out about any graph is exactly what the numbers represent.

Once you’ve identified what is being presented in a graph, you can begin to look for trends in the data. The main reason for using a graph is to show how one characteristic of the data tends to influence other characteristics.

For a coordinate graph, notice how a change on the horizontal axis (or $x$-axis) relates to the position of the variable on the vertical axis (or $y$-axis). If the curve shows angles upward from lower left to upper right (as in Figure 1a), then, as the variable shown on the $x$-axis increases, so does the variable on the $y$-axis (a direct relationship). An example of a direct relationship is that a person’s weight increases as his or her height increases. If the curve goes from the upper left to the lower right (as in Figure 1b), then, as the variable on the $x$-axis increases, the variable on the $y$-axis decreases (an inverse relationship). An example of an inverse relationship is that the more players there are on a soccer team, the less time each of them gets to play (assuming everyone gets equal playing time). If the graph shows a vertical or horizontal line (as in Figure 1c), the variables are probably unrelated.

![Figure 1](https://example.com/figure1.png)
Sometimes, a question will ask you to estimate a value for one characteristic based on a given value of another characteristic that is beyond the limits of the curve shown on the graph. In this case, the solution will require you to **extrapolate**, or extend, the graph. If the curve is a relatively straight line, just use your pencil to extend that line far enough for the value called for to be included. If the graphed line is a curve, use your best judgment to extend the line to follow the apparent pattern. Figure 2 shows how to extend both types of graphs.

![Figure 2](image)

Another type of graph problem asks you to estimate a value that falls between two known values on a curve. This process is called **interpolation**. If the curve is shown, it amounts to finding a point on the curve that corresponds to a given value for one characteristic and reading the value for the other characteristic. (For example, “For a given x, find y.”) If only scattered points are shown on the graph, draw a “best-fit line,” a line that comes close to all of the points. Use this line to estimate the middle value. Figure 3 shows a best-fit line.

![Figure 3](image)
One very useful kind of graph shows more than one curve on the same pair of axes. Such a graph might be used when the results of a number of experiments are compared or when an experiment involves more than two variables. Analysis of this sort of graph requires that you determine the relationship shown by each curve and then determine how the curves are related to one another. Figure 4 shows a graph with multiple curves.

![Figure 4](image)

Make the Most of the Information in Tables

To understand what a table is showing you, you need to identify the information or data presented. You need to know two things about the information or data: the purpose it serves in the experiment and the unit (or units) of measurement used to quantify it. Generally, experiments intentionally vary one characteristic (the independent variable) to see how it affects another (the dependent variable). Tables may report results for either or both.

Once you have identified the variables, it might be helpful to sketch a graph to illustrate the relationship between them. You might sketch an x-axis and a y-axis next to the table and decide which variable to represent on each axis. Mark off the axes with evenly spaced intervals that enable all of the numbers for a category to fit along each axis. Plot some points. Again, draw a best-fit line and characterize the relationship shown.

As with graphs and diagrams, you may be asked to look for trends in the data. For example, do the numbers representing the dependent variable increase or decrease as the numbers representing the independent variable increase or decrease? If no pattern is clear, you may want to sketch a rough graph as discussed above. You may also need to make predictions about values of quantities between the data points shown (interpolation) or beyond the limits of those shown on the table (extrapolation). Another type of problem may require you to compare data from multiple columns of a table or between two or more graphs or tables. A simple examination of the numbers may be enough to see a relationship, but you may find it helpful to sketch a graph containing a curve for each category. The curves may be compared as described previously in “Make the Most of the Information in Graphs.”
Develop an Understanding of Scientific Investigations

When working with a Research Summaries passage, you should be able to understand scientific processes. This includes identifying the designs of experiments, identifying assumptions and hypotheses underlying the experiments, identifying controls and variables, determining the effects of altering the experiments, identifying similarities and differences between the experiments, identifying the strengths and weaknesses of the experiments, developing other experiments that will test the same hypothesis, making hypotheses or predictions from research results, and creating models from research results.

Carefully Analyze Conflicting Viewpoints

When reading a Conflicting Viewpoints passage, first read the introductory information. This describes the phenomena about which the viewpoints will differ. It may also present a graph, table, or diagram, as well as discuss aspects that all of the viewpoints share. Then, read each viewpoint closely and note what is the same and different in each. Note each viewpoint's strengths and weaknesses. Use your own scientific knowledge and common sense to draw conclusions about each viewpoint. Which viewpoint sounds most credible? Which has the most evidence to back it up? With an understanding of and opinion about each viewpoint, you are better equipped to understand and answer questions about them.
Chapter 9: Improving Your Score on the Optional Writing Test

On the ACT writing test, you have 40 minutes to read a prompt and to plan and write an essay in response to it. The prompts on the writing test cover a variety of subjects intended to reflect engaging conversations about contemporary issues, and they are designed to be appropriate for response in a 40-minute timed test.

The writing test is an optional test on the ACT. Should you decide to take the writing test, it will be administered after the four multiple-choice tests. Taking the writing test will not affect your scores on any of the multiple-choice tests or the Composite score. Rather, in addition to your scores from the multiple-choice tests and your Composite score, you may receive an English Language Arts score (ELA).

You will have a short break between the end of the last multiple-choice test and the beginning of the writing test.
Improving Your Score on the Optional Writing Test

Content of the ACT Writing Test

The writing test describes an issue and provides three different perspectives on the issue. You are asked to “evaluate and analyze” the perspectives, to “state and develop” your own perspective, and to “explain the relationship” between your perspective and those given. The test also offers guidance and structure for planning and prewriting, but planning and prewriting are optional and do not count toward the score. Your score will also not be affected by the perspective you take on the issue. Your essay will be evaluated based on the evidence that it provides of your ability to do the following:

- Analyze and evaluate multiple perspectives on a complex issue
- State and develop your own perspective on the issue
- Explain and support your ideas with logical reasoning and detailed examples
- Clearly and logically organize your ideas in an essay
- Effectively communicate your ideas in standard written English

How Your Essay Will Be Scored

Your essay will be scored analytically using a rubric with four domains that correspond to different writing skills (turn to chapter 3 for a copy of the actual scoring rubric for the ACT writing test). Two trained readers will separately score your essay, giving it a rating from 1 (low) to 6 (high) in each of the following four domains: ideas and analysis, development and support, organization, and language use and conventions. Each domain score represents the sum of the two readers’ scores and is reported on a scale of 2 to 12. If the readers’ ratings differ by more than one point, a third reader will evaluate the essay and resolve the discrepancy. Your writing score is calculated from your domain scores and is reported on a scale of 1 to 36. **You can find the most current information on scoring the ACT writing test in the bonus online content.**

The readers take into account that you had merely 40 minutes to compose and write your essay. Within that time limit, polish your essay as best as you can. Make sure that all words are written clearly and neatly. Although handwriting is not scored, it could negatively affect your score if the readers can’t decipher it. With careful planning, you should have time to briefly review and edit your essay after you have finished writing it. Keep in mind that you probably will not have time to rewrite or even recopy your essay. Instead, you should take a few minutes to think through your essay and jot preliminary notes on the planning pages in the scoring booklet before you begin to write. Prewriting (planning) helps you organize your ideas, manage your time, and keep you on track as you compose your essay.

Sample Prompt and Essays

In preparation for the ACT writing test, examine the sample writing prompt, essays, and scoring explanations in the following sections. The sample prompt shows what you can expect to encounter on test day; the sample essays serve as models of low-, medium-, and high-scoring essays; and the scoring explanations provide insight into the criteria the readers will use to score your essay.
Sample ACT Writing Test Prompt

Writing test prompts are similar to the following example. The standard directions in the second paragraph are a part of all prompts used in the writing test. You might want to practice by writing in response to this prompt for 40 minutes before you look ahead to the sample responses from other writers. Note that readers who have already taken the practice test in chapter 3 do not need to do so here.
Free Music

Free music is now available through many legal sources, from streaming services to online radio stations, making it largely unnecessary to purchase an album or even a single song. As sales figures continue to drop, some musicians, both high-profile and relatively unknown, have even quit trying to sell their music altogether, choosing instead to release new material for free online. Perhaps this trend is a matter of simple economics: cheap is good, but free is better. But it is worth considering whether our apparent unwillingness to spend money on music is an indication that its value in our lives is changing.

*Read and carefully consider these perspectives. Each suggests a particular way of thinking about the changing value of music in our lives.*

<table>
<thead>
<tr>
<th>Perspective One</th>
<th>Perspective Two</th>
<th>Perspective Three</th>
</tr>
</thead>
<tbody>
<tr>
<td>Digital technologies and the Internet have changed our relationship with music. It is so plentiful and readily available now that all value has been diluted.</td>
<td>Music competes for our attention with many other kinds of inexpensive entertainment these days. We still value it, but we also have a lot of other ways to spend our money.</td>
<td>With so many free sources, people are listening to more music and discovering more new musicians than ever before. Wide availability has only increased our appreciation of music.</td>
</tr>
</tbody>
</table>

**Essay Task**

Write a unified, coherent essay in which you evaluate multiple perspectives on the changing value of music in our lives. In your essay, be sure to:

- analyze and evaluate the perspectives given
- state and develop your own perspective on the issue
- explain the relationship between your perspective and those given

Your perspective may be in full agreement with any of the others, in partial agreement, or wholly different. Whatever the case, support your ideas with logical reasoning and detailed, persuasive examples.
Sample Essay Responses

The essays that follow are sample essays produced in response to the given writing prompt. The essays illustrate how writing at different levels is evaluated and scored for the ACT writing test. The essays in no way represent a full range of ideas, approaches, or styles that could be used. Although we all can learn from reading other people's writing, you are encouraged to bring your own distinct voice and writing skills to the test. You want to produce your own best essay for the writing test—not an imitation of someone else's essay writing.

The following essays have been evaluated using the scoring rubric for the ACT writing test (see chapter 3). This same rubric will be used to score the response that you write for the ACT writing test. Each essay is followed by a scoring explanation that comments on the essay.

You can find the most current information on scoring the ACT writing test in the bonus online content.
I say three because with so many
sources the people are listening more on
more music and it is discovering more
with new musicians than they ever before.
And they said a matter of simple economics;
cheap is good, but free is better.
Free music is to online music and radio
stations and choosing instead to release
new music.
Sample Essay 1 (Score: 1111)

Score Explanation
The writer’s attempt to rearrange the prompt does not demonstrate skill in writing an argumentative essay.

Ideas and Analysis (1): The writer’s intentions are hard to discern. Although the first sentence suggests that the essay will argue in favor of Perspective Three, there is no analysis to help shape or clarify the main idea of this essay. Instead, there is a confusing attempt to piece together ideas from the prompt. It is difficult to determine what this writer is trying to convey, and thus it is difficult to identify an intelligible argument.

Development and Support (1): Reasoning and illustration are unclear. Instead of elaborating on the idea that Perspective Three is favorable (“I say three”), the writer simply repeats the perspective (“because with so many sources the people are listening more and more music and […] discovering more with new musicians than they ever before”). Attempts to develop this point further are incoherent, because subsequent explanations do not clearly relate to a main idea (“And they said a matter of simple economics; cheap is good, but free is better,” “Free music is to online music and radio stations and choosing instead to release new music”).

Organization (1): This response does not exhibit an organizational structure. Although the piece does assume the appearance of a paragraph, the presentation of ideas within this paragraph is disorderly. Because these ideas do not clearly relate to one another, they cannot be logically grouped. Although the writer uses transitional language (“because,” “And they said”), the transitions fail to logically connect ideas.

Language Use (1): This essay is unsuccessful in communicating a larger idea, and many of its shortcomings can be attributed to poor language control. Even though this response is heavily dependent on language drawn from the prompt, usage errors are abundant (“people are listening more and more music and it is discovering more with new musicians than they ever before”) and sentences are poorly formed (“And they said a matter of simple economics; cheap is good, but free is better”). As a result, the writer fails to demonstrate skill in using language to convey an argument.
What makes you appreciate music?

Is it the many ways you can get access to it, how about being able to get it free. Also there are so many different genres of music that you could choose from. Everyone has got so many row artists catching people's eyes now and days that they give you a huge variety to choose from.

There are so many ways you can get music. Such as computers, going to radio's and CDs. There are so many sources to get music from that almost anyone can listen to it. Every where you see students listen to music in school and at college. So many young people listen to it.

Who can beat free? No one; that's the best it can get free!

If you need more space, please continue on the back of this page.
WRITING TEST

Music is so wide spread that people don't have to pay for music anymore. You can get it free anywhere except from some brick and online music stores. Who would pay for music besides those who live to have CD albums? That's the only case I see that people would pay for their music.

To add there are so many artists and genres out in the music world that anyone can pick to listen to. It's an easy way to listen to anyone person you want to. Such a gallery to pick from. Some people believe getting music for free makes music value go way down. People go to concerts and buy tickets and remember what it made their artists money.

To bundle everything together having free music is awesome. You have access anywhere and everywhere. Having free music gives folks unlimited supply to any artist and genre they want to listen to. Although some feel it decreases the value of music. There are concerts and places you can go to but buy tickets, and artist supply.

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**Sample Essay 2 (Score: 2222)**

**Score Explanation**

The writer generates an argument in response to the task, but the argument is imprecise in its focus and inconsistent in its execution.

**Ideas and Analysis (2):** The writer generates an argument that weakly responds to multiple perspectives on the issue. Although something of a thesis is evident—“free music is awesome” because of the benefits to music lovers—it is only loosely related to the prompt's question of whether the value of music in our lives is changing. Analysis of the issue and its perspectives is incomplete and, in some respects, irrelevant. For example, it is unclear how the writer's point that “there are so many ways you can get music […] you see students listen to music in school and at college” is related to the thesis or even to the concept of free music. The writer’s critique of the idea that free music causes the value we place on music to decline is similarly imprecise (“Some people believe [free music] make music value go way down. People go to concerts and buy tickets and memorbila that it make them atists money”).

**Development and Support (2):** Development and support fail to fully clarify the argument and contribute to the inconsistent sense of purpose exhibited by this response. In many cases, reasoning and illustration are circular (“There are so many ways you can get music. Such as computers, phones, radios and CD’s. There are so many sources to get music from that almost anyone can listen to it”) and redundant (“Who can beat free? No one; that's the best it can get free! Music is so wide spread that people don’t have to pay for music anymore. You can get it free anywhere except from name brand online music store”).

**Organization (2):** This response does exhibit an organizational structure. The writer offers an introduction and conclusion, and the body paragraphs in between are each seemingly dedicated to a main idea. A closer examination of this structure, however, reveals a number of inconsistencies. Grouping of ideas, for example, is somewhat unclear—the final body paragraph includes a counterargument that doesn’t seem to address the main point of the paragraph. Furthermore, the absence of transitions within paragraphs contributes to the repetitive quality of the development.

**Language Use (2):** Imprecise word choices, repetitive phrasing, unclear sentence structures, and grammatical errors: these are the markers of inconsistent skill in using language, and these markers are prevalent in this essay. A number of phrases appear multiple times throughout the essay (“their/there are so many,” in particular), reflecting imprecision in vocabulary and word choice; a number of fragments and run-on sentences reveal weak mechanical control. Although the writer’s exuberant voice (“that's the best it can get free!”) is generally appropriate for the rhetorical purpose—after all, the argument is that free music is awesome—this relative strength does not outweigh the essay’s many weaknesses in the use of language.
Begin WRITING TEST here.

Over the past years music has become easier and cheaper to listen to than ever before. While people have begun spending less money on music, its value has not gone down. People are still willing to pay for music. However, there has been a big decline in the amount of music bought. With music becoming free more people are able to listen and the value of music continues to go up.

The decreasing price of music has had many positive effects. Before, it was hard to listen to a lot of music because the price was too high. Now people are able to listen to music and spend their money on other things. Some think that the value of music has gone down because people aren’t willing to spend money on it. However, this is not true. People are still willing to pay for some music and to go to concerts. The lowered price of music has caused music to be available to more people and has not caused the value to go down.

The fact that music has become free has had some negative effects as well. Since people are able to get music for free they spend much less money for the music. Some artists have decided to stop selling their music and just put it out for free. This causes a decline in all music sales. Instead of spending money on music people have begun to spend it on other things.

If you need more space, please continue on the back of this page.
The price people are willing to pay continues to drop. Although there have been negative effects of free music, the value of music has not gone down. Overall, the positive effects are much higher than the negative ones.

Even though the prices of music have dropped, its value has gone up. More musicians are being discovered, and our appreciation of music has only become higher. With its availability, more people are able to hear the music, which causes people to spend their money on concerts. People are still willing to pay to see music, but now they have more money, so they are able to spend it on other things as well. As more music continues to be free, more people will continue to listen to it. Without music becoming free, its value would have gone down because it was too expensive. The rise of free music has increased its value.

Throughout time, music has become more inexpensive than ever. Now more people can hear and appreciate it while having money left over. While there are some negative effects, the positive effects are higher. While people aren’t spending as much money on music, the value has gone up. People everywhere are now able to listen. Free music has made a big impact on the world of music forever.

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Improving Your Score on the Optional Writing Test

WRITING TEST

STOP here with the Writing Test.

Do not write in this shaded area.
Sample Essay 3 (Score: 3333)

Score Explanation
The writer generates an analytical argument that considers other perspectives, but the essay exhibits lapses in clarity that keep it from achieving a higher score.

Ideas and Analysis (3): The writer generates the thesis that, despite the trend toward free music, the value of music is rising. Although this idea reflects a clear focus on the issue, its execution reveals lapses in thought and purpose. In analyzing the issue and its perspectives, the writer discusses the positive and negative effects of free music. This contextual framework proves to be limited, because it results in simplistic analysis of the perspectives (see, for example, the writer's rebuttal of Perspective One and the writer's affirmation of Perspective Two). Furthermore, the negative effects the writer articulates occasionally contradict the positive effects: in the second paragraph, the writer claims that people still pay for music, but the third paragraph states that “[i]nstead of spending money on music people have began to spend it on other things.” Finally, it is not always clear how the positive and negative effects the writer outlines are intended to relate to the question of the value we place on music and thus to the thesis. Though the writer attempts to make these connections (“Although there have been negative effects of free music the value of music has not gone down”), the juxtaposition of positive and negative effects, as an analytical technique, is only somewhat clear in this argument.

Development and Support (3): The argument's thesis takes shape through reasoning and illustration, which offer clarifying explanations of the positive and negative effects the writer perceives. However, this development, although relevant, is overly general (“People are still willing to pay to see music, but now they have more money, so they are able to spend it on other things as well. As more music continues to be free, more people will continue to listen to it. Without music becoming free its value would have gone down because it was too expensive”), and key ideas go unsupported (“Overall the positive effects are much higher than the negative ones”).

Organization (3): The positive-negative framework provides a basic organizational structure, allowing the ideas in this response to cohere as an argument. Transitions, particularly in the topic sentences of the body paragraphs, signal shifts in the discussion and are somewhat successful in connecting ideas across the essay. Despite these strengths, however, the piece falls short of adequacy in the Organization domain. The thesis is intended to control the argument but is unable to do so; the question of the value we place on music falls in and out of focus. Furthermore, the arrangement of the discussions on positive and negative effects is a bit haphazard; the writer jumps back and forth between these discussions without an evident purpose in doing so.

Language Use (3): The use of language exhibits basic clarity. Sentence structures are clear; errors, although distracting, rarely impede understanding; and the writer's voice and tone are appropriate for the purpose. However, as in the other three domains, language use demonstrates only developing skill. Though the writer makes reasonable word choices, vocabulary and phrasing are often overly general (“The lowered price of music has caused music to be available to more people and has not caused the value to go down,” “Throughout time music has become more inexpensive than ever”), leading to imprecision in expression.
Begin WRITING TEST here.

Music has played a constant role in society throughout time. It has adapted to the circumstances, whether it be as a way of expressing oneself or as a way to react or stand against something. But one thing has changed about music in more recent times—the cost. Music has always cost something, whether it meant buying it online or from a store. However, recently it has been becoming more available for no price at all. Many people see this as a bad thing as it dilutes our value of music and makes feel that it actually has broadened our appreciation of music. In reality, it is actually a mix between both views. By having music be available for free, it has made discovery of new musicians, styles, and thus new cultures more accessible.

Many often see a limitation on what people can buy. Since music is now more often free, people from all areas in the economic stance can listen and expand their realm of experiences. People are more likely to try out new music styles or artists because it is free and there is nothing stopping them from listening. If they have to pay money for music they aren’t sure they are going to like, then people will not be willing to take a risk and try something new. To go along with today’s society, if a person does decide to listen to new music due to being free, they are then open to.

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WRITING TEST

Immerse themselves in different cultures. This will help
broaden their knowledge of music and things that affect it thus
increasing their appreciation of it. It allows for exploration.

However, music does elevate the value of it. By having it be
available to everyone whenever they want, it does decrease the
sacredness of it. People can now opt to turn it for granted because
it is there and always will be. When music wasn’t free, people treasured
the music they did have and when they acquired new, they
traded to treasure and understand the value of their music. This is
because to get it, they had to work for it and really try to obtain it.

Now, it is also available to anyone and for free, making it
not as special. They did not have to work for it and therefore, don’t
have the same protective feeling as they would have if they were paid
for it.

Music offers people a way of escape and a way of expression.
While a few people think music takes away or puts away things to
spend money on, music is a great way source of entertainment
that offers a journey through time and experiences that other things
don’t offer like velocities.

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Improving Your Score on the Optional Writing Test

WRITING TEST

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Sample Essay 4 (Score: 4444)

Score Explanation
This argument engages with multiple perspectives on the issue in the prompt, building its case around the implications of two conflicting views.

Ideas and Analysis (4): This argument recognizes a complexity inherent to the issue and its perspectives: it may be possible that the availability of free music allows us to build a greater appreciation for music and causes music to lose some of its value. The writer makes this argument by analyzing Perspectives One and Three, touching on implications of both (“When music wasn’t free, people treasured the music they did have and when they aquired more, they tended to treasure and understand the value of their music […] Now, it is available to anyone and for no price, making it not as special,” “Since music is now more often free, people from all areas in the economic status can listen and expand their realm of experiences. People are more likely to try out new music styles or artists because it is there and there is nothing stopping them from listening”). Had the writer pursued this apparent contradiction further, the argument would have become more complex, perhaps receiving a higher score. Even so, ideas and analysis in this response exhibit a degree of clarity and sophistication that are absent in the previous responses, earning the essay a score of 4 in this domain.

Development and Support (4): Lines of clear reasoning and illustration clarify meaning and purpose as the writer develops the thesis. The second paragraph, for example, provides clear reasoning to support the idea that free music builds our appreciation for music; similarly, the third paragraph rationalizes the idea that we don’t value music as much as we used to. Although the writer is able to provide support for the argument, anticipating and addressing questions from the reader—How can it be that the value of music is both appreciating and depreciating? Is it possible that we’re talking about more than one type of value?—would have brought these lines of reasoning together and strengthened the argument by considering factors that may complicate it.

Organization (4): The shape of this argument reflects its controlling idea, which is first presented in the introduction. Ideas are grouped and sequenced: within paragraphs, ideas unfold logically, and the two premises of the argument are connected clearly, with a transition to move the reader from the first premise into the second (“However, free music does dilute the value of it”). The sequence of ideas does not conclude logically; the final paragraph seems to summarize a discussion that was never carried out. Perhaps this was an attempt to leave the reader with an interesting idea to consider, but the relevance of this idea (music offers experiences other forms of entertainment cannot match) to the larger argument is entirely unclear.

Language Use (4): Some precise word choices (“dilute,” “sacredness,” “treasure,” “limitation,” “realm of experiences”) underscore the meaning of the argument. However, this precision is counterbalanced by awkward phrasing (“However, recently it has been becoming more available for no price at all”) and many vague and ambiguous pronouns (“By having it be available to everyone whenever they want, it does decrease the sacredness of it”). Although these issues and errors don’t always impede understanding, they negatively affect the overall quality of expression.
Begin WRITING TEST here.

Free music is so universal that people may no longer need to actually purchase music. However, this does not mean that people do not value or appreciate it. In fact, the lowering of the financial barrier to accessing music may have only caused music to become more prevalent in our society, exposing more people to it, and allowing those who create music to receive attention more quickly. The value of music in our society is not decreasing, we still view music as a vital aspect in our lives.

Digital technologies have caused music to become cheaper, because it is now so plentiful; however, a decrease in monetary value of individual songs does not mean that we now view music with less appreciation. Much of today’s music can be viewed or listened to online for free, but this is just a means for artists to more easily allow more people to view their work. By releasing free online editions of their music, many artists have become far more well-known than they would have otherwise. For example, the Korean pop star Psy, who has released several songs barely containing any English, has become an international celebrity through the viewing of his work for free on the internet. This can be seen from the hundreds of millions of views that his music videos on YouTube received; without this free platform to connect the Korean rapper...
to the rest of the world, it is uncertain whether he could have attained fame so quickly. After the release of his videos, the videos went viral, quickly becoming the center of attention for the media for weeks. Pay received and accepted numerous requests to sing and perform in many different places including television shows in Australia where thousands of people flocked to see his performances. Though music may be free, we still greatly appreciate music and it continues to have a profound impact on our lives.

In today's society, there are also many other relatively inexpensive forms of entertainment, aside from music that compete for our attention, such as movies, TV shows, just to name a few. However, the vast majority of these kinds of entertainment also includes music. No movie today is produced without a soundtrack, possibly consisting of the work of multiple artists. Nearly all forms of digital entertainment include music to make the experience more enjoyable, showing that music continues to hold great value in all forms of entertainment, and our society as well.

The ubiquitous and affordable nature of music in today's society has only increased our appreciation of music and allowed the discovery of many new musicians. A personal example would be my discovery of the band 5 Seconds of Summer. Through online and free sources, I discovered their music and enjoyed the upbeat, rythmic, and cheerful mood in many of their songs. If I had to spend money on an expensive album to get access to their music, it is likely that I would never have gotten the satisfaction.

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of listening to their work, and the band would have been deprived of another person who appreciates their music.

Though we may be spending less on music, we still appreciate it and acknowledge that it occupies a vital position in entertainment. Through digital technology, music has been connected with an even larger audience.
Sample Essay 5 (Score: 5555)

Score Explanation

The writer uses an extended example to analyze and evaluate multiple perspectives on the issue, addressing implications and critiquing underlying values.

Ideas and Analysis (5): The argument productively engages with multiple perspectives. For example, the writer uses Perspective Three as a basis for analyzing and evaluating Perspective One. In doing so, the writer addresses Perspective One's assumption that “a decrease in monetary value of individual songs” also means that “we now view music with less appreciation.” This analysis serves to refine and advance a precise thesis: the value of music in our society is not decreasing; instead, by making music more accessible, we are only growing in our appreciation of music, and artists are benefitting as a result. Subsequent analysis is not quite as critical—the second point, that many other kinds of entertainment include music, is of a lower order, and the personal example does not meaningfully contribute to the discussion that precedes it. Even so, this thoughtful argument is worthy of a 5 in the Ideas and Analysis domain.

Development and Support (5): Development and support deepen understanding. Although some of the details in this example are probably unnecessary, the treatment as a whole is channeled toward conveying and bolstering the significance of the idea that free music affords musicians greater exposure, which is an important piece of the thesis. Other ideas are not developed quite so thoroughly, and the argument as a whole would be considerably stronger were it to consider complicating factors, such as objections that might be raised by someone with an opposing viewpoint on the issue. On balance, however, this is a well-developed essay.

Organization (5): Although this response does not achieve the unity and coherence required of a 6, it does exhibit the markers of a productive organizational strategy. The introduction presents the controlling idea, and the argument takes its shape around this idea, with all the writer’s points working to advance and support the larger argument. A logical sequence of ideas contributes to the effectiveness of the argument; the discussion on our appreciation of music (paragraph two) is followed with a discussion on the role of music in other forms of entertainment (paragraph three), and these discussions work together to build and refine the idea that free music is not causing us to lose appreciation for music. Unfortunately, the momentum of the argument is halted by the fourth paragraph, which introduces a personal example that does not differ meaningfully from the discussion carried out in paragraph two.

Language Use (5): Advanced sentence structures convey ideas with precision (“No movie today is produced without a soundtrack, possibly consisting of the work of several artists”), and word choice is precise (“this free platform,” “caused music to be more prevalent in our society, “financial barrier”). Although the response does exhibit some clunky syntax (“After the release of his videos, the videos went viral”) and a few minor usage errors (“the vast majority of these kinds of entertainment also includes music”), meaning is never in doubt.
Musicians create in order to share their experience with others. As listeners, we make emotional connections with music. Songs can lighten our moods, inspire us, and even make us feel less alone. Such an emotional connection is much deeper than a monetary connection to music and that people seek. This connection is how we know that music still has great cultural value. In the modern technological environment, the value of music in our culture only increases.

Today, digital technology is the driving force behind free music. Various online sources offer music to anyone with internet access. There are many people who are unwilling to pay for music since they can get it for free from these sources. This situation has come about through basic economics. A surplus of any commodity will necessarily drive down the price of that commodity, and thanks to digital technology, there is today a surplus of music. But just because people are taking advantage of this surplus doesn't mean that our culture has not maintained its enjoyment of music. If we only consider economics, we might conclude that our preference for free music suggests that we place less value on music than we did in the past.

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a look at the role music plays in our culture suggests that we value it as much as ever.

Think of how often we encounter music in our daily lives. We carry music with us in our pockets wherever we go. Music plays a role in the grocery store, at the coffee shop, at the mall. Advertisements rely on music. Baseball players have “walk-up” songs and people spend outrageous amounts of money on customized stereo systems for their cars. Student use music for school projects, teachers use songs to help kids learn. Then of course there are our more direct experiences with music, like attending a concert or making music ourselves. The prevalence of music has not diminished; in fact it has increased. Even the fact that we take advantage of all the free music available demonstrates how much we value music.

Even though economics have caused the monetary value of music to decline, its cultural value remains strong. People have shared musical experiences with each other for thousands of years, and for much of this time, free music has been readily available. Though its monetary value may shift across time, the cultural value of music is consistent.
Sample Essay 6 (Score: 6666)

Score Explanation

This argument earns the highest scores because of a sustained, critical examination of the implications of the issue and its perspectives.

Ideas and Analysis (6): This argument is driven by a nuanced, precise thesis: shifting economic circumstances may have changed our purchasing habits when it comes to music, but these changes in consumption do not reflect a change in the value our culture places on music. By viewing the issue and its perspectives through the lens of culture and economics, the writer has employed an insightful context for analysis. Within this context, the writer is able to examine the implications of Perspective Two (the discussion on surplus) while critiquing Perspective One’s assumption that this economic phenomenon is also a cultural matter. In doing so, the writer has generated an argument that critically engages with multiple perspectives on the issue.

Development and Support (6): In developing and supporting the argument, the writer keeps the thesis in full focus and thus produces an integrated line of reasoning and illustration. A concise explanation of the concept of surplus deepens the argument’s insights, and the importance of this concept to the larger argument is made clear by way of an important qualification—this is an economic issue, but it is also a cultural matter—that enriches and bolsters the thesis (“If we only consider economics, we might conclude that our preference for free music suggests that we place less value on music than we did in the past; however, a look at the role music plays in our culture suggests that we value it as much as ever”). In supporting the idea that our culture has not devalued music, the writer makes skillful use of a list of examples that, in their accumulation, fortify the claim that “[t]he prevalence of music has not diminished; if anything it has increased.” In these ways, reasoning and illustration are effective in conveying the meaning and importance of this argument.

Organization (6): The precise thesis brings unity and cohesion to this argument. The thesis guides a logical progression of ideas: the piece begins by introducing the main idea before discussing its central premises in turn. An effective conclusion reinforces the thesis and even manages to advance the discussion further by making efficient use of a historical context (“People have shared experiences with each other through song for thousands of years, and for much of this time, free music has been readily available. Though its monetary value may shift across time, the cultural value of music is consistent”). Transitions, both within paragraphs (“Then, of course, there are our more direct experiences with music”) and between them (“however, a look at the role music plays in our culture suggests that we value it as much as ever/Think of how often we encounter music in our daily lives”) form strong connections between ideas and make for smooth movement across the argument’s premises.

Language Use (6): The use of language enhances this argument. Precise word choices communicate the conceptual understanding on which this argument depends (“surplus,” “commodity”) and the fine distinctions on which it rests (“Such an emotional connection is much deeper than a monetary connection”). Stylistic choices are strategic and effective, as the writer shifts from a more formal register when discussing economic considerations (“A surplus of any commodity will necessarily drive down the price of that commodity”) to a more informal register...
when discussing culture (“We carry music with us, in our pockets, wherever we go. Music plays at the grocery store, at the coffee shop, at the mall”). Errors in grammar, usage, and mechanics are virtually nonexistent.

**Strategies for Taking the ACT Writing Test**

Although your writing score reflects the quality of the product (the essay) you write, the writing process you follow can have a major impact on your score. For example, if you do not spend a few minutes prewriting (planning) before you start writing, you could “paint yourself into a corner” by following a line of logic that leads to an illogical conclusion and having no time left to start over.

The following sections present a few writing, prewriting, and postwriting strategies to improve the process you follow when writing your essay. Of course, no writing process can make up for a lack of knowledge and skill, which take years of study and practice to develop. If you need to sharpen your writing skills, we recommend that you take a course in English composition and practice writing and study others’ writing frequently.

**Prewrite**

Some writers like to plunge right in, but this is seldom a good way to do well on a timed essay. Prewriting gets you acquainted with the issue, suggests patterns for presenting your thoughts, and gives you a little breathing room to come up with interesting ideas for introducing and concluding your essay. Before writing, then, carefully consider the prompt and make sure you understand it—reread it if you aren't sure. Decide how you want to answer the question in the prompt. Then jot down your ideas on the topic: this might simply be a list of ideas, reasons, and examples that you will use to explain your point of view on the issue. Write down what you think someone might say in opposition to your point of view and think about how you would refute their argument. Think of how best to organize the ideas in your essay. You should do your prewriting on the pages provided in your writing test booklet. You can refer back to these notes as you write the essay itself on the lined pages in your answer document.

**Write**

When you’re ready to write your essay, proceed with the confidence that you have prepared well and that you will have attentive and receptive readers who are interested in your ideas. At the beginning of your essay, make sure readers will see that you understand the issue. Explain your point of view in a clear and logical way. If possible, discuss the issue in a broader context or evaluate the implications or complications of the issue. Address other perspectives presented in the prompt. Also consider what others might say to refute your point of view and present a counterargument. Use specific examples to explain and illustrate what you’re saying. Vary the structure of your sentences, and choose varied and precise words. Make logical relationships clear by using transitional words and phrases. Don’t wander off the topic. End with a strong conclusion that summarizes or reinforces your position.
Is it advisable to organize the essay by using a formula, such as “the five-paragraph essay”? Points are neither awarded nor deducted for following familiar formulas, so feel free to use one or not as best suits your preference. Some writers find formulas stifling, other writers find them a solid basis on which to build a strong argument, and still other writers just keep them handy to use when needed. The exact numbers of words and paragraphs in your essay are less important than the clarity and development of your ideas. Writers who have something to say usually find that their ideas have a way of sorting themselves out at reasonable length and in an appropriate number of paragraphs.

**Review Your Essay**

Take a few minutes at the end of the testing session to read over your essay. Correct any mistakes in grammar, usage, punctuation, and spelling. If you find any words that are hard to read, recopy them so your readers can read them easily. Make any corrections and revisions neatly, between the lines (but not in the margins). Your readers take into account that you had merely 40 minutes to compose and write your essay. Within that time limit, try to make your essay as polished as you can.

**Practice**

There are many ways to prepare for the ACT writing test. You may be surprised that these include reading newspapers and magazines, listening to news analysis on television or radio, and participating in discussions and debates about issues and problems. These activities help you become more familiar with current issues, with different perspectives on those issues, and with strategies that skilled writers and speakers use to present their points of view and respond to a range of viewpoints.

Of course, one of the best ways to prepare for the ACT writing test is to practice writing. Practice writing different kinds of texts, for different purposes, with different audiences in mind. The writing you do in your English classes will help you. So will practice in writing essays, stories, poems, plays, editorials, reports, letters to the editor, a personal journal, or other kinds of writing that you do on your own. Strive for your writing to be well developed and well organized, using precise, clear, and concise language. Because the ACT writing test asks you to explain your perspective on an issue in a convincing way, writing opportunities such as editorials or letters to the editor of a newspaper are especially helpful. Practicing a variety of different kinds of writing will help make you a versatile writer able to adjust to different writing occasions and assignments.

Share your writing with others and get feedback. Feedback helps you anticipate how readers might interpret your writing and what types of questions they might have. It will also help you identify your strengths and weaknesses as a writer. Also, keep in mind what the ACT readers will be looking for as they score your essay by examining the scoring rubric for the ACT writing test (in chapter 3). Make sure your writing meets the criteria described for the high-scoring essays.

You should also get some practice writing within a time limit. This will help build skills that are important in college and career. Taking the practice ACT writing tests in this book will give you a good idea of what timed writing is like and how much additional practice you may need.
Part Four: Taking Additional Practice Tests

In This Part
This part features two additional practice tests. Here, you take and score the tests and look at your scores from a number of different perspectives, so you can use the results more effectively in your educational and career planning. Specifically, this part gives you the opportunity to do the following:

- Take two additional practice tests
- Score your practice tests to determine your raw score, scaled scores (similar to the scores the ACT reports), and your estimated percentage rank (how well you did compared to other students who took the tests)
- Evaluate your ACT scores from different perspectives to gain insight into what your scores mean in terms of college and career planning
- Find out more about using ACT Profile (a free online service) to obtain additional insight to and guidance for college and career planning
Chapter 10: Taking Additional Practice Tests

In this chapter, you’ll find two additional practice ACT tests, copies of real answer documents for recording your answers, and explanatory answers for the questions on all of the multiple-choice tests.

Each practice test features the contents of the tests in the same order as they will be on the ACT: the English test, the mathematics test, the reading test, the science test, and the optional writing test. Following each complete practice test, you will find the explanatory answers for the multiple-choice questions on that test in the same pattern as the individual tests (English, mathematics, reading, and science).

Two copies of the answer documents that you can tear out and use to record your answers for the multiple-choice tests precede each practice test. (Two copies of these answer documents have been provided in case you make errors or if you would like to retake a practice test. When you take the actual ACT test, however, only one answer document will be provided.) One copy of the writing test answer document, which you can tear out (or photocopy) and use to write your essay, is provided for each practice writing test.
Simulating Testing Conditions

We recommend that you take all practice tests under conditions similar to those you will experience on test day. See chapter 3 for instructions.
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ALL Blocks B, C, and D are required for all examinees. Find the MATCHING INFORMATION on your ticket. Enter it EXACTLY the same way, even if any of the information is missing or incorrect. Fill in the corresponding ovals. If you do not complete these blocks to match your previous information EXACTLY, your scores will be delayed up to 8 weeks.

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THE ONLY Official Prep Guide from the Makers of the ACT

The ACT® Sample Answer Sheet

A NAME, MAILING ADDRESS, AND TELEPHONE
(Please print.)

Last Name

First Name

MI (Middle Initial)

House Number & Street (Apt. No.); or PO Box & No.; or RR & No.

City

State/Province

ZIP/Postal Code

IM-(A)194993-001:654321

DATE OF BIRTH

B MATCHING NAME
(First 5 letters of last name)

C MATCHING NUMBER

D DATE OF BIRTH

Month

Day

Year

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I understand that ACT owns the assessment questions and responses and affirm that I will not share any assessment questions or responses with anyone by any form of communication before, during, or after the assessment administration. I understand that assuming anyone else’s identity to take this assessment is strictly prohibited and may violate the law and subject me to legal penalties.

2. Copy the Certification shown below (only the text in italics) on the lines provided. Write in your normal handwriting.

Certification: I agree to the Statement above and certify that I am the person whose name and address appear on this answer sheet.

Your Signature

Today’s Date

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The ACT® Sample Answer Sheet

A NAME, MAILING ADDRESS, AND TELEPHONE (Please print.)

Last Name  First Name  MI (Middle Initial)

House Number & Street (Apt. No.); or PO Box & No.; or RR & No.

City  State/Province  ZIP/Postal Code

Area Code  Number  Country

ACT, Inc.—Confidential Restricted when data present

ALL examinees must complete block A – please print.

Blocks B, C, and D are required for all examinees. Find the MATCHING INFORMATION on your ticket. Enter it EXACTLY the same way, even if any of the information is missing or incorrect. Fill in the corresponding ovals. If you do not complete these blocks to match your previous information EXACTLY, your scores will be delayed up to 8 weeks.

B MATCHING NUMBER (First 5 letters of last name)

C MATCH NUMBER

D DATE OF BIRTH

Month  Day  Year

EXAMINEE STATEMENT, CERTIFICATION, AND SIGNATURE

1. Read the following Statement: By submitting this answer sheet, I agree to comply with and be bound by the Terms and Conditions: Testing Rules and Policies for the ACT® provided in the ACT registration materials for this assessment, including those concerning test security, score cancellation, examinee remedies, arbitration, and consent to the processing of my personally identifying information, including the collection, use, transfer and disclosure of information as described in the ACT Privacy Policy (www.act.org/privacy.html).

   International Examinees: By my signature I am also providing my consent to ACT to transfer my personally identifying information to the United States to ACT, or a third party service provider for processing, where it will be subject to use and disclosure under the laws of the United States. I acknowledge and agree that it may also be accessible to law enforcement and national security authorities in the United States.

   I understand that ACT owns the assessment questions and responses and affirm that I will not share any assessment questions or responses with anyone by any form of communication before, during, or after the assessment administration. I understand that assuming anyone else’s identify to take this assessment is strictly prohibited and may violate the law and subject me to legal penalties.

2. Copy the Certification shown below (only the text in italics) on the lines provided. Write in your normal handwriting.

Certification: I agree to the Statement above and certify that I am the person whose name and address appear on this answer sheet.

Your Signature  Today’s Date

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### Marking Directions

Mark only one oval for each question. Fill in response completely. Erase errors cleanly without smudging.

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Practice Test 2

EXAMINEE STATEMENT, CERTIFICATION, AND SIGNATURE

1. Read the following Statement: By opening this test booklet, I agree to comply with and be bound by the Terms and Conditions: Testing Rules and Policies for the ACT® provided in the ACT registration materials for this assessment, including those concerning test security, score cancellation, examinee remedies, arbitration, and consent to the processing of my personally identifying information, including the collection, use, transfer and disclosure of information as described in the ACT Privacy Policy (available at www.act.org/privacy.html).

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Certification: I agree to the Statement above and certify that I am the person whose name appears on this form.

3. Sign your name as you would any official document and enter today’s date.

Your Signature: ___________________________ Today’s Date: _________________

Directions

This booklet contains tests in English, mathematics, reading, and science. These tests measure skills and abilities highly related to high school course work and success in college. Calculators may be used on the mathematics test only.

The questions in each test are numbered, and the suggested answers for each question are lettered. On the answer document, the rows of ovals are numbered to match the questions, and the ovals in each row are lettered to correspond to the suggested answers.

For each question, first decide which answer is best. Next, locate on the answer document the row of ovals numbered the same as the question. Then, locate the oval in that row lettered the same as your answer. Finally, fill in the oval completely. Use a soft lead pencil and make your marks heavy and black. Do not use ink or a mechanical pencil.

Mark only one answer to each question. If you change your mind about an answer, erase your first mark thoroughly before marking your new answer. For each question, make certain that you mark in the row of ovals with the same number as the question.

Only responses marked on your answer document will be scored. Your score on each test will be based only on the number of questions you answer correctly during the time allowed for that test. You will not be penalized for guessing. It is to your advantage to answer every question even if you must guess.

You may work on each test only when the testing staff tells you to do so. If you finish a test before time is called for that test, you should use the time remaining to reconsider questions you are uncertain about in that test. You may not look back to a test on which time has already been called, and you may not go ahead to another test. To do so will disqualify you from the examination.

Lay your pencil down immediately when time is called at the end of each test. You may not for any reason fill in or alter ovals for a test after time is called for that test. To do so will disqualify you from the examination.

Do not fold or tear the pages of your test booklet.

DO NOT OPEN THIS BOOKLET UNTIL TOLD TO DO SO.
PASSAGE I

The Kam Wah Chung & Co. Museum

To the casual observer, the Kam Wah Chung & Co. building, located in the eastern Oregon community of John Day, that is, simply a small, unassuming structure made of rock and wood. To those with an interest in history, however, it’s a unique building that preserves a part of the legacy of the Chinese community in the nineteenth-century American West.

Built in the 1860s, the Kam Wah Chung building first served as a trading post for travelers who attract to the land east of the Cascade Mountains by news of gold strikes there.

1. A. NO CHANGE
   B. is
   C. it’s
   D. DELETE the underlined portion.

2. Given that all the choices are true, which one most effectively introduces the historical and cultural significance of the Kam Wah Chung & Co. building?
   F. NO CHANGE
   G. has seven rooms: a front room, an herb shop, two bedrooms, a stockroom, a general store, and a kitchen and bunk room.
   H. is cooperatively preserved and operated by the Oregon Parks and Recreation Department and the City of John Day.
   J. has a kitchen that holds antique tables, a large woodstove, and a variety of Chinese teas and cooking utensils.

3. A. NO CHANGE
   B. will be attracted
   C. were attracted
   D. are attracted

GO ON TO THE NEXT PAGE.
In 1887, the original owner sold the building. The men combined their skills, organized a group of investors, and remains in business together for more than fifty years. Educated in the Chinese classics and fluent in English, Lung On was a skilled merchant who built a successful textile and import business. He also sold food and supplies to local miners. His partner, Doc Hay, established an herbal medicine clinic. Hay became famous throughout central and eastern Oregon when he would make perceptive diagnoses and curing patients whose previous treatments had failed. Over time, the partners’ building evolved into a social, medical, and supply center, as well as a post office, library, and herb shop.

4. At this point, the writer is considering adding the following accurate information:

   to two enterprising young Chinese immigrants, Ing “Doc” Hay and Lung On

   Should the writer make this addition here?
   F. Yes, because it builds upon a claim made about Hay and On in the preceding sentence.
   G. Yes, because it provides a logical link to the information that follows in the essay.
   H. No, because it unnecessarily states information that’s implied later in the essay.
   J. No, because it provides little information about Hay and On’s partnership.

5. A. NO CHANGE
   B. has remained
   C. have remain
   D. remained

6. F. NO CHANGE
   G. for making
   H. as he made
   J. and made

7. A. NO CHANGE
   B. who experienced that their previous treatments
   C. being previous treatments which
   D. of whom previous treatments

8. The writer is considering deleting the preceding sentence. Should the sentence be kept or deleted?
   F. Kept, because it provides information that suggests why Hay’s work was particularly noteworthy.
   G. Kept, because it presents examples of Hay’s most challenging and successful diagnoses.
   H. Deleted, because it doesn’t make clear whether On was involved with Hay’s herbal medicine clinic.
   J. Deleted, because it doesn’t fit logically in this paragraph about On’s accomplishments.

9. If the writer were to delete the preceding sentence, the paragraph would primarily lose a statement that:
   A. demonstrates the scope of services eventually provided in the Kam Wah Chung & Co. building.
   B. makes clear that the social aspect of Kam Wah Chung & Co. was most important to visitors.
   C. provides a summary of one regular visitor’s experiences at Kam Wah Chung & Co.
   D. indicates for how long Hay and On’s businesses prospered.
[1] Hay and On’s businesses prospered through the turn of the century, during the Great Depression, and beginning the 1940s. [2] Because the climate in eastern Oregon is semi-arid, the artifacts left inside—including gold-mining tools, rare antique furniture, financial documents, and a thousand different herbs—were preserved. [3] Although On died in 1940, Hay continued to run Kam Wah Chung & Co. until 1948. [4] After Hay’s death, his nephew inherited the building and donated it to the city of John Day. [5] For almost twenty years, it remained locked. [6] The building was restored by the state of Oregon in the 1970s and has become the Kam Wah Chung & Co. Museum. [7] Designated as being called a National Historic Landmark in 2005, besides, it encapsulates an era.

10. F. NO CHANGE
G. as it entered
H. becoming
J. into

11. A. NO CHANGE
B. have become
C. became
D. become

12. F. NO CHANGE
G. with the appropriation of
H. in being identified as a
J. a

13. A. NO CHANGE
B. in conclusion,
C. in time,
D. DELETE the underlined portion.

14. For the sake of the logic and coherence of this paragraph, Sentence 2 should be placed:
F. where it is now.
G. before Sentence 1.
H. after Sentence 3.
J. after Sentence 5.

15. Suppose the writer’s goal had been to write a brief essay that outlined the steps the state of Oregon took to restore the Kam Wah Chung & Co. building. Would this essay accomplish that goal?
A. Yes, because it makes clear that the Kam Wah Chung & Co. building was renovated in the 1970s.
B. Yes, because it explains why the artifacts that were inside the Kam Wah Chung & Co. building were preserved.
C. No, because it instead focuses on describing the history of the Kam Wah Chung & Co. building and the building’s uses.
D. No, because it instead focuses on critiquing both On’s business philosophies and Hay’s medical diagnoses and treatments.

GO ON TO THE NEXT PAGE.
PASSAGE II

One Fair Season

At first glance a Renaissance fair, looks a lot like a theme park. Crowds of people mill about, moseying they’re way past costumed characters and colorful booths. Being that roller coasters and Ferris wheels, the fair’s attractions are the sights, sounds, and tastes inspired by sixteenth-century England. Musicians, magicians, and archers demonstrate their talents to curious fairgoers. Horses carrying knights to a jousting match walk along the streets.

Vendors, ranging from king-sized turkey legs to suits of armor, peddle wares.

I’ve always enjoyed attending Renaissance fairs, and I found out just how interesting they are. Those of us working at the fair spent weeks perfecting our characters’ accents and mannerisms. We also incorporated sixteenth-century English vocabulary into our speech. Substituting good morrow for “good morning” and gramercy for “thank you.” In my role

16. F. NO CHANGE
   G. glance, a Renaissance fair,
   H. glance, a Renaissance fair
   J. glance a Renaissance fair;

17. A. NO CHANGE
   B. they’re way passed
   C. their way passed
   D. their way past

18. F. NO CHANGE
   G. Yet instead of
   H. Because of
   J. Given that

19. A. NO CHANGE
   B. Horses, carrying knights,
   C. Horses carrying knights,
   D. Horses, carrying knights

20. Which choice best conveys the horses’ movement in a way that adds a sensory detail to the description of the fair?
   F. NO CHANGE
   G. clip-clop
   H. move
   J. travel

21. A. NO CHANGE
   B. Peddling wares, ranging from king-sized turkey legs to suits of armor are vendors.
   C. Ranging from king-sized turkey legs to suits of armor, vendors peddle wares.
   D. Vendors peddle wares ranging from king-sized turkey legs to suits of armor.

22. Which choice best introduces the subject of the paragraph and the rest of the essay?
   F. NO CHANGE
   G. but it wasn’t until I spent a summer working at one that I understood how much effort went into re-creating the past.
   H. and I knew that getting a job at one would be the easiest way to experience one and have fun at the same time.
   J. so one summer’s day, some friends and I decided to attend a nearby fair.

23. A. NO CHANGE
   B. speech, we substituted
   C. speech, substituting
   D. speech; substituting
as a lady-in-waiting, I often used the sixteenth-century expressions while I served the queen’s meals or introduced her to guests.

It was exhausting to spend every day in the hot summer temperatures while pretending to be a person whom had lived in a different country and century. The physical demands were especially strenuous for the queen and us ladies-in-waiting because our costumes, they consisted of confining corsets, several scratchy petticoats, and heavy velvet gowns.

We strove to make the fairgoers’ experience as authentic as possible. Things that had come into existence more recently after the sixteenth century had to be explained in Renaissance terms. However, when a guest wished to take a photograph, we would marvel at the camera and ask how such lifelike paintings were created inside the tiny box.

After three tiring months of rehearsals and performances, the fair closed for the season, and I bade fare thee well to my Renaissance character when the summer months were over. Although it had been a wonderful trip back in time, it was a relief to return to the comforts of my own century.

We strove to make the fairgoers’ experience as authentic as possible. Things that had come into existence more recently after the sixteenth century had to be explained in Renaissance terms. However, when a guest wished to take a photograph, we would marvel at the camera and ask how such lifelike paintings were created inside the tiny box.

After three tiring months of rehearsals and performances, the fair closed for the season, and I bade fare thee well to my Renaissance character when the summer months were over. Although it had been a wonderful trip back in time, it was a relief to return to the comforts of my own century.
PASSAGE III

Uncovered at Johnson’s Shut-Ins

In Reynolds County, Missouri, a one-billion-gallon blast of water caused by a breach of the Taum Sauk reservoir roared down Proffit Mountain into the east fork of the Black River on December 14, 2005. They ripped a channel through Johnson’s Shut-Ins, one of Missouri’s most popular state parks. Though flood damage marred the park’s beauty for a time, the scar the raging water left in its wake specifically revealed over a billion years’ worth of Earth’s geologic history.

The area known today as Johnson’s Shut-Ins State Park had begun to develop 1.5 billion years ago. When the volcanoes that created the St. Francois Mountains exploded. Slow-moving magma cooled down its temperature and crystallized to form silica-rich rhyolite rock. Over time sedimentary rock such as limestone and shale, formed from material deposited by shallow inland seas, buried the rhyolite. After the seas had receded, gravel-rich rivers and streams eventually chipped away the soft sedimentary rock in some areas.

31. A. NO CHANGE
   B. water caused by,
   C. water caused, by
   D. water, caused by

32. F. NO CHANGE
   G. That they
   H. Which
   J. It

33. A. NO CHANGE
   B. park’s beauty for a time,
   C. parks’ beauty for a time,
   D. park’s beauty for a time

34. F. NO CHANGE
   G. ultimately
   H. instead
   J. thus

35. A. NO CHANGE
   B. begun developing
   C. began to develop
   D. begun to develop

36. F. NO CHANGE
   G. ago; when
   H. ago when
   J. ago

37. A. NO CHANGE
   B. cooled down to a lower temperature
   C. lowered its temperature to cool
   D. cooled

38. F. NO CHANGE
   G. form silica-rich, rhyolite,
   H. form silica-rich rhyolite,
   J. form, silica-rich rhyolite
exposing the erosion-resistant rhyolite rock and creating pockets and pits. In low places, the Black River was confined (or “shut in”) by the rhyolite and creating the natural waterslides and canyon-like gorges that have become a summer playground for thousands of visitors.

Although the flood left the shut-ins unscathed, the surge of water that tore through the park in 2005 stripped away all trees, soil, and sedimentary rock in its path. Left behind is a channel that is composed of granite—and previously unexposed rhyolite rock—and contain rocks from at least three other geological eras. The menacing floodwaters also revealed a half-billion-year-old beach made of both sand and gravel.

Five years of work has restored most of the park surrounding the shut-ins. Some have returned back. Geologists from around the world visit to get a close look at the ancient volcanic rock along what has been named the “Scour Channel.” The “Scour Channel” now rivals the park’s other geologic curiosities for most frequently visited site.
PASSAGE IV

A Birthplace of Stars

The winter night I attempted to see the famed Orion Nebula, I didn’t expect to succeed. I was an inexperienced astronomer peering through light-polluted skies. But I was eager to test my new telescope’s capabilities, and the nebula being one of the greatest sights in the night sky. So I bundled up, set out my scope to cool down (its mirrors must adjust to the cold air for optimal viewing), and scanned for the constellation Orion.

I had prepared for this night by studying constellations in my astronomy books. Orion appears as a hunter who, in some mythologies, is fighting Taurus the Bull, another constellation. [A] Even in bright skies, the telltale three stars marking Orion’s belt has been easy to spot. [B] I knew to follow the belt to Orion’s sword, a dim line of stars extending south. [C] The middle of these is actually not a star but a nebula, the Great Orion Nebula, a birthplace of stars. [D] When gravity causes the gas and dust to collapse, forming stars.

The nebula, is home to thousands of young stars, is often called a galactic “nursery.”

45. A. NO CHANGE
B. astronomer, peering through,
C. astronomer: peering through
D. astronomer peering through,

46. F. NO CHANGE
G. is by them said to be
H. is said to be
J. having been

47. A. NO CHANGE
B. hunter, who in some mythologies,
C. hunter who, in some mythologies
D. hunter who in, some mythologies,

48. F. NO CHANGE
G. were being
H. are
J. is

49. A. NO CHANGE
B. collapse to form stars.
C. collapse, stars form.
D. collapse and form stars.

50. F. NO CHANGE
G. nebula is home to thousands of young stars, and
H. nebula, home to thousands of young stars, and
J. nebula, home to thousands of young stars,

51. The writer wants to add the following sentence to the preceding paragraph:
   Located 1,300 light-years from Earth, the nebula is a massive cloud of gas and dust.
   This sentence would most logically be placed at:
A. Point A.
B. Point B.
C. Point C.
D. Point D.

GO ON TO THE NEXT PAGE.
I centered my scope where the nebula should be, inserted my lowest-powered eyepiece, and leaned in to look. I just made out a dull smudge. I couldn’t get much improvement even when I adjusted the focuser.

Coincidentally, I switched to a higher-powered eyepiece and tried a trick I’d read about for viewing faint objects: using averted vision.

The principle of averted vision states that the eye can often see distant objects better by looking to their one side rather than directly at them. I focused my eye on an area beside the smudge, and, sure enough, my peripheral vision yielded far more of a better view of the nebula’s swirling clouds. I even saw the Trapezium star cluster, illuminated by four bright young stars nestled in the nebula like birds’ eggs.
Taking Additional Practice Tests

59. Given that all the following statements are true, which one, if added here, would best conclude the paragraph and the essay by referring back to the opening paragraph?

A. Observing these features made my winter trek outdoors worthwhile, teaching me that a change in focus is sometimes helpful to see more clearly.
B. In addition to averted vision, it is also important to eliminate stray light and use the correct magnification when observing the night sky.
C. Although my initial goal was to observe Orion’s belt and sword, the constellation is also very useful as an aid to locating other constellations such as Taurus and Gemini.
D. The Trapezium star cluster was originally discovered in 1617 by Galileo, whom I’d read about extensively in my astronomy books.

60. Suppose the writer’s goal had been to write an essay about a personal experience with astronomy. Would this essay accomplish that goal?

F. Yes, because the narrator recounts several past adventures and challenges of using the telescope to view the night sky.
G. Yes, because the narrator describes a stargazing session from start to finish, from setting up the telescope to observing an actual constellation.
H. No, because it primarily focuses on the Orion Nebula and its process of star formation.
J. No, because it describes a universally used technique for viewing distant objects in the night sky.

PASSAGE V

Chords of Color

Some viewers see the paintings of abstract artist James Little as impersonal, discordant rainbows. Others see them as minimalistic distillations of emotion, in other words, they are metaphors for Little’s feelings about social issues and historical events. He paints large-scale patterns of shapes—mostly triangles and narrow rectangles in vibrant contrasting hues.

61. A. NO CHANGE
B. emotion, they see the paintings as
C. emotion the works offer
D. emotion,

62. Which choice is correctly punctuated and makes clear that all the shapes that Little paints are painted in vibrant and contrasting hues?

F. NO CHANGE
G. shapes—mostly triangles and narrow rectangles— in vibrant,
H. shapes—mostly triangles—and narrow rectangles in vibrant,
J. shapes, mostly triangles and narrow rectangles in vibrant

GO ON TO THE NEXT PAGE.
His paintings explore the ambiguity of space, the energy of movement, and the coming together of unlikely elements. But his subject he says is color.

In 2011, working out of his studio in Brooklyn, New York, Little is painting on canvas using his own blends of beeswax and oil paint. He applies at least fifteen layers of these paints that he blended himself to achieve a thick, smooth, color-soaked, luminescent surface. Most of his paintings are voluminous, about six feet by eight feet. To create sharp visual breaks and clean edges of color in these expansive works, he paints slashing diagonal lines and rays.

In his 2005 painting *Bittersweet Victory*, by all means, the canvas is bisected by a vertical, beige line. On the left half, three orange triangles in a row, each one which stretched from the bottom to the top of the canvas’s left half, angle slightly to the right on a purple
Taking Additional Practice Tests

1. background. On the right half, three vertical bands of dark green, one edge of each band slanting to create a point that touches the top of the canvas, cuts through a lime-green background. Little explains that the internal spaces in his paintings (created by lines and blocks of color) need to play off of each other in a way that lends rhythm and unity to the whole work. The effect is much like something that would remind you of a perfect jazz collaboration.

One of Little’s favorite assessments of his work came from a woman who told him that his paintings are optimistic. Little believes the bold, positive energy infusing his work comes from what he observes around him. His paintings reflect what he considers the essence of our experiences as human beings. The malleable nature of space, the surprising shifts, but, in the end, a balance.

71. A. NO CHANGE  
    B. cuts crossed  
    C. cut through  
    D. cut crossed

72. F. NO CHANGE  
    G. on the entirety of the  
    H. into the whole  
    J. with the entire

73. A. NO CHANGE  
    B. reminiscent of something that echoes  
    C. much like that of  
    D. being like

74. If the writer were to delete the preceding sentence, the paragraph would primarily lose a description of Little’s work that:  
    F. builds on the subtle musical reference in the paragraph to create a comparison between Little’s paintings and jazz.  
    G. indicates the popularity of Little’s paintings by drawing a comparison between his work and jazz collaborations.  
    H. provides a transition to the following paragraph’s focus on several assessments of Little’s work by art critics.  
    J. emphasizes the idea that Little’s methods allowed him to reach the goals he uniquely set for his piece **Bittersweet Victory**.

Question 75 asks about the preceding passage as a whole.

75. Suppose the writer’s primary purpose had been to describe how an artist uses simple elements to convey large ideas. Would this essay accomplish that purpose?  
    A. Yes, because it focuses primarily on one viewer’s conclusion that the lines of color in Little’s **Bittersweet Victory** communicate the idea of optimism.  
    B. Yes, because it conveys that Little uses shapes and color to capture what he sees as the movement and rhythm of the human experience.  
    C. No, because it focuses too heavily on describing the metaphor that Little hoped to create with **Bittersweet Victory** but does not explain what that painting looked like.  
    D. No, because it indicates that Little focuses on color in his work but does not suggest the effect that his work achieves.

END OF TEST 1

STOP! DO NOT TURN THE PAGE UNTIL TOLD TO DO SO.
1. A restaurant occupying the top floor of a skyscraper rotates as diners enjoy the view. Ling and Sarah notice that they began their meal at 7:00 p.m. looking due north. At 7:45 p.m. they had rotated 180° to a view that was due south. At this rate, how many degrees will the restaurant rotate in 1 hour?
   A. 90°
   B. 180°
   C. 240°
   D. 270°
   E. 400°

2. The cost of a gym membership is a onetime fee of $140, plus a monthly fee of $40. Brendan wrote a $500 check to pay his gym membership for a certain number of months, including the onetime fee. How many months of membership did he pay for?
   F. 3
   G. 4
   H. 9
   J. 12
   K. 13

3. A museum offers a 2-hour guided group tour. For groups with fewer than 25 people the cost is $9.25 per person; for groups with 25 people or more the cost is $8.50 per person. The 27 people in the 9:00 a.m. tour group each paid $9.25 in advance. What is the total refund that the museum owes the 9:00 a.m. group?
   A. $12.50
   B. $13.00
   C. $18.75
   D. $20.25
   E. $25.00
Taking Additional Practice Tests

4. The 13-member math club needs to choose a student government representative. They decide that the representative, who will be chosen at random, CANNOT be any of the 3 officers of the club. What is the probability that Samara, who is a member of the club but NOT an officer, will be chosen?

F. 0  
G. \( \frac{1}{13} \)  
H. \( \frac{1}{10} \)  
J. \( \frac{3}{13} \)  
K. \( \frac{1}{3} \)

5. Mele earned scores of 75, 70, 92, 95, and 97 points (a total of 429 points) on the first 5 tests in Economics II. Solving which of the following equations for \( s \) gives the score he needs to earn on the 6th test to average exactly 85 points for all 6 tests?

A. \( \frac{429}{5} + s = 85 \)  
B. \( \frac{429}{6} + s = 85 \)  
C. \( \frac{s + 429}{5} = 85 \)  
D. \( \frac{s + 429}{6} = 85 \)  
E. \( \frac{s + 429}{6} = \frac{85}{100} \)

6. The figure below shows quadrilateral \( ABCD \). What is the measure of \( \angle C \)?

F. 120°  
G. 115°  
H. 105°  
J. 100°  
K. 80°

7. In the figure below, \( \triangle ABC \) and \( \triangle DEF \) are similar triangles with the given side lengths in meters. What is the perimeter, in meters, of \( \triangle DEF \)?

A. 3  
B. 8  
C. 11  
D. 12  
E. 13

DO YOUR FIGURING HERE.
8. \( |3(-2) + 4| = ? \)
   - F. \(-2\)
   - G. \(2\)
   - H. \(5\)
   - J. \(9\)
   - K. \(10\)

9. What are the values for \(x\) that satisfy the equation \((x + a)(x + b) = 0\) ?
   - A. \(-a\) and \(-b\)
   - B. \(-a\) and \(b\)
   - C. \(-ab\)
   - D. \(a\) and \(-b\)
   - E. \(a\) and \(b\)

10. In the figure below, \(G\) is the center of the circle, \(LK\) is a diameter, \(H\) lies on the circle, \(J\) lies outside the circle on \(LK\), and \(JM\) is tangent to the circle at \(M\). Which of the following angles or minor arcs has the greatest degree measure?

   - F. \(\overline{LM}\)
   - G. \(\overline{MK}\)
   - H. \(\angle JMG\)
   - J. \(\angle LHK\)
   - K. \(\angle MJL\)

11. Points \(B\) and \(C\) lie on \(\overline{AD}\) as shown below. The length of \(\overline{AD}\) is 30 units; \(\overline{AC}\) is 16 units long; and \(\overline{BD}\) is 20 units long. How many units long, if it can be determined, is \(\overline{BC}\) ?

   - A. 4
   - B. 6
   - C. 10
   - D. 14
   - E. Cannot be determined from the given information

12. If \(12x = -8(10 - x)\), then \(x = ?\)
   - F. 20
   - G. 8
   - H. \(\frac{73}{11}\)
   - J. \(\frac{62}{13}\)
   - K. \(-20\)
Ken baked, frosted, and decorated a rectangular cake for the last Math Club meeting. The cake was 3 inches high, 12 inches wide, and 16 inches long. He centered the cake on a piece of cardboard whose rectangular top surface had been covered with aluminum foil, as shown in the figure below.

13. Ken used a piece of cardboard large enough to allow the cardboard to extend 2 inches beyond the cake on all sides. What is the area, in square inches, of the aluminum foil that is exposed on the top surface of the cardboard?
   A. 60
   B. 64
   C. 88
   D. 96
   E. 128

14. At the Math Club meeting, Principal Gonzales cut the entire cake into pieces. Each piece is 2 inches wide, 2 inches long, and 3 inches high. What is the number of pieces Principal Gonzales cut the cake into?
   F. 16
   G. 20
   H. 28
   J. 48
   K. 96

15. The Math Club will pay Ken $5.00 for preparing the cake and will also pay him for the cost of the cake mix at $1.73, the frosting mix at $2.67, and the sales tax of 5% on these 2 items. What is the total amount the Math Club will pay Ken?
   A. $4.67
   B. $9.40
   C. $9.45
   D. $9.62
   E. $9.87

GO ON TO THE NEXT PAGE.
16. What is the \( y \)-intercept of the line in the standard \((x,y)\) coordinate plane that goes through the points \((-3,6)\) and \((3,2)\) ?

- F. 0
- G. 2
- H. 4
- J. 6
- K. 8

17. A machine part is diagrammed in the figure below with the dimensions given in inches. If the centers of the circles lie on the same line parallel to the bottom of the part, what is the distance, in inches, between the centers of the 2 holes in the machine part?

- A. \( \frac{5}{16} \)
- B. \( \frac{5}{16} \)
- C. 5
- D. \( \frac{13}{16} \)
- E. \( \frac{3}{16} \)

18. The depth of a pond is 180 cm and is being reduced by 1 cm per week. The depth of a second pond is 160 cm and is being reduced by \( \frac{1}{2} \) cm per week. If the depths of both ponds continue to be reduced at these constant rates, in about how many weeks will the ponds have the same depth?

- F. 10
- G. 20
- H. 40
- J. 80
- K. 140
19. When graphed in the standard \((x,y)\) coordinate plane, which of the following equations does NOT represent a line?

A. \(x = 4\)
B. \(3y = 6\)
C. \(x - y = 1\)
D. \(y = \frac{3}{4}x - 2\)
E. \(x^2 + y = 5\)

20. In the right triangle shown below, which of the following statements is true about \(\angle A\)?

F. \(\cos A = \frac{12}{13}\)
G. \(\sin A = \frac{12}{13}\)
H. \(\tan A = \frac{12}{13}\)
J. \(\cos A = \frac{13}{12}\)
K. \(\sin A = \frac{13}{12}\)

21. A park has the shape and dimensions in blocks given below. A water fountain is located halfway between point \(B\) and point \(D\). Which of the following is the location of the water fountain from point \(A\)?

(Note: The park’s borders run east-west or north-south.)

A. \(3\frac{1}{2}\) blocks east and 6 blocks north
B. 5 blocks east and \(4\frac{1}{2}\) blocks north
C. 5 blocks east and 6 blocks north
D. \(8\frac{1}{2}\) blocks east and \(4\frac{1}{2}\) blocks north
E. 9 blocks east and \(7\frac{1}{2}\) blocks north
22. The braking distance, $y$ feet, for Damon’s car to come to a complete stop is modeled by $y = \frac{3(x^2 + 10x)}{40}$, where $x$ is the speed of the car in miles per hour. According to this model, which of the following is the maximum speed, in miles per hour, Damon can be driving so that the braking distance is less than or equal to 150 feet?

F. 10  
G. 30  
H. 40  
J. 50  
K. 60

23. If $f(x) = x^2 + x + 5$ and $g(x) = \sqrt{x}$, then what is the value of $\frac{g(4)}{f(1)}$?

A. $\frac{2}{7}$  
B. $\frac{25}{7}$  
C. $\frac{2}{25}$  
D. 2  
E. 4

24. At a school picnic, 1 junior and 1 senior will be selected to lead the activities. If there are 125 juniors and 100 seniors at the picnic, how many different 2-person combinations of 1 junior and 1 senior are possible?

F. 25  
G. 100  
H. 125  
J. 225  
K. 12,500

GO ON TO THE NEXT PAGE.
25. The scatterplot in the standard \((x, y)\) coordinate plane below contains data points showing a strong linear correlation between the variables \(x\) and \(y\). Mia drew the line shown to model the data. One of the following equations represents Mia’s line. Which one?

\[
\begin{align*}
A. & \quad y = -3x + 8 \\
B. & \quad y = -3x + 10 \\
C. & \quad y = -2x + 10 \\
D. & \quad y = 2x + 10 \\
E. & \quad y = 2x + 8
\end{align*}
\]

26. The temperature, \(t\), in degrees Fahrenheit, in a certain town on a certain spring day satisfies the inequality \(|t - 24| \leq 30\). Which of the following temperatures, in degrees Fahrenheit, is NOT in this range?

F. \(-10\)  
G. \(-6\)  
H. \(-5\)  
J. \(0\)  
K. \(54\)

27. If 5 times a number \(n\) is subtracted from 15, the result is negative. Which of the following gives the possible value(s) for \(n\)?

A. \(0\) only  
B. \(3\) only  
C. \(10\) only  
D. All \(n > 3\)  
E. All \(n < 3\)

28. For all \(x > 21\), \[
\frac{(x^2 + 8x + 7)(x - 3)}{(x^2 + 4x - 21)(x + 1)} = ?
\]

F. \(1\)  
G. \(\frac{9}{7}\)  
H. \(\frac{x - 3}{x + 3}\)  
J. \(\frac{2(x - 3)}{x + 1}\)  
K. \(\frac{4(x - 3)}{x + 1}\)
29. The median of a set of data containing 9 items was found. Four data items were added to the set. Two of these items were greater than the original median, and the other 2 items were less than the original median. Which of the following statements must be true about the median of the new data set?

A. It is the average of the 2 new lower values.
B. It is the same as the original median.
C. It is the average of the 2 new higher values.
D. It is greater than the original median.
E. It is less than the original median.

30. The figure below shows 2 tangent circles such that the 10-centimeter diameter of the smaller circle is equal to the radius of the larger circle. What is the area, in square centimeters, of the shaded region?

F. 10
G. 75
H. $5\pi$
J. $10\pi$
K. $75\pi$

31. The sign of $a$ is positive. The sign of $b$ is negative. If it can be determined, what is the sign of the mean of $a$ and $b$?

A. Positive
B. Negative
C. Both positive and negative
D. Neither positive nor negative
E. Cannot be determined from the given information

Use the following information to answer questions 32–34.

The curve $y = 0.005x^2 - 2x + 200$ for $0 \leq x \leq 200$ and the line segment from $F(0,200)$ to $G(200,0)$ are shown in the standard $(x,y)$ coordinate plane below.
32. What is the y-coordinate for the point on the curve with x-coordinate 20?
   F. 160  
   G. 162  
   H. 164  
   J. 166  
   K. 168

33. The length of this curve is longer than FG. About how many coordinate units long is FG?
   A. 20  
   B. 141  
   C. 200  
   D. 283  
   E. 400

34. Tran wants to approximate the area underneath the curve \( y = 0.005x^2 - 2x + 200 \) for \( 0 \leq x \leq 200 \), shown shaded in the graph below.

   He finds an initial estimate, \( A \), for the shaded area by using FG and computing
   \[ A = \frac{1}{2} (200 \text{ units})(200 \text{ units}) = 20,000 \text{ square units}. \]

   The area of the shaded region is:
   F. less than 20,000 square units, because the curve lies under FG.
   G. less than 20,000 square units, because the curve lies over FG.
   H. equal to 20,000 square units.
   J. greater than 20,000 square units, because the curve lies under FG.
   K. greater than 20,000 square units, because the curve lies over FG.
35. A cargo ship is 4.2 miles from a lighthouse, and a fishing boat is 5.0 miles from the lighthouse, as shown below. The angle between the straight lines from the lighthouse to the 2 vessels is 5°. The approximate distance, in miles, from the cargo ship to the fishing boat is given by which of the following expressions?

(Note: The law of cosines states that for any triangle with vertices \( A, B, \) and \( C \) and the sides opposite those vertices with lengths \( a, b, \) and \( c, \) respectively, \( c^2 = a^2 + b^2 - 2ab \cos C.\))

A. \( \sqrt{(5.0)^2 - (4.2)^2} \)
B. \( \sqrt{(4.2)^2 + (5.0)^2 - 2 \cdot 4.2 \cdot 5.0 \cos 5^\circ} \)
C. \( \sqrt{(4.2)^2 + (5.0)^2 + 2 \cdot 4.2 \cdot 5.0 \cos 5^\circ} \)
D. \( \sqrt{(4.2)^2 + (5.0)^2 - 2 \cdot 4.2 \cdot 5.0 \cos 85^\circ} \)
E. \( \sqrt{(4.2)^2 + (5.0)^2 + 2 \cdot 4.2 \cdot 5.0 \cos 85^\circ} \)

36. Which of the following equations expresses \( c \) in terms of \( a \) for all real numbers \( a, b, \) and \( c \) such that \( a^3 = b \) and \( b^3 = c \)?

F. \( c = a^6 \)
G. \( c = a^5 \)
H. \( c = 2a^3 \)
J. \( c = \frac{1}{2}a \)
K. \( c = a \)

37. After visiting Florida State University during spring break, Francisco rents a car for 2 days to travel around Florida. He has $255 to spend on car rental for the 2 days. Sea Horse Car Rental charges $50 per day and $0.25 per mile. Ocean Blue Car Rental charges $60 per day and $0.20 per mile. Which company, if either, allows him to travel more miles for the 2 days, and how many miles more?

(Note: Taxes are already included in the rental charges.)

A. Sea Horse, 20
B. Ocean Blue, 55
C. Ocean Blue, 100
D. Sea Horse, 135
E. Francisco would get the same maximum number of miles from each company.
38. In the standard \((x, y)\) coordinate plane below, the points \((0,0), (10,0), (13,6),\) and \((3,6)\) are the vertices of a parallelogram. What is the area, in square coordinate units, of the parallelogram?

- F. 30
- G. 60
- H. \(30\sqrt{3}\)
- J. \(30\sqrt{5}\)
- K. \(60\sqrt{5}\)

39. For every pair of natural numbers \(n\) and \(m\), to which of the following sets must \(n + m\) belong?

- I. The natural numbers
- II. The integers
- III. The rational numbers
- IV. The real numbers
- V. The complex numbers

A. I, II, and III only
B. II, III, and IV only
C. III, IV, and V only
D. II, III, IV, and V only
E. I, II, III, IV, and V

40. A certain perfect square has exactly 4 digits (that is, it is an integer between 1,000 and 9,999). The positive square root of the perfect square must have how many digits?

- F. 1
- G. 2
- H. 3
- J. 4
- K. Cannot be determined from the given information

41. A certain hotel has 80 rooms. Based on many previous years' occupancy rates, the owners of the hotel constructed the table below showing the daily occupancy rates and their probabilities of occurring for the coming summer season. Based on the probability distribution in the table, to the nearest whole number, what is the expected number of rooms that will be occupied on any day during the coming summer season?

<table>
<thead>
<tr>
<th>Occupancy rate</th>
<th>Probability</th>
</tr>
</thead>
<tbody>
<tr>
<td>0.60</td>
<td>0.20</td>
</tr>
<tr>
<td>0.70</td>
<td>0.40</td>
</tr>
<tr>
<td>0.80</td>
<td>0.30</td>
</tr>
<tr>
<td>0.90</td>
<td>0.10</td>
</tr>
</tbody>
</table>

A. 20
B. 25
C. 58
D. 60
E. 75

GO ON TO THE NEXT PAGE.
42. What is the matrix product \[ \begin{bmatrix} a & 0 & -a \\ 2a & 0 & -2a \\ 3a & 0 & -3a \end{bmatrix} \] ?

F. \[ \begin{bmatrix} a & 0 & -a \\ 2a & 0 & -2a \\ 3a & 0 & -3a \end{bmatrix} \]

G. \[ \begin{bmatrix} a & 2a & 3a \\ 0 & 0 & 0 \\ -a & -2a & -3a \end{bmatrix} \]

H. \[ [2a 0 -2a] \]

J. \[ [6a 0 -6a] \]

K. \[ 0 \]

43. What is the degree measure of the smaller of the 2 angles formed by the line and the ray shown in the figure below?

![Diagram of angles](image.png)

A. 14°
B. 28°
C. 29°
D. 58°
E. Cannot be determined from the given information

44. Let \( a \) equal \( 2b + 3c - 5 \). What happens to the value of \( a \) if the value of \( b \) decreases by 1 and the value of \( c \) increases by 2?

F. It increases by 4.
G. It increases by 2.
H. It increases by 1.
J. It is unchanged.
K. It decreases by 2.

45. Shima will mix 1 fluid ounce of fertilizer in water for every 40 square feet of soil. At this rate, which of the following expressions gives the number of gallons of fertilizer that Shima will mix in water for 0.5 acres of soil?

(Note: 1 acre = 43,560 square feet; 1 gallon = 128 fluid ounces)

A. \( \frac{0.5(40)(128)}{43,560} \)
B. \( \frac{40(128)}{0.5(43,560)} \)
C. \( \frac{0.5(43,560)}{40(128)} \)
D. \( \frac{43,560}{0.5(40)(128)} \)
E. \( \frac{0.5(43,560)(40)}{128} \)
46. A restaurant has 10 booths that will seat up to 4 people each. If 20 people are seated in booths, and NO booths are empty, what is the greatest possible number of booths that could be filled with 4 people?

- F. 0
- G. 1
- H. 2
- J. 3
- K. 5

47. Let A and B be independent events. Denote \( P(A) \) as the probability that Event A will occur, and denote \( P(A \cap B) \) as the probability that Events A and B will both occur. Which of the following equations must be true?

- A. \( P(A) = P(B) \)
- B. \( P(A) = 1 - P(B) \)
- C. \( P(A \cap B) = P(A) + P(B) \)
- D. \( P(A \cap B) = P(A) \cdot P(B) \)
- E. \( P(A \cap B) = P(A) + P(B) - (P(A) \cdot P(B)) \)

48. In the standard \((x,y)\) coordinate plane below, an angle is shown whose vertex is the origin. One side of this angle with measure \( \theta \) passes through \((4,-3)\), and the other side includes the positive \(x\)-axis. What is the cosine of \( \theta \)?

- F. \(-\frac{4}{5}\)
- G. \(-\frac{3}{4}\)
- H. \(-\frac{3}{5}\)
- J. \(\frac{4}{5}\)
- K. \(\frac{5}{4}\)

49. Which of the following expressions, if any, are equal for all real numbers \(x\)?

- I. \(\sqrt{(-x)^2}\)
- II. \(|-x|\)
- III. \(-|x|\)

- A. I and II only
- B. I and III only
- C. II and III only
- D. I, II, and III
- E. None of the expressions are equivalent.
50. In the figure below, \(A, C, F,\) and \(D\) are collinear; \(B, C,\) and \(E\) are collinear; and the angles at \(A, E,\) and \(F\) are right angles, as marked. Which of the following statements is NOT justifiable from the given information?

F. \(AB \parallel EF.\)
G. \(DE \perp BE.\)
H. \(\angle ACB \cong \angle FCE.\)
J. \(\triangle BAC \sim \triangle EFC.\)
K. \(CE \parallel ED.\)

51. In the figure below, all line segments are either horizontal or vertical and the dimensions given are in inches. What is the perimeter, in inches, of the figure?

A. 10
B. 12
C. 13
D. 14
E. 16

52. Triangle \(\triangle ABC\) has vertices \(A(8,2), B(0,6),\) and \(C(-3,2).\) Point \(C\) can be moved along a certain line, with points \(A\) and \(B\) remaining stationary, and the area of \(\triangle ABC\) will not change. What is the slope of that line?

F. \(-\frac{1}{2}\)
G. \(-\frac{3}{4}\)
H. 0
J. \(\frac{4}{3}\)
K. 2
53. On his first day as a telemarketer, Marshall made 24 calls. His goal was to make 5 more calls on each successive day than he had made the day before. If Marshall met, but did not exceed, his goal, how many calls had he made in all after spending exactly 20 days making calls as a telemarketer?

A. 670
B. 690
C. 974
D. 1,430
E. 1,530

54. Which of the following is the graph of the function \( f(x) \) defined below?

\[
f(x) = \begin{cases} 
  x^2 - 2 & \text{for } x \leq 1 \\
  x - 7 & \text{for } 1 < x < 5 \\
  4 - x & \text{for } x \geq 5 
\end{cases}
\]

A. F
B. G
C. H
D. J
E. K

55. Which of the following expressions gives the number of permutations of 15 objects taken 5 at a time?

A. \( 15(5) \)
B. \( (15 - 5)! \)
C. \( \frac{15!}{5!} \)
D. \( \frac{15!}{(15 - 5)!} \)
E. \( \frac{15!}{(5!)(15 - 5)!} \)
56. For all \( x > 0 \), which of the following expressions is equivalent to \( \frac{i}{\sqrt{x} - i} \), where \( i = \sqrt{-1} \)?

F. \( i \)

G. \( \frac{\sqrt{x}}{x} \)

H. \( \frac{\sqrt{x} - 1}{x + 1} \)

J. \( \frac{i\sqrt{x} + 1}{x - 1} \)

K. \( \frac{i\sqrt{x} - 1}{x + 1} \)

57. Vectors \( \overrightarrow{AB} \) and \( \overrightarrow{CD} \) are shown in the standard \((x, y)\) coordinate plane below. One of the following is the unit vector notation of the vector \( \overrightarrow{AB} + \overrightarrow{CD} \). Which one?

A. \(-6i + 3j\)

B. \(3i - 1j\)

C. \(3i + 9j\)

D. \(9i + 1j\)

E. \(9i + 11j\)

58. A simple pendulum consists of a small mass suspended from a string that is fixed at its upper end and has negligible mass. The length of time, \( t \) seconds, for a complete swing of a simple pendulum can be modeled by the equation \( t = 2\pi \sqrt{\frac{L}{32}} \), where \( L \) is the length, in feet, of the string. If the time required for a complete swing of Pendulum 1 is triple the time required for a complete swing of Pendulum 2, the length of Pendulum 1’s string is how many times the length of Pendulum 2’s string?

F. \( \frac{1}{3} \)

G. 3

H. 6

J. 9

K. 27
59. If \( \log_a x = s \) and \( \log_a y = t \), then \( \log_a (xy)^2 = ? \)
   - A. \( 2(s + t) \)
   - B. \( s + t \)
   - C. \( 4st \)
   - D. \( 2st \)
   - E. \( st \)

60. Jennifer’s best long jump distance increased by 10% from 1990 to 1991 and by 20% from 1991 to 1992. By what percent did her best long jump distance increase from 1990 to 1992?
   - F. 32%
   - G. 30%
   - H. 20%
   - J. 15%
   - K. 2%

END OF TEST 2
STOP! DO NOT TURN THE PAGE UNTIL TOLD TO DO SO.
DO NOT RETURN TO THE PREVIOUS TEST.
LITERARY NARRATIVE: This passage is adapted from the novel *Homeland* by John Jakes (©1993 by John Jakes).

Joseph Emanuel Crown, owner of the Crown Brewery of Chicago, was a worried man. Worried on several counts, the most immediate being a civic responsibility he was scheduled to discuss at an emergency meeting this Friday, the fourteenth of October; a meeting he had requested.

Joe Crown seldom revealed inner anxieties, and that was the case as he worked in his office this morning. He was a picture of steadiness, rectitude, prosperity. He wore a fine suit of medium gray enlivened by a dark red four-in-hand tied under a high collar. Since the day was not yet too warm, he kept his coat on.

Joe’s hair was more silver than white. He washed it daily, kept it shining. His eyes behind spectacles with silver wire frames were dark brown, rather large, and alert. His mustache and imperial showed careful attention; he had an appointment at twelve for the weekly trim. His hands were small but strong. He wasn’t handsome, but he was commanding.

Three principles ruled Joe Crown’s business and personal life, of which the most important was order. In German, *Ordnung*. Without order, organization, some rational plan, you had chaos.

The second principle was accuracy. Accuracy was mandatory in brewing, where timing and temperatures were critical. But accuracy was also the keystone of any business that made money instead of losing it. The primary tool for achieving accuracy was mathematics. Joe Crown had a towering belief in the potency of correct information, and the absolute authority of numbers which provided it.

In Germany, he’d learned his numbers before he learned to read. Though a mediocre student in most school subjects, at ciphering he was a prodigy. He could add a column of figures, or do calculations in his head, with astonishing speed. In Cincinnati, his first stop in America, he’d begged the owner of a Chinese laundry to teach him to use an abacus. One of these ancient counting devices could be found in his office, sitting on a low cabinet, within reach. Money measured success; counting measured money.

Questions he asked of his employees often involved numbers. “What is the exact temperature?” “How large is the population in that market?” “How many barrels did we ship last week?” “What’s the cost, per square foot, of this expansion?”

As for his third principle, modernity, he believed that, too, was crucial in business. Men who said the old ways were the best ways were fools, doomed to fall behind and fail. Joe was always searching for the newest methods to improve the brewery’s product, output, efficiency, cleanliness. He hadn’t hesitated to install expensive pasteurization equipment when he opened his first small brewery in Chicago. He’d been among the first to invest heavily in refrigerated freight cars. He insisted that modern machines be used in the office. From his desk he could hear the pleasing ratchet noise of a mechanical adding machine. This blended with the clicking keys and pinging bell on the black iron typewriter used for correspondence by his chief clerk, Stefan Zwick.

Originally Stefan had resisted Joe’s suggestion that he learn to operate a typewriter. “Sir, I respectfully decline, a quill pen suits me perfectly.”

“But Stefan,” Joe said to him in a friendly but firm way, “I’m afraid it doesn’t suit me, because it makes Crown’s look old-fashioned. However, I’ll respect your feelings. Please place a help wanted advertisement. We’ll hire one of those young women who specialize in using the machines. I believe they too are called typewriters.”

Zwick blanched. “A woman? In my office?”

“I’m sorry, Stefan, but you leave me no choice if you won’t learn to typewrite.”

Stefan Zwick learned to typewrite.

Every solid house or building was supported by a strong foundation; and so there was a foundation on which Joe Crown’s three principles rested. It was not unusual, or peculiar to him. It was the cheerful acceptance, not to say worship, of hard work. Among other
artifacts, advertising sheets, flags and fading brown photographs of annual brewery picnics decorating his office there was a small framed motto which his wife had done colorfully in cross-stitch and put into a frame of gilded wood. *Ohne Fleiss, kein Preis*, it said. In rough translation, this reminded you that without industry there was no reward. From his desk Joe Crown couldn't see the gold-framed motto; it hung on the wall behind him, slightly to his right. But he didn't need to see it. Its truth was in him deeper than the marrow of his bones. He was a German.

1. If a stereotype of Germans is that they are tidy, meticulous, and industrious, does the characterization of Crown in this passage reinforce or weaken this stereotype?
   A. It firmly reinforces the stereotype.
   B. It initially reinforces and subsequently weakens the stereotype.
   C. It reinforces the meticulous aspect of the stereotype but weakens the industrious aspect.
   D. It weakens the stereotype in that Crown likes his surroundings tidy but expects others to do the tidying up.

2. It can reasonably be inferred that in relation to the appointment referred to in the third paragraph (lines 13–19), the meeting referred to in the first paragraph occurs:
   F. on the same day.
   G. several days earlier.
   H. several days later.
   J. several years later.

3. The passage's description of Zwick reveals that compared to Crown, he is:
   A. equally fastidious about meeting a deadline.
   B. less inclined to embrace new technology.
   C. less afraid to state his preferences to his superiors.
   D. more concerned with the company's public image.

4. The dialogue in line 72 reveals Zwick's:
   F. indignation over Crown's proposed solution to the problem the two men are discussing.
   G. panic over having a surprise visitor to his office.
   H. excitement over meeting a new employee of Crown Brewery.
   J. insensitivity to his recently hired female coworker.

5. At the time described in the passage's opening, what is Crown's most immediate preoccupation?
   A. Whether he will be on time for his weekly trim
   B. Whether to install expensive pasteurization equipment at his brewery
   C. Zwick's impertinent behavior
   D. A civic responsibility

6. The passage states that Crown was what kind of student?
   F. Exceptionally gifted, especially in ciphering
   G. Mediocore, except in ciphering
   H. Successful when he applied himself, otherwise poor
   J. Increasingly successful as he gained the use of counting aids

7. Based on the passage, which of the following questions would be most characteristic of the kind Crown typically asked his employees?
   A. “Was your weekend a most pleasant one?”
   B. “Have you had a chance to repair that old typewriter?”
   C. “By what figure will our sales increase if we advertise in that publication?”
   D. “Who among you has a better idea for how we can work well as a team?”

8. At the time in which the passage is set, which of the following devices are still apparently being used in offices in the United States even as those same devices are, in Crown's view, becoming increasingly obsolete?
   F. Typewriters
   G. Mechanical adding machines
   H. Quill pens
   J. Abacuses

9. The metaphor the author uses to help describe Crown's three principles primarily draws upon imagery from what discipline?
   A. Architecture
   B. Business
   C. Astronomy
   D. Education

10. Which of the following is a detail from the passage that indicates the length of time Crown has been in the brewery business?
    F. Some outdated refrigerators from when he first opened his business
    G. A newly hung cross-stitched phrase framed and placed on his office wall
    H. Photographs of annual company picnics decorating his office
    J. A bell, the ringing of which has marked the start of his workday for the last twenty years

GO ON TO THE NEXT PAGE.
Passage II

SOCIAL STUDIES: This passage is adapted from the book The Age of Wonder by Richard Holmes (©2008 by Richard Holmes).

In the summer of 1785 astronomer William Herschel embarked on his revolutionary new project to observe and resolve the heavens with a telescope more powerful than ever previously attempted.

5 What he intended to build was a telescope ‘of the Newtonian form, with an octagon tube 40 foot long and five feet in diameter; the specula [mirrors] of which it would be necessary to have at least two, or perhaps three’. The telescope would have to be mounted in an enormous wooden gantry, capable of being turned safely on its axis by just two workmen, but also susceptible to the finest fingertip adjustments by the observing astronomer.

The forty-foot would be higher than a house. The astronomer (William) would be required to climb a series of ladders to a special viewing platform perched at the mouth of the telescope. The assistant (William’s sister, Caroline) would have to be shut in a special booth below to avoid light pollution, where she would have her desk and lamp, celestial clocks, and observation journals. Astronomer and assistant would be invisible to each other for hours on end, shouting commands and replies, although eventually connected by a metal speaking-tube.

25 William had decided that his grand project required a new house with larger grounds for constructing and erecting the telescope. On 3 April 1786 they moved to ‘The Grove’, a quite small and rather dilapidated country house on the edge of the tiny village of Slough, England.

The house itself was not large, but it had sheds and stables which were gradually converted into workshops and laboratories. Above the stables were a series of haylofts which could be converted into a separate apartment. Caroline claimed these for her own. A small outside staircase led up to a flat roof from which she hoped to carry out her comet ‘sweeps’ in security and independently. She would check over the calculations of William’s nebulae by day, and make her own sweeps up on the roof by night.

40 William had built Caroline a special two-foot Newtonian reflector. Because of its large aperture, its tube appeared much fatter, heavier and stubbier than normal reflectors of this type. Suspended from a pivot at the top of the box-frame, the telescope could be precisely raised or lowered by a system of pulleys operated by a winding handle. These adjustments were easy to make, and extremely fine.

This beautiful instrument was designed specifically for its huge light-gathering power and its wide angle of vision. The magnification was comparatively low at twenty-four times. As with modern binoculars, this combination of low power with a large viewing field allowed the observer to see faint stellar objects very brightly, while placing them within a comparatively wide context of surrounding stars. The telescope was perfectly designed to spot any strange or unknown object moving through the familiar field of ‘fixed stars’. In other words, to catch new planets or new comets.

On 1 August 1786, only two nights after starting her new sweeps, Caroline thought she had spotted an unknown stellar object moving through Ursa Major (the Great Bear constellation). It appeared to be descending, but barely perceptibly, towards a triangulation of stars in the beautifully named constellation Coma Berenices. To find something so quickly, and in such a familiar place (the Great Bear or Big Dipper being the first stop of every amateur stargazer wanting to locate the Pole Star), seemed wildly unlikely. Caroline’s Observation Book conveys meticulous caution, but also remarkable certainty.

Unable to calculate the mathematical coordinates of the object, she accompanied her observations with a series of three neat drawings or ‘figures’, over an eighty-minute time lapse. These showed the circular viewing field of her telescope, with an asterisk shape very slightly changing position relative to three known fixed stars. The account written into her ‘Book of Work Done’ catches something of her growing excitement.

80 August 1st. I have calculated 100 nebulae today, and this evening I saw an object which I believe will prove tomorrow night to be a Comet. August 2nd. I o’clock, the object of last night IS A COMET. August 3rd. I did not go to rest till I had written to Dr Blagden [at the Royal Society] and Mr Aubert to announce the Comet.

The verification of Caroline’s comet was achieved much more rapidly than William’s discovery of the planet Uranus had been. Its movement through Coma Berenices was relatively easy to ascertain, and its fine hazy tail or coma was unmistakable.

11. Which of the following statements best describes how the passage characterizes William’s response to Caroline’s discovery of a comet?

A. The passage makes it clear that although William applauded Caroline’s discovery, he was disappointed that Caroline wasn’t looking for nebulae.

B. The passage claims that William supported Caroline’s discovery by verifying the comet himself.

C. The passage suggests that William resented the fact that Caroline’s comet was recognized so quickly.

D. The passage does not give a clear indication of how William felt about Caroline’s discovery.

GO ON TO THE NEXT PAGE.
12. In the passage, the author emphasizes the large size of William’s powerful telescope’s octagon tube by comparing the tube’s height to that of a:
   F. series of ladders.
   G. wooden gantry.
   H. hayloft.
   J. house.

13. The primary function of the fifth paragraph (lines 31–40) is to:
   A. explain the methods Caroline used to perform her comet sweeps.
   B. shift the passage’s focus from William’s project to Caroline’s own astronomical work.
   C. describe the renovations Caroline made to the stables in order to accommodate William’s telescope.
   D. introduce the passage’s discussion of how Caroline’s observation techniques compared to William’s.

14. In the context of the passage, the excerpt from Caroline’s “Book of Work Done” primarily serves to:
   F. outline the process by which Caroline determined her finding was a comet.
   G. provide an example of the types of observation notes Caroline made for William.
   H. illustrate Caroline’s growing sense of excitement about her discovery.
   J. explain Dr. Blagden’s and Mr. Aubert’s role in verifying Caroline’s discovery.

15. As it is used in line 12, the word finest most nearly means:
   A. slightest.
   B. fairest.
   C. thinnest.
   D. greatest.

16. The passage most strongly suggests that while William operated his telescope, Caroline would have to work below in a special booth because:
   F. she would be relaying William’s instructions to the workmen who turned the telescope.
   G. she preferred seclusion when working on calculations.
   H. the telescope’s viewing platform would not be large enough to hold both William and Caroline.
   J. the light from her lamp would interfere with William’s view of the night sky.

17. Which of the following questions is most directly answered by the passage?
   A. What inspired William to embark on his project to observe and resolve the heavens?
   B. Why did Caroline and William move to “The Grove”?
   C. Why couldn’t Caroline calculate the coordinates of the comet she discovered?
   D. How long did it take the Royal Society to confirm Caroline’s discovery was a new comet?

18. It can most reasonably be inferred from the passage that compared to normal telescopes of its type, the two-foot Newtonian reflector William built had:
   F. a larger aperture.
   G. a smaller box-frame.
   H. more magnifying power.
   J. less light-gathering power.

19. According to the passage, when Caroline first saw her comet, it appeared to be moving through:
   A. Coma Berenices and descending toward the Pole Star.
   B. Coma Berenices and descending toward stars in the Big Dipper.
   C. Ursa Major and descending toward stars in Coma Berenices.
   D. a triangulation of stars, which included the Pole Star, and descending toward Coma Berenices.

20. The passage indicates that Caroline’s discovery of a new comet was unlikely because Caroline:
   F. found the comet quickly in a part of the sky that was familiar to astronomers and stargazers.
   G. knew more about nebulae than she knew about comets.
   H. had already discovered a planet while performing observations with William.
   J. had little experience calculating the mathematical coordinates of stellar objects.
Questions 21–24 ask about Passage A.

21. The main purpose of the first two paragraphs of Passage A (lines 1–16) is to:
   A. establish the popularity of Gornick’s book by indicating that people wanted to meet her after reading the book.
   B. introduce the idea that the characters in Gornick’s memoir are not exactly like their real-life counterparts.
   C. illustrate Gornick’s frustration with some of her contemporaries.
   D. suggest that Gornick’s memoir should be classified as fiction, not as nonfiction.

GO ON TO THE NEXT PAGE.
22. Which of the following quotations from Passage A most directly relates to the party guest’s disappointment upon meeting the author of Fierce Attachments?
   F. “We ourselves were just a rough draft of the written characters” (lines 20–21).
   G. “I had become my mother” (line 32).
   H. “This complicated insight was my bit of wisdom” (line 33).
   J. “The story was the insight” (line 37).

23. According to Passage A, Gornick believes the heart of her memoir to be:
   A. the walks she took with her mother in Manhattan.
   B. the revelation that she had become her mother.
   C. her childhood experiences in the Bronx.
   D. her shared history with her mother.

24. According to Passage A, Gornick believes that memoirs belong to the category of:
   F. journalism.
   G. personal diaries.
   H. historical narratives.
   J. literature.

25. According to Passage B, the protagonists in Hemingway’s fiction are often:
   A. composites of Hemingway’s friends.
   B. based on Hemingway’s family members.
   C. projections of Hemingway himself.
   D. completely made-up characters.

26. Based on Passage B, the question of accuracy in A Moveable Feast is particularly difficult because:
   F. Hemingway used the book to create a particular portrait of himself and his contemporaries.
   G. Hemingway’s contemporaries were writing conflicting memoirs during the same time period.
   H. Hemingway could not produce any documents to support his stories.
   J. Hemingway said his memory was excellent, but others doubt this.

27. Which of the following statements best expresses the opinion the author of Passage B seems to have about A Moveable Feast?
   A. It stands alongside Hemingway’s fiction as one of his best works.
   B. It is a complex example of a book that combines fact and fiction.
   C. It provides an accurate look at a specific time in Hemingway’s life.
   D. It should be read with other books from the same time period.

28. Based on the passages, Gornick’s and Hemingway’s approaches to writing their memoirs are similar in that both writers:
   F. put real characters into wholly fictional situations.
   G. wanted to portray themselves in a flattering way.
   H. were motivated to settle old scores and present their own versions of personal relationships.
   J. used only material from their lives that served the story they each wanted to tell.

29. Based on the passages, it can most reasonably be inferred that Gornick and Hemingway would agree that when it comes to a writer’s responsibility to be truthful in a memoir:
   A. the degree of truthfulness should be the same as that for fiction.
   B. if a writer can’t remember the exact details of a certain event, that event should be left out of the memoir.
   C. it is more important to create an artistic whole than to relate only facts.
   D. the writer should only include incidents that have documented evidence to support them.

30. Another author wrote the following about the role of truth in memoir:
    A memoir is a story, not a history, and real life doesn’t play out as a story.
Which passage most closely echoes the view presented in this quotation?
   F. Passage A, because it offers a story about what happens when you meet someone who doesn’t live up to your expectations.
   G. Passage A, because it stresses that what happens in life is only raw material for a memoirist.
   H. Passage B, because it states that Hemingway viewed A Moveable Feast as his literary testament.
   J. Passage B, because it states that Hemingway seldom lied about pure facts.

GO ON TO THE NEXT PAGE.
Passage IV

NATURAL SCIENCE: This passage is adapted from the article “The Next Wave: What Makes an Invasive Species Stick?” by Robert R. Dunn (©2010 by Natural History Magazine, Inc.).

Like many biologists, Andrew V. Suarez struggled for years with the question of which colonizing organisms fail and which succeed. He studied it the hard way—with fieldwork and lab experiments—until 1999, when he found some brown jars. He had gone to the Smithsonian Institution National Museum of Natural History’s National Insect Collection to look for early samples of Argentine ants collected in the United States or at its borders. He hoped to find out how vintage specimens of Argentine ants were related to the existing populations.

At the museum, among many thousands of jars of insects labeled with taxonomic notes, locations, and dates, Suarez ultimately found relatively few samples of Argentine ants. But what he found besides them was, to his mind, far more interesting: some of the ethanol-filled jars were jammed with vials of ants collected at ports of entry in the eastern U.S. from 1927 to 1985. They were ants that border agents had picked from plants being shipped into the U.S. Could those ants be identified as members of species that had failed or succeeded as colonists, and if so, could the specimens be used to compare the two groups?

In the jars and vials were 394 separate samples of ants. Suarez solicited the help of two friends, ant ecologist David A. Holway of the University of California, San Diego, and Philip S. Ward, guru of ant gurus, at the University of California, Davis. Altogether they identified 232 distinct species.

Suarez considered the traits possessed by each of the ant species in an attempt to see what might have predisposed some of them to survival. He measured whether they were big or small. He examined whether each lived in the canopy or on the ground, and whether they were from one subfamily or another. He also looked at a simpler possibility: that “survivor species” tended to be those introduced more than once. The evidence in the jars showed, for example, that Argentine ants had arrived at least twice. Were successes just a consequence of the number of tries?

When a pioneering group sets up camp and starts living in a new place, possible futures diverge. One species might be wiped out within a generation or two. A second might survive, but never become common. Yet another species might thrive, eventually spreading across states, continents, and even the world! Even if surviving in a new environment is sometimes a matter of being introduced again and again, thriving is a different story. Relatively few invasive species truly prevail.

One curious thing about Argentine ants is that they go, yet somehow they have managed to overpower the big, tough native ants.

There’s another strange thing about Argentine ants. If you take an Argentine ant from what looks like one colony and put it together with one from a distant colony, they accept each other. In fact, you can perform that trick over much of California and very few of the ants will fight. It is as though all of the Argentine ants in California are part of a few huge colonies—“supercolonies,” they’ve come to be called.

Biologist Ted Case joined forces with Holway and Suarez for an experiment to test whether the lack of aggression among those ant colonies somehow helped them to compete with other species. Might it simply be that by not fighting with their neighbors, the Argentine ants wasted less energy on war and could spend more time on the good stuff? It turned out that, yes, aggressive ants wasted energy fighting (and dying), and so gathered less food and fared poorly, in general. Peace pays (at least peace with one’s kin), and so Argentine ants have made bank everywhere they have moved.

In fact, it isn’t just for the Argentine ant that peace seems to pay. Supercolonies and the unicolonial populations they create look to be common among invasive ants.

Ants flash chemical badges identifying their home nest. Without such markers, no one knows who is friend or foe. When the clarity of “us versus them” breaks down, peace breaks out among colonies of an ant species. Different nests swap workers and queens, and the term “colony” becomes fuzzy. Experiments seemed to show that one conglomeration of Argentine ants stretched the length of California, another from Italy to Portugal . . . until, in 2009, workers from those two “colonies” (along with a third from Japan) were put together, and they didn’t fight. Thus, across the entire globe, a few peaceful supercolonies could exist and expand.

31. The main purpose of this passage is to:
A. describe events that led to the discovery of Argentine ants in the United States.
B. examine the physical differences between Argentine ants and other insects.
C. highlight the technology that scientists used to determine the size of supercolonies.
D. discuss factors that contribute to a colonizing organism’s success as an invasive species.

32. The author makes repeated use of which of the following in order to help establish the passage’s somewhat casual tone?
F. Personal anecdotes
G. Idiomatic expressions
H. Humorous quotations
J. Self-critical asides
33. Which of the following events mentioned in the passage occurred first chronologically?
   A. Case joined Holway and Suarez to assist them with an experiment.
   B. Workers from three Argentine ant supercolonies in different parts of the world were brought together.
   C. Suarez found samples of Argentine ants in the Smithsonian insect collection.
   D. Holway and Ward were recruited by Suarez to assist with his research.

34. The main purpose of the fifth paragraph (lines 41–49) is to:
   F. explain how Argentine ants are able to survive in new areas and discuss their spread throughout the world.
   G. describe possible outcomes for a pioneering species and stress the improbability that the species will thrive.
   H. define the concept of invasive species as it relates to ants.
   J. compare the behaviors of Argentine ants to those of other, more successful pioneering species.

35. The author’s claim that the Argentine ant behavior described in lines 56–58 is unusual is based upon which of the following assumptions?
   A. Supercolonies are common among several species of ants.
   B. Argentine ants in California are less aggressive than Argentine ants elsewhere.
   C. California’s ecosystem is especially suited for Argentine ants.
   D. Ants from different colonies typically fight one another.

36. According to the passage, the question of which colonizing organisms fail and which succeed is one that has been studied by:
   F. many biologists for a number of years.
   G. many biologists beginning in 1999.
   H. the Smithsonian exclusively.
   J. Suarez exclusively.

37. The passage makes clear which of the following about the ant samples Suarez found in the Smithsonian insect collection?
   A. Most of the samples were of Argentine ants.
   B. Ward and Holway had collected the samples as part of a larger study of US insect populations.
   C. Suarez discovered that most of the samples were of previously undiscovered species of ants.
   D. Suarez was most interested in the samples that had been collected at eastern US ports of entry.

38. According to the passage, which of the following is true of Argentine ants?
   F. They are stingless.
   G. They are physically dominant.
   H. They were first discovered in the United States by Suarez.
   J. They have failed to thrive in Japan.

39. The passage indicates that compared to peaceful ants, aggressive ants:
   A. live in larger colonies.
   B. spend less time gathering food.
   C. are less likely to live in a colony.
   D. are more likely to be a “survivor species.”

40. The passage most clearly establishes which of the following facts about ants?
   F. In order for ant colonies to combine to form supercolonies, the colonies must have identical chemical badges.
   G. Ants identify their home nests by flashing chemical badges.
   H. Ant colonies from different species commonly swap workers and queens.
   J. The largest supercolony of ants in the world stretches from Italy to Portugal.
Passage I

The figure below is a pedigree that shows the inheritance of a trait, Trait G, in a family. The presence of Trait G in an individual is determined entirely by Gene G. Gene G has 2 alleles: \( G \), which is dominant, and \( g \), which is recessive.

Each individual represented in the pedigree was assigned a number (shown below the symbol for the individual) for reference. Scientists determined that the Gene G genotype of Individual 20 is \( gg \) and that the Gene G genotype of Individual 21 is \( Gg \). Based on this information, the scientists concluded that Trait G is a recessive trait.

1. How many generations are shown in the figure?
   A. 3  
   B. 4  
   C. 22  
   D. 24

2. Based on the figure, the 2 individuals in which of the following pairs most likely have the greatest genetic similarity across their genomes?
   F. Individual 3 and Individual 4  
   G. Individual 12 and Individual 13  
   H. Individual 16 and Individual 24  
   J. Individual 18 and Individual 21

3. Suppose that Individual 23 and Individual 24 have 4 biological children. Based on the figure, how many of the children, if any, have Trait G?
   A. 0  
   B. 1  
   C. 3  
   D. 4

4. According to the figure, how many of the grandchildren of Individual 1 and Individual 2, if any, have Trait G?
   F. 0  
   G. 1  
   H. 2  
   J. 7

GO ON TO THE NEXT PAGE.
5. Based on the figure, is it likely that Trait G is a sex-linked trait?
   A. Yes, because mothers with Trait G always passed Trait G to their sons.
   B. Yes, because mothers with Trait G did not always pass Trait G to their sons.
   C. No, because mothers with Trait G always passed Trait G to their sons.
   D. No, because mothers with Trait G did not always pass Trait G to their sons.

6. Based on the information provided, will an individual with the Gene G genotype \( Gg \) have Trait G?
   F. Yes, because Trait G is a dominant trait.
   G. Yes, because Trait G is a recessive trait.
   H. No, because Trait G is a dominant trait.
   J. No, because Trait G is a recessive trait.
Passage II

**Heliconia metallica** is a plant found in the understory of tropical rain forests. (The **understory** is the area below the forest canopy.) *H. metallica* flowers are normally pollinated by hummingbirds. The flowers can be **self-pollinated** (egg and pollen are from the same *H. metallica* plant) or **cross-pollinated** (egg and pollen are from different *H. metallica* plants). The following study was conducted to investigate the effects of different pollination treatments on fruit production and seed mass in a population of *H. metallica*.

**Study**

Before pollination could occur, the **anthers** (pollen-producing structures) were removed from each of 400 *H. metallica* flowers. Then, the flowers were covered with nylon bags to prevent the normal pollinators from pollinating the flowers. The covered flowers were divided equally into 4 groups (Groups 1−4), and each group received a different pollination treatment (see Table 1). Four weeks after the pollination treatments, the percent of flowers that produced fruit and the average mass per seed were determined for each group (see Figures 1 and 2, respectively).

<table>
<thead>
<tr>
<th>Group</th>
<th>Pollination treatment</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>self-pollination*</td>
</tr>
<tr>
<td>2</td>
<td>cross-pollination with pollen collected from a single donor <em>H. metallica</em> plant</td>
</tr>
<tr>
<td>3</td>
<td>cross-pollination with a mixture of pollen collected from 6 donor <em>H. metallica</em> plants</td>
</tr>
<tr>
<td>4</td>
<td>no pollination</td>
</tr>
</tbody>
</table>

*Each flower was pollinated with pollen from its removed anthers.

Table and figures adapted from Matthias Schleuning et al., "Effects of Inbreeding, Outbreeding, and Supplemental Pollen on the Reproduction of a Hummingbird-pollinated Clonal Amazonian Herb." ©2010 by The Author(s).
7. The data that were averaged to produce the results shown in Figure 2 were most likely collected using which of the following pieces of equipment?
   A. Balance
   B. pH meter
   C. Telescope
   D. Thermometer

8. One of the questions about H. metallica plants that the study was designed to answer was which of the following?
   F. Does the location of the plants in the understory of tropical rain forests determine whether the flowers are self-pollinated or cross-pollinated?
   G. Are the percent of flowers that produce fruit and the average mass per seed different when flowers are self-pollinated than when flowers are cross-pollinated?
   H. How long after the plants are pollinated does the fruit ripen?
   J. Are the flowers normally pollinated by hummingbirds?

9. The pollination treatments received by Groups 1 and 2 differed in which of the following ways? The pollen received by each Group 1 flower was:
   A. from the same plant as the flower, whereas the pollen received by each Group 2 flower was from a different plant than the flower.
   B. from a different plant than the flower, whereas the pollen received by each Group 2 flower was from the same plant as the flower.
   C. collected from 1 plant, whereas the pollen received by each Group 2 flower was collected from 6 plants.
   D. collected from 6 plants, whereas the pollen received by each Group 2 flower was collected from 1 plant.

10. For any group, the value shown in Figure 1 was most likely calculated using which of the following expressions?
    F. \( \frac{\text{number of seeds}}{\text{total seed mass}} \times 100 \)
    G. \( \frac{\text{total seed mass}}{\text{number of seeds}} \times 100 \)
    H. \( \frac{\text{number of flowers producing fruit}}{\text{total number of flowers}} \times 100 \)
    J. \( \frac{\text{total number of flowers}}{\text{number of flowers producing fruit}} \times 100 \)

11. The anthers were most likely removed from the flowers for the purpose of ensuring that the flowers:
    A. would spontaneously self-pollinate.
    B. would not spontaneously self-pollinate.
    C. would be pollinated by hummingbirds.
    D. would not be pollinated by hummingbirds.

12. Do the results of the study indicate that the nylon bags successfully prevented the normal pollinators from pollinating the H. metallica flowers?
    F. Yes; only 20% of the flowers receiving the self-pollination treatment produced fruit.
    G. Yes; none of the flowers receiving the no pollination treatment produced fruit.
    H. No; only 20% of the flowers receiving the self-pollination treatment produced fruit.
    J. No; none of the flowers receiving the no pollination treatment produced fruit.

13. What was the total mass of the seeds produced by the Group 3 flowers?
    A. 0 mg
    B. 45 mg
    C. 85 mg
    D. Cannot be determined from the given information

GO ON TO THE NEXT PAGE.
When 2 types of bacteria found in the soil of a wetland (land having a high water table) break down organic matter, gases are generated. Aerobic bacteria, which require O$_2$, generate CO$_2$. Anaerobic bacteria, which require little or no O$_2$, generate CH$_4$.

**Study**

At the beginning of a particular summer, 3 soil sections, each 1.5 m long, 1 m wide, and 0.6 m deep, were removed intact from the surface of each of 2 wetlands—a bog and a fen—after all live plants had been removed from the sections. Each section was placed in a separate 100 L tank having sides and a lid made entirely of glass. An instrument to measure gas emissions was mounted on the underside of the lid, above the soil. All the tanks were placed at an outdoor site near the wetlands.

Different amounts of water were added to the 3 tanks containing bog soil sections to produce a water table (WT) 1 cm above the surface (+1 cm) of the first soil section, a WT 10 cm below the surface (−10 cm) of the second soil section, and a WT 20 cm below the surface (−20 cm) of the third soil section. This procedure was repeated for the 3 tanks containing fen soil sections. All the lids were then closed.

Over the next 3 months, gas emissions from each soil section were measured, in moles of carbon per square meter (mol C/m$^2$). Throughout this period, the temperature inside the tanks was kept the same as the outdoor temperature. Figure 1 shows the total emission of CO$_2$ and the total emission of CH$_4$ from each bog soil section due to bacterial activity; Figure 2 does the same for each fen soil section.

---

**Figure 1**

**Figure 2**

Figures adapted from Karen Updegraff et al., “Response of CO$_2$ and CH$_4$ Emissions from Peatlands to Warming and Water Table Manipulations.” ©2001 by the Ecological Society of America.
14. The researchers who conducted the study most likely chose to conduct it during the summer rather than during the winter because organic matter in soil is broken down:

F. in the summer by aerobic bacteria only and in the winter by anaerobic bacteria only.
G. in the summer by anaerobic bacteria only and in the winter by aerobic bacteria only.
H. by both aerobic and anaerobic bacteria more rapidly in the summer than in the winter.
J. by both aerobic and anaerobic bacteria less rapidly in the summer than in the winter.

15. According to the results of the study, as the water table for the bog soil sections and the fen soil sections became progressively lower, did the total CO$_2$ emission increase or decrease, and did the total CH$_4$ emission increase or decrease?

<table>
<thead>
<tr>
<th>total CO$_2$ emission</th>
<th>total CH$_4$ emission</th>
</tr>
</thead>
<tbody>
<tr>
<td>A. increased</td>
<td>decreased</td>
</tr>
<tr>
<td>B. decreased</td>
<td>increased</td>
</tr>
<tr>
<td>C. increased</td>
<td>increased</td>
</tr>
<tr>
<td>D. decreased</td>
<td>decreased</td>
</tr>
</tbody>
</table>

16. One of the reasons that the lid on each tank was kept closed for the 3-month period was to:

F. minimize the amount of emitted gas that exited the tank.
G. maximize the amount of atmospheric gas that entered the tank.
H. prevent bacteria from leaving the tank.
J. prevent sunlight from entering the tank.

17. The 2 types of wetland investigated in this study—bogs and fens—have different levels of the nutrients that sustain bacterial growth. Do the results of the study suggest that the levels of the nutrients that sustain aerobic bacteria are higher in bogs or in fens, and do the results of the study suggest that the levels of the nutrients that sustain anaerobic bacteria are higher in bogs or in fens?

<table>
<thead>
<tr>
<th>higher nutrients for aerobic bacteria</th>
<th>higher nutrients for anaerobic bacteria</th>
</tr>
</thead>
<tbody>
<tr>
<td>A. bogs</td>
<td>bogs</td>
</tr>
<tr>
<td>B. bogs</td>
<td>fens</td>
</tr>
<tr>
<td>C. fens</td>
<td>bogs</td>
</tr>
<tr>
<td>D. fens</td>
<td>fens</td>
</tr>
</tbody>
</table>

18. Based on the results of the study for the 2 soil sections that were completely submerged in water, were aerobic bacteria present in those sections?

F. Yes; CO$_2$ was emitted from those sections.
G. Yes; CH$_4$ was emitted from those sections.
H. No; only CO$_2$ was emitted from those sections.
J. No; only CH$_4$ was emitted from those sections.

19. Consider the total CO$_2$ emission from the fen soil section having a WT of $-10$ cm. Based on that result, over the 3 months, the average CO$_2$ emission from that soil section per month would have been closest to which of the following?

A. 10 mol C/m$^2$
B. 13 mol C/m$^2$
C. 16 mol C/m$^2$
D. 19 mol C/m$^2$

20. The study was conducted at an outdoor site near the wetlands to ensure that the tanks would be nearly identical to the wetlands with respect to which of the following conditions?

F. Amount of precipitation
G. Types of plants present
H. Volume of soil
J. Hours of daylight
Passage IV

Physics students performed 3 studies to determine the forces that several doors exerted on their hinges. The doors had various weights, \( W \), and widths, \( D \). Each door had 2 hinges; the hinges could be moved to vary the distance, \( S \), between them. None of the doors had a doorknob.

The 2 hinges on each door were equidistant from the center of mass of the door (see the diagram).

Each hinge was fitted with 2 force sensors. With the door attached to a door frame, one of the sensors detected the horizontal force exerted by the door on the hinge, \( F_h \), and the other sensor detected the vertical force exerted by the door on the hinge, \( F_v \). Once \( F_h \) and \( F_v \) were determined for each hinge, \( F_h \) was averaged over the 2 hinges, yielding the average horizontal force per hinge, \( F_{h, av} \), and \( F_v \) was averaged over the 2 hinges, yielding the average vertical force per hinge, \( F_{v, av} \). From \( F_{h, av} \) and \( F_{v, av} \), the average net force per hinge, \( F_{n, av} \), could be calculated.

In the 3 studies, all forces were recorded in pounds (lb) and all lengths were recorded in inches (in).

**Study 1**

For a door with \( W = 61 \text{ lb} \) and \( D = 30 \text{ in} \), the students determined \( F_{h, av} \) and \( F_{v, av} \) at various \( S \). The results are shown in Figure 1.

**Study 2**

For 3 doors, each with \( D = 30 \text{ in} \) but a different \( W \), the students determined \( F_{n, av} \) at various \( S \). The results are shown in Figure 2.

**Study 3**

For 3 doors, each with \( W = 61 \text{ lb} \) but a different \( D \), the students determined \( F_{n, av} \) at various \( S \). The results are shown in Figure 3.

21. In which study, if any, was the door with the greatest mass tested?

A. Study 1  
B. Study 2  
C. Study 3  
D. None of the studies; all the doors tested in the 3 studies had the same mass.

GO ON TO THE NEXT PAGE.
22. Which of the following statements regarding \( W \) and \( D \) best describes a difference between Study 2 and Study 3?

In Study 2:

F. \( W \) was varied while \( D \) was held constant, whereas in Study 3, \( W \) was held constant while \( D \) was varied.

G. \( W \) was held constant while \( D \) was varied, whereas in Study 3, \( W \) was varied while \( D \) was held constant.

H. both \( W \) and \( D \) were varied, whereas in Study 3, both \( W \) and \( D \) were held constant.

J. both \( W \) and \( D \) were held constant, whereas in Study 3, both \( W \) and \( D \) were varied.

23. If a door having \( W = 90 \text{ lb}, \ D = 30 \text{ in}, \) and \( S = 50 \text{ in} \) had been tested in Study 2, \( F_{n, av} \) for this door would most likely have been:

A. less than 20 lb.

B. between 20 lb and 30 lb.

C. between 30 lb and 45 lb.

D. greater than 45 lb.

24. For the door tested in Study 1, when \( S \) was less than 30 in, was \( F_{h, av} \) less than \( F_{v, av} \) or greater than \( F_{v, av} \)?

When \( S \) was greater than 30 in, was \( F_{h, av} \) less than \( F_{v, av} \) or greater than \( F_{v, av} \)?

\( S \) less than 30 in | \( S \) greater than 30 in
---|---
F. less | less
G. less | greater
H. greater | less
J. greater | greater

25. In Studies 2 and 3, which combination of \( W, D, \) and \( S \) resulted in the lowest \( F_{h, av} \)?

<table>
<thead>
<tr>
<th>( W ) (lb)</th>
<th>( D ) (in)</th>
<th>( S ) (in)</th>
</tr>
</thead>
</table>
A. 51 | 30 | 20 |
B. 51 | 30 | 70 |
C. 61 | 24 | 20 |
D. 61 | 24 | 70 |

26. In Study 1, which average force, \( F_{h, av} \) or \( F_{v, av} \), was independent of \( S \)?

F. \( F_{h, av} \), because as \( S \) increased, \( F_{h, av} \) decreased.

G. \( F_{h, av} \), because as \( S \) increased, \( F_{h, av} \) remained constant.

H. \( F_{v, av} \), because as \( S \) increased, \( F_{v, av} \) decreased.

J. \( F_{v, av} \), because as \( S \) increased, \( F_{v, av} \) remained constant.

27. Suppose that, due to a manufacturing defect, a particular pair of hinges will break when a net force greater than 57 lb is exerted on each hinge. Based on Study 3, the hinges will most likely break if used on a 61 lb door with which of the following combinations of \( D \) and \( S \)?

<table>
<thead>
<tr>
<th>( D ) (in)</th>
<th>( S ) (in)</th>
</tr>
</thead>
</table>
A. 30 | 20 |
B. 30 | 70 |
C. 36 | 20 |
D. 36 | 70 |

GO ON TO THE NEXT PAGE.
Passage V

In a chemistry class, the teacher placed 0.5 g of porous steel wool, composed mostly of iron (Fe), inside a small heat-resistant quartz tube. She then used silicone hoses to connect the quartz tube to 2 airtight glass syringes (see figure). Each syringe contained 8 mL of air, and the total volume of air in the closed apparatus was 20 mL.

A Bunsen burner was then used to heat the contents of the quartz tube for 2 min. During heating, the plungers were moved up and down to pass the air back and forth through the steel wool. The total volume of gas in the apparatus steadily declined over the 2 min. Once the apparatus and its contents returned to room temperature, the total volume of gas in the apparatus was 16 mL.

The teacher asked each of 4 students to explain what occurred during the demonstration.

**Student 1**  
Fe and N

During heating, the Fe in the steel wool reacted with all the N\(_2\) in the air to form solid iron nitride (FeN), which was deposited on the steel wool. Air contains about 20% N\(_2\) by volume. As a result of the reaction, the total volume of gas in the apparatus decreased by about 20%, so almost all the gas remaining in the apparatus was O\(_2\).

**Student 2**  
Fe and O\(_2\)

During heating, the Fe in the steel wool reacted with some of the O\(_2\) in the air to form solid iron oxide (FeO\(_x\)), which was deposited on the steel wool. Air contains about 80% O\(_2\) by volume. As a result of the reaction, the total volume of gas in the apparatus decreased by about 20%. Almost all the gas remaining in the apparatus was a mixture of about 75% O\(_2\) and 25% N\(_2\) by volume.

**Student 3**  
Same as 2 but less O\(_2\)

Student 2 is correct, except that (1) the Fe in the steel wool reacted with all the O\(_2\) in the air and (2) air contains about 20% O\(_2\) by volume. After the reaction, almost all the gas remaining in the apparatus was N\(_2\).

**Student 4**  
Fe and CO\(_2\)

During heating, the Fe in the steel wool reacted with all the CO\(_2\) in the air to form solid iron carbonate (FeCO\(_3\)), which was deposited on the steel wool. Air contains about 20% CO\(_2\) by volume. As a result of the reaction, the total volume of gas in the apparatus decreased by about 20%, so almost all the gas remaining in the apparatus was O\(_2\).
28. Air contains less than 1% argon by volume. This information weakens the explanations given by which of the students, if any?
   F. Students 1 and 2 only
   G. Students 3 and 4 only
   H. All of the students
   J. None of the students

29. Silicone hoses were most likely used to connect the quartz tube to the syringes because silicone has which of the properties listed below?
   I. Strong resistance to heat
   II. Low chemical reactivity
   III. High solubility in water

   A. I and II only
   B. I and III only
   C. II and III only
   D. I, II, and III

30. Based on Student 4's explanation, during the demonstration, did the percent CO₂ by volume in the apparatus increase or decrease, and did the percent O₂ by volume in the apparatus increase or decrease?

   F. increase increase
   G. increase decrease
   H. decrease decrease
   J. decrease increase

31. Which of the students would be likely to agree that by volume, air contains more O₂ than N₂?

   A. Students 1 and 2 only
   B. Students 1 and 3 only
   C. Students 1, 2, and 4 only
   D. Students 1, 3, and 4 only

32. Based on Student 3's explanation, the reaction that occurred during the demonstration would be represented by which of the following balanced chemical equations?

   F. 2Fe₂O₃ → 4Fe + 3O₂
   G. 2FeN → 2Fe + N₂
   H. 4Fe + 3O₂ → 2Fe₂O₃
   J. 2Fe + N₂ → 2FeN

33. Which of the students, if any, would be likely to agree that at the end of the demonstration, the gas remaining in the apparatus was at least 20% N₂ by volume?

   A. Student 2 only
   B. Students 2 and 3 only
   C. All of the students
   D. None of the students

34. In a chemical reaction, the limiting reactant is the reactant that is in the shortest supply and thus limits the amount of product that can be produced. Which student would be the most likely to agree that the limiting reactant during the demonstration was the iron in the steel wool?

   A. Student 1
   B. Student 2
   C. Student 3
   D. Student 4

GO ON TO THE NEXT PAGE.
Quarks constitute 1 of the 3 classes of elementary particles that form all matter in the universe. Three quarks bound together form a type of particle called a baryon. A quark’s effective mass (mass when bound to other quarks) is greater than its single-quark mass (mass when unbound). In addition, all quarks possess a property called spin. A quark’s spin can be oriented in 1 of 2 directions, spin-up (↑) or spin-down (↓).

Table 1 lists the symbol, electric charge, and approximate single-quark mass for each of the 6 quarks.

<table>
<thead>
<tr>
<th>Quark</th>
<th>Symbol</th>
<th>Electric charge</th>
<th>Single-quark mass (MeV*)</th>
</tr>
</thead>
<tbody>
<tr>
<td>Down</td>
<td>d</td>
<td>$-\frac{1}{3}$</td>
<td>5</td>
</tr>
<tr>
<td>Up</td>
<td>u</td>
<td>$+\frac{2}{3}$</td>
<td>3</td>
</tr>
<tr>
<td>Strange</td>
<td>s</td>
<td>$-\frac{1}{3}$</td>
<td>104</td>
</tr>
<tr>
<td>Charm</td>
<td>c</td>
<td>$+\frac{2}{3}$</td>
<td>1,270</td>
</tr>
<tr>
<td>Bottom</td>
<td>b</td>
<td>$-\frac{1}{3}$</td>
<td>4,200</td>
</tr>
<tr>
<td>Top</td>
<td>t</td>
<td>$+\frac{2}{3}$</td>
<td>171,200</td>
</tr>
</tbody>
</table>

*million electron volts

Table 2 gives the symbol, mass, quark content, and quark spins for several baryons.

<table>
<thead>
<tr>
<th>Baryon</th>
<th>Symbol</th>
<th>Mass (MeV)</th>
<th>Quark content</th>
<th>Quark spins</th>
</tr>
</thead>
<tbody>
<tr>
<td>Proton</td>
<td>p</td>
<td>938</td>
<td>uud</td>
<td>↑↑</td>
</tr>
<tr>
<td>Neutron</td>
<td>n</td>
<td>939</td>
<td>udd</td>
<td>↑↑</td>
</tr>
<tr>
<td>Lambda-zero</td>
<td>$\Lambda^0$</td>
<td>1,115</td>
<td>uds</td>
<td>↑↑</td>
</tr>
<tr>
<td>Delta-zero</td>
<td>$\Delta^0$</td>
<td>1,233</td>
<td>udd</td>
<td>↑↑↑</td>
</tr>
<tr>
<td>Delta-minus</td>
<td>$\Delta^-$</td>
<td>1,234</td>
<td>ddd</td>
<td>↑↑↑</td>
</tr>
<tr>
<td>Omega-minus</td>
<td>$\Omega^-$</td>
<td>1,673</td>
<td>sss</td>
<td>↑↑↑</td>
</tr>
</tbody>
</table>

Tables adapted from C. Amsler et al., “Review of Particle Physics.” ©2008 by Elsevier B.V.
35. For all quarks, the amount of spin is always \( \frac{1}{2} \hbar \), where \( \hbar \) is a constant. A spin-up quark has spin \( +\frac{1}{2} \hbar \), and a spin-down quark has spin \( -\frac{1}{2} \hbar \). Given that the spin of a baryon equals the sum of its quark spins, what are the spins of the \( \Lambda^0 \) and \( \Delta^0 \) baryons listed in Table 2?

\[
\begin{array}{cc}
\Lambda^0 & \Delta^0 \\
A. & -\frac{1}{2} \hbar & -\frac{3}{2} \hbar \\
B. & -\frac{1}{2} \hbar & -\frac{1}{2} \hbar \\
C. & +\frac{1}{2} \hbar & +\frac{3}{2} \hbar \\
D. & +\frac{3}{2} \hbar & +\frac{3}{2} \hbar
\end{array}
\]

36. Which of the following diagrams represents the quark content and quark spins for an electrically neutral baryon having only 2 quark spins oriented in the same direction?

- **F.**
  - u↑
  - c↑
  - t↑
- **G.**
  - d↓
  - u↑
  - s↑
- **H.**
  - t↓
  - c↓
  - s↑
- **J.**
  - t↑
  - c↑
  - d↑

37. Is the information in Tables 1 and 2 consistent with the known electric charge for the proton?
   A. No, because Tables 1 and 2 indicate the proton has an electric charge of 0.
   B. No, because Tables 1 and 2 indicate the proton has an electric charge of +1.
   C. Yes, because Tables 1 and 2 indicate the proton has an electric charge of 0.
   D. Yes, because Tables 1 and 2 indicate the proton has an electric charge of +1.

38. Based on Tables 1 and 2, the \( \Omega^- \) baryon has the same electric charge as a baryon containing which of the following quark combinations?
   - **F.** \( dsb \)
   - **G.** \( ssc \)
   - **H.** \( sst \)
   - **J.** \( usc \)

39. Based on Tables 1 and 2, atomic nuclei are made up of which types of quarks?
   A. \( u \) and \( d \) only
   B. \( d \) and \( s \) only
   C. \( u \) and \( s \) only
   D. \( u, d, \) and \( s \) only

40. The 6 quarks are grouped into 3 generations as shown in the table below.

<table>
<thead>
<tr>
<th>Generation</th>
<th>Quarks</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>( d, u )</td>
</tr>
<tr>
<td>2</td>
<td>( s, c )</td>
</tr>
<tr>
<td>3</td>
<td>( b, t )</td>
</tr>
</tbody>
</table>

For which generation, if any, is the statement “Positively charged quarks are more massive than negatively charged quarks” NOT true?

- **F.** Generation 1
- **G.** Generation 2
- **H.** Generation 3
- **J.** None of the generations; the statement is true for all 3 generations.

END OF TEST 4
STOP! DO NOT RETURN TO ANY OTHER TEST.
You may wish to photocopy these sample answer document pages to respond to the practice ACT Writing Test.

Please enter the information at the right before beginning the Writing Test.

Use a soft lead No. 2 pencil only. Do NOT use a mechanical pencil, ink, ballpoint, or felt-tip pen.

**Begin WRITING TEST here.**

If you need more space, please continue on the next page.
If you need more space, please continue on the next page.
STOP here with the Writing Test.
Directions

This is a test of your writing skills. You will have forty (40) minutes to read the prompt, plan your response, and write an essay in English. Before you begin working, read all material in this test booklet carefully to understand exactly what you are being asked to do.

You will write your essay on the lined pages in the answer document provided. Your writing on those pages will be scored. You may use the unlined pages in this test booklet to plan your essay. Your work on these pages will not be scored.

Your essay will be evaluated based on the evidence it provides of your ability to:

- analyze and evaluate multiple perspectives on a complex issue
- state and develop your own perspective on the issue
- explain and support your ideas with logical reasoning and detailed examples
- clearly and logically organize your ideas in an essay
- effectively communicate your ideas in standard written English

Lay your pencil down immediately when time is called.

DO NOT OPEN THIS BOOKLET UNTIL TOLD TO DO SO.
Declining Event Attendance

For many years, the only way to see a large public event—a concert, a movie, a baseball game—was to attend in person. More than just a function of necessity, though, physically attending a large event was seen as an opportunity to build community and fellowship through shared experience. In recent years, however, attendance at public events has declined steadily. Given the long-standing cultural role of public events, it is worth considering what declining attendance might indicate about our shifting cultural values.

Read and carefully consider these perspectives. Each suggests a particular way of thinking about declining event attendance as a reflection of shifting cultural values.

### Perspective One
People these days value convenience over community. It’s easier to watch a game from home than to attend in person, so we do it, even though it keeps us isolated from one another.

### Perspective Two
For many people, attending an event is a luxury they can’t afford. When time and resources are scarce, we choose what’s most practical first, even if that means sacrificing community participation.

### Perspective Three
Today, physical presence isn’t necessary for participating in an event and building community. TV, the Internet, and social media offer shared experience to more people than large public events ever could before.

**Essay Task**

Write a unified, coherent essay in which you evaluate multiple perspectives on declining event attendance as a reflection of shifting cultural values. In your essay, be sure to:

- analyze and evaluate the perspectives given
- state and develop your own perspective on the issue
- explain the relationship between your perspective and those given

Your perspective may be in full agreement with any of the others, in partial agreement, or wholly different. Whatever the case, support your ideas with logical reasoning and detailed, persuasive examples.
Planning Your Essay

Your work on these prewriting pages will not be scored.

Use the space below and on the back cover to generate ideas and plan your essay. You may wish to consider the following as you think critically about the task:

Strengths and weaknesses of the three given perspectives
- What insights do they offer, and what do they fail to consider?
- Why might they be persuasive to others, or why might they fail to persuade?

Your own knowledge, experience, and values
- What is your perspective on this issue, and what are its strengths and weaknesses?
- How will you support your perspective in your essay?

If you need more space to plan, please continue on the back of this page.
Planning Your Essay

Use this page to continue planning your essay. Your work on this page will not be scored.
Scoring Your Practice Tests

How to score practice test 2 and practice test 3 is covered in chapter 11.

Explanatory Answers
Passage I

Question 1. The best answer is B because it uses a simple present tense singular verb that agrees with the singular noun building. It also creates a complete sentence.

The best answer is NOT:

A because it attaches the main verb is to the relative pronoun that, creating a clause that interrupts the sentence and creates a sentence fragment (an incomplete sentence).

C because the contraction it’s (meaning “it is”) creates a faulty conjunction resulting in a fragment connected to an independent clause.

D because it removes the main verb from the sentence, resulting in a sentence fragment.

Question 2. The best answer is F because it mentions the “legacy of the Chinese community,” which refers to the cultural significance of the building, and “the nineteenth-century American West,” which refers to the building’s historical significance.

The best answer is NOT:

G because it names specific features of the building. The features themselves do not introduce the building’s historical and cultural significance.

H because it identifies the groups responsible for preserving and operating the building today but does not introduce the historical and cultural significance of the building.

J because it mentions some of the contents of the building’s kitchen. The contents of the kitchen do not introduce the historical and cultural significance of the building.

Question 3. The best answer is C because it correctly uses the past tense verb were attracted, which is consistent with served.

The best answer is NOT:

A because it uses the present tense in a sentence that requires the past tense. Also, it creates an illogical thought regarding what travelers might have been attracted to the land.

B because it uses the future tense in a sentence that requires the past tense.

D because it uses the present tense in a sentence that requires the past tense.
Question 4. The best answer is G because it provides a link to the information that follows by providing the names of the two young Chinese men who are referred to in the next sentence and the rest of the essay.

The best answer is NOT:

F because the preceding sentence does not make a claim about Hay and On.

H because the introduction of the men’s names is necessary. Knowing that Hay and On are the men who bought the building is necessary for understanding the essay at this point.

J because it incorrectly suggests that this part of the essay focuses on Hay and On’s partnership rather than on introducing Hay and On as the men who bought the building.

Question 5. The best answer is D because it uses a plural past tense verb remained. The essay’s content calls for the past tense, and the sentence’s verb must agree with its subject, men.

The best answer is NOT:

A because it uses a present tense verb remains, which does not agree with the sentence’s subject. Also, it is not parallel with the other verbs in the sentence (combined and organized).

B because it uses the auxiliary verb has, which does not agree in number with the sentence’s subject and is not parallel with the other verbs in the sentence.

C because it combines the correct auxiliary verb have with the incorrect verb remain, resulting in an improperly formed verb. Also, it is not parallel with the other verbs in the sentence.

Question 6. The best answer is G because it creates a parallel structure in which making and curing (used later in the sentence) are in the same form. The preposition for correctly applies to both verbs.

The best answer is NOT:

F because it inserts a dependent clause, creating a sentence in which the verbs are not parallel.

H because it inserts a dependent clause that isn’t parallel with the verb curing.

J because it makes the latter half of the sentence into a compound predicate, which creates a problem with parallelism with the verb curing.
Question 7. **The best answer is A** because it uses the possessive pronoun *whose*, which clearly explains that the treatments were those of the patients.

**The best answer is NOT:**

B because it is unnecessarily wordy and redundant; the idea of previous treatments explains that the treatments were already experienced.

C because it illogically indicates that the patients were the previous treatments.

D because the phrase “of whom” creates an illogical sentence with an unclear meaning.

**Question 8. The best answer is F** because the preceding sentence discusses Hay’s medical expertise as the reason for his fame and noteworthiness.

**The best answer is NOT:**

G because the sentence does not mention any specific examples of Hay’s diagnoses.

H because the resulting paragraph would be unevenly weighted toward On when the essay describes the two men as partners. The information about Hay is important regardless of On’s involvement with the medical clinic.

J because the paragraph is about both Hay and On, not On only.

**Question 9. The best answer is A** because the preceding sentence lists six services that the building eventually provided. If the sentence were deleted, the paragraph would lose the details that indicate the scope of services.

**The best answer is NOT:**

B because the sentence provides no claims about which aspect of Kam Wah Chung & Co. was most important to visitors.

C because the sentence does not provide a summary of one visitor’s experiences at Kam Wah Chung & Co.

D because the sentence provides no indication of how long Kam Wah Chung & Co. was prosperous.
**Question 10.** The best answer is **J** because the word *into* is grammatical and clearly indicates a transition from the Great Depression to the 1940s.

The best answer is **NOT**:

F because *beginning* is a present participle, not a preposition. The sentence has a series of prepositional phrases (“through the turn of the century” and “during the Great Depression”). This final phrase needs to match the structure of the two preceding phrases.

G because the pronoun *it* is singular and cannot refer to the plural *businesses*. This *it* has no clear referent. The resulting sentence does not make clear what entered the 1940s.

H because it creates an illogical statement; *businesses* cannot become the 1940s.

**Question 11.** The best answer is **C** because the past tense is called for in the sentence, and the verb form *became* aligns with *was restored*, a past tense verb used previously in the sentence.

The best answer is **NOT**:

A because *has became* is an incorrect verb form.

B because the auxiliary verb *have* does not agree in number with the singular subject of the sentence, *building*.

D because *become* is a present tense verb form; the context and structure of the sentence call for a past tense verb.

**Question 12.** The best answer is **J** because it is the only option that does not introduce a redundancy into the sentence.

The best answer is **NOT**:

F because it is unnecessarily wordy and redundant. The word *designated* already conveys the idea that the museum was called a National Historic Landmark.

G because it is redundant; *designated* already conveys the idea of having the appropriation of.

H because it is redundant; *designated* already conveys the idea of being identified as.
Question 13. The best answer is D because no transitional word or phrase is needed in the sentence.

The best answer is NOT:

A because the word *besides* indicates that a previous idea is being added onto, which isn’t the case.

B because the phrase “in conclusion” does not offer a logical transition from the idea of the museum being designated a national landmark to the idea that the museum encapsulates an era.

C because the sentence gives an exact year when the building became a National Historic Landmark (2005), so “in time” is illogical here.

Question 14. The best answer is J because sentence 2 explains why the artifacts left inside the building were preserved. It is logical to infer that they wouldn’t need to be preserved unless the building had been closed for a long time, which is exactly what sentence 5 states. Placing sentence 2 after sentence 5 makes the paragraph logical by putting the events in chronological order.

The best answer is NOT:

F because as it is now, sentence 2 interrupts the historical discussion of how Kam Wah Chung & Co. prospered and shifted in leadership over the years.

G because placing sentence 2 before sentence 1 illogically presents the information about the preservation of artifacts prior to mentioning the closing of Kam Wah Chung & Co.

H because placing sentence 2 after sentence 3 interrupts the historical discussion of how Kam Wah Chung & Co. shifted in leadership.

Question 15. The best answer is C because the focus of the essay is on the historical role of the Kam Wah Chung & Co. building. The essay details how the building was founded, who used it, and for what purposes. The essay does not outline the steps the state of Oregon took to restore the building.

The best answer is NOT:

A because although the essay mentions the restoration of the building, it primarily offers an overview of the building’s historical role rather than explaining the steps the state of Oregon took to restore the building.

B because although the essay mentions how the artifacts were preserved, it primarily offers an overview of the building’s historical role rather than explaining the steps the state of Oregon took to restore the building.

D because the essay does not critique On’s business philosophies or Hay’s medical diagnoses and treatments.
Passage II

**Question 16. The best answer is H** because it correctly inserts a comma only after the prepositional phrase that begins the sentence.

*The best answer is NOT:*

F because it incorrectly inserts a comma between the subject (*fair*) and the verb (*looks*).

G because it incorrectly inserts a comma between the subject (*fair*) and the verb (*looks*) and sets off the subject (“a Renaissance fair”) as nonessential information.

J because it incorrectly adds a semicolon after *fair*. A semicolon must separate two independent clauses. In this case, it separates two fragments (incomplete sentences).

**Question 17. The best answer is D** because it correctly uses the possessive pronoun *their* and the preposition *past* to explain the direction of movement; the people are passing by costumed characters and colorful booths.

*The best answer is NOT:*

A because it uses the contraction *they’re* (they are) in place of *their* (possessive).

B because it uses the contraction *they’re* (they are) in place of *their* (possessive) and the past tense verb *passed* in place of the preposition *past*.

C because it uses the past tense verb *passed* in place of the preposition *past*.

**Question 18. The best answer is G** because it creates a logical sentence that contrasts theme parks and Renaissance fairs. This comparison makes sense in the paragraph, which has been describing how theme parks and Renaissance fairs are similar up to this point.

*The best answer is NOT:*

F because it illogically suggests that roller coasters and Ferris wheels are the reason why Renaissance fair attractions are inspired by sixteenth-century England.

H because it creates an illogical cause-effect relationship between the roller coasters and Ferris wheels of theme parks and the sixteenth-century inspirations of Renaissance fairs.

J because it creates an illogical cause-effect relationship. Roller coasters and Ferris wheels are not the reason why Renaissance fair attractions are inspired by sixteenth-century England.
Question 19. The best answer is A because no punctuation is needed here. The absence of punctuation creates the clearest indication that the sentence is referring to the horses that are carrying knights.

The best answer is NOT:

B because it makes “carrying knights” appear as nonessential information and results in a clause that lacks a verb: Horses to a jousting match.

C because it incorrectly places a comma between the subject (“horses carrying knights”) and the prepositional phrase that explains where they are going (“to a jousting match”).

D because it offers the beginning of a nonessential phrase (“carrying knights to . . .”) that has no second comma later in the sentence to close it. This creates an ungrammatical sentence.

Question 20. The best answer is G because the verb clip-clop provides the sound the horses’ hooves make on the streets, which is a sensory detail about the horses’ movement.

The best answer is NOT:

F because the verb walk does not provide a sensory detail that clearly conveys the horses’ movement.

H because the verb move only conveys the vague idea of movement without providing any sensory details.

J because the verb travel only conveys the vague idea of movement from one place to another without providing any sensory details.

Question 21. The best answer is D because it correctly positions the phrase “ranging from king-sized turkey legs to suits of armor” so that it modifies wares. The wares are the things that vary in this way.

The best answer is NOT:

A because it incorrectly suggests that the vendors are what range from turkey legs to suits of armor.

B because it offers the action (“peddling wares”) before the subject (vendors) and separates the two with the modifier about the types of wares. The result is an unclear sentence.

C because it incorrectly modifies vendors, suggesting that the vendors range from turkey legs to suits of armor.
Taking Additional Practice Tests

ENGLISH • PRACTICE TEST 2 • EXPLANATORY ANSWERS

**Question 22.** The best answer is G because it effectively introduces the subject that is developed in the paragraph and in the rest of the essay: the hard work that goes into re-creating the past at the Renaissance fair.

The best answer is NOT:

F because it misleads the reader into thinking that what follows will be about how interesting Renaissance fairs are instead of about the challenges of working at a Renaissance fair.

H because it suggests that what follows will focus on the fun of working at the Renaissance fair instead of on the challenges of working there.

J because it suggests that the paragraph and essay will focus on a specific day when the narrator attended a Renaissance fair whereas the paragraph and essay explain the challenges of working at a Renaissance fair.

**Question 23.** The best answer is C because it results in a complete sentence with a comma separating the main clause from the participial phrase that begins with substituting.

The best answer is NOT:

A because it improperly has substituting as the beginning of a sentence, which results in a sentence fragment.

B because it creates a comma splice (two or more complete sentences separated by only a comma). The two complete sentences joined by the comma both begin with the subject we.

D because it incorrectly places a semicolon between a main clause and a participial phrase. A semicolon must separate two independent clauses.

**Question 24.** The best answer is F because it uses the past tense verb introduced, which is parallel with the verb served (the other verb in the sentence's compound predicate). The past tense is used in most of the essay.

The best answer is NOT:

G because it incorrectly uses the infinitive to introduce when the past tense is needed. Also, it is not parallel with the verb served.

H because it incorrectly uses the participle introducing when the past tense is called for. Like G, it isn't parallel with served.

J because it shifts the tense from the past to the present and, similar to G and H, isn’t parallel with served.
Question 25. The best answer is D because it correctly uses the pronoun who to introduce the clause that describes the person the narrator was pretending to be. In this sentence, who is required because it functions as the subject of the clause.

The best answer is NOT:

A because it uses the object pronoun whom instead of the subject pronoun who.

B because by using the verb were in this sentence, the writer is incorrectly describing a past event as if it were a hypothetical future one.

C because it, like A, uses the object pronoun whom instead of the subject pronoun who.

Question 26. The best answer is J because no punctuation is needed here. The absence of punctuation creates the clearest and most understandable sentence that links the subject costumes to the verb consisted.

The best answer is NOT:

F because it creates the nonessential clause “they consisted of confining corsets.” The resulting sentence lacks a necessary verb between costumes and the attributes of the costumes (confining corsets, several scratchy petticoats, and heavy velvet gowns).

G because it creates a comma splice (two or more complete sentences separated by only a comma). The word they becomes the subject of the second complete sentence.

H because it inserts the preposition of, which creates the ungrammatical phrase “because of our costumes consisted.”

Question 27. The best answer is C because the sentence about the costumes theme park characters wear isn’t very relevant in an essay about working at a Renaissance fair, especially given that the first paragraph makes a distinction between Renaissance fairs and theme parks.

The best answer is NOT:

A because although Renaissance fairs and theme parks are compared earlier in the essay, this sentence doesn’t pertain to this paragraph’s discussion of the costumes the narrator wore at the Renaissance fair.

B because although the preceding sentence does discuss uncomfortable costumes, it relates to the narrator’s experience at a Renaissance fair, not at a theme park.

D because the information about costumes worn by characters at theme parks is not found elsewhere in the essay.
Question 28. The best answer is H because it most clearly and concisely refers to all manner of inventions. It does not repeat the same idea, and it does not add unnecessary words to the sentence.

The best answer is NOT:

F because it is redundant and wordy. The phrase “after the sixteenth century” already conveys the idea of things that had come into existence more recently.

G because it adds wordiness and redundancy. The phrase “any kind of object or type of item” is redundant, as is the phrase “created and introduced for use.”

J because it creates a notable shift in tone. “Stuff from” is more informal than the tone in the rest of the essay.

Question 29. The best answer is B because the phrase “for example” serves as a transition from the preceding sentence, which discusses describing things in Renaissance terms, to this sentence, which has the narrator describing a photograph as a small painting in a tiny box.

The best answer is NOT:

A because the adverbial conjunction however implies that the ideas in this sentence contrast with the ideas in the preceding sentence, which isn't the case.

C because the phrase “one time” suggests that the incident with the camera happened only once, an idea that is contradicted by the sentence's use of the auxiliary verb would, which suggests that the event happened more than once.

D because instead suggests that this event happened in place of what was described in the previous sentence. This isn't the case since the sentence offers an idea that is in line with the preceding sentence.

Question 30. The best answer is J because it removes unnecessary and redundant phrases from the sentence.

The best answer is NOT:

F because it is redundant. The essay makes clear that the narrator worked at the Renaissance fair during summer and that the fair closed once the three months were over.

G because it needlessly repeats the idea that the narrator's work ended when the fair closed.

H because it is redundant; the essay has already made clear that the fair took place during the summer.
Passage III

**Question 31. The best answer is A** because no punctuation is needed here. The absence of punctuation creates the clearest and most understandable sentence explaining that the blast of water was caused by a breach in the reservoir.

The best answer is NOT:

B because it adds an unnecessary and confusing comma between *by* and *a breach*.

C because it adds an unnecessary and confusing comma between *caused* and *by*.

D because it adds an unnecessary and confusing comma between *water* and *caused*. This comma sets up the information about the cause as nonessential, but it leaves the first part of the sentence as a fragment.

**Question 32. The best answer is J** because it begins the sentence with the pronoun *it*, which agrees in number with the singular noun *blast*, to which *it* refers.

The best answer is NOT:

F because it begins the sentence with the plural pronoun *they*, which does not agree in number with the noun *blast*, which is singular.

G because it begins the sentence with the subordinating conjunction *that*, which results in a sentence fragment (an incomplete sentence).

H because it begins the sentence with a subordinating conjunction *which* and therefore results in a sentence fragment.

**Question 33. The best answer is B** because the singular possessive form *park’s* is the correct punctuation here. In addition, a comma is required after the word *time* in order to set off the dependent clause that begins the sentence from the main clause of the sentence.

The best answer is NOT:

A because it uses the plural *parks* rather than the possessive *park’s*, which would correctly show possession.

C because it incorrectly uses the plural possessive *parks’*. The phrase “one of Missouri’s most popular state parks” clearly identifies Johnson’s Shut-Ins as one state park.

D because it fails to include a comma after *time*, which is required to set off the dependent clause that begins the sentence from the main clause of the sentence.
ENGLISH • PRACTICE TEST 2 • EXPLANATORY ANSWERS

Question 34. The best answer is G because the word ultimately is logical and indicates chronology. Despite the marred beauty, over a billion years’ worth of history was revealed in the end (or, ultimately).

The best answer is NOT:

F because the word specifically calls for one or more precise examples. The sentence instead mentions a large swath of history without specific examples.

H because the word instead signals a change from what was expected, which doesn't make sense in the context of the sentence.

J because the word thus indicates a cause-effect relationship between the marred beauty and the revealing of over a billion years’ worth of Earth's geologic history. No such cause-effect relationship exists.

Question 35. The best answer is C because it uses the verb began, which is the appropriate tense and verb form in this sentence.

The best answer is NOT:

A because had began is an incorrect verb form.

B because the verb begun needs an auxiliary verb, such as had, in order to be correct.

D because it uses the verb begun without an accompanying auxiliary verb.

Question 36. The best answer is H because no punctuation is needed here. The dependent clause that begins with when should follow immediately after the main clause.

The best answer is NOT:

F because adding a period after ago results in a sentence fragment (incomplete sentence) beginning with the word when.

G because it incorrectly adds a semicolon after ago, separating a dependent clause from an independent clause. A semicolon must separate two independent clauses.

J because it removes the subordinating conjunction when, resulting in a run-on, or fused, sentence.
**Question 37. The best answer is D** because it is the only concise and clear option that presents the idea of cooling without being redundant.

**The best answer is NOT:**

A because it is unnecessarily wordy; *cooling* already encapsulates the idea of temperature.

B because “cooled down” means to come to a lower temperature; the phrase is redundant.

C because “lowered its temperature” means to cool; the phrase is redundant.

**Question 38. The best answer is F** because no punctuation is needed here. The absence of punctuation creates the clearest and most understandable sentence about the substance that was formed, rhyolite.

**The best answer is NOT:**

G because the punctuation suggests that the word *rhyolite* provides a definition or clarification about silica-rich. As a noun (rather than an adjective), *rhyolite* cannot serve this function.

H because it suggests that *rock* (all rock) is silica-rich rhyolite formed by the cooling and crystallizing of slow-moving magma, which is illogical.

J because it adds an unnecessary and confusing comma between the verb *form* and the noun indicating what was formed, silica-rich rhyolite rock.

**Question 39. The best answer is B** because it provides information that helps explain the park’s name (*Johnson’s Shut-Ins*), which otherwise might confuse readers.

**The best answer is NOT:**

A because the essay provides no evidence that people feel shut in when visiting the park.

C because the phrase does not depart from the overall tone of the essay, which is neither formal or informal. Rather, the phrase has a direct relationship to the park’s name and should be included.

D because the phrase contributes to, rather than interrupts, the description of the Black River.
Question 40. The best answer is H because it places a comma between the main clause and the explanatory participial phrase that follows it.

The best answer is NOT:

F because it inserts the conjunction and before the word creating. This creates a compound predicate wherein the two verbs must be parallel. In this case, creating is not parallel with confined.

G because it incorrectly places a semicolon between a main clause and a participial phrase. A semicolon must separate two independent clauses.

J because it places a comma between the two verbs in a compound predicate. A conjunction is needed to make this construction grammatical.

Question 41. The best answer is A because it uses the singular possessive pronoun its, which agrees with the singular noun surge, and it uses the preposition in to clearly describe the water cutting a path through the region.

The best answer is NOT:

B because it uses the preposition on, which suggests that the surge of water followed a path that was already there. It also uses the plural possessive pronoun their, which does not agree in number with the singular noun surge.

C because it uses the plural possessive pronoun their, which does not agree in number with the singular noun surge.

D because it uses the preposition on, which suggests that the path was already there. In more clearly indicates that the surge of water created the path.

Question 42. The best answer is J because it uses the singular verb contains, which agrees in number with the subject of the sentence, channel, which is also singular.

The best answer is NOT:

F because it uses the plural verb contain, which does not agree in number with subject of the sentence, channel.

G because it uses the verb have, which does not agree in number with the sentence's subject, channel.

H because are does not agree in number with the sentence's subject, channel.
Question 43. The best answer is C because it is clearest about who is returning to the park (swimmers, hikers, and campers), and its tone is consistent with the rest of the essay.

The best answer is NOT:

A because it uses the vague pronoun some, which does not clearly explain who or what has returned to the park.

B because it features an informal tone that departs from the tone of the rest of the essay.

D because it features an informal tone that doesn't fit in the essay.

Question 44. The best answer is J because it is the only option that does not introduce a redundancy into the sentence.

The best answer is NOT:

F because it is redundant; the idea contained in the word back is already conveyed by returned.

G because it is redundant; the idea of coming back to the park is already conveyed by returned.

H because it is redundant; to revisit the park is already conveyed by returned.

Passage IV

Question 45. The best answer is A because no punctuation is needed here. The absence of punctuation creates the clearest and most understandable sentence explaining that the narrator was peering through light-polluted skies.

The best answer is NOT:

B because it incorrectly sets off “peering through” as nonessential information and leaves the main clause incomplete: “inexperienced astronomer light-polluted skies.”

C because it incorrectly places a colon after astronomer, suggesting that the phrase “peering through light-polluted skies” defines the term “inexperienced astronomer.”

D because it incorrectly uses a comma to separate the preposition through from the noun light-polluted skies.
**Question 46. The best answer is H** because it correctly creates an independent clause, which is necessary following a comma plus and construction.

The best answer is NOT:

F because it has the participle being, which cannot function as a main verb. The result is that the second part of the sentence is not an independent clause.

G because it includes the pronoun them, which does not clearly refer to a noun previously mentioned in the paragraph. Also, “by them” interrupts the verb phrase “is said to be.”

J because it uses the participle having in place of a main verb, which means that the second part of the sentence is not an independent clause.

**Question 47. The best answer is A** because it correctly uses commas to set off the phrase “in some mythologies.” In this sentence, the phrase is nonessential information, so using commas around the phrase is appropriate.

The best answer is NOT:

B because it sets off the phrase “who in some mythologies” from the rest of the sentence and results in a confusing sentence that suggests Orion and the hunter are separate figures and that Orion only appears when a hunter fights Taurus the Bull: “Orion appears as a hunter is fighting Taurus the Bull, another constellation.”

C because it indicates that the phrase “in some mythologies is fighting Taurus the Bull” is nonessential information. Setting off the phrase in this way results in an ungrammatical sentence: “Orion appears as a hunter who another constellation.”

D because it sets off the phrase “some mythologies” as nonessential and results in an ungrammatical sentence: “Orion appears as a hunter who in is fighting Taurus the Bull, another constellation.”

**Question 48. The best answer is H** because it uses the plural verb are, which agrees in number with the plural subject of the sentence, stars. In addition, the verb form are is in the present tense, as are the verbs in the preceding sentence.

The best answer is NOT:

F because it uses the singular verb has, which does not agree in number with the sentence’s subject, stars.

G because it uses the past progressive were being when the context of this sentence and the preceding sentence call for the present tense.

J because it uses the singular verb is, which does not agree in number with the sentence’s subject, stars.
**Question 49.** The best answer is C because it is the only option that contains a main clause and, therefore, is the only one that is a complete sentence.

The best answer is NOT:

A because it does not contain a main clause. The dependent clause “when gravity causes gas and dust to collapse” is followed by a participial phrase that lacks a subject, “forming stars.”

B because it lacks a main clause. This option is one long dependent clause.

D because it lacks a main clause, consisting instead of one dependent clause.

**Question 50.** The best answer is J because it correctly punctuates the appositive phrase “home to thousands of young stars” by putting commas around it. This phrase adds nonessential information that helps define nebula.

The best answer is NOT:

F because it offers two phrases that begin with the verb is and connects those phrases only with a comma; this sentence structure would require the linking word and in place of the comma.

G because it incorrectly connects the two phrases beginning with is with a comma and the linking word and (rather than with the linking word alone).

H because it correctly sets off “home to thousands of young stars” as nonessential but incorrectly adds the conjunction and, which results in an ungrammatical sentence: “The nebula and is often called a ‘galactic nursery.’”

**Question 51.** The best answer is D because the Great Orion Nebula is introduced in the sentence preceding Point D. The added sentence expands on the discussion of that nebula.

The best answer is NOT:

A because the nebula has not yet been mentioned at this point in the paragraph, so placing the sentence here is illogical and confusing.

B because the nebula has not yet been mentioned at this point in the paragraph.

C because the nebula has not yet been mentioned at this point in the paragraph.
Question 52. The best answer is J because the word *so* serves as a logical transition from the preceding sentence, which discusses the narrator’s struggle to get the nebula in focus, to this sentence, which explains that the narrator switches to a higher-powered eyepiece. The word *so* conveys the idea of intent or purpose; the narrator switches the eyepiece in an attempt to bring the nebula into focus.

The best answer is NOT:

F because the narrator purposely switches to a higher-powered eyepiece to bring the nebula into focus. The switch is not coincidental.

G because the word *similarly* indicates a comparison; no comparison is stated or implied in the paragraph.

H because the word *besides* indicates that a previous idea is being added onto, which isn’t the case.

Question 53. The best answer is A because it correctly uses the past tense verbs *tried* and *had* (*I’d*). At this point in the essay, the narrator is describing a past event, so the past tense is called for.

The best answer is NOT:

B because the contraction “I’d have” suggests the conditional “I would have.” This shifts the meaning to a hypothetical situation in the past that is not supported by the essay.

C because it uses the present tense *try* rather than the past tense *tried*.

D because it uses the present tense *try* rather than the past tense *tried*.

Question 54. The best answer is G because it correctly uses the word *them* to refer to the distant objects, whereas the phrase “one side of them” clearly explains that the viewer is looking to one side of the distant objects.

The best answer is NOT:

F because it is unclear and illogically suggests that objects have only one side.

H because it incorrectly substitutes the contraction *they’re* for the possessive pronoun *their*.

J because *one’s* is ambiguous in meaning. This could mean a distant object’s side or a viewer’s side.
Question 55. The best answer is B because the sentence explains how averted vision works. Deleting the sentence would result in an essay that is less clear.

The best answer is NOT:

A because it does not elaborate on why the narrator was capable of using averted vision. Rather, the sentence explains how averted vision works.

C because the level of technical detail is not out of place in this essay, which describes details about using a telescope to view a nebula.

D because the main point of the paragraph is to explain how the narrator was able to view the nebula. Using the principle of averted vision was the key strategy for the narrator. Rather than digressing from the main point, it helps explain the main point.

Question 56. The best answer is H because it correctly establishes the comparison the narrator is making. The view with averted vision is far better than the view when looking directly at the nebula.

The best answer is NOT:

F because it indicates the wrong comparison. This phrase suggests that both averted and direct vision resulted in a better view, but averted vision permitted more of that same better view. The essay does not support this comparison.

G because it suggests that averted vision resulted in a farther view and incorrectly adds a comma between the modifier (farther) and the object it modifies (view). This is confusing in meaning and is not supported by the essay.

J because it indicates that far and better are coordinate adjectives (adjectives that can be switched without affecting the meaning of the sentence). The idea of a better, far view is unclear and unsupported by the essay.

Question 57. The best answer is A because the word illuminated makes sense in this context. The four bright stars help reveal the Trapezium star cluster.

The best answer is NOT:

B because the word emanated suggests that the cluster was spread out by or flowed from the bright stars. The bright stars are part of the cluster; the cluster does not emanate from them and is not emanated by them.

C because the word emulated suggests the idea of copying; the four bright stars are not copying the star cluster.

D because the word eliminated suggests that the bright stars are destroying the cluster. This is not supported by the essay.
ENGLISH • PRACTICE TEST 2 • EXPLANATORY ANSWERS

Question 58. The best answer is F because the plural possessive birds’ and the plural eggs correctly convey that the stars look like eggs laid by birds in a nest.

The best answer is not:

G because it uses the singular possessive bird’s instead of the plural possessive. To be correct, the pronoun would need to be preceded by an article such as a, but no such article is present.

H because the noun birds lacks the apostrophe that is necessary to convey the idea of possession.

J because it lacks an apostrophe with birds and uses an erroneous apostrophe after eggs, suggesting that the eggs possess something. No such possession is supported by the essay.

Question 59. The best answer is A because it concludes the essay by referring back to an idea presented in the first paragraph of the essay, as required by the stem. The sentence refers to the narrator’s trek outside during the winter, which is mentioned in the first paragraph of the essay.

The best answer is not:

B because it introduces additional tips for using telescopes rather than referring back to the first paragraph of the essay.

C because it suggests that the narrator’s goal was to view Orion’s belt and sword and explains that Orion is useful in locating other constellations. Orion’s sword and belt and any relationship between Orion and other constellations are not mentioned in the first paragraph of the essay.

D because it introduces more information about the Trapezium star cluster and the narrator’s reading. These ideas do not have any connection to the first paragraph of the essay.

Question 60. The best answer is G because the essay focuses on one particular experience of viewing the constellation Orion, from setting up the telescope to focusing on one specific part of the constellation, the nebula.

The best answer is not:

F because it states that the essay recounts several past events, yet only one experience is discussed in the essay.

H because it indicates that the essay focuses on the Orion Nebula and its process of star formation are the focus of the essay. Although the Orion Nebula is a significant part of the essay, the essay does not discuss the process of star formation in the nebula. Rather, it focuses on the narrator’s experience.

J because it implies that averted vision is the main subject of the essay, which isn't the case. Additionally, the fact that the narrator describes the averted vision technique in brief does not demonstrate that the essay is about a personal experience with astronomy.
Passage V

**Question 61. The best answer is D** because it results in a complete sentence with a comma separating the main clause from the appositive phrase “metaphors for Little’s feelings about social issues and historical events.”

The best answer is NOT:

A because it creates a comma splice (two or more complete sentences separated by only a comma). The word *they* becomes the subject of the second complete sentence. The sentence requires a conjunction after the comma in order to be grammatical. The phrase “in other words” cannot function as a conjunction.

B because it creates a comma splice with the second sentence beginning with *they*.

C because it creates a run-on, or fused, sentence (two complete sentences with no punctuation between them).

**Question 62. The best answer is G** because it meets both criteria of the question. It is punctuated correctly with dashes that set off the phrase “mostly triangles and rectangles.” This punctuation also indicates that all Little’s shapes, not just his triangles and rectangles, are painted in vibrant and contrasting hues.

The best answer is NOT:

F because although the punctuation is acceptable, the resulting sentence suggests that only the triangles and rectangles are painted in vibrant and contrasting hues.

H because it is not correctly punctuated. The phrase “and narrow rectangles” should be included in the dashes along with “mostly triangles.” Also, it is unclear whether all the shapes (or only the rectangles) are painted in vibrant and contrasting hues.

J because although the punctuation is acceptable, the resulting sentence suggests that only the triangles and rectangles are painted in vibrant and contrasting hues.

**Question 63. The best answer is B** because it correctly sets off the nonessential phrase “he says” using commas.

The best answer is NOT:

A because it fails to use punctuation to set off the phrase “he says” from the rest of the sentence.

C because it incorrectly sets off his subject as nonessential information, creating an ungrammatical sentence: “But he says is color.”

D because it lacks the necessary comma after *says* that closes the nonessential phrase “he says.”
**Question 64. The best answer is H** because the sentence, although informative, is not strongly related to the paragraph’s general discussion of Little’s art. Adding information about Syracuse University would blur the focus of the first paragraph.

**The best answer is NOT:**

F because the sentence does not contain the kind of biographical information that would clearly connect to the paragraph that follows and therefore would not make for a smooth transition.

G because the sentence does not state that Little first became focused on color at Syracuse University.

J because the sentence does not create confusion about Little’s work with geometric figures; it simply offers a detail about the school where Little earned his MFA, Syracuse University.

**Question 65. The best answer is D** because it is the only option that does not introduce a redundancy into the sentence.

**The best answer is NOT:**

A because it repeats the idea that Little blends his own paint, which is mentioned in the previous sentence.

B because it repeats the idea from the previous sentence that Little blends his own paint. Also, the idea that Little does so is already conveyed in the action word *applies*.

C because it repeats the idea that Little makes his own blends of paint. This is mentioned in the previous sentence. Also, the phrase “his own blends that he made” is redundant; it is unnecessary to state that his own blends are those that he made.

**Question 66. The best answer is J** because it most clearly and logically conveys the idea that Little’s paintings are big, as the measurements (6 feet by 8 feet) make clear.

**The best answer is NOT:**

F because *voluminous* would convey an idea about how much something can hold or about a three-dimensional aspect; this is an illogical descriptor for a painting and is not supported by the two-dimensional measurements that follow in the sentence.

G because it contradicts other information in the sentence. The measurements of the paintings are provided in the sentence, so it clearly cannot be immeasurable.

H because *mountainous* suggests a three-dimensional shape that is neither conveyed nor supported by the two-dimensional measurements that follow in the sentence.
Question 67. The best answer is B because the phrase “for example” serves as a transition from the preceding sentence, which discusses Little's use of color and lines, to this paragraph, which provides a specific description of one of Little's paintings that uses lines.

The best answer is NOT:

A because the phrase “by all means” doesn't make sense in this context. This idiomatic expression has no connection to the sentence in which it is placed. On a literal level, the lines do not bisect the painting in all directions or by all methods.

C because the phrase “in contrast” suggests that Bittersweet Victory differs from Little's other work. Yet the essay explains that Little often uses lines and then focuses on the lines in Bittersweet Victory as a specific example.

D because the word thereafter doesn’t make sense in this context, especially because Bittersweet Victory was painted before the work discussed in the preceding paragraph.

Question 68. The best answer is G because it is the only unacceptable alternative to the underlined phrase. The phrase “vertically beige” offers a misplaced modifier; something cannot be beige in a vertical way.

The best answer is NOT:

F because it conveys the same idea as the underlined phrase. The canvas is bisected in a vertical direction by a beige line.

H because it conveys the same idea as the underlined phrase, that the canvas is bisected by a vertical, beige line.

J because it conveys the same idea as the underlined phrase, that the canvas is bisected by a vertical, beige line.

Question 69. The best answer is C because the participle stretching creates a grammatical sentence that also makes sense.

The best answer is NOT:

A because it inserts the subordinating which into this clause, which was already subordinated from the main clause. This creates a confusing sentence structure. This option also shifts verb tense from the present to the past.

B because it inserts the subordinating which, creating multiple and confusing levels of subordinating clauses.

D because it creates an independent clause (“each one stretches from the bottom to the top of the canvas”) in the middle of another independent clause (“three orange triangles angle slightly to the right”). The result is an unclear sentence created from a series of phrases that are spliced together.
Question 70. The best answer is J because it is the only option that does not introduce a redundancy into the sentence.

The best answer is NOT:

F because it mentions that the orange triangles are on the canvas’s left half, which is a detail that appears previously in the sentence.

G because it repeats the idea that the triangles are on the left half of the canvas.

H because it repeats the idea, stated previously in the sentence, that the triangles appear on the left half of the canvas.

Question 71. The best answer is C because it uses the plural verb cut, which agrees in number with the plural subject of the sentence, bands. It also uses the preposition through, which makes sense in the sentence.

The best answer is NOT:

A because it uses the singular verb cuts, which does not agree in number with the plural subject of the sentence, bands.

B because it uses the singular verb cuts, which does not agree in number with the plural bands. It also uses the past tense verb crossed as if it were a preposition, which is incorrect.

D because it uses the past tense verb crossed as if it were a preposition, which is incorrect.

Question 72. The best answer is F because it attaches the preposition to to the verb lends, which creates a correct idiomatic expression.

The best answer is NOT:

G because it uses the preposition on with lends, which isn’t a correct idiomatic expression. It also doesn’t make sense logically.

H because it uses the preposition into with lends, which creates an incorrect idiomatic expression. Also, this phrase doesn’t make logical sense.

J because it uses the preposition with with lends, which creates an incorrect idiomatic expression.
Question 73. The best answer is C because it conveys the comparison between the effect of Little's work and a jazz collaboration in the most clear and concise way. It does not repeat the same idea, and it does not add unnecessary words to the sentence.

The best answer is NOT:

A because the idea that something is like something else already conveys the idea that it might remind you of something else.

B because reminiscent of and echoes are redundant, making the phrase itself unnecessarily wordy.

D because it appears to be more concise, but the meaning is unclear. It could suggest that the effect of Little's work is like a jazz collaboration, that Little's work makes the viewer feel like he or she is in a jazz collaboration, or that Little's work makes it seem like he is part of a jazz collaboration.

Question 74. The best answer is F because it builds on the paragraph's previous reference to rhythm and unity by mentioning a perfect jazz collaboration and offers a comparison between Little and this jazz collaboration.

The best answer is NOT:

G because the comparison to jazz does not indicate anything about the popularity of Little's paintings.

H because the following paragraph mentions one person's assessment of Little's work, not several people's.

J because the essay does not suggest that Little had any unique goals for Bittersweet Victory. Rather, the paragraph about Bittersweet Victory provides a specific example of the ideas the essay presents about Little's work in general.

Question 75. The best answer is B because the essay discusses how Little uses bright colors and shapes to convey energy and the essence of people's experiences as human beings.

The best answer is NOT:

A because the essay does not focus on one viewer's conclusion that the lines in Bittersweet Victory communicate optimism.

C because the essay does not focus on what Little hoped to create with Bittersweet Victory, and it does explain what the painting looks like.

D because the essay does in fact suggest some of the effects Little's work achieves.
**Question 1.** The correct answer is C. The restaurant is rotating 180° in 45 minutes. That is 60° every 15 minutes. That is 240° every 60 minutes. You might want to sketch something similar to the following drawing:

If you like an algebraic solution, you can set up a proportion \( \frac{180°}{45 \text{ min}} = \frac{x°}{60 \text{ min}} \) and solve it:

\[ x = \left( \frac{180}{45} \right) 60 = 4 \cdot 60 = 240. \]

Most people who do not get this right choose D, which is a reasonable approximation.

**Question 2.** The correct answer is H. After subtracting the onetime fee from the amount on Brendan's check ($500 − $140), the remaining $360 goes toward the amount spent on monthly fees. You can find the number of months of membership covered by the check by dividing the remaining $360 by the monthly fee of $40 per month, giving 9 months as the result.

You could also solve this problem by setting up and solving the equation 140 + 40m = 500, where the expression 140 + 40m represents the cost of a gym membership for m months.

**Question 3.** The correct answer is D. The group of 27 people paid a total of $249.75 (27 × $9.25 per person) in advance. Because the group consisted of more than 25 people, the actual cost was $229.50 ($27 × $8.50 per person). The refund is the difference between the amount paid and the actual cost, which is $249.75 − $229.50 = $20.25. If you chose C, you could have failed to read the problem carefully and figured the refund for a group of 25 people.

**Question 4.** The correct answer is H. The number of possible outcomes (that is, the total number of members eligible to be chosen as representative) is 13 − 3 = 10, and the number of favorable outcomes (choosing Samara only) is 1. The probability of the favorable outcomes is equal to \( \frac{\text{the number of favorable outcomes}}{\text{the number of possible outcomes}} \). So, the probability of Samara being chosen as representative would be \( \frac{1}{10} \). Careful reading is essential; if you chose G, you may have overlooked the words CANNOT and NOT.
**Question 5. The correct answer is D.** Let \( s \) represent the score on the sixth test. Then the average score on the 6 tests is equal to \( \frac{75 + 70 + 92 + 95 + 97 + s}{6} \), or equivalently \( \frac{s + 429}{6} \). Be sure to read carefully: the average is 85 points, not percent. Interpreting the average as a percent leads to E (the most common incorrect answer), rather than the correct answer of \( \frac{s + 429}{6} = 85 \).

**Question 6. The correct answer is F.** The sum of the measures of all four interior angles in any quadrilateral is always 360°. The given three angle measures add up to 65° + 100° + 75° = 240°, so the missing angle measure is 360° − 240° = 120°.

If \( \overline{AB} \) was parallel to \( \overline{CD} \), then the measure of \( \angle B \) and the measure of \( \angle C \) would add up to 180° and the answer would be G. But the problem does not say that those sides are parallel, and it turns out that they are not parallel.

If you chose K, you may have calculated the average of the three given angle measures.

**Question 7. The correct answer is C.** The shorter two sides are the same length in \( \triangle ABC \), so the same thing has to happen in any triangle similar to it. That means that \( \overline{DE} \) is the same length as \( \overline{EF} \), which is 3 meters. Then, the perimeter of \( \triangle DEF \) is 3 + 3 + 5 = 11 meters.

The most common incorrect answer is A, correctly finding the length of \( \overline{DE} \) and stopping there.

**Question 8. The correct answer is G.** Follow the correct order of operations to simplify the expression. \( |3(-2) + 4| = |-6 + 4| = |-2| = 2 \). Keep in mind that absolute value of a rational number is its distance from 0 on the number line.

You may have chosen F if you did not take the absolute value of −2. You may have chosen H if you did \( |3 - 2 + 4| \). You may have chosen J if you did \( |3 + 2 + 4| \). You may have chosen K if you did \( |3(2) + 4| \).

**Question 9. The correct answer is A.** This problem is asking you to figure out when two quantities multiplied together can be zero. The only way two quantities can be multiplied together to get an answer of zero is if at least one of the quantities is zero. So, either \( (x + a) = 0 \) or \( (x + b) = 0 \). The first of these equations is true when \( x = -a \) and the second when \( x = -b \). These are the two solution values for \( x \).

As a check, substitute \(-a\) in for \( x \). The original equation becomes \( (-a + a)(-a + b) \), which simplifies to \( (0)(-a + b) \), and zero times anything is zero, so the original equation holds when \( x = -a \). You could check \( x = -b \) in the same manner.

If you chose E, you may have solved the two equations incorrectly, or you may have just looked at the quantities and chosen the +\( a \) and +\( b \) that appeared in the problem.

If you missed this problem, you might try substituting a value of \( x \) from your answer into the original equation to see what happens.
Question 10. The correct answer is F. Because $\angle LM > 90^\circ$ and $\angle MK$, $\angle JMG$, $\angle LHK$, $\angle MJL$ are all less than or equal to $90^\circ$, $LM$ has the greatest degree measure.

We know that $\angle JMG = 90^\circ$ (H is NOT correct) because the tangent to a circle is always perpendicular to the radius drawn to the point of tangency. Because $\triangle MGJ$ is a right triangle with right angle $\angle JMG$, the other angles in the triangle, $\angle MJG$ and $\angle MGJ$, are acute. This means that $\angle MJL < 90^\circ$ (K is NOT correct) and $\angle MK < 90^\circ$. Because the degree measure of an arc of a circle is equal to the measure of the central angle that intercepts that arc, $\angle MK = \angle LM$. Therefore, $\angle MK < 90^\circ$ (G is NOT correct). Because $\angle LHK$ is inscribed in semicircle $LH$, $\angle LHK = 90^\circ$ (J is NOT correct).

Question 11. The correct answer is B. To find $BC$ when $AD$ is 30 units, $AC$ is 16 units, $BD$ is 20 units, and the points are along $\overline{AD}$ as shown in the following, you must notice that $BC$ is the intersection of $AC$ and $BD$.

So the sum of the lengths of $\overline{AC}$ and $\overline{BD}$ would be the same as the sum of the lengths of $\overline{AD}$ and $\overline{BC}$, because $AC = AB + BC$, $BD = BC + CD$, and $AD = AB + BC + CD$. By substitution, $AC + BD = AB + BC + BD = BC + CD = AB + BC + CD + BC = AD + BC$.

By substituting lengths $AD + BC = AC + BD$, or $30 + BC = 16 + 20$, or $30 + BC = 36$. Subtracting 30 from both sides yields $BC = 6$.

If you chose A, you probably subtracted 16 from 20. If you chose E, you probably thought you needed more information to solve the problem.

Question 12. The correct answer is K. There are many ways to solve this equation. One solution is the following:

<table>
<thead>
<tr>
<th>Step</th>
<th>Equation</th>
</tr>
</thead>
<tbody>
<tr>
<td>start with</td>
<td>$12x = -8(10 - x)$</td>
</tr>
<tr>
<td>divide both sides by $-8$</td>
<td>$\Rightarrow \frac{3}{2}x = 10 - x$</td>
</tr>
<tr>
<td>add $x$ to both sides</td>
<td>$\Rightarrow \frac{1}{2}x = 10$</td>
</tr>
<tr>
<td>multiply both sides by $-2$</td>
<td>$\Rightarrow x = -20$</td>
</tr>
</tbody>
</table>

Another solution method would be to graph $y = 12x$ and $y = -8(10 - x)$ and see where the two graphs intersect. A calculator would produce these graphs, and you could find an approximate solution. That is good enough for this problem because the answer choices are spread apart.
This is a problem in which checking your answer is easy and can pay off. When \( x = -20 \), the left side of the original equation is \( 12(-20) \), which is \( -240 \). The right side is \( -8(10 - (-20)) \), which simplifies to \( -8(10 + 20) \), then to \( -8(30) \), and then to \( -240 \). This solution checks. No other answer choice would satisfy the equation.

If you chose H or J, you may have multiplied out \( -8(10 - x) \) to get \( -80 + x \) or \( -80 - x \) and done the rest of the steps correctly. You could have caught this by checking your answer. If you made an error with minus signs, you may have chosen one of the other answer choices.

**Question 13. The correct answer is E.** Because the cardboard extends 2 inches beyond the cake on all sides, the cardboard forms a rectangle whose length and width are each 4 inches longer than the length and width of the rectangular cake, as shown in the following figure. The area of aluminum foil that is exposed (the shaded region in the figure) equals the area of the foil covering the entire cardboard surface (or area of the cardboard) minus the area of the foil covered by the cake. So the area, in square inches, of aluminum foil exposed equals \( 20(16) - 16(12) = 320 - 192 = 128 \).

![Figure](https://via.placeholder.com/150)

**Question 14. The correct answer is J.** The following figure shows the cake after it has been cut. The length of the cut cake is \( (16 \text{ inches}) \div (2 \text{ inches per piece}) = 8 \text{ pieces} \). The width of the cut cake is \( (12 \text{ inches}) \div (2 \text{ inches per piece}) = 6 \text{ pieces} \). Because the cake has 6 rows each containing 8 pieces, the cake was cut into \( 6(8) = 48 \) pieces.

![Figure](https://via.placeholder.com/150)
**Question 15. The correct answer is D.** The following table lists all expenses for Ken’s cake that were given in the problem.

<table>
<thead>
<tr>
<th>Expenses for cake</th>
<th>cost</th>
</tr>
</thead>
<tbody>
<tr>
<td>Cake preparation</td>
<td>$5.00</td>
</tr>
<tr>
<td>Cake mix</td>
<td>$1.73</td>
</tr>
<tr>
<td>Frosting mix</td>
<td>$2.67</td>
</tr>
<tr>
<td>Tax on items purchased</td>
<td>0.05($1.73 + $2.67) = $0.22</td>
</tr>
</tbody>
</table>

The total amount the Math Club will pay Ken is the sum of the costs shown in the table, $5.00 + $1.73 + $2.67 + $0.22 = $9.62.

**Question 16. The correct answer is H.** Sketching a picture can be helpful.

These points are on opposite sides of the y-axis, and an equal distance away from the y-axis, because the x-coordinates are 3 and –3. So, the midpoint will be the y-intercept of the line. The y-coordinate of the midpoint is \( \frac{6 + (-2)}{2} \), which is 4.

If the points were not so nicely spaced with the y-axis, you could find the equation of the line through the two points and use it to identify the y-intercept. The slope of the line would be the change in y divided by the change in x, \( \frac{6 - (-2)}{3 - (-3)} = \frac{8}{6} \). The point-slope form of the equation is then \( y - 2 = -\frac{4}{3}(x - 3) \). Next, put this into slope-intercept form \( y - 2 = -\frac{4}{3}x + 2 \Rightarrow y = -\frac{4}{3}x + 2 + 2 \Rightarrow y = -\frac{4}{3}x + 4 \), and the 4 is the y-intercept.

From the picture alone, you could deduce that the line had to cross the y-axis between 2 and 6. This observation eliminates all the answer choices except the correct one.
Question 17. The correct answer is D. Let \( x \) (shown in the following figure) represent the distance between the centers of the 2 holes. Because the 3 segments with lengths \( 2\frac{1}{16} \) inches, \( x \) inches, and \( 4\frac{3}{4} \) inches are collinear, the sum of their lengths must be \( 11\frac{5}{8} \). Therefore,

\[
x = 11\frac{5}{8} - 2\frac{1}{16} - 4\frac{3}{4} = \frac{93}{8} - \frac{33}{16} - \frac{19}{4} = \frac{186}{16} - \frac{33}{16} - \frac{76}{16} = \frac{27}{16} = 4\frac{13}{16} \text{ inches.}
\]

Question 18. The correct answer is H. Each week, both ponds get shallower. The following table shows what happens for the first few weeks.

<table>
<thead>
<tr>
<th></th>
<th>Now</th>
<th>1 week</th>
<th>2 weeks</th>
<th>3 weeks</th>
<th>4 weeks</th>
</tr>
</thead>
<tbody>
<tr>
<td>First pond</td>
<td>180 cm</td>
<td>179 cm</td>
<td>178 cm</td>
<td>177 cm</td>
<td>176 cm</td>
</tr>
<tr>
<td>Second pond</td>
<td>160 cm</td>
<td>159.5 cm</td>
<td>159 cm</td>
<td>158.5 cm</td>
<td>158 cm</td>
</tr>
<tr>
<td>Difference</td>
<td>20 cm</td>
<td>19.5 cm</td>
<td>19 cm</td>
<td>18.5 cm</td>
<td>18 cm</td>
</tr>
</tbody>
</table>

The ponds are getting closer and closer to the same depth, at the rate of 0.5 cm per week. Because the ponds started out 20 cm different, it will take \( 20 \div 0.5 = 40 \) weeks to bring them to the same depth.

You could also check the answer choices. Answer F is not correct because, after 10 weeks, the first pond would be \( 180 - 10 = 170 \) cm deep, and the second pond would be \( 160 - 5 = 155 \) cm deep. The other incorrect answers can be eliminated in the same way.

The most common incorrect answer was G. If you chose that answer, you may have reasoned that it would take 20 weeks for the first pond to get down to the level of the second pond. And that is correct, except that the second pond has become shallower during those 20 weeks, so the ponds are not the same depth.

Question 19. The correct answer is E. A line will always have an equation of the form \( x = a \) or \( y = mx + b \), for suitable constants \( a \), \( m \), and \( b \). And, if a graph has an equation that can be put into one of these forms, the graph is a line.

Equation A is already in the first form, where \( a = 4 \).

Starting with Equation B, divide both sides by 3 and you will get \( y = 2 \). This is the second form, with \( m = 0 \) and \( b = 2 \).

Equation C can be manipulated into the second form as follows: \( x - y = 1 \Rightarrow -y = 1 - x \Rightarrow y = -1 + x \Rightarrow y = x - 1 \), which has \( m = 1 \) and \( b = -1 \).

Equation D is already in the second form, with \( m = \frac{3}{4} \) and \( b = -2 \).
Equation E can be written as $y = -x^2 + 5$. This is the equation of a parabola, shown below. It is the only one of the equations that is not a line.

![Parabola Graph]

**Question 20. The correct answer is G.** All the answer choices are in terms of $\angle A$. Many people remember the trigonometric functions in the context of a right triangle, in terms of the lengths of the side opposite the angle, the side adjacent to the angle, and the hypotenuse. For the triangle given in the problem, the side opposite $\angle A$ has length 12 cm, the side adjacent to $\angle A$ has length 5 cm, and the hypotenuse has length 13 cm. The values of the trig functions are $\cos A = \frac{\text{adjacent}}{\text{hypotenuse}} = \frac{5}{13}$, $\sin A = \frac{\text{opposite}}{\text{hypotenuse}} = \frac{12}{13}$, and $\tan A = \frac{\text{opposite}}{\text{adjacent}} = \frac{5}{12}$.

The only answer choice that gives one of these is G.

If you chose F, you may have been expecting the angle to be at one end of the horizontal base of the triangle. The value of $\cos B$ is $\frac{12}{13}$. Triangles can be rotated to any position. The terms opposite, adjacent, and hypotenuse are chosen to apply when the triangle is in an arbitrary position.

**Question 21. The correct answer is D.** To find the location of the water fountain located halfway between points B and D, it makes sense to give coordinates to the points relative to point A (see the following diagram). The first coordinate is the number of blocks east, and the second coordinate is the number of blocks north.

![Triangle Diagram]

The water fountain is at the midpoint of $\overline{BD}$, and so the midpoint formula applies. For points with coordinates $(x_1, y_1)$ and $(x_2, y_2)$, the midpoint has coordinates $\left(\frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2}\right)$. For $B(10,0)$ and $D(7,9)$, the midpoint is $\left(\frac{10 + 7}{2}, \frac{0 + 9}{2}\right) = \left(\frac{17}{2}, \frac{9}{2}\right) = \left(8\frac{1}{2}, 4\frac{1}{2}\right)$. 
**Question 22. The correct answer is H.** Although it may not be worth your time to sketch a graph during the ACT, you should at least have a general idea of the situation in your mind. This is the equation of a parabola. Common sense will tell you that if the car is going faster, it will take a longer distance to brake to a stop. So the parabola is opening upward.

The horizontal dashed line on the graph is where the braking distance is 150 feet. Only half of the parabola is shown. There are two points where the parabola intersects this line. One would be to the left of the y-axis, which represents a negative speed for the car. If you solve an equation to find the intersection points, you will have to discard the intersection point with a negative speed.

If you took the time to create a graph, perhaps even on a graphing calculator, you might be able to estimate closely enough to choose among the answer choices. The desired speed is the x-coordinate of the intersection point.

To get this speed algebraically, the desired braking distance is 150 feet, and the equation $y = \frac{3(x^2 + 10x)}{40}$ gives the relation between speed $(x)$ and braking distance $(y)$. So you can solve the equation $150 = \frac{3(x^2 + 10x)}{40}$. One solution path starts by multiplying both sides by 40 and continues as follows:

$$150 \cdot 40 = 3(x^2 + 10x) \Rightarrow 6000 = x^2 + 10x \Rightarrow x^2 + 10x - 2000 = 0 \Rightarrow (x + 50)(x - 40) = 0 \Rightarrow x = -50 \text{ or } x = 40.$$ 

You must discard the first solution. The only remaining solution is $x = 40$, which represents a speed of 40 miles per hour.
If you chose J, you may have done everything correctly except that when you solved \((x + 50)(x - 40) = 0\), you thought \(x = 50\) was a solution. If you substitute 50 for \(x\) in the equation \((x + 50)(x - 40) = 0\), you will see that it is not a solution.

If you chose F, you may have made a numerical mistake when you substituted \(x = 10\) into the breaking-distance equation. The value is \(\frac{3(100^2 + 10 \cdot 10)}{40} = \frac{3(200)}{40}\). It might be tempting to reduce \(\frac{200}{40}\) to 50 and then get 3(50) = 150, which is what you are looking for. But \(\frac{200}{40}\) is 5, not 50.

Substituting the answer choices into the equation is a reasonable strategy for this problem. You can use the results from one of the answer choices to help you choose the next one to substitute, because you probably know that it takes longer to stop if you are going faster. The results of these substitutions are given in the following:

<table>
<thead>
<tr>
<th>Speed (mph)</th>
<th>Calculations</th>
<th>Braking distance (ft)</th>
</tr>
</thead>
<tbody>
<tr>
<td>F</td>
<td>10</td>
<td>(\frac{3(200)}{40}) = 3(5)</td>
</tr>
<tr>
<td>G</td>
<td>30</td>
<td>(\frac{3(1200)}{40}) = 3(30)</td>
</tr>
<tr>
<td>H</td>
<td>40</td>
<td>(\frac{3(2000)}{40}) = 3(50)</td>
</tr>
<tr>
<td>J</td>
<td>50</td>
<td>(\frac{3(3000)}{40}) = 3(75)</td>
</tr>
<tr>
<td>K</td>
<td>60</td>
<td>(\frac{3(4200)}{40}) = 3(105)</td>
</tr>
</tbody>
</table>

**Question 23.** The correct answer is A. Substitution gives \(g(4) = \sqrt{4} = 2\) and \(f(1) = 1^2 + 1 + 5 = 7\). Then \(\frac{g(4)}{f(1)} = \frac{2}{7}\).

If you chose C, you may have started substituting 4 in function \(g\) and then continued substituting 4 into function \(f\). The value of \(\frac{g(4)}{f(4)}\) is \(\frac{2}{25}\).

**Question 24.** The correct answer is K. There are 125 juniors who could be chosen. For each of those 125 juniors, there are 100 seniors who could be chosen. That makes \(125 \cdot 100 = 12,500\) different pairs of students who could be chosen.

If you chose J, you probably added 125 and 100. If you chose G, perhaps you were figuring that once 100 pairs were formed, there would be no seniors left to put into another pair. Only one pair will be chosen, but there are many more than 100 pairs that are possible choices.

**Question 25.** The correct answer is B. The line on the graph has a negative linear correlation because as \(x\) increases \(y\) decreases. The line Mia drew goes through the points (0,10) and (3,1). To find the slope, \(m\), we use \(m = \frac{y_2 - y_1}{x_2 - x_1}\), and we get \(m = \frac{10 - 1}{0 - 3} = \frac{9}{-3} = -3\). The \(y\)-intercept, where the line crosses the \(y\)-axis, is at positive 10. Inserted into \(y = mx + b\), where
b is the y-intercept, we get the equation \( y = -3x + 10 \). If you thought A, you did not determine the correct y-intercept. If you thought C or D, you did not determine the correct slope. If you thought E, you did not determine the correct y-intercept or slope.

**Question 26. The correct answer is F.** You could certainly test all of the answer choices to solve this problem. The first choice, –10, leaves the left side of the relation as |–10 – 24|, which simplifies to |–34|, which is 34. And 34 \( \leq 30 \) is false, so this is the correct answer.

Another way to solve this problem is to think about the interpretation of absolute value as a distance: \(|t – 24| \leq 30\) means that the distance on the number line between \( t \) and 24 is at most 30 units. This distance would be greater than 30 only when \( t \) was more than 30 above 24 or more than 30 below 24. That is when \( t \) is more than 54, or \( t \) is less than –6. Answer choices G–K are all closer to 24 than this.

The most common wrong answer is 54 (K), which is right at the limit of how far away it can get from 24. Still, –10 is farther away from 24 than 54 is.

**Question 27. The correct answer is D.** The phrase “5 times a number \( n \)” can be represented as \( 5n \). If this is subtracted from 15, the expression \( 15 – 5n \) represents the result. Saying that this result is negative can be represented as \( 15 – 5n < 0 \). Subtracting 15 from both sides gives \(-5n < –15\), and then dividing both sides by –5 gives \( n > 3 \) (remember to reverse the direction of the inequality).

Most people who missed this chose E. This could come from not reversing the inequality in the last step of the solution, or it could come from subtracting 15 from \( 5n \) rather than subtracting \( 5n \) from 15.

Answer choice B is the result of solving \( 15 – 5n = 0 \). This would give the boundary where the expression changes from positive to negative, so it’s closely related to the problem you were asked to solve. If you chose this, you would still need to find the values of \( n \) where the expression is negative, knowing that \( n = 3 \) is the only place the expression is zero.

**Question 28. The correct answer is F.** Because \((x^2 + 8x + 7) = (x + 7)(x + 1)\), you can factor the numerator further into the product \((x + 1)(x + 7)(x – 3)\). Similarly, because \((x^2 + 4x – 21) = (x + 7)(x – 3)\), you can factor the denominator further into the product \((x + 7)(x – 3)(x + 1)\). Then, as long as the denominator is not zero (that is, as long as \( x \) is not equal to \(-7, 3, \) or \(-1\), which is guaranteed by the requirement that \( x > 21\)), you can write the given rational function as \(\frac{(x + 1)(x + 7)(x – 3)}{(x + 7)(x – 3)(x + 1)}\). Using the Commutative Property for Multiplication, the factors in the numerator can be reordered, producing the equivalent expression \(\frac{(x + 7)(x – 3)(x + 1)}{(x + 7)(x – 3)(x + 1)}\). Because the numerator and denominator are equal, this rational expression is equal to 1.
Question 29. The correct answer is B. Imagine the original 9 data items in order from smallest to largest. You might sketch a picture something like that shown in the following. The median is the fifth item in this list, because it is the middle value in the set.

When the additional 4 data items are put into the list, there are 9 + 4 = 13 items on the list. Because 2 of these items are greater than the original median and 2 of these items are less than the original median, the original median is the middle value in the new set. That makes the original median the new median.

Question 30. The correct answer is K. The shaded area is the area of the larger circle minus the area of the smaller circle. The area of the larger circle is $\pi r^2 = \pi (10)^2 = 100\pi$ square centimeters. The area of the smaller circle is $\pi (5)^2 = 25\pi$ square centimeters. The difference is $75\pi$ square centimeters.

If you chose J, you probably found the difference in the perimeters of the two circles. You may have used the perimeter formula rather than the area formula. Another possibility is that you calculated $10^2$ as $2 \cdot 10$ and $5^2$ as $2 \cdot 5$. But $10^2$ is $10 \cdot 10$, and $5^2$ is $5 \cdot 5$.

Question 31. The correct answer is E. The mean of $a$ and $b$ is $\frac{a+b}{2}$. Because $a$ is positive and $b$ is negative $\frac{a+b}{2} = \frac{|a|-|b|}{2}$. If $|a| > |b|$, then the mean is positive. If $|a| < |b|$, then the mean is negative. If $|a| = |b|$, then the mean is 0. Because we only know the sign of $a$ and $b$ and NOT their magnitudes, we cannot determine if the mean is positive, negative, or 0.

If you chose A, you might not have realized that if $a = 3$ and $b = -4$, the mean of $a$ and $b$ is a negative number: $\frac{3 + (-4)}{2} = -\frac{1}{2}$. If you chose B, you might not have realized that if $a = 4$ and $b = -4$, the mean of $a$ and $b$ is 0: $\frac{4 + (-4)}{2} = 0$. If you chose C, you might not have realized that every number is positive (greater than 0), negative (less than 0), or neither (equal to 0). If you chose D, you might not have realized that the mean could be a positive number or a negative number: if $a = 4$ and $b = -2$, $\frac{4 + (-2)}{2} = \frac{2}{2} = 1$; if $a = 3$ and $b = -4$, $\frac{3 + (-4)}{2} = -\frac{1}{2}$.

Question 32. The correct answer is G. If the $x$-coordinate is 20, then the $y$-coordinate can be found by substituting 20 for $x$.

$$0.005(20)^2 - 2(20) + 200 = 0.005(400) - 40 + 200 = 0.5(4) + 160 = 2 + 160.$$  

In theory, you could read the value off the graph, but you would not be able to read it accurately enough.
Many incorrect answers are caused by mistakes with the first term, $0.005x^2$. If you chose F, you may have made a decimal error calculating $0.005(20)^2$ and gotten 0.2 rather than 2.0. Other errors in calculating this term lead to H, J, and K.

**Question 33. The correct answer is D.** The distance formula (or the Pythagorean theorem) gives this distance directly. It is $\sqrt{(200 - 0)^2 + (0 - 200)^2} = \sqrt{200^2 + 200^2} = \sqrt{2 \cdot 200^2} = 200\sqrt{2} = 200(1.414) = 282.8$

Another way to solve this is to notice that the length of $\overline{FO}$ is 200 units, and $\overline{FG}$ is longer. Also, the path from F to O to G is 400 units long, and the direct path along $\overline{FG}$ is shorter than this path. So D is the only reasonable answer among those given.

**Question 34. The correct answer is F.** The shaded region is entirely contained in the given triangle because the curve is below the hypotenuse of the triangle, $\overline{FG}$. The area of the triangle is made up of the shaded area plus the unshaded area above the curve and inside the triangle. So the shaded area is less than the area of the triangle.

**Question 35. The correct answer is B.** With $a = 4.2$, $b = 5.0$, and a $5^\circ$ measure for $\angle C$, then the law of cosines gives the length of the third side of the triangle (the distance between the cargo ship and the fishing boat) as $\sqrt{(4.2)^2 + (5.0)^2 - 2 \cdot 4.2 \cdot 5.0 \cdot \cos 5^\circ}$.

If you chose C, you probably missed the minus sign in the middle of the expression. About half the students who do not get the correct answer choose C.

The $85^\circ$ angle in answer choices D and E would be the angle measure by the fishing boat, but only if the angle by the cargo ship was a right angle. It turns out that it isn’t a right angle.

**Question 36. The correct answer is F.** Because $a^3 = b$, then $b^2 = (a^3)^2$. Substituting this into the equation $c = b^2$ gives $c = (a^3)^2$. Because $(a^3)^2 = a^6$, the result is $c = a^6$.

The most common incorrect answer is G. If you chose that answer, you probably wrote $(a^3)^2$ as $a^5$. If you write $(a^3)^2$ out as $(a^3)(a^3)$ and then $(a \cdot a \cdot a)(a \cdot a \cdot a)$, you can see that it is $a^6$.

If you chose H, you probably wrote $(a^3)^2$ as $2(a^3)$.

**Question 37. The correct answer is B.** The cost of renting a car from Sea Horse for 2 days is $2(50) + 0.25m$ where $m$ is the number of miles driven. Because Francisco has $255 to spend, the maximum number of miles he can drive if he rents from Sea Horse is the solution to the equation $100 + 0.25m = 255$, or $m = 160$.

Similarly, the maximum number of miles Francisco can drive if he rents from Ocean Blue is the solution to $2(60) + 0.20m = 255$, or $m = 675$, because $675 - 620 = 55$. If Francisco rents from Ocean Blue, he can travel 55 miles more than if he rents from Sea Horse. If you chose A, you may have made an error when solving $100 + 0.25m = 255$ and $2(60) + 0.20m = 255$. If you chose C, you may have divided cost per day by the cost per mile for each company, and then subtracted those quotients; Ocean Blue Car Rental has the greater quotient. If you
chose D, you may have subtracted the daily cost of rental from Ocean Blue Car Rental from the total allotted amount. If you chose E, you may have found that each car rental would give Francisco the same number of miles.

**Question 38. The correct answer is G.** The area of a parallelogram is given by $bh$, where $b$ is the length of the base and $h$ is the height (here, the distance between the bottom and the top). It sometimes helps to picture this formula geometrically.

![Parallelogram Diagram](image)

If you cut off the right triangle from the right side, it fits exactly onto the left side to form a rectangle. The rectangle has the same area as the parallelogram. The rectangle's area is $bh$, where $b$ is the length of the base and $h$ is the height. This is even the same formula as for the parallelogram. The difference is that $h$ is the length of a side of the rectangle, but it is not the length of a side of the parallelogram.

And so, for either the rectangle or the parallelogram, $b = 10$ coordinate units and $h = 6$ coordinate units, making the area $bh = 10 \cdot 6 = 60$ square coordinate units.

The distance from (0,0) to (3,6) is $\sqrt{3^2 + 6^2} = 3\sqrt{1^2 + 2^2} = 3\sqrt{5}$ coordinate units. If you chose J, you probably multiplied this side length by the length of the base, 10 coordinate units. This is the stereotypical mistake when figuring the area of a parallelogram. The picture shows why the height is the right thing to use, not the length of the side.

If you chose H, you may have calculated the length from (0,0) to (3,6) as $\sqrt{6^2 - 3^2} = 3\sqrt{2^2 - 1^2} = 3\sqrt{3}$ and multiplied by the length of the base.

**Question 39. The correct answer is E.** Because $n$ and $m$ are both natural numbers, the sum of $n$ and $m$ is another natural number, $n + m$. Natural numbers are a subset of integers, integers are a subset of rational numbers, rational numbers are a subset of real numbers, and real numbers are a subset of complex numbers. Therefore, $n + m$ belongs to the sets found in I, II, III, IV, and V. If you chose A, you might not have realized that rational numbers are a subset of real numbers and therefore a subset of complex numbers. If you chose B, you might not have realized that the sum of two natural numbers is another natural number, and that real numbers are a subset of complex numbers. If you chose C, you might not have realized that the sum of two natural numbers is another natural number, which is also an integer. If you chose D, you might not have realized that sum of two natural numbers is another natural number.
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Question 40. The correct answer is G. If you don’t see a way to approach this problem right off, a useful general technique is to look for some concrete numbers that illustrate the conditions. One thought is to start checking numbers from 1,000 on up to find a perfect square. A calculator would be a good idea. $\sqrt{1,000} \approx 31.62$, $\sqrt{1,001} \approx 31.64$, $\sqrt{1,002} \approx 31.65$, oh, this will take a while. A perfect square between 1,000 and 9,999 would have to have its square root between $\sqrt{1,000}$ and $\sqrt{9,999}$ because the square root function is an increasing function. This will help you find examples more quickly: $25^2 = 625$ is too low; $35^2 = 1,225$ is in the interval. The smallest perfect square in this interval is $32^2 = 1,024$. Because $100^2 = 10,000$, the largest perfect square in this interval has to be $99^2 = 9,801$. The square roots of all these perfect squares are the integers from 32 up to 99. All these square roots have 2 digits.

A quicker way is to find $\sqrt{1,000} \approx 31.62$ and $\sqrt{9,999} \approx 99.99$, which is a range that contains all possible square roots of the perfect squares. Any integer in this range has 2 digits.

The most common incorrect answer is K. If you chose this answer, perhaps you made a calculation error that led you to believe you’d found a perfect square between 1,000 and 9,999 whose square root had 3 digits. And then you correctly found one whose square root had 2 digits. Your logic was correct. Some students probably choose K because they do not know how to solve the problem. Maybe that’s as good a guess as any, but looking for concrete numbers would be a good strategy if you have time.

Question 41. The correct answer is C. The expected occupancy rate is the sum of the products of each occupancy rate and its corresponding probability:

$$0.6(0.2) + 0.7(0.4) + 0.8(0.3) + 0.9(0.1) = 0.73.$$ To calculate the expected number of rooms that will be occupied during the coming summer season, multiply the expected occupancy rate by the total number of rooms: $0.73(80) \approx 58$.

If you chose A, you might have calculated the average of the probabilities and multiplied that by the total number of rooms: $\left(\frac{0.2 + 0.4 + 0.3 + 0.1}{4}\right)(80)$. If you chose B, you might have converted the probabilities in the table to percentages and then found the average percentage: $\frac{20 + 40 + 30 + 10}{4}$. If you chose D, you might have calculated the average of the complement probabilities and multiplied that by the total number of rooms: $\left(\frac{0.8 + 0.6 + 0.7 + 0.9}{4}\right)(80)$. If you chose E, you might have calculated the complement of the probabilities, converted those complement probabilities to percentages, and then found the average complemented probability: $\frac{60 + 70 + 80 + 90}{4}$.

Question 42. The correct answer is F. To calculate a matrix product, you go across each row in the first matrix and down each column in the second matrix. You multiply the terms from a row by the corresponding terms from the column, and you add all those terms together for the row-column combination and put the sum in that row-column of the result matrix. You do this for each row-column combination.
That explanation is correct but pretty abstract. Your math text might have some examples that you can look over to make things more concrete.

In this case, there is only 1 element in each row of the first matrix, and 1 element in each column in the second matrix. The matrix product is:

\[
\begin{bmatrix}
  a \\
  2a \\
  3a
\end{bmatrix}
\begin{bmatrix}
  1 & -1 \\
  0 & 1 \\
-1 & 0
\end{bmatrix}
= 
\begin{bmatrix}
  a \cdot 1 & a \cdot 0 & a \cdot (-1) \\
  2a \cdot 1 & 2a \cdot 0 & 2a \cdot (-1) \\
 3a \cdot 1 & 3a \cdot 0 & 3a \cdot (-1)
\end{bmatrix}
= 
\begin{bmatrix}
  a & 0 & -a \\
  2a & 0 & -2a \\
3a & 0 & -3a
\end{bmatrix}
\]

The computations in G are basically correct, but the terms were put in the wrong places.

If you chose K, you may have reasoned that whatever role the 1 played in the second matrix, the –1 would cancel it out, and the 0 would not change that. If all the terms were combined, that would be the case. But a matrix can keep the terms separate.

**Question 43. The correct answer is D.** Because the base is a straight line, these two angle measures add up to 180°. In the language of algebra, this can be represented as

\[(4x + 6) + (2x) = 180.\]

Solving this for \(x\) gives

\[4x + 6 + 2x = 180, \quad x + 1 = 30, \quad x = 29.\]

This makes one angle measure \(4(29) + 6 = 122\) degrees and the other angle measure \(2(29) = 58\) degrees. (Check: Is 122° + 58° equal to 180°? Yes.)

The problem asks for the measure of the smallest of these two angles. That is 58°.

If you chose C, you probably just stopped as soon as you found the value of \(x\). The problem asks for something different. The other popular incorrect answer is E.

**Question 44. The correct answer is F.** The new value of \(b\) is \((b - 1)\), and the new value of \(c\) is \((c + 2)\). Substituting into the expression for \(a\) gives \(2(b - 1) + 3(c + 2) - 5\), which simplifies to \(2b - 2 + 3c + 6 - 5\). Because you are looking for the change in \(a\), try to write this expression in terms of the original expression for \(a\). You can do this as \(2b + 3c - 5\) minus \(2 + 6\), which simplifies to \((2b + 3c - 5) + 4\). And that is the old value of \(a\) increased by \(4\).

If you chose H, you may have expanded \(2(b - 1) + 3(c + 2)\) to \(2b - 1 + 3c + 2\).

**Question 45. The correct answer is C.** We want to find the number of gallons of fertilizer, \(x\), for which the rate \(\frac{x}{0.5\text{ acre}}\) is equal to \(\frac{1\text{ fl. oz}}{40\text{ sq. ft}}\). We do this by solving for \(x\):

\[x = \frac{1\text{ fl. oz}}{40\text{ sq. ft}} \times \frac{0.5\text{ acre}}{1}\]

and then multiplying by the conversion factor given in the item. We want to eliminate all units besides gallons to get the answer:

\[x = \frac{1\text{ fl. oz}}{40\text{ sq. ft}} \times \frac{0.5\text{ acre}}{1} \times \frac{43,650\text{ sq. ft}}{1\text{ acre}} \times \frac{1\text{ gal}}{128\text{ fl. oz}} = \frac{0.5(43,560)}{40(128)}\text{ gallons.}\]

You may have gotten A if your conversion setup did not eliminate acres in the numerator and had gallon in the denominator, so you got acre per gallon.
You may have gotten B if your conversions were inverted and you found per gallon. You may have gotten D if you divided by 0.5 acre instead of multiplying by 0.5 acre and therefore got gallon per acre. You may have gotten E if your conversion did not eliminate square feet in the numerator and fluid ounces in the denominator and got square feet times gallon per fluid ounce.

**Question 46. The correct answer is J.**

Because no booths can be empty, imagine 1 person sitting in each booth. That leaves 10 people standing around waiting for you to tell them where to sit. How many booths can you fill up with another 3 people each? Well, you can get 3 groups of 3 people from the 10 who are still standing, with 1 person left over. That means that you can fill at most 3 booths with 4 people. There will be 1 booth with 2 people, and the other 6 booths will have 1 person. (Check: Are there 20 people? 3(4) + 0(3) + 1(2) + 6(1) = 12 + 2 + 6 = 20. Yes. Are there 10 booths? 3 + 0 + 1 + 6 = 10. Yes.)
If you chose K, you filled up 5 booths with 4 people each. But, you left the other 5 booths with no one sitting there. The problem specified that NO booths are empty. (This is the most common wrong answer.)

If you chose G, you may have just miscounted. Make sure you check your work. You might want to draw a diagram for problems like this so that you can check your work more easily.

**Question 47. The correct answer is D.** You can calculate the chances of Events A and B both occurring by multiplying the probability of each event occurring. That means that the correct expression is \( P(A \cap B) = P(A) \cdot P(B) \).

If you chose A, you might have thought the probability of Event A occurring is the same as the probability of Event B occurring. If you chose B, you might have thought the probability of Event A occurring is the complement of the probability of Event B occurring. If you chose C, you might have confused the formula for the probability of A and B both occurring with the formula for the probability of A or B occurring, \( P(A \cup B) = P(A) + P(B) - (P(A) \cdot P(B)) \).

**Question 48. The correct answer is J.** The following figure shows the 3-4-5 right triangle with sides formed by the x-axis, the vertical line through (4,–3), and the terminal side of \( \theta \). The angle, \( \alpha \), formed by the terminal side and the x-axis is called the reference angle of \( \theta \). The relationship between \( \theta \) and \( \alpha \) is \( \cos \alpha = |\cos \theta| \). From the figure, you can see that \( \cos \alpha = \frac{\text{the length of the side adjacent to } \alpha}{\text{the length of the hypotenuse}} = \frac{4}{5} = |\cos \theta| \). Because the terminal side of \( \theta \) lies in Quadrant IV, \( \cos \theta \) is positive. Therefore, \( \cos \theta = \frac{4}{5} \).
**Question 49.** The correct answer is A. If \( x \) is a negative number, then let \( y = -x \), where \( y \) is a positive number. Then \( \sqrt{y^2} \) is just \( y \). In terms of \( x \), this says \( \sqrt{(-x)^2} = -x \). For example, let \( x \) be -5. The left side is \( \sqrt{(-5)^2} \), which simplifies to \( \sqrt{25} \), and then to 5. The right side is \( -(−5) \), which is also 5.

For any number \( x \), its square and the square of its opposite are equal: \( (x)^2 = (−x)^2 \). For example, \( (5)^2 = (−5)^2 \). This shows that \( \sqrt{(-x)^2} = \sqrt{x^2} \). When \( x \) is a positive number, or zero, then \( \sqrt{x^2} = x \). Putting these last two statements together, \( \sqrt{(-x)^2} = x \) whenever \( x \) is a positive number or zero. For example, when \( x = 5 \), \( \sqrt{(-5)^2} = 5 \).

Summarizing, you now know that \( \sqrt{(-x)^2} = -x \) whenever \( x \) is a negative number, and \( \sqrt{(-x)^2} = x \) whenever \( x \) is positive or zero. Another way of saying this is \( \sqrt{(−x)^2} = |x| \).

Because \( |x| = |-x| \) for all values of \( x \), the paragraphs above show that I and II are saying the same thing—they’re equivalent.

However, II is always positive or zero, and III is always negative or zero, so the only time they are equal is when \( x \) is zero. For example, when \( x = 1 \), \(|-1| = 1 \) but \(-|1| = -1 \). So II and III are not equivalent.

The most common incorrect answer is C. Even though statements II and III look a lot alike—they have the exact same symbols in almost the same order—they are not equivalent. One is never negative and one is never positive.

If you answered E, you probably saw that II and III are not equivalent. Expression I looks so much different than either of the others that it is tempting to just say it can’t be the same. One approach would be to test a few numbers in the expressions. Be sure that one is positive and one is negative. If you substitute these into I and into II correctly, you will find they match. Then, you should suspect that I and II could be equivalent and look for a way to convince yourself of this.

**Question 50.** The correct answer is K. Statement F, that \( \overline{AB} \) and \( \overline{EF} \) are parallel, is true because both are perpendicular to the same other line, \( \overline{AD} \).

Because \( \angle DEB \) is marked with a right angle, \( \overline{DE} \) is perpendicular to \( \overline{BE} \), and so G is true.

The two angles, \( \angle ACB \) and \( \angle FCE \), are vertical angles, so H is true.

Statement J is true because the angles in \( \triangle ABC \) are congruent to the angles in \( \triangle EFC \). First, \( \angle A \) is congruent to \( \angle F \) because they are both right angles. Next, \( \angle ACB \) and \( \angle FCE \) are vertical angles. And third, the remaining angles must have the same measure because the sum of the interior angle measures in any triangle is 180°.
Because all of the other statements are true, you would expect statement K to be false. The following diagram shows such a case. Only if $\angle ECF$ is congruent to $\angle EDF$ can $\overline{CE}$ be congruent to $\overline{DE}$.

**Question 51. The correct answer is D.** This geometric figure has six sides, but you are only given the length of four of those sides. One of the slickest ways to find the perimeter is to move two of the sides to form a rectangle with the same perimeter. The following drawing shows the new rectangle:

The bottom of this rectangle is 4 inches long, and the right side is 3 inches long. So, the perimeter is $4 + 3 + 4 + 3 = 14$ inches.

An alternate method is to deduce that the left side is 3 inches long because it is the same length as the vertical sides on the right. And the last unknown side is 1 inch long because it is the difference between the horizontal 4-inch side on the bottom and the horizontal 3-inch side on the top. Then the perimeter (going clockwise) is $4 + 3 + 3 + 2 + 1 + 1 = 14$ inches.

If you chose C, you may have forgotten to add in the horizontal side that connects the vertical 2-inch side and the vertical 1-inch side.

If you chose A, you may have added just the numbers given directly on the figure. Or you may have calculated the area instead of the perimeter.
**Question 52. The correct answer is F.** Because points $A$ and $B$ are stationary, the side $\overline{AB}$ of $\triangle ABC$ will not change in length or direction. The *altitude* of $\triangle ABC$ with respect to side $\overline{AB}$ is the segment having one endpoint at point $C$ that is perpendicular to $\overline{AB}$. The area of $\triangle ABC$, in square coordinate units, can be found using the following formula:

$$\text{area} = \frac{1}{2}(\overline{AB})(\text{the length of the altitude from } C \text{ to } \overline{AB})$$

Because the length $AB$ must remain constant, the altitude from $C$ of any new triangle whose area is equal to that of the original $\triangle ABC$ must have the same length. Three of these new triangles (and their altitudes from $C$) are shown in the following figures:

In order that all altitudes from the moving point $C$ have equal lengths, $C$ must lie on the line $l$ (shown in each figure), where line $l$ is parallel to $\overline{AB}$. Because line $l$ is parallel to $\overline{AB}$, the lines must have equal slopes. Therefore, the slope of line $l = \text{slope of } \overline{AB} = \frac{6 - 2}{8 - 4} = \frac{4}{4} = -\frac{1}{2}$.

**Question 53. The correct answer is D.** Marshall made 24 calls on the first day. He makes 5 more calls each day than he had the day before. That means he made 29 calls on the second day. The following table shows the number of calls he made on each of the 20 days:

<table>
<thead>
<tr>
<th>Day</th>
<th>1</th>
<th>2</th>
<th>3</th>
<th>4</th>
<th>5</th>
<th>6</th>
<th>7</th>
<th>8</th>
<th>9</th>
<th>10</th>
</tr>
</thead>
<tbody>
<tr>
<td>No. calls</td>
<td>24</td>
<td>29</td>
<td>34</td>
<td>39</td>
<td>44</td>
<td>49</td>
<td>54</td>
<td>59</td>
<td>64</td>
<td>69</td>
</tr>
<tr>
<td>Day</td>
<td>11</td>
<td>12</td>
<td>13</td>
<td>14</td>
<td>15</td>
<td>16</td>
<td>17</td>
<td>18</td>
<td>19</td>
<td>20</td>
</tr>
<tr>
<td>No. calls</td>
<td>74</td>
<td>79</td>
<td>84</td>
<td>89</td>
<td>94</td>
<td>99</td>
<td>104</td>
<td>109</td>
<td>114</td>
<td>119</td>
</tr>
</tbody>
</table>

You could try to add all of these up. You might make a mistake, even with a calculator but that method is straightforward and would work.

Another approach is to notice that the number of calls for the first day and the last day add up to 143, as do the number of calls for Day 2 and Day 19, as do the number for Day 3 and Day 18, as do all the other pairs of days, working forward from the beginning and backward from the end. There are 10 pairs of days, each with 143 calls. That is 1,430 calls for the 20 days.
A third approach is to notice that this is an arithmetic series, where each term is 24 + 5k, where k represents the numbers from 0 to 19. When k is 0, then it is Day 1, and there are 24 + 0 calls. With sigma notation, the sum of all the calls on the 20 days can be represented as $\sum_{k=0}^{19} (24+5k)$. This is equivalent to $\left(\sum_{k=0}^{19} 24\right) + 5 \left(\sum_{k=0}^{19} k\right)$, which is equivalent to

$$\left(\sum_{k=0}^{19} 24\right) + 5 \left(\sum_{k=0}^{19} k\right).$$

The first summation is saying to add 24 + 24 + ... + 24, where there are 20 of the 24s added together. That is just $24 \cdot 20 = 480$. The second summation is a common one and simplifies to $\frac{(19)(19+1)}{2} = 190$. That makes the series sum to 

$$480 + 5(190) = 480 + 950 = 1,430 \text{ calls.}$$

A fourth approach relies on accurately remembering the following formula for the sum of an arithmetic series: $S_n = \frac{n}{2}[2a + (n-1)d]$, where the first term in the series is a, the common difference between terms is d, there are n terms in the series, and the sum is $S_n$. Substituting the quantities you know gives $\frac{20}{2}[2 \cdot 24 + (20-1) \cdot 5] = 10[48 + 95] = 10[143] = 1,430 \text{ calls.}$

If you used the summation approach and got C, you may have simplified $\sum_{k=0}^{19} (24+5k)$ to $24 + 5 \left(\sum_{k=0}^{19} k\right)$, leaving out the multiplier of 24.

If you chose B, you may have simplified the summation to $(24)(20) + \left(\sum_{k=0}^{19} k\right)$, leaving out the factor of 5. Or, you may have calculated the number of calls for Day 10 and multiplied this by 10.

**Question 54. The correct answer is K.** This is called a piecewise-defined function because it is pieces of different functions put together to form a single function. When $x \leq 1$, the equation is $f(x) = x^2 - 2$, so $f(1) = 1^2 - 2 = -1$ and $f(0) = 0^2 - 2 = -2$. (Actually, this information is enough to eliminate all the graphs except the correct one. But you might want to read the rest of this explanation anyhow.)

The graph of $y = x^2 - 2$ is a parabola, opening upward. Its graph is shown on page 446. The only part of the graph that applies for this piecewise-defined function is the part where $x \leq 1$. The rest of the graph is represented with dashes.
When $1 < x < 5$, then $f(x) = x - 7$, so $f(2) = 2 - 7 = -5$ and $f(4) = 4 - 7 = -3$. This is a straight line. A graph is shown in the following, with the parts outside $1 < x < 5$ shown with dashes.

When $x \geq 5$, the equation is $f(x) = 4 - x$, so $f(5) = 4 - 5 = -1$ and $f(6) = 4 - 6 = -2$. This is also a straight line. Its graph is shown in the following, with the part outside $x \geq 5$ shown with dashes.

K puts all these pieces together.
Mathematics • Practice Test 2 • Explanatory Answers

Question 55. The correct answer is D. The formula for calculating the number of permutations of \( n \) objects taken \( r \) at a time is \( \frac{n!}{(n-r)!} \). Therefore, the correct expression is \( \frac{15!}{(15-5)!} \). If you chose A, B, C, or E, you may have used the incorrect formula. The expression in A gives 5 times the number of objects. The expression in B gives the total permutations for 10 objects. The expression in C gives the number of permutations for 15 objects taken 10 at a time. The expression in E gives the number of combinations of 15 objects taken 5 at a time.

Question 56. The correct answer is K. To find an equivalent expression, you could simplify the expression by multiplying the numerator and denominator by the complex conjugate of the denominator, \( \sqrt{x+i} \).

\[
\frac{i}{\sqrt{x+i}} = \frac{i\sqrt{x+i}^2}{(\sqrt{x+i})(\sqrt{x+i})} = \frac{i\sqrt{x} + (\sqrt{-1})^2}{x - (\sqrt{-1})^2} = \frac{i\sqrt{x} - 1}{x + 1}.
\]

If you chose F, you might have incorrectly thought that you could eliminate the \( x \)'s and the 1's in the expression \( \frac{i\sqrt{x} + 1}{x - 1} \). If you chose G, you might have incorrectly thought that you could eliminate the \( i \)'s in the expression \( \frac{1}{\sqrt{x} - i} \). If you chose H, you might have incorrectly multiplied the expression by its complex conjugate. If you chose J, you might have incorrectly thought that \( i^2 = 1 \).

Question 57. The correct answer is E. You can use the fact that Point A has coordinates \((-6, -2)\) and Point B has coordinates \((3, 4)\), so the component form of \( \overrightarrow{AB} \) is \( \langle 3 - (-6), 4 - (-2) \rangle = \langle 9, 6 \rangle \). Point C has coordinates \((4, -2)\) and Point D has coordinates \((4, 3)\), so the component form of \( \overrightarrow{CD} \) is \( \langle 4 - 4, 3 - (-2) \rangle = \langle 0, 5 \rangle \). Writing \( \overrightarrow{AB} \) and \( \overrightarrow{CD} \) in terms of the unit vectors, \( \mathbf{i} = \langle 1, 0 \rangle \) and \( \mathbf{j} = \langle 0, 1 \rangle \) results in \( \overrightarrow{AB} = 9\mathbf{i} + 6\mathbf{j} \) and \( \overrightarrow{CD} = 0\mathbf{i} + 5\mathbf{j} \). Therefore, vector \( \overrightarrow{AB} + \overrightarrow{CD} = (9 + 0)\mathbf{i} + (6 + 5)\mathbf{j} = 9\mathbf{i} + 11\mathbf{j} \).

If you chose A, you may have incorrectly thought that \( \overrightarrow{AB} = \langle -6, -2 \rangle \). If you chose B, you may have incorrectly thought that \( \overrightarrow{AB} = \langle 3, 4 \rangle \) and \( \overrightarrow{CD} = \langle 0, -5 \rangle \). If you chose C, you may have incorrectly thought that \( \overrightarrow{AB} = \langle 3, 4 \rangle \). If you chose D, you may have incorrectly thought that \( \overrightarrow{CD} = \langle 0, -5 \rangle \).

Question 58. The correct answer is J. Let \( L_1 \) feet be the length of Pendulum 1 and \( t_1 \) seconds be the time for a complete swing of Pendulum 1. Let \( L_2 \) and \( t_2 \) describe Pendulum 2 in the same way. The time for a complete swing of Pendulum 1 is triple the time required for a complete swing of Pendulum 2. This means that \( t_1 = 3t_2 \).

The most common approaches to solving problems like this involve finding an equation that contains the two variables the question asks about, here \( L_1 \) and \( L_2 \), and solving for one variable or solving for the ratio of the variables.
By the equation that relates $L$ to $t$, the equation $t_1 = 3t_2$ becomes $2\pi \sqrt{\frac{L_1}{32}} = 3 \cdot 2\pi \sqrt{\frac{L_2}{32}}$ (which is an equation that contains both $L_1$ and $L_2$). Dividing both sides by $2\pi$ gives the equation $\frac{L_1}{32} = 3 \cdot \frac{L_2}{32}$. Squaring both sides gives $\frac{L_1}{32} = 9 \cdot \frac{L_2}{32}$. Multiplying both sides by 32 gives $L_1 = 9L_2$. So, Pendulum 1’s string is 9 times the length of Pendulum 2’s string.

The most common incorrect answer is G. If you chose that, you might have reasoned that if one variable triples, then any other variable must also triple. This happens for some functions, notably linear functions, but the function in this problem is not linear. The value of $L$ must go up by a factor of 9 so that the square root will go up by a factor of 3.

If you chose H, you may have reasoned that, in order for the square root to go up by a factor of 3, the quantity under the square root must go up by a factor of 6. That would mean that $L$ would go up by a factor of 6. This turns out not to be enough, because if $L$ goes up by a factor of 6, the square root will only go up by a factor of $\sqrt{6}$, which is less than 3.

**Question 59. The correct answer is A.** By properties of logarithms, $\log_a(xy)^2 = 2 \log_a(x)\log_a(y) = 2(s + t)$.

If you chose D, you may have done all of the previous steps correctly, except for thinking that $\log_a(xy) = \log_a(x) \cdot \log_a(y)$ (using multiplication rather than addition on the right side).

Answer C could come from thinking that $\log_a(xy)^2 = \log_a(x^2y^2) = \log_a(x^2) \cdot \log_a(y^2) = 2 \log_a(x) \cdot 2 \log_a(y)$. The first and last steps are correct, but not the middle one.

**Question 60. The correct answer is F.** Let $d$ be her distance in 1990. Her distance in 1991 would be $1.1 \cdot d$. And her distance in 1992 would be $1.2(1.1 \cdot d)$, which simplifies to $1.32 \cdot d$. This represents an increase of 32% from 1990 to 1992.

The most common incorrect answer is G. If you chose this, you probably added the 10% and the 20% to get 30%. This would work fine if the percents were percents of the same thing. But the first increase is a percent of the 1990 distance, while the second is a percent of the 1991 distance.

One good strategy for investigating problems like this is to choose a specific number to represent the initial distance. Say you choose 10 feet for her 1990 distance. The 1991 distance would be the original 10 feet plus a 10% increase, which is 1 more foot, for a total of 11 feet. To find the 1992 distance, take the 11 feet and add 20% of this amount, which is 2.2 feet. Then, the 1992 distance is $11 + 2.2 = 13.2$ feet. The percent increase from the original 10 feet is $\left(\frac{13.2 - 10}{10}\right)(100\%) = (0.32)(100\%) = 32\%$. These are the same operations done in the first method, but the calculations are done with concrete numbers rather than abstract variables.
Passage I

**Question 1.** The best answer is A because throughout the passage Crown is explicitly characterized as industrious and fastidious; his life and business are described as being ruled by the three tenets of order, accuracy, and modernity, all of which are grounded in his reverence for hard work. This description and characterization firmly reinforce the stereotype that Germans are tidy, meticulous, and industrious.

**The best answer is NOT:**

B because Crown is characterized consistently throughout the passage as adhering to the principles of order and industry in all aspects of his life and work; there is no evidence in the passage that he weakens the German stereotype.

C because Crown is explicitly described as accepting and even revering the principle of hard work. His personal philosophy that “without industry there was no reward” (lines 86–87) is described as being ingrained in him “deeper than the marrow of his bones” (lines 90–91). This clearly does not weaken the industrious aspect of the German stereotype.

D because there is no evidence in the passage that Crown expects others to do the tidying up for him.

**Question 2.** The best answer is H because it can most reasonably be inferred that the “appointment at twelve” referred to in line 17 would occur that day, whereas the “emergency meeting” referred to in lines 4–5 is scheduled to take place “this Friday” (line 5), indicating that the meeting would happen in the near future.

**The best answer is NOT:**

F because “this Friday” in line 5 indicates that the meeting will happen on a day in the near future, whereas the appointment is indicated as being scheduled for that day. If the meeting and the appointment were meant to happen on the same day, the narrator likely would have said “today” instead of “this Friday.”

G because the passage makes it clear that the meeting “this Friday” has not yet occurred, especially considering it is described as an immediate concern of Crown’s.

J because the passage makes it clear that the meeting is an immediate concern of Crown’s, and that the meeting will happen “this Friday,” indicating the near future, not years in the future.
Question 3. The best answer is B because lines 47–57 describe the principle of modernity to which Crown unwaveringly subscribes, giving examples of how quickly he embraces new technology. Zwick, however, is reluctant to move from using an old-fashioned quill pen to a modern typewriter (lines 62–64), learning to typewrite only when he is compelled to.

The best answer is NOT:

A because there is no clear evidence in the passage that Zwick adheres to a certain level of fastidiousness regarding the meeting of deadlines.

C because the passage characterizes Zwick as being clearly unafraid to state his preferences to his superior (Crown), but there is no evidence in the passage that Crown is afraid to state his preferences to his superiors. Indeed, there is no suggestion in the passage that Crown has superiors.

D because there is no evidence in the passage that Zwick holds concern about the company’s public image; Crown, however, is clearly concerned with the company’s image, as evidenced in lines 66–67, when he says that using quill pens instead of typewriters “makes Crown’s look old-fashioned.”

Question 4. The best answer is F because when Zwick is said to have “blanched” in line 72, it is in response to Crown’s proposal that a woman be hired as a typewriter if Zwick refuses to learn typewriting. Zwick’s indignation is expressed in the rest of line 72: “A woman? In my office?”

The best answer is NOT:

G because the passage makes clear that the woman is a theoretical employee, not an actual visitor in the office.

H because the passage makes clear from context that Zwick is not excited about the prospect of a female employee; the passage also makes clear that the female employee being discussed is theoretical.

J because the passage makes clear that Crown will hire a female employee only if Zwick continues to refuse to learn to typewrite; Crown has not actually hired anyone.
**Question 5. The best answer is D** because lines 2–5 clearly state that Crown’s “most immediate” worry was a “civic responsibility” that he would soon be discussing at a meeting.

**The best answer is NOT:**

A because there is no evidence in the passage that Crown is preoccupied with whether he will be on time for his weekly trim; the appointment for the trim is only mentioned as a passing matter of fact.

B because the passage makes clear in lines 52–54 that Crown had no hesitation in installing expensive pasteurization equipment in his brewery; the passage also makes clear that this is not a preoccupation of his at the time described in the passage’s opening.

C because the passage does not indicate that Crown is at all preoccupied with Zwick’s behavior, and the passage also indicates that Crown’s exchange with Zwick in lines 62–74 took place before the time described in the passage’s opening.

**Question 6. The best answer is G** because the passage states that Crown was “a mediocre student in most school subjects” but that “at ciphering he was a prodigy” (lines 33–34).

**The best answer is NOT:**

F because the passage states that Crown was a “mediocre student in most school subjects” (lines 33–34); he was exceptionally gifted only at ciphering.

H because there is no evidence in the passage that Crown was a successful student whether he applied himself or not; he is simply described as being a mediocre student outside of his talent at ciphering.

J because there is no evidence in the passage that Crown’s success as a student increased as he mastered counting aids.

**Question 7. The best answer is C** because the passage characterizes Crown in lines 42–46 as prone to asking questions of his employees that would elicit a specific answer, likely one that involved numbers. The question about sales figures in C best fits these characteristics.

**The best answer is NOT:**

A because there is no evidence in the passage supporting the idea that Crown is likely to ask an open-ended, personal question of his employees.

B because the passage most strongly suggests in lines 42–46 that Crown’s questions to his employees most likely involve numbers, and a question about repairing old equipment does not involve numbers.

D because there is no evidence in the passage supporting the idea that Crown is concerned about team dynamics among his employees to the point where he would ask such a question of them. Lines 42–46 also most strongly suggest that Crown’s questions to his employees involve numbers, and the question about team-building does not involve numbers.
Question 8. The best answer is H because the passage describes Crown as subscribing to the principle of modernity, and his exchange with Zwick in lines 62–74 most nearly suggests that quill pens were the status quo in offices in the United States at the time the passage was set, though more advanced technology was beginning to become available. To Crown, who wanted his business to use the “newest methods” (line 51) of technology, such as typewriters and mechanical adding machines, these quill pens seemed “old-fashioned” (line 67).

The best answer is NOT:

F because the passage indicates that the typewriter is among the “modern machines” (line 56) that Crown insists be used in his office.

G because the passage indicates in lines 56–58 that the mechanical adding machine is one of the “modern machines” (line 56) that Crown insists be used in his office.

J because the passage gives no clear evidence that abacuses are widely used in US offices at the time the passage is set. The abacus mentioned in the passage is described as an ancient counting device (line 39) that Crown keeps in his office, “within reach” (line 40). Presumably such an ancient counting device is not widely used in US offices at the time the passage is set, but Crown does not necessarily seem to see the abacus as becoming increasingly obsolete.

Question 9. The best answer is A because the metaphor used in the passage to describe Crown’s three principles primarily includes language about building, which is a fundamental part of architecture as a discipline. Line 26 describes Crown’s second principle of accuracy as a “keystone,” and lines 76–78 compare Crown’s three principles to a “solid house or building” that is “supported by a strong foundation”: Crown’s attitude toward hard work.

The best answer is NOT:

B because business is only mentioned in the passage in the very literal sense of Crown’s brewery business and its operations.

C because astronomy is not mentioned in the passage.

D because education is mentioned in the passage only in the literal sense of Crown’s education as a student.
Question 10. The best answer is H because the passage describes the photographs of annual brewery picnics decorating Crown's office as "fading" and "brown" (line 81), indicating that they have hung on the wall of his office (and thus that Crown has been in the brewery business) for a length of time.

The best answer is NOT:

F because the passage makes no mention of outdated refrigerators; it only mentions that Crown invested in "refrigerated freight cars" (lines 55–56), which represented a new technology at the time.

G because the passage makes no mention of how long the cross-stitch made by Crown's wife has been hanging on his office wall.

J because there is no mention of such a bell in the passage; it only mentions the "pinging bell on the black iron typewriter" (lines 59–60).

Passage II

Question 11. The best answer is D because there is no mention in the passage of William's response to Caroline's discovery, thus there is no clear indication of how he felt about her discovery.

The best answer is NOT:

A because there is no evidence in the passage that William either applauded Caroline's discovery or was disappointed that she wasn't looking for nebulae.

B because there is no evidence in the passage that William either supported Caroline's discovery or verified it himself.

C because there is no evidence in the passage that William resented how quickly Caroline's discovery was verified.

Question 12. The best answer is J because the passage states that "the forty-foot [octagon tube] would be higher than a house" (line 14). This is a direct comparison used to emphasize the enormous size of the "octagon tube 40 foot long" (line 6).

The best answer is NOT:

F because the series of ladders mentioned in line 16 is a description of part of the telescope itself; the telescope is not being compared to the ladders.

G because the wooden gantry mentioned in line 10 is described as something the telescope would have to be mounted in; the telescope itself isn't compared to the gantry.

H because the haylofts mentioned in line 34 are described as part of the stables that could be converted into an apartment; the telescope is not compared to the haylofts.
Question 13. The best answer is B because the first four paragraphs in the passage focus on William Herschel and his telescope project, but the remainder of the passage focuses primarily on his sister Caroline and her astronomical work; the fifth paragraph serves as a transition, moving the passage's discussion from details about William's telescope project to details about Caroline's work.

The best answer is NOT:

A because the passage does not explain any specific methods Caroline used to perform her comet sweeps.

C because the passage does not say that Caroline herself made renovations to the stables, nor does it specify that the renovations would be done to accommodate William's telescope.

D because the passage does not compare Caroline's observation techniques with William's; at this point, the passage shifts to a discussion of Caroline's astronomical work.

Question 14. The best answer is H because the passage says in lines 79–80 that “The account written into [Caroline's] 'Book of Work Done' catches something of her growing excitement.” This statement is then supported and illustrated by the excerpt from Caroline's “Book of Work Done” that immediately follows. Her writing “IS A COMET” in capital letters (line 85), and the statement that she “did not go to rest” until she had written to the Royal Society about the comet (lines 85–88), also reveal her enthusiasm about her discovery.

The best answer is NOT:

F because though the excerpt in the passage indicates that it took Caroline a bit of time to verify that her finding was a comet, the passage contains no clear outline of the process by which Caroline determined her finding was a comet.

G because the passage indicates that the excerpt contains notes from Caroline's own work, not that the notes were made for William in particular.

J because though the passage implies that Dr. Blagden and Mr. Aubert were points of authority regarding astronomical discovery at the time, it does not explain the role they may have had in verifying Caroline's discovery.
Question 15. The best answer is A because in the context of lines 9–13, it is clear that the word finest is being used in juxtaposition with the description of the enormous telescope and its workings. The telescope was so massive that it would have to be mounted in an enormous gantry and turned by two workmen, but it would be so intricate and precise that it could be adjusted in “fine,” or “slight,” ways by the astronomer.

The best answer is not:

B because the word fairest generally denotes either lightness in complexion or appearance, or it pertains to justice and equity. However, the word finest in the context of lines 9–13 is meant to indicate precision, not any of the concepts associated with fairness.

C because the context of lines 9–13 indicates that the word finest is being used in the sense of precision, and it would be inaccurate to describe precise or exact fingertip adjustments as thin.

D because the word greatest denotes either size or level of excellence. The word finest in the context of lines 9–13 is clearly meant to indicate the precision involved in the adjustments, not any of the concepts associated with greatness.

Question 16. The best answer is J because the sentence in lines 17–21 states that Caroline would have to be in the special booth below William “to avoid light pollution, where she would have her desk and lamp, celestial clocks, and observation journals,” meaning that the light from her lamp (which she needed to record her observations) would have affected William’s ability to observe the night sky though the telescope.

The best answer is not:

F because the passage states that both Caroline and William would be “shouting commands and replies” (lines 22–23); there is no evidence that Caroline would be relaying William’s instructions to workmen.

G because there is no evidence in the passage that Caroline preferred seclusion when working on calculations; the passage states that she would work in the booth “to avoid light pollution” (line 19), not because she wanted to be alone.

H because the passage does not indicate the size of the viewing platform or the number of people it could hold, so there is no evidence in the passage to support the idea that the platform wouldn’t be large enough to hold both William and Caroline.
Question 17. The best answer is B because lines 25–27 directly answer the question of why William and Caroline moved to “The Grove”: “William had decided that his grand project required a new house with larger grounds for constructing and erecting the telescope.” They moved to “The Grove,” which is described as meeting these requirements.

The best answer is NOT:

A because the passage makes no mention of what motivated William to embark on his project; it only mentions when he was inspired to begin the project (“in the summer of 1785” (line 1)).

C because the passage mentions that Caroline was “unable to calculate the mathematical coordinates” of the comet she discovered, but it does not give any reason as to why she was unable to do so.

D because the passage does say that “the verification of Caroline’s comet was achieved much more rapidly than William’s discovery of the planet Uranus” (lines 89–91), but it does not directly specify how long it took the Royal Society to verify that Caroline’s discovery was a comet.

Question 18. The best answer is F because the passage states that because of the reflector’s “large aperture, its tube appeared much fatter, heavier and stubbier than normal reflectors of this type” (lines 42–44). Thus it can most reasonably be inferred that the reflector’s aperture was larger than those of typical telescopes of that type at the time.

The best answer is NOT:

G because there is no mention in the passage of the size of the reflector’s box-frame.

H because the passage states that the reflector’s magnification was “comparatively low at twenty-four times” (lines 51–52), meaning that it had less magnifying power compared to similar telescopes at the time.

J because the passage states that the reflector was “designed specifically for its huge light-gathering power” (lines 49–50), indicating that, if anything, it likely had more light-gathering power than similar telescopes at that time, not less.
Question 19. The best answer is C because the passage states in lines 62–66 that “Caroline thought she had spotted an unknown stellar object moving through Ursa Major” which “appeared to be descending, but barely perceptibly, towards a triangulation of stars in the beautifully named constellation Coma Berenices.”

The best answer is not:

A because lines 62–66 clearly state that the comet was moving “towards” the stars in Coma Berenices, not through Coma Berenices or toward the Pole Star.

B because lines 62–66 clearly state that the comet was moving “towards” the stars in Coma Berenices, not through Coma Berenices or toward the Big Dipper.

D because lines 62–66 clearly state that the comet was moving “through” Ursa Major and “towards” the triangulation of stars in Coma Berenices, not through them.

Question 20. The best answer is F because the passage states in lines 67–70 that “to find something so quickly, and in such a familiar place (the Great Bear or Big Dipper being the first stop of every amateur stargazer wanting to locate the Pole Star), seemed wildly unlikely.” Thus the passage indicates that Caroline’s find was unlikely because she found the comet quickly in a part of the sky that was very familiar to stargazers.

The best answer is not:

G because there is no evidence in the passage that Caroline had more knowledge of nebulae than she did of comets.

H because the passage mentions in lines 90–91 “William’s discovery of the planet Uranus,” but there is no mention of Caroline being involved in that discovery.

J because the passage indicates that Caroline had plenty of experience with mathematical calculations in astronomy, and though line 73 does state that she was “unable to calculate the mathematical coordinates” of her comet, the passage gives no indication that her discovery was unlikely because she had little experience with such calculations.
Passage III

Question 21. The best answer is B because the first paragraph of passage A reveals Gornick’s belief that her mother and the character of her mother in her memoir are not exactly the same; the second paragraph reveals Gornick’s belief that, similarly, the narrator of the memoir and her actual self are not quite the same. Together, in the context of the passage as a whole, these paragraphs serve to introduce the idea that the characters in Gornick’s memoir differ from the people they are based on.

The best answer is not:

A because though the paragraphs provide a few details implying a measure of popularity for Gornick’s book, the main purpose of these two paragraphs, especially in the context of the passage as a whole, is to establish the idea in B, not to establish her book’s popularity.

C because there is no indication in the passage that Gornick is overly frustrated with her readers’ questions and comments.

D because Gornick argues in line 42 that “memoirs belong to the category of literature,” but she is not suggesting that memoirs are fiction and should be classified as such. Her argument is that “emotional truth” is more important in memoirs than are completely literal and accurate details.

Question 22. The best answer is F because lines 8–16 explain that the party guest was disappointed because she felt Gornick was “nothing like the woman who wrote Fierce Attachments!” The quotation “We ourselves were just a rough draft of the written characters” (lines 20–21) exemplifies the discrepancy between an actual person and a character depicted in a memoir that led to the guest’s disappointment.

The best answer is not:

G because the party guest’s disappointment had nothing to do with Gornick’s perceived similarity to Gornick’s mother. The guest’s disappointment stemmed from the fact that the narrator of the book and Gornick herself were “not exactly the same” (line 16).

H because the quotation in question refers to the idea that Gornick had hoped to express in her memoir, whereas the party guest’s disappointment had to do with the unexpected difference between the narrator in the book and Gornick herself.

J because the quotation in question refers to the insight that Gornick had hoped to express in her memoir, whereas the party guest’s disappointment had to do with the unexpected difference between the narrator in the book and Gornick herself.
**Question 23. The best answer is B** because Gornick identifies the heart of her memoir in lines 31–32: the revelation that “I could not leave my mother because I had become my mother.”

**The best answer is not:**

A because the author indicates that the walks she took with her mother in Manhattan in the 1980s are part of “the context in which the book is set” (lines 34–35), but the passage does not indicate that Gornick believes them to be the heart of her memoir.

C because the author indicates that her childhood experiences in the Bronx in the 1950s are part of “the context in which the book was set” (lines 34–35), but the passage does not indicate that Gornick believes them to be the heart of her memoir.

D because the author states in lines 31–32 that she believes the heart of her memoir is the revelation she had about having become her mother, not just that they had a shared history.

**Question 24. The best answer is J** because the author claims in lines 42–43 that “memoirs belong to the category of literature, not of journalism.”

**The best answer is not:**

F because the author explicitly states in lines 42–43 that memoirs do not belong to the category of journalism.

G because the author explicitly claims in line 42 that “memoirs belong to the category of literature”; personal diaries are not mentioned in the passage.

H because the author explicitly claims in line 42 that “memoirs belong to the category of literature”; she also goes on to say that memoirs need not be as literally accurate as historical narrative (lines 43–46).

**Question 25. The best answer is C** because the first paragraph asserts that Hemingway’s fiction contained autobiographical elements and his “protagonists are often conscious projections and explorations of the self” (lines 55–56).

**The best answer is not:**

A because the passage states in lines 53–56 that Hemingway’s fictional protagonists are often projections of the self; there is no mention in the passage of Hemingway basing his protagonists on composites of his friends.

B because the passage states in lines 53–56 that Hemingway’s fictional protagonists are often projections of the self; there is no mention in the passage of Hemingway basing his protagonists on family members.

D because the passage states in lines 53–56 that Hemingway’s fictional protagonists are often projections of the self; there is no mention in the passage of Hemingway’s protagonists being completely made-up characters.
Question 26. The best answer is F because the passage explains in lines 61–73 that “A Moveable Feast is particularly complex because Hemingway was clearly conscious that it would be his literary testament” and that he thus used the book to portray himself and his contemporaries in a certain light. Lines 73–76 state that “A Moveable Feast could hardly be an objective portrayal of its author and his contemporaries, and the accuracy of the anecdotes becomes an issue that can never be entirely resolved.”

The best answer is NOT:

G because though the passage mentions that Hemingway “felt that he had been unfairly portrayed by some of his contemporaries” (lines 67–68), the passage indicates that the question of accuracy has to do with Hemingway’s own writing, not with the writings of others.

H because the passage makes no mention of Hemingway being unable to produce documents to support his stories.

J because the passage makes no mention of Hemingway claiming the excellence of his memory or of others doubting such a claim.

Question 27. The best answer is B because the author of passage B states that “A Moveable Feast is particularly complex” (line 61) and that it “appears as a fascinating composite of relative factual accuracy and clear dishonesty of intent” (lines 87–88). These statements, in addition to details the author provides throughout the passage about Hemingway’s purposeful blurring of fact and fiction, support the idea that the passage author believes A Moveable Feast to be a complex example of a book that combines fact and fiction.

The best answer is NOT:

A because the passage author makes no particular claim about the quality of any of Hemingway’s other works, nor does she compare A Moveable Feast to any of Hemingway’s other works.

C because the passage author makes clear that she believes the accuracy of A Moveable Feast is in question and “an issue that can never be entirely resolved” (lines 75–76).

D because the passage author does not suggest anywhere in the passage that A Moveable Feast should be read alongside other books from the time period; her argument pertains primarily only to A Moveable Feast.
Question 28. The best answer is J because in passage A, Gornick’s point is that her memoir was not necessarily literally true; what mattered to her was portraying “not the literalness of the situation, but the emotional truth of the story” (lines 38–39). She explains that the characters in her memoir differed from the actual people they were based on in that “these characters could not live independent of the story which had called them into life, as they existed for the sole purpose of serving that story” (lines 21–24). Similarly, throughout passage B, Hemingway is described as selectively using material from his life and blurring fact and fiction in order to best serve the story he wanted to tell: “He clearly overlooked a great deal of material, distorted some, and generally selected the episodes so that they would show him as innocent, honest, dedicated, and thoroughly enjoying life” (lines 83–86).

The best answer is NOT:

F because the passages indicate that both Gornick and Hemingway may not have been completely literally accurate in their memoirs, but their stories were based on a foundation of real-life situations—not wholly fictional ones.

G because though passage B states that Hemingway wanted “to leave to the world a flattering self-portrait” (lines 72–73), nowhere in passage A does Gornick indicate that she was concerned with portraying herself in a flattering way in her memoir.

H because though passage B states that Hemingway wanted to “present his own version of personal relationships” (lines 68–69) and “get back at people against whom he held a grudge” (lines 70–71), nowhere in passage A does Gornick indicate that she was motivated to write her memoir to “settle old scores.”
**Question 29. The best answer is C** because in passage A, Gornick explains her belief that, in memoir, complete literal accuracy is not necessary but that the point is to convey the “emotional truth of the story” (line 39), “trying, as honestly as possible, to get at the bottom of the tale at hand” (lines 48–49). She states that “what actually happened is only raw material; what matters is what the memoirist makes of what happened” (lines 39–41). Similarly, in passage B, Hemingway is portrayed as focusing on the particular stories he wanted to portray rather than focusing on factual accuracy: “He invented and lied relatively seldom about pure facts. When he did so, it was usually in order to reinforce the pattern he had created . . .” (lines 79–81). Thus it seems that both Gornick and Hemingway would agree that creating a cohesive, meaningful, and artistic whole is more important than detailing plain facts in a memoir.

**The best answer is NOT:**

A because there is no evidence in either passage that Gornick or Hemingway would believe that a writer has as much license to create when writing memoir as he or she does when writing fiction.

B because both passages indicate that the exact details of events are less important than the story the memoirist wants to tell that is based on memories of events. There is no evidence in either passage that Gornick or Hemingway would believe a writer should exclude an event entirely from a memoir if he or she cannot remember the exact details of the event.

D because there is no evidence in either passage that either Gornick or Hemingway would believe memoirists should write only about incidents that have documented evidence supporting their stories; neither author is concerned with evidence as fact.

**Question 30. The best answer is G** because the main idea expressed in passage A is that Gornick believes that “what actually happened is only raw material; what matters is what the memoirist makes of what happened” (lines 39–41). This idea echoes the quotation, which indicates that there is necessarily a difference between a memoir, which is a story, and the details and facts of real life.

**The best answer is NOT:**

F because though there is an anecdote about Gornick not meeting a particular reader’s expectation, that story is simply supporting Gornick’s point that characters in memoirs differ from real people; the anecdote does not relate to the quotation’s claim that a memoir is a story and not a history.

H because the statement in passage B about Hemingway viewing *A Moveable Feast* as his literary testament explains only his motivation for writing the story the way he did; it doesn’t relate to the quotation’s claim that a memoir is a story and not a history.

J because the statement in passage B claiming that Hemingway seldom lied about pure facts focuses on the factual accuracy of his memoir or how much it reflected history, and this idea stands in contrast to the quotation’s claim that memoir is in fact a story and not a history.
Passage IV

**Question 31. The best answer is D** because the passage focuses on Suarez’s research on colonizing ants and his conclusions about what enables some species to survive over others.

**The best answer is NOT:**

A because the passage makes clear that Argentine ants living in the United States had already been discovered; in order to examine why some colonizing organisms fail and some succeed, Suarez hoped to examine “early samples of Argentine ants collected in the United States” (lines 7–8).

B because the passage primarily focuses on ant species and does not compare the physical characteristics of ants to other insects. The passage also focuses more exclusively on the behavior of ants rather than their physical characteristics.

C because the passage makes no mention of the technology scientists use to determine the size of supercolonies.

**Question 32. The best answer is G** because peppered throughout this passage are certain colloquial phrases not often seen in scientific tracts, including that a scientist did it “the hard way” (lines 3–4), that one scientist was the “guru of ant gurus” (line 27), that Argentine ants were “wimps” (line 52), and that certain species always “made bank” (line 73). The use of such relaxed language helps create a casual tone for the reader.

**The best answer is NOT:**

F because the passage includes no personal anecdotes, never even mentioning the author’s life or incorporating the use of the word I.

H because the passage author uses informal language at times but includes no quotations that are humorous.

J because the passage includes no “self-critical” asides, as again the author does not place himself in the passage in any way other than through his use of colloquial language.
**Question 33.** The best answer is C because the first paragraph tells readers that Suarez “found some brown jars” at the Smithsonian in 1999, meaning this event occurred before the turn of the century, well before the other choices.

**The best answer is NOT:**

A because lines 63–66 state that “Case joined forces with Holway and Suarez” to study ant aggression but that happened only after Suarez and Holway had been classifying the ants (lines 28–29), which happened only after Suarez found the jars.

B because line 86 states that those ants were brought together “in 2009,” a full decade after Suarez first found the brown jars.

D because lines 25–28 state that Holway and Ward were “solicited” to help Suarez with classifying the jars Suarez had previously found in the Smithsonian, which couldn’t have happened until Suarez found the jars.

**Question 34.** The best answer is G because the opening sentence of the fifth paragraph states the focus of the paragraph: that when a group moves to a new area, “possible futures diverge” (line 42). What follows in the paragraph are examples of these possible futures and the indication that it’s unlikely for a species to survive, let alone thrive in a new area.

**The best answer is NOT:**

F because the paragraph is not focused specifically on Argentine ants but discusses pioneering species in general and the likelihood that they will survive.

H because the paragraph does not provide a definition of invasive species, nor does the paragraph specifically mention ants.

J because the paragraph does not mention or focus on Argentine ants specifically, nor does it compare their survival rates with those of other species.

**Question 35.** The best answer is D because lines 56–58 state that if Argentine ants from different colonies are placed together, “they accept each other.” This is noted directly after line 55 describes this as “strange” behavior, so it can be assumed that in most similar situations ants would fight one another, not accept one another.

**The best answer is NOT:**

A because the lines in question have nothing to do with the prevalence of supercolonies among ant species but with the trait of Argentina ants to accept each other.

B because the passage does not differentiate in these lines between California’s Argentine ants and the same ants in other places.

C because the lines in question don’t discuss California’s ecosystem in any way.
Question 36. The best answer is F because lines 1–3 state that Suarez was “like many biologists” who “struggled for years with the question of which colonizing organisms fail and which succeed.”

The best answer is NOT:

G because lines 1–3 make it clear that Suarez was one of many; no dates are attached to the work done by the others.

H because lines 1–3 make it clear that many biologists struggled with this question. Moreover, there is no indication in the passage that Suarez was affiliated with the Smithsonian, and he worked alongside others—Holway and Ward—who were affiliated with different universities.

J because lines 1–3 state that Suarez was “like many biologists.”

Question 37. The best answer is D because lines 15–18 state that what Suarez found in the brown jars other than Argentine ants was “far more interesting: some of the ethanol-filled jars were jammed with vials of ants collected at ports of entry in the eastern U.S. from 1927 to 1985.” Those ants provided the basis for Suarez’s research.

The best answer is NOT:

A because lines 14–15 state that “Suarez ultimately found relatively few samples of Argentine ants,” meaning they were not “most of the samples” at all.

B because lines 25–28 state that Suarez recruited Ward and Holway to help him, not that they had accrued all these samples.

C because line 24 states that the brown jars revealed “394 separate samples” which line 29 explains were “232 distinct species,” but the passage otherwise does not say how many of those ants might have been previously “undiscovered.”
Question 38. The best answer is F because line 52 clearly states Argentine ants are “squishy, small, stingless wimps.”

The best answer is NOT:

G because lines 51–53 describe those ants as “ecologically dominant,” yet small and not physically dominant.

H because the passage makes clear Suarez found samples of the ants in the Smithsonian, not that he discovered the species himself.

J because lines 84–88 state that “one conglomeration of Argentine ants stretched the length of California, another from Italy to Portugal . . . until, in 2009, workers from those two “colonies” (along with a third from Japan) were put together . . .” Thus, the passage makes clear that Argentine ants existed in Japan to such a degree that they could form with other colonies to create a supercolony. There is no indication in the passage that the species did not thrive in Japan.

Question 39. The best answer is B because lines 69–71 say that studies show that “aggressive ants wasted energy fighting (and dying), and so gathered less food and fared poorly.”

The best answer is NOT:

A because the passage does not indicate that aggressive ants live in larger colonies than do peaceful ants.

C because the passage does not indicate that aggressive ants are more likely than peaceful ants to live in a colony.

D because the passage does not indicate that aggressive ants are more likely than peaceful ants to be a “survivor species.” In fact, lines 69–71 state that aggressive ants spend more time “dying” because they fight so much.

Question 40. The best answer is G because this fact is stated clearly in lines 78–79: “Ants flash chemical badges identifying their home nest.”

The best answer is NOT:

F because this idea is not supported by the passage, as lines 79–80 indicate that without those chemical markers, “no one knows who is friend or foe,” with the end result of that being that peace breaks out. When peace breaks out, the term colony gets muddied and supercolonies form, with nests exchanging workers and queens.

H because the passage makes clear that supercolonies form only when chemical markers are absent and that swapping ants between colonies is not normal.

J because the passage discusses conglomerations of Argentine ants in supercolonies that go “the length of California, another from Italy to Portugal” (lines 85–86), but the passage doesn’t indicate which of those is bigger or if one of those is the “largest” supercolony in the world.
Passage I

1. **The best answer is B.** The figure shows the first generation (Individuals 1 and 2), the second generation (Individuals 4, 6, and 7), the third generation (Individuals 10, 11, 12, 13, 15, 16, and 17), and the fourth generation (Individuals 18–23). A, C, and D are incorrect; the figure shows four generations. B is correct.

2. **The best answer is G.** In order to answer this item, the examinee must know that the more closely related two individuals are to each other, the greater the genetic similarity is likely to be. According to the figure, Individuals 12 and 13 are sisters and would likely have the greatest genetic similarity. F is incorrect; individuals 3 and 4 are mates, not siblings. G is correct; Individuals 12 and 13 are sisters and would have the greatest genetic similarity. H is incorrect; Individuals 16 and 24 are not blood relatives. J is incorrect; Individuals 18 and 21 are second cousins.

3. **The best answer is D.** In order to answer this item, the examinee must know how to work a genetic cross. According to the figure, both Individuals 23 and 24 have Trait G. According to the passage, Trait G is recessive. It follows that Individuals 23 and 24 both have the gg genotype and that all their children will also have the gg genotype. All their children will therefore have Trait G. A, B, and C are incorrect; all four of the children will have Trait G. D is correct.

4. **The best answer is H.** According to the figure, the grandchildren of Individuals 1 and 2 are Individuals 10, 11, 12, 13, 15, 16, and 17. According to the key for the figure, a black circle and black square represent individuals with Trait G. Of the grandchildren, only Individuals 10 and 16 have Trait G. F, G, and J are incorrect; two of the grandchildren have Trait G. H is correct.

5. **The best answer is D.** In order to answer this item, the examinee should know that with a sex-linked trait, an affected female passes the trait to all her sons. According to the figure, Individuals 4 and 10 were the only females with Trait G who had a son. Individual 4’s son, Individual 11, did not have Trait G. It follows that Trait G is not a sex-linked trait. A and B are incorrect; Trait G is not a sex-linked trait. C is incorrect; Individual 4 did not pass Trait G to her son. D is correct.

6. **The best answer is J.** According to the passage, Individual 21 has the Gene G genotype Gg. According to the figure, Individual 21 does not have Trait G. The passage states that Trait G is the recessive trait. An individual with the Gg genotype will have the dominant trait. F and G are incorrect; an individual with the Gg genotype will not have Trait G. C is incorrect; Trait G is a recessive trait. J is correct; the individual will not have Trait G, the recessive trait.
Passage II

7. **The best answer is A.** In order to answer this item, the examinee must know that a balance is used to determine mass. Figure 2 gives the average mass per seed for each group. In order to determine the average mass per seed, the scientists would have to measure the mass of the seeds using a balance. A is correct. B is incorrect; the pH was not measured in this experiment. C is incorrect; a telescope is typically used for viewing distant objects and would not have been needed for this experiment. D is incorrect; a thermometer is used to measure temperature.

8. **The best answer is G.** According to the passage, the experiment was conducted to investigate the effects of different pollination treatments on fruit production and seed mass. F is incorrect; the location of the plants was not a variable in the experiment. G is correct; the experiment investigated different types of pollination. H is incorrect; the experiment did not measure the amount of time until fruit ripened. J is incorrect; the scientists did not question whether or not the flowers were typically pollinated by hummingbirds.

9. **The best answer is A.** According to Table 1, the flowers in Group 1 were self-pollinated whereas the flowers in Group 2 were cross-pollinated, using pollen from a single donor. A is correct. B is incorrect; the pollen used for Group 1 was from the same plant as the flowers in Group 1. C is incorrect; the pollen received by each Group 2 flower was collected from a single donor. D is incorrect; the pollen used for Group 1 was from a single plant.

10. **The best answer is H.** Figure 1 shows the percent of flowers that produced fruit. In order to calculate this percentage, the examinee must divide the number of flowers that produced fruit by the total number of flowers. F and G are incorrect; the number and mass of seeds is not relevant. H is correct. J is incorrect; the number of flowers producing fruit should be in the numerator, and the total number of flowers should be in the denominator.

11. **The best answer is B.** According to the passage, the anthers are the pollen-producing structures in the flower. By removing the anthers, the flower would not be able to spontaneously self-pollinate. A is incorrect; without the anthers present, the flowers would not be able to spontaneously self-pollinate. B is correct. C and D are incorrect; the presence or absence of anthers would not affect the ability of the flowers to be pollinated by hummingbirds.

12. **The best answer is G.** According to Figure 1, 0% of the flowers in Group 4 produced fruit. This suggests that the nylon bags successfully prevented the normal pollinators from pollinating the flowers, because none of the flowers in Group 4 were pollinated. F is incorrect; 20% of the flowers receiving self-pollination treatments produced fruit. G is correct; 0% of the flowers in Group 4 produced fruit, indicating that the nylon bags prevented normal pollinators from pollinating the flowers. H and J are incorrect; the data suggest that the bags did prevent the normal pollinators from pollinating the flowers.
13. **The best answer is D.** The results given indicate the average mass per seed but not the number of seeds. Without knowing the number of seeds, one cannot figure out the total mass of the seeds. A, B, and C are incorrect; there is not enough information to determine the total mass of the seeds produced by the flowers. D is correct.

**Passage III**

14. **The best answer is H.** F and G are incorrect; both CH$_4$ and CO$_2$ were produced indicating that the organic matter was being broken down by both aerobic and anaerobic bacteria. H is correct; the organic material was most likely broken down more rapidly during the warmer summer months. J is incorrect; the organic material was most likely broken down less rapidly in the winter.

15. **The best answer is A.** According to Figures 1 and 2, for both bog soil and fen soil, as the water table levels decreased from +1 cm to −20 cm, the total CO$_2$ emissions increased. The figures also show that for both bog soil and fen soil, as the water table levels decreased, the total CH$_4$ emissions also decreased. A is correct. B is incorrect; the total CO$_2$ emissions increased. C is incorrect; the total CH$_4$ emissions decreased. D is incorrect; the total CO$_2$ emissions increased.

16. **The best answer is F.** According to the passage, gas emissions for each soil section were measured. By keeping a lid on each tank, the scientists would have been able to collect and measure all the gases emitted by each section. F is correct; the scientists would get a better measurement if none of the emitted gases were lost from the tank. G is incorrect; the scientists’ results would be incorrect if atmospheric gases entered the tank. H is incorrect; the bacteria were in the soil and were not likely to leave the tanks. J is incorrect; the tanks were made of glass allowing sunlight to enter the tanks.

17. **The best answer is D.** According to Figures 1 and 2, the amount of CO$_2$ emitted from the fen soil at each WT level was greater than the amount emitted from the bog soil. The amount of CH$_4$ emitted from the fen soil at each WT level was also greater than the amount emitted from the bog soil. One may conclude that the levels of nutrients that sustain both types of bacteria are greater in the fen soil than in the bog soil. A is incorrect; the data suggest that the fen soil contains higher levels of nutrients for both aerobic and anaerobic bacteria. B is incorrect; the data suggest that there are higher levels of nutrients for aerobic bacteria in fen soil. C is incorrect; the data suggest that there are higher levels of nutrients for anaerobic bacteria in fen soil. D is correct.

18. **The best answer is F.** According to the passage, aerobic bacteria generate CO$_2$. The results illustrated in Figures 1 and 2 show that CO$_2$ was produced in both types of soil at all WT levels, indicating that aerobic bacteria were present in the soil sections that were completely submerged in water. F is correct. G is incorrect; CO$_2$ was also emitted from those sections. H and J are incorrect; the results indicate that aerobic bacteria were present in all the sections.
19. **The best answer is C.** According to Figure 2, the fen soil section with a WT of −10 cm had a total CO₂ emission of 48 mol C/m² over the 3-month period. The average CO₂ emission per month is 48/3 = 16 mol C/m². A is incorrect; an average CO₂ emission of 10 mol C/m² would result in a total emission of 30 mol C/m². B is incorrect; an average CO₂ emission of 13 mol C/m² would result in a total emission of 39 mol C/m². C is correct; an average CO₂ emission of 16 mol C/m² would result in a total emission of 48 mol C/m². D is incorrect; an average CO₂ emission of 19 mol C/m² would result in a total emission of 57 mol C/m².

20. **The best answer is J.** F is incorrect; because the tanks were covered, no precipitation would fall on the samples. G is incorrect; all live plants were removed from the sections. H is incorrect; the volume of each sample was much less than the wetlands. J is correct; because the tanks were made of glass, the samples would be exposed to the same amount of daylight as the wetlands.

**Passage IV**

21. **The best answer is B.** Because the weight of an object is related to its mass, the door with the greatest mass is the door with the greatest weight. According to the passage, the door with the greatest weight had a weight of 76 lb and was used in Study 2. A is incorrect; the door used in Study 1 had a weight of 61 lb. B is correct; doors with weights of 51 lb, 61 lb, and 76 lb were used in Study 2. C is incorrect; the doors used in Study 3 each had a weight of 61 lb. D is incorrect; the doors tested in Study 2 had different masses.

22. **The best answer is F.** According to the passage, in Study 2, D was held constant, and W and S were varied. In Study 3, W was held constant, and D and S were varied. F is correct. G is incorrect; W was varied in Study 2. H is incorrect; W was varied in Study 2 only. J is incorrect; W was held constant in Study 3 only.

23. **The best answer is D.** According to the results of Study 2, when D = 30 in and S = 50 in, \( F_{n,av} \) increases as W increases. When \( W = 76 \) lb, \( F_{n,av} = 46 \) lb. If an additional door with \( W = 90 \) lb had been tested, \( F_{n,av} \) would most likely have been greater than 46 lb. A, B, and C are incorrect; \( F_{n,av} \) would have been greater than 45 lb. D is correct.

24. **The best answer is H.** Figure 1 shows that \( F_{v,av} \) remained constant at all values of S. Figure 1 also shows that \( F_{h,av} \) was greater than \( F_{v,av} \) for all \( S < 30 \) in, equal to \( F_{v,av} \) for \( S = 30 \) in, and less than \( F_{v,av} \) for all \( S > 30 \) in. F and G are incorrect; \( F_{h,av} \) was greater than \( F_{v,av} \) for all \( S < 30 \) in. H is correct; \( F_{h,av} \) was greater than \( F_{v,av} \) for all \( S < 30 \) in, and less than \( F_{v,av} \) for all \( S > 30 \) in. J is incorrect; \( F_{h,av} \) was less than \( F_{v,av} \) for all \( S > 30 \) in.
25. The best answer is B. According to Figure 2, in Study 2, the lowest $F_{n,av}$ was 27 lb. According to Figure 3, in Study 3, the lowest $F_{n,av}$ was 33 lb. The lowest value for $F_{n,av}$ of 27 lb was measured when $W = 51$ lb, $D = 30$ in, and $S = 70$ in. A is incorrect; under these conditions, $F_{n,av} = 45$ lb. B is correct; under these conditions, $F_{n,av} = 27$ lb. C is incorrect; under these conditions, $F_{n,av} = 48$ lb. D is incorrect; under these conditions, $F_{n,av} = 33$ lb.

26. The best answer is J. Figure 1 shows that as $S$ was varied, there was no change in $F_{v,av}$, while $F_{h,av}$ decreased as $S$ increased. $F_{v,av}$ was independent of $S$. F is incorrect; this shows that $F_{h,av}$ was dependent on $S$. G is incorrect; $F_{h,av}$ did not remain constant as $S$ increased. H is incorrect; $F_{v,av}$ did not decrease as $S$ increased. J is correct; $F_{v,av}$ remained constant as $S$ increased.

27. The best answer is C. A is incorrect; according to Figure 3, under these conditions, the net force on each hinge was 55 lb and the hinge would not break. B is incorrect; under these conditions, the net force on each hinge was 35 lb and the hinge would not break. C is correct; under these conditions, the net force on each hinge was 62 lb and the hinge would break. D is incorrect; under these conditions, the net force on each hinge was 37 lb and the hinge would not break.

Passage V

28. The best answer is J. According to the passage, none of the students mentioned argon. All four students referred to “almost all the gas remaining . . . ,” which suggests that other gases, such as argon, could be present. The fact that air contains less than 1% argon by volume does not weaken the explanation given by any of the students. F, G, and H are incorrect; the information does not weaken any of the explanations. J is correct.

29. The best answer is A. Because the quartz tube was heated with a Bunsen burner, it was important that the silicone hoses had a strong resistance to heat. Because a chemical reaction was taking place when the steel wool was heated, it was important that the silicone hoses have a low chemical reactivity. No water was used in the experiment, nor was water generated, and therefore the solubility of the silicone hoses in water would not be important. A is correct; it is most important that the silicone hoses be resistant to heat and have a low chemical reactivity. B is incorrect; the hoses should also have low chemical reactivity, and the water solubility of the hoses is not relevant. C is incorrect; the hoses should also have strong resistance to heat, and the water solubility of the hoses is not relevant. D is incorrect; the water solubility of the hoses is not relevant.
30. **The best answer is J.** According to Student 4, the Fe reacted with CO$_2$ in the air, and after the reaction, almost all the remaining gas was O$_2$. Because the CO$_2$ was used up, the percent CO$_2$ by volume decreased. Because the remaining gas was nearly all O$_2$, the percent O$_2$ by volume increased as the CO$_2$ reacted. F is incorrect; the percent CO$_2$ decreased as the CO$_2$ reacted with the Fe. G is incorrect; the percent CO$_2$ decreased and the percent O$_2$ increased. H is incorrect; the percent O$_2$ increased as the amount of CO$_2$ decreased. J is correct.

31. **The best answer is C.** According to Student 1, air contains 20% N$_2$ by volume, and after the N$_2$ reacted with the Fe, almost all the gas remaining was O$_2$. It follows that Student 1 believes air is approximately 80% O$_2$. Student 2 states that air contains about 80% O$_2$. Student 3 states that air contains 20% O$_2$ by volume, and after the O$_2$ reacted with the Fe, almost all the gas remaining was N$_2$. It follows that Student 3 believes air is approximately 80% N$_2$. According to Student 4, air contains about 20% CO$_2$ by volume, and after the CO$_2$ reacted with the Fe, almost all the gas remaining was O$_2$. It follows that Student 4 believes air is approximately 80% O$_2$. Students 1, 2, and 4 all believe that air contains approximately 80% O$_2$ by volume and therefore would agree that, by volume, air contains more O$_2$ than N$_2$. A, B, and D are incorrect; Students 1, 2, and 4 would agree that, by volume, air contains more O$_2$ than N$_2$. Student 3 states that air is approximately 80% N$_2$. C is correct.

32. **The best answer is H.** In order to answer this item, the examinee needs to understand how reactants and products are placed in chemical equations. According to Student 3, the Fe reacted with the O$_2$ to form Fe$_2$O$_3$. Fe and O$_2$ are reactants and will appear on the left side of the equation. Fe$_2$O$_3$ is the product and will appear on the right side of the equation. F is incorrect; the reactants and product are on the wrong sides of this equation. G is incorrect; N$_2$ and FeN are not involved in the reaction. H is correct. J is incorrect; N$_2$ and FeN are not involved in the reaction.

33. **The best answer is B.** According to the passage, Students 1 and 4 claim that almost all the gas remaining is O$_2$. Student 2 claims that almost all the remaining gas is a mixture of about 75% O$_2$ and 25% N$_2$. Student 3 claims that almost all the remaining gas is N$_2$. Students 2 and 3 would agree that the gas remaining was at least 20% N$_2$ by volume. A is incorrect; Student 3 would also agree. B is correct. C is incorrect; Students 1 and 4 would not agree. D is incorrect; Students 2 and 3 would agree.

34. **The best answer is G.** According to Student 1, the Fe reacted with *all* the N$_2$, indicating that N$_2$ is the limiting reagent, and Fe is present in excess. Student 2 stated that the Fe reacted with *some* of the O$_2$, indicating the Fe is the limiting reagent and O$_2$ is present in excess. Student 3 stated that the Fe reacted with *all* the O$_2$, indicating that O$_2$ is the limiting reagent and Fe is present in excess. Student 4 stated that the steel wool reacted with *all* the CO$_2$, indicating that CO$_2$ was the limiting reagent and Fe was present in excess. Only Student 2 would likely agree that Fe was the limiting reagent. F, H, and J are incorrect; only Student 2 would agree that Fe was the limiting reagent. G is correct.
Passage VI

35. The best answer is C. According to Table 2, the $\Lambda^0$ baryon contains 2 spin-up quarks and 1 spin-down quark. The sum of those spins is therefore $+\frac{1}{2} \hbar$. The $\Delta^0$ baryon contains 3 spin-up quarks. The sum of those spins is therefore $+\frac{3}{2} \hbar$. $A$, $B$, and $D$ are incorrect; the spin of the $\Lambda^0$ baryon is $+\frac{1}{2} \hbar$, and the spin of the $\Delta^0$ baryon is $+\frac{3}{2} \hbar$. $C$ is correct.

36. The best answer is G. In order to answer this item, the examinee needs to know that an “electrically neutral” particle has an electric charge of 0. The quark charges are given in Table 1. $F$ is incorrect; $u$, $c$, and $t$ quarks each have a charge of $+\frac{2}{3}$ so the net charge is +2. $G$ is correct; a $u$ quark has a charge of $+\frac{2}{3}$ and the $d$ and $s$ quarks each have a charge of $-\frac{1}{3}$, so the net charge is 0. $H$ is incorrect; this baryon has 3 spin-down quarks. $J$ is incorrect; this baryon has 3 spin-up quarks.

37. The best answer is D. In order to answer this item, the examinee needs to know that the charge on a proton is +1. According to Table 2, the quark content of a proton is $uud$. According to Table 1, a $u$ quark has a charge of $+\frac{2}{3}$ and each $d$ quark has a charge of $-\frac{1}{3}$, so the net charge is +1, which is consistent with the known charge of a proton. $A$, $B$, and $C$ are incorrect. $D$ is correct.

38. The best answer is F. According to Table 2, the quark content of a $\Omega^-$ baryon is $sss$. According to Table 1, each $s$ quark has a charge of $-\frac{1}{3}$ and, therefore, the net charge of a $\Omega^-$ baryon is $-1$. $F$ is correct; the $d$, $s$, and $b$ quarks each have a charge of $-\frac{1}{3}$, so the net charge is $-1$. $G$ is incorrect; each $s$ quark has a charge of $-\frac{1}{3}$ and the $c$ quark has a charge of $+\frac{2}{3}$, so the net charge is 0. $H$ is incorrect; each $s$ quark has a charge of $-\frac{1}{3}$ and the $t$ quark has a charge of $+\frac{2}{3}$, so the net charge is 0. $J$ is incorrect; the $u$ and $c$ quarks each have a charge of $+\frac{2}{3}$ and the $s$ quark has a charge of $-\frac{1}{3}$, so the net charge is +1.

39. The best answer is A. In order to answer this item, the examinee must know that nucleons are limited to protons and neutrons. According to Table 2, the quark content of a proton is $uud$, and the quark content of a neutron is $udd$. Based on this information, one can conclude that nuclei are made up of $u$ and $d$ quarks. $A$ is correct. $B$, $C$, and $D$ are incorrect; there are only $u$ and $d$ quarks in protons and neutrons.

40. The best answer is F. The masses and charges for the quarks are given in Table 1. $F$ is correct; the $d$ quark has a mass of 5 MeV and a negative charge. The $u$ quark has a mass of 3 MeV and a positive charge. The quark with a positive charge is *not* more massive than the quark with the negative charge. $G$ is incorrect; the $s$ quark has a mass of 104 MeV and a negative charge. The $c$ quark has a mass of 1,270 MeV and a positive charge. The positively charged quark is more massive than the negatively charged quark. $H$ is incorrect; the $b$ quark has a mass of 4,200 MeV and a negative charge. The $t$ quark has a mass of 171,200 MeV and a positive charge. The positively charged quark is more massive than the negatively charged quark. $J$ is incorrect; the statement is not true for Generation 1.
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**DATE OF BIRTH**

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**USE A SOFT LEAD NO. 2 PENCIL ONLY.**

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Marking Directions: Mark only one oval for each question. Fill in response completely.

Correct mark: \(\Box\)

Incorrect marks: \(\bigcirc\) or \(\bigotimes\)

Do NOT use these incorrect or bad marks.

Overlapping mark: [ ]

Cross-out mark: [ ]

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Print your 5-character Test Form in the boxes above and fill in the corresponding oval at the right.

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#### TEST 2

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#### TEST 3

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#### TEST 4

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Practice Test 3

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Today’s Date

Directions

This booklet contains tests in English, mathematics, reading, and science. These tests measure skills and abilities highly related to high school course work and success in college. Calculators may be used on the mathematics test only.

The questions in each test are numbered, and the suggested answers for each question are lettered. On the answer document, the rows of ovals are numbered to match the questions, and the ovals in each row are lettered to correspond to the suggested answers.

For each question, first decide which answer is best. Next, locate on the answer document the row of ovals numbered the same as the question. Then, locate the oval in that row lettered the same as your answer. Finally, fill in the oval completely. Use a soft lead pencil and make your marks heavy and black. Do not use ink or a mechanical pencil.

Mark only one answer to each question. If you change your mind about an answer, erase your first mark thoroughly before marking your new answer. For each question, make certain that you mark in the row of ovals with the same number as the question.

Only responses marked on your answer document will be scored. Your score on each test will be based only on the number of questions you answer correctly during the time allowed for that test. You will not be penalized for guessing. It is to your advantage to answer every question even if you must guess.

You may work on each test only when the testing staff tells you to do so. If you finish a test before time is called for that test, you should use the time remaining to reconsider questions you are uncertain about in that test. You may not look back to a test on which time has already been called, and you may not go ahead to another test. To do so will disqualify you from the examination.

Lay your pencil down immediately when time is called at the end of each test. You may not fold or tear the pages of your test booklet. DO NOT OPEN THIS BOOKLET UNTIL TOLD TO DO SO.

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DIRECTIONS: In the five passages that follow, certain words and phrases are underlined and numbered. In the right-hand column, you will find alternatives for the underlined part. In most cases, you are to choose the one that best expresses the idea, makes the statement appropriate for standard written English, or is worded most consistently with the style and tone of the passage as a whole. If you think the original version is best, choose “NO CHANGE.” In some cases, you will find in the right-hand column a question about the underlined part. You are to choose the best answer to the question. You will also find questions about a section of the passage, or about the passage as a whole. These questions do not refer to an underlined portion of the passage, but rather are identified by a number or numbers in a box.

For each question, choose the alternative you consider best and fill in the corresponding oval on your answer document. Read each passage through once before you begin to answer the questions that accompany it. For many of the questions, you must read several sentences beyond the question to determine the answer. Be sure that you have read far enough ahead each time you choose an alternative.

PASSAGE I

Miami Time

My family is part of the Miami

tribe, a Native American, people, with strong

ties to territory in present-day Ohio, Indiana,

and Illinois. Growing up in the Midwest, I often

heard my grandmother talk about “Miami time.”

When she was doing something she loved, whether

it was making freezer jam or researching tribal history,

she refused to be rushed in a hurry. “I’m on Miami time

today,” she would say. Conversely, if we were running

late for an appointment. She would chide us by saying,

“Get a move on. We’re not running on Miami time today,

you know.”
It was a difficult concept for me to grasp. My grandmother tried to explain that “Miami time” referred to those moments, when time seemed to slow down or stand still. Recently, the meaning of her words started to sink in.

One morning, my son and I will inadvertently slip out of the world measured in seconds, minutes, and hours, and into one measured by curiosity and sensation.

[1] On a familiar trail near our house, I was pushing Jeremy in his stroller and were thinking of the day ahead and the tasks I had to complete. [2] Suddenly, he squealed with pure delight and pointed toward a clearing. [3] There, two does and three fawns stood watching us. [4] Five pairs of ears flicked like antennae seeking a signal. [5] After a few moments, the deer lowered their heads and began to eat, as if they had decided we were harmless. [6] By then, my son’s face was full of wonder.

We spent the rest of the morning veering from the trail to investigate small snatches of life. Lizards lazing in the sun and quail rustled through grasses surprised us. Wild blackberries melted on our tongues. For example, the aroma of crushed eucalyptus leaves tingled in our noses.

5. Given that all the choices are true, which one provides the best opening to this paragraph?
A. NO CHANGE
B. I remember being late for a doctor’s appointment one day.
C. My grandmother lived with us, and as a result she and I became close over the years.
D. My son asks me about my grandmother, whom he never met.

6. F. NO CHANGE
G. moments when
H. moments, as if
J. moments, because

7. A. NO CHANGE
B. spoken statements to my ears
C. expressed opinions on the matter
D. verbal remarks in conversation

8. F. NO CHANGE
G. inadvertently slip
H. are inadvertently slipping
J. inadvertently slipped

9. A. NO CHANGE
B. were having thoughts
C. thinking
D. DELETE the underlined portion.

10. F. NO CHANGE
G. does, and three fawns
H. does and three fawns,
J. does and, three fawns

11. For the sake of the logic and coherence of this paragraph, Sentence 3 should be placed:
A. where it is now.
B. before Sentence 1.
C. after Sentence 1.
D. after Sentence 4.

12. F. NO CHANGE
G. rustling
H. were rustling
J. DELETE the underlined portion.

13. A. NO CHANGE
B. On the other hand, the
C. Just in case, the
D. The

GO ON TO THE NEXT PAGE.
By the time we found our way back to the car, the sun was high in the sky. We had taken three hours to complete a hike we usually finished in forty-five minutes. Yet the hike felt shorter than ever. As we drove off, I remembered something else my grandmother used to say: “Miami time passes all too quickly.”

14. F. NO CHANGE  
G. more shorter then  
H. the shortest than  
J. shorter than

15. Suppose the writer’s goal had been to write a brief essay conveying a personal experience with “Miami time.” Would this essay successfully fulfill that goal?  
A. Yes, because it presents the narrator’s firsthand experience of a morning spent in Miami time.  
B. Yes, because it reveals that after a conversation with the grandmother, the narrator decided to live in Miami time.  
C. No, because it shares the views of more than one person with regard to the meaning of Miami time.  
D. No, because the term “Miami time” belonged to the grandmother, not to the narrator.

PASSAGE II

Faith Ringgold’s Quilting Bee

The artist Faith Ringgold has made a name for herself with her “story quilts,” lively combinations of painting, quilting, and storytelling. Each artwork consists of a painting framed by quilted squares of fabric and story panels. One of these artworks, The Sunflowers Quilting Bee at Arles, depicts a scene of women at work on a quilt in a field of towering yellow flowers that eight African American women sit around the quilt that covers their laps. Who are these people stitching among the flowers? What brings them so close that their shoulders touch?

16. F. NO CHANGE  
G. flowers and eight  
H. flowers. Eight  
J. flowers, eight

GO ON TO THE NEXT PAGE.
Thus, the answers to these questions can be found in the artwork itself. Ringgold has told the story of this gathering on two horizontal panels of text. One panel is sewn into the piece’s top border, the other into its bottom border. These eight women the story explains, strove in their various ways to support the cause of justice in the world.

In reality, these women never met to piece together a quilt. The scene comes out of the artist’s imagination as a statement of the unity of purpose that she perceives in their lives. Sojourner Truth and Harriet Tubman fought to abolish slavery and, later, was active in the crusade for suffrage. Newspaper journalist Ida B. Wells courageously spoke out for social and racial justice in the late nineteenth and early twentieth centuries.
Establishing her own hair products business, herself in the first decade of the twentieth century, millions of dollars were later bequeathed by Madam C. J. Walker to charities and educational institutions. Among the schools that benefited from this generosity, were those that Mary McLeod Bethune opened and ran in order to provide a better education for Black students. And Fannie Lou Hamer, Ella Baker, and Rosa Parks showed leadership and strength during the civil rights movement, it happened in the 1950s and 1960s. In the artwork, Ringgold has surrounded these women with bright sunflowers. The flowers seem to celebrate the women’s accomplishments and the beauty of their shared vision.

PASSAGE III

1902: A Space Odyssey

Our technologically advanced times has allowed filmmakers to create spectacular science fiction films to intrigue us with worlds beyond our experience. Imagine the excitement in 1902 when audiences first saw Le Voyage dans la lune (A Trip to the Moon), a groundbreaking movie produced by Georges Méliès.
[1] Undaunted, Méliès honed his photographic skills to tell fantasy stories instead. [2] Méliès, a French magician, was fascinated by the workings of the new motion picture camera. [3] Specializing in stage illusions, he thought the camera offered potential to expand its spectacular magic productions. [4] By 1895, he was working with the new invention. [5] He found out, however, that the public preferred live magic acts to filmed versions.

Méliès’s magician’s eye led him to discover the basics of special effects. He experimented with effects such as speeding up and slowing down the action, reversing it for backward movement, and superimposing images of fantastic creatures over real people. Using overhead pulleys and trapdoors, he was able to do interesting things.

Aware of the popularity of Jules Verne’s science fiction novels, Méliès saw exciting possibilities in filming a space odyssey. The interplanetary travel film that he created, A Trip to the Moon, had production costs of $4,000, highly excessively for its time. In this film, a space capsule that is fired and thereby launched and projected from a cannon lands in the eye of the Man in the Moon.
In a strange terrain filled with hostile creatures, the space travelers experience many adventures. They escape back to Earth in the capsule by falling off the edge of the moon, landing in the ocean, they bob around until a passing ship finally rescues them.

Producing the film long before interplanetary explorations had begun, Méliès could arouse his audience’s curiosity with unconstrained fantasy.

People are still going to theaters to see science fiction films.

40. F. NO CHANGE
   G. creatures, who they now realize live there,
   H. creatures, whom they are encountering,
   J. creatures who are found there,

41. A. NO CHANGE
   B. moon after landing
   C. moon, Landing
   D. moon, after landing

42. F. NO CHANGE
   G. would of begun,
   H. have began,
   J. had begun,

43. Which of the following alternatives to the underlined word would be LEAST acceptable?
   A. whet
   B. stimulate
   C. awaken
   D. disturb

44. Given that all the choices are true, which one would most effectively express the writer’s viewpoint about Méliès’s role in science fiction filmmaking?
   F. NO CHANGE
   G. This first space odyssey provided the genesis for a film genre that still packs theaters.
   H. Méliès made an important contribution to filmmaking many years ago.
   J. In Méliès’s production even the film crew knew a lot about space.

45. Suppose the writer’s goal had been to write a brief essay highlighting the contributions a single artist can make to a particular art form. Would this essay fulfill that goal?
   A. Yes, because the essay asserts that Méliès’s work as a magician never would have succeeded without the contributions of the artists in the film industry.
   B. Yes, because the essay presents Méliès as a magician who used his talents and curiosity to explore and excel in the film world.
   C. No, because the essay focuses on the process of making science fiction films, not on a single artist’s work.
   D. No, because the essay suggests that it took many artists working together to create the success that Méliès enjoyed.

Question 45 asks about the preceding passage as a whole.

GO ON TO THE NEXT PAGE.
Nancy Drew in the Twenty-First Century

I thought the Nancy Drew mystery series had went out of style. I was sure that girls growing up today would have more up-to-date role models and my generation’s favorite sleuth would of been retired to the library’s dusty, back rooms. I was wrong.

Nancy Drew, the teenaged heroine of heaps of young adult mystery novels, is alive and well and still on the job. I know because my niece, Liana, and her friends were reading that all summer long. By the time Liana went back to school and had followed Nancy Drew on a safari to solve The Spider Sapphire Mystery and had explored Incan ruins for clues to The Secret of the Crossword Cipher.

With Nancy’s help, Liana had read about different places and various cultures all over the world.
When I was a girl in the 1960s, my friends and I loved Nancy Drew. We loved her loyal companions, her bravado, and there was a love for her freedom to do what she wanted. We also loved how smart she was and how pretty, how confident and successful. We were surprised and delighted that eighteen-year-old Nancy was so accomplished at so many things. She was able to solve crimes, win golf tournaments, kick bad guys in the shins, and impress her father’s distinguished clients. She did it all—and without scuffing her shoes or losing her supportive boyfriend, Ned.

Liana and her friends don’t seem to care that Nancy is pretty or popular. They laugh, mockingly I think, at Nancy’s friend Bess, who squeals at spiders. They prefer her other girlfriend George, the judo expert and computer whiz. They skip over the long descriptions of outfits and fashion accessories. According to Liana, they just want to get on with the story.

55. At this point, the writer is thinking about adding the following true statement:

One of a number of series that have featured the young female detective, the Nancy Drew Mystery Story series was begun in 1930 and now totals 173 books.

Should the writer make this addition here?
A. Yes, because it supports statements about the longevity and popularity of this series.
B. Yes, because it helps to explain why the narrator “loved Nancy Drew.”
C. No, because it distracts the reader from the main focus of this paragraph.
D. No, because it fails to include relevant information about the author of the series.

56. F. NO CHANGE
G. a love for her freedom to do what she wanted.
H. her freedom to do what she wanted.
J. the freedom to do as one wants.

57. Which of the following alternatives to the underlined portion would be LEAST acceptable?
A. furthermore
B. therefore
C. likewise
D. DELETE the underlined portion.

58. F. NO CHANGE
G. was capable of solving crimes,
H. was good at crime solving,
J. solved crimes,

GO ON TO THE NEXT PAGE.
Perhaps I am overly optimistic, but I’d like to believe that Liana’s generation doesn’t love Nancy Drew because she’s a successful girl detective. They don’t need to be reminded that girls can be successful they know that. What these girls need and love are the stories themselves: those exciting adventure tales spiced with mystery.

PASSAGE V

Visiting Mars on a Budget

With its distinctive red tint and its polar ice caps, the planet Mars has fascinated humans for thousands of years. There were ancient Babylonian astronomers who associated Mars with their war god Negral, to twentieth-century science fiction writers whose works become best-sellers, this planet has often been a symbol of ill will and danger.

The United States has competed with other countries to explore space. By 2003, the National Aeronautics and Space Administration (NASA) would of sent thirty spacecraft to the red planet, speculation has been prompted that a human voyage may no longer be the stuff of fiction.

59. A. NO CHANGE  
B. successful they already know  
C. successful; they know  
D. successful, knowing

60. Which choice most effectively supports the point being made in the first part of this sentence?  
F. NO CHANGE  
G. the answers to the mysteries of their lives.  
H. a strong role model for their generation.  
J. the ability to overcome obstacles.

61. A. NO CHANGE  
B. When  
C. From  
D. Those

62. Given that all the choices are true, which one is most relevant to the statement that follows in this sentence?  
F. NO CHANGE  
G. with their wild imaginations about outer space,  
H. who penned spine-tingling stories of “little green men from Mars,”  
J. who created images of Mars in literature.

63. Given that all the choices are true, which one best leads from the preceding paragraph to the subject of this paragraph?  
A. NO CHANGE  
B. Today, such negative associations seem to be dissipating.  
C. In 1958, the United States founded an agency to run its space program.  
D. Earth and Mars are both planets in the inner solar system.

64. F. NO CHANGE  
G. had sent  
H. send  
J. have sent

65. A. NO CHANGE  
B. to which speculation has prompted  
C. prompting speculation  
D. which is speculation

GO ON TO THE NEXT PAGE.
Few would deny that the idea of a human mission to Mars is exciting, who is ready to pay for such an expedition?

Recent reports suggest that the cost of a human voyage to Mars could run as high as 100 billion dollars. This is a startling number, especially in light of the fact that the International Space Station, the most ambitious NASA project yet, carried a projected price tag of “only” 17 billion dollars. In the end, NASA overspent on the International Space Station.

One can only imagine if the final price of a human voyage to Mars would be.

In contrast, the two Mars Rovers—robotic spacecraft launched in 2003—carried a combined price tag of less than one billion dollars. These Rovers are sophisticated pieces of technology, with the capacity and ability to examine soil and rocks. Their equipment may answer questions that have long been posed about the presence of water and life on Mars.

66. F. NO CHANGE
   G. Maybe a few
   H. Although few
   J. Few, if any,

67. A. NO CHANGE
   B. yet
   C. yet:
   D. yet—

68. The writer is considering adding the following true information to the end of the preceding sentence (placing a comma after the word Station):
   with a final construction cost of almost 30 billion dollars.
   Should the writer make this addition?
   F. Yes, because it strengthens the assertion made in this sentence by adding explicit detail.
   G. Yes, because it proves space flight will be more affordable in the future.
   H. No, because it weakens the point made in the paragraph about the cost of human flight to Mars.
   J. No, because it detracts from the essay’s focus on the human experience in travel to Mars.

69. A. NO CHANGE
   B. what
   C. how
   D. DELETE the underlined portion.

70. Given that all the choices are true, which one most effectively describes what the Mars Rovers are?
   F. NO CHANGE
   G. which captured the imagination of the general public—
   H. the products described at length in the media—
   J. familiar to many who watched the news coverage at the time—

71. A. NO CHANGE
   B. genuine capacity
   C. potential capacity
   D. capacity
Sending machines unaccompanied by humans to Mars does drain some of the romance out of aging or older visions of space travel. In other words, we need to keep in mind that the right equipment can accomplish as much as any crew of scientists, if not more—such as a fraction of the cost. Before any astronaut boards a spacecraft for that distant planet, the staggering expense of such a mission should be carefully considered.

72. F. NO CHANGE
G. old age
H. aging old
J. age-old

73. A. NO CHANGE
B. For that reason alone,
C. In that time frame,
D. Even so,

74. F. NO CHANGE
G. at
H. but only
J. DELETE the underlined portion.

75. The writer is considering ending the essay with the following statement:

With the passage of time, humans will continue to gaze in awe toward the heavenly skies as a source of inspiration and mystery.

Should the writer add this sentence here?
A. Yes, because it captures the emotion that is the basis for the space exploration described in the essay.
B. Yes, because it invites the reader to reflect on the insignificance of money in relation to the mystery of space.
C. No, because it does not logically follow the essay’s chronological history of people who traveled in space.
D. No, because it strays too far from the essay’s focus on Mars and the cost of sending humans there.

END OF TEST 1
STOP! DO NOT TURN THE PAGE UNTIL TOLD TO DO SO.
MATHEMATICS TEST
60 Minutes—60 Questions

DIRECTIONS: Solve each problem, choose the correct answer, and then fill in the corresponding oval on your answer document.

Do not linger over problems that take too much time. Solve as many as you can; then return to the others in the time you have left for this test.

You are permitted to use a calculator on this test. You may use your calculator for any problems you choose, but some of the problems may best be done without using a calculator.

Note: Unless otherwise stated, all of the following should be assumed.

1. Illustrative figures are NOT necessarily drawn to scale.
2. Geometric figures lie in a plane.
3. The word line indicates a straight line.
4. The word average indicates arithmetic mean.

1. On level ground, a vertical rod 12 feet tall casts a shadow 4 feet long, and at the same time a nearby vertical flagpole casts a shadow 12 feet long. How many feet tall is the flagpole?
   A. 4
   B. 8
   C. 12
   D. 20
   E. 36

2. Kalino earned 85, 95, 93, and 80 points on the 4 tests, each worth 100 points, given so far this term. How many points must he earn on his fifth test, also worth 100 points, to average 90 points for the 5 tests given this term?
   F. 87
   G. 88
   H. 90
   J. 92
   K. 97

3. If \( x = -5 \), what is the value of \( \frac{x^2 - 1}{x+1} \)?
   A. -6
   B. -4
   C. 4
   D. \( 5 \frac{4}{5} \)
   E. 19

DO YOUR FIGURING HERE.

GO ON TO THE NEXT PAGE.
4. Kaya ran $1\frac{2}{5}$ miles on Monday and $2\frac{1}{3}$ miles on Tuesday. What was the total distance, in miles, Kaya ran during those 2 days?

F. $3\frac{2}{15}$
G. $3\frac{3}{8}$
H. $3\frac{2}{3}$
J. $3\frac{7}{15}$
K. $3\frac{11}{15}$

5. Consider the 3 statements below to be true.
   - All insects that are attracted to honey are ants.
   - Insect I is not an ant.
   - Insect J is attracted to honey.

Which of the following statements is necessarily true?
A. Insect I is an ant not attracted to honey.
B. Insect I is an ant attracted to honey.
C. Insect I is attracted to honey.
D. Insect J is not attracted to honey.
E. Insect J is an ant.

6. What is the value of the expression $\sqrt{\frac{m}{x-3}}$ when $x = -1$ and $m = -16$?

F. $-2$
G. 2
H. $2\sqrt{2}$
J. $2i$
K. $2i\sqrt{2}$

7. Tickets for a community theater production cost $6 each when bought in advance and $8 each when bought at the door. The theater group’s goal is at least $2,000 in ticket sales for opening night. The theater group sold 142 opening-night tickets in advance. What is the minimum number of tickets they need to sell at the door on opening night to make their goal?

A. 143
B. 144
C. 192
D. 250
E. 357
8. Mark and Juanita own a sandwich shop. They offer 3 kinds of bread, 5 kinds of meat, and 3 kinds of cheese. Each type of sandwich has a combination of exactly 3 ingredients: 1 bread, 1 meat, and 1 cheese. How many types of sandwiches are possible?
   F. 11
   G. 15
   H. 30
   J. 45
   K. 120

9. If $12(x - 11) = -15$, then $x = ?$
   A. $\frac{-49}{4}$
   B. $\frac{-13}{6}$
   C. $\frac{-5}{4}$
   D. $\frac{-1}{3}$
   E. $\frac{39}{4}$

10. In the figure below, A, D, C, and E are collinear. $\overline{AD}$, $\overline{BD}$, and $\overline{BC}$ are all the same length, and the angle measure of $\angle ABD$ is as marked. What is the degree measure of $\angle BCE$?

   F. 50°
   G. 100°
   H. 105°
   J. 130°
   K. 160°

11. If $f(x) = 9x^2 + 5x - 8$, then $f(-2) = ?$
   A. -54
   B. -18
   C. 18
   D. 36
   E. 38

12. What is the least common multiple of 30, 20, and 70?
   F. 40
   G. 42
   H. 120
   J. 420
   K. 42,000
13. While doing a problem on his calculator, Tom meant to divide a number by 2, but instead he accidentally multiplied the number by 2. Which of the following calculations could Tom then do to the result on the calculator screen to obtain the result he originally wanted?
   A. Subtract the original number
   B. Multiply by 2
   C. Multiply by 4
   D. Divide by 2
   E. Divide by 4

14. The 8-sided figure below is divided into 5 congruent squares. The total area of the 5 squares is 125 square inches. What is the perimeter, in inches, of the figure?
   F. 25
   G. 60
   H. 80
   J. 100
   K. 125

15. Hai has $100 available to buy USB drives to back up data for his business computers. Each USB drive has a price of $8, and Hai will pay a sales tax of 7% of the total price of the USB drives. What is the maximum number of USB drives Hai can buy?
   A. 11
   B. 12
   C. 13
   D. 14
   E. 15

16. A certain computer performs $1.5 \times 10^8$ calculations per second. How many seconds would it take this computer to perform $6.0 \times 10^{16}$ calculations?
   F. $2.5 \times 10^{-9}$
   G. $9.0 \times 10^9$
   H. $4.0 \times 10^2$
   J. $4.0 \times 10^8$
   K. $9.0 \times 10^{24}$

17. One of the following is an equation of the linear relation shown in the standard (x, y) coordinate plane below. Which equation is it?
   A. $y = 5x$
   B. $y = 2x$
   C. $y = 5x + 2$
   D. $y = 2x - 5$
   E. $y = 2x + 5$
18. A square is circumscribed about a circle of 7-foot radius, as shown below. What is the area of the square, in square feet?

F. 49
G. 56
H. 98
J. $49\pi$
K. 196

19. Two workers were hired to begin work at the same time. Worker A’s contract called for a starting salary of $20,000 with an increase of $800 after each year of employment. Worker B’s contract called for a starting salary of $15,200 with an increase of $2,000 after each year of employment. If $x$ represents the number of full years’ employment (that is, the number of yearly increases each worker has received), which of the following equations could be solved to determine the number of years until B’s yearly salary equals A’s yearly salary?

A. $20,000 + 800x = 15,200 + 2,000x$
B. $20,000 + 2,000x = 15,200 + 800x$
C. $(20,000 + 800)x = (15,200 + 2,000)x$
D. $(2,000 + 800)x = 20,000 - 15,200$
E. $(2,000 - 800)x = 20,000 + 15,200$

20. A ramp for loading trucks is 13 feet long and covers 12 feet along the level ground, as shown below. How many feet high is the highest point on the ramp?

F. 1
G. 2
H. 4
J. 5
K. $6\frac{1}{4}$
21. The expression $7(x + 3) - 3(2x - 2)$ is equivalent to:
   A. $x + 1$
   B. $x + 15$
   C. $x + 19$
   D. $x + 23$
   E. $x + 27$

22. If 115% of a number is 460, what is 75% of the number?
   F. 280
   G. 300
   H. 320
   J. 345
   K. 400

23. When $(2x - 3)^2$ is written in the form $ax^2 + bx + c$, where $a$, $b$, and $c$ are integers, $a + b + c = ?$
   A. $-17$
   B. $-5$
   C. 1
   D. 13
   E. 25

24. What is the area, in square feet, of the figure below?

   F. 60
   G. 80
   H. 275
   J. 375
   K. 450

GO ON TO THE NEXT PAGE.
25. Barb is going to cover a rectangular area 8 feet by 10 feet with rectangular paving blocks that are 4 inches by 8 inches by 2 inches to make a flat patio. What is the minimum number of paving blocks she will need if all the paving blocks will face the same direction? (Note: Barb will not cut any of the paving blocks.)

A. 80
B. 360
C. 601
D. 960
E. 1,213

26. What is the slope of the line represented by the equation $6y - 14x = 5$?

F. $\frac{-14}{6}$
G. $\frac{5}{6}$
H. $\frac{7}{3}$
J. 6
K. 14

27. Let $m$ and $n$ be 2 positive integers, such that $m < n$. Which of the following compound inequalities must be true?

A. $0 < \sqrt{mn} < m$
B. $1 < \sqrt{mn} < m$
C. $m < \sqrt{mn} < n$
D. $\sqrt{m} < \sqrt{mn} < \sqrt{n}$
E. $\sqrt{m} - n < \sqrt{mn} < \sqrt{m + n}$

28. Two similar triangles have perimeters in the ratio 3:5. The sides of the smaller triangle measure 3 cm, 5 cm, and 7 cm, respectively. What is the perimeter, in centimeters, of the larger triangle?

F. 15
G. 18
H. 20
J. 25
K. 36
29. Thomas and Jonelle are playing darts in their garage using the board with the point values for each region shown below. The radius of the outside circle is 10 inches, and each of the other circles has a radius 2 inches smaller than the next larger circle. All of the circles have the same center. Thomas has only 1 dart left to throw and needs at least 30 points to win the game. Assuming that his last dart hits at a random point within a single region on the board, what is the percent chance that Thomas will win the game?

A. 36%
B. 30%
C. 16%
D. 9%
E. 1 1/2%

30. When asked his age, the algebra teacher said, “If you square my age, then subtract 23 times my age, the result is 50.” How old is he?

F. 23
G. 25
H. 27
J. 46
K. 50

31. The distance, \( d \), an accelerating object travels in \( t \) seconds can be modeled by the equation \( d = \frac{1}{2}at^2 \), where \( a \) is the acceleration rate, in meters per second per second. If a car accelerates from a stop at the rate of 20 meters per second per second and travels a distance of 80 meters, about how many seconds did the car travel?

A. Between 1 and 2
B. Between 2 and 3
C. Between 3 and 4
D. 4
E. 8

32. Which of the following is the set of all real numbers \( x \) such that \( x + 3 > x + 5 \)?

F. The empty set
G. The set containing all real numbers
H. The set containing all negative real numbers
J. The set containing all nonnegative real numbers
K. The set containing only zero
A survey in a study skills class asked the 20 students enrolled in the class how many hours (rounded to the nearest hour) they had spent studying on the previous evening. The 20 responses are summarized by the histogram below.

33. What fraction of the students responded that they had spent less than 3 hours studying?

- A. \( \frac{13}{100} \)
- B. \( \frac{1}{3} \)
- C. \( \frac{3}{10} \)
- D. \( \frac{13}{20} \)
- E. \( \frac{17}{20} \)

34. The teacher decides to show the data in a circle graph (pie chart). What should be the measure of the central angle of the sector for 3 hours?

- F. 18°
- G. 20°
- H. 36°
- J. 72°
- K. 90°

35. To the nearest tenth of an hour, what is the average number of hours for the 20 survey responses?

- A. 2.0
- B. 2.1
- C. 2.3
- D. 2.5
- E. 3.0
36. Pentagons have 5 diagonals, as illustrated below.

How many diagonals does the octagon below have?

F. 8  
G. 16  
H. 20  
J. 30  
K. 40

37. The bottom of the basket of a hot-air balloon is parallel to the level ground. One taut tether line 144 feet long is attached to the center of the bottom of the basket and is anchored to the ground at an angle of 72°, as shown in the figure below. Which of the following expressions gives the distance, in feet, from the center of the bottom of the basket to the ground?

A.  \( \frac{144}{\cos 72^\circ} \)  
B.  \( \frac{144}{\sin 72^\circ} \)  
C.  144 \( \tan 72^\circ \)  
D.  144 \( \cos 72^\circ \)  
E.  144 \( \sin 72^\circ \)

38. The coordinates of the endpoints of \( \overline{GH} \), in the standard \((x, y)\) coordinate plane, are \((-8, -3)\) and \((2, 3)\). What is the \(x\)-coordinate of the midpoint of \( \overline{GH} \)?

F.  -6  
G.  -3  
H.  0  
J.  3  
K.  5

GO ON TO THE NEXT PAGE.
39. Let \(2x + 3y = 4\) and \(5x + 6y = 7\). What is the value of \(8x + 9y\)?
   A. \(-10\)
   B. \(-1\)
   C. \(2\)
   D. \(7\)
   E. \(10\)

40. What are the values of \(\theta\), between 0 and \(2\pi\), when \(\tan \theta = -1\)?
   F. \(\frac{\pi}{4}\) and \(\frac{3\pi}{4}\) only
   G. \(\frac{\pi}{4}\) and \(\frac{5\pi}{4}\) only
   H. \(\frac{3\pi}{4}\) and \(\frac{7\pi}{4}\) only
   J. \(\frac{3\pi}{4}\) and \(\frac{7\pi}{4}\) only
   K. \(\frac{\pi}{4}\), \(\frac{3\pi}{4}\), \(\frac{5\pi}{4}\), and \(\frac{7\pi}{4}\)

41. For the complex number \(i\) and an integer \(x\), which of the following is a possible value of \(i^x\)?
   A. \(0\)
   B. \(1\)
   C. \(2\)
   D. \(3\)
   E. \(4\)

42. A can of soda pop has the shape of a right circular cylinder with an inside height of 6 inches and an inside diameter of 2 inches. When you pour the soda pop from the full can into a cylindrical glass with an inside diameter of 3 inches, about how many inches high is the soda pop in the glass?
   (Note: The volume of a right circular cylinder is \(\pi r^2 h\).)
   F. \(2\frac{2}{3}\)
   G. 4
   H. 5
   J. \(6\frac{2}{3}\)
   K. 8
43. The height and radius of the right circular cylinder below are given in meters. What is the volume, in cubic meters, of the cylinder?

A. \(30\pi\)  
B. \(31\pi\)  
C. \(150\pi\)  
D. \(180\pi\)  
E. \(900\pi\)

44. Lines \(l_1\) and \(l_2\) intersect each other and 3 parallel lines, \(l_3\), \(l_4\), and \(l_5\), at the points shown in the figure below. The ratio of the perimeter of \(\triangle ABC\) to the perimeter of \(\triangle AFG\) is 1:3. The ratio of \(DE\) to \(FG\) is 2:3. What is the ratio of \(AC\) to \(CE\)?

F. 1:1  
G. 1:2  
H. 1:3  
J. 2:1  
K. 3:1

45. A rocket lifted off from a launch pad and traveled vertically 30 kilometers, then traveled 40 kilometers at 30° from the vertical, and then traveled 100 kilometers at 45° from the vertical, as shown in the figure below. At that point, the rocket was how many kilometers above the height of the launch pad?

A. 100  
B. 170  
C. 190  
D. \(20\sqrt{3} + 50\sqrt{2}\)  
E. \(30 + 20\sqrt{3} + 50\sqrt{2}\)

GO ON TO THE NEXT PAGE.
46. Machine A produces 500 springs a day. The number of defective springs produced by this machine each day is recorded for 60 days. Based on the distribution given below, what is the expected value of the number of defective springs produced by Machine A in any single day?

<table>
<thead>
<tr>
<th>Number, n, of defective springs produced</th>
<th>Probability that n defective springs are produced in any single day</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.70</td>
</tr>
<tr>
<td>1</td>
<td>0.20</td>
</tr>
<tr>
<td>2</td>
<td>0.05</td>
</tr>
<tr>
<td>3</td>
<td>0.05</td>
</tr>
</tbody>
</table>

F. 0.00  
G. 0.45  
H. 0.70  
J. 1.00  
K. 1.50

47. The height above the ground, h units, of an object t seconds after being thrown from the top of a building is given by the equation \( h = -2t^2 + 10t + 48 \). An equivalent factored form of this equation shows that the object:

A. starts at a point 2 units off the ground.  
B. reaches a maximum height of 3 units.  
C. reaches a maximum height of 8 units.  
D. reaches the ground at 3 seconds.  
E. reaches the ground at 8 seconds.

48. For all positive values of g and h, which of the following expressions is equivalent to

\[ g^2 \sqrt[5]{g^3 \cdot h^4} \] ?

F. \( g^2h^2 \sqrt[5]{g^3h^4} \)  
G. \( g^3h \sqrt[5]{g^2h^4} \)  
H. \( g^2h^3 \sqrt[5]{g^3h^2} \)  
J. \( g^4h^4 \sqrt[5]{gh} \)  
K. \( g^7h \)

49. The value of \( \log_5 (5^{12}) \) is between which of the following pairs of consecutive integers?

A. 0 and 1  
B. 4 and 5  
C. 5 and 6  
D. 6 and 7  
E. 9 and 10
A storage facility is currently offering a special rate to customers who sign contracts for 6 months or more. According to this special rate, the first month’s rent is $1, and for each month after the first month, customers pay the regular monthly rental rate. The table below shows the storage unit sizes available, the floor dimensions, and the regular monthly rental rate. All the units have the same height.

<table>
<thead>
<tr>
<th>Size</th>
<th>Floor dimensions, in meters</th>
<th>Regular monthly rental rate</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>$2 \times 4$</td>
<td>$30$</td>
</tr>
<tr>
<td>2</td>
<td>$4 \times 4$</td>
<td>$60$</td>
</tr>
<tr>
<td>3</td>
<td>$4 \times 8$</td>
<td>$100$</td>
</tr>
<tr>
<td>4</td>
<td>$8 \times 8$</td>
<td>$150$</td>
</tr>
<tr>
<td>5</td>
<td>$8 \times 16$</td>
<td>$200$</td>
</tr>
</tbody>
</table>

50. Daria will sign a contract to rent a Size 3 unit for 12 months at the current special rate. The amount Daria will pay for 12 months at the current special rate represents what percent decrease from the regular rental rate for 12 months?

F. 8.25%
G. 8.33%
H. 8.42%
J. 9.00%
K. 9.09%

51. Size 5 units can be subdivided to form other sizes of units. What is the greatest number of Size 1 units that can be formed from a single Size 5 unit?

A. 2
B. 4
C. 8
D. 10
E. 16

52. Janelle, the owner of the storage facility, is considering building new units that have floor dimensions larger than Size 5 units. She will use the floor area to determine the heating requirements of these larger units. For this calculation, Janelle will use the same relationship between the unit size number and the respective floor area for Sizes 1 through 5. Which of the following expressions gives the floor area, in square meters, of a Size \(x\) storage unit?

F. \(2^x\cdot x\)
G. \(2^x\)
H. \(2(2^{x-1})\)
J. \(2(x + 1)^2\)
K. \((x + 2)^2\)
53. A trigonometric function with equation $y = a \sin(bx + c)$, where $a$, $b$, and $c$ are real numbers, is graphed in the standard $(x,y)$ coordinate plane below. The period of this function $f(x)$ is the smallest positive number $p$ such that $f(x + p) = f(x)$ for every real number $x$. One of the following is the period of this function. Which one is it?

A. $\frac{\pi}{2}$  
B. $\pi$  
C. $2\pi$  
D. $4\pi$  
E. 2

54. The component forms of vectors $u$ and $v$ are given by $u = (5,3)$ and $v = (2,-7)$. Given that $2u + (-3v) + w = 0$, what is the component form of $w$?

F. $(-16, 15)$  
G. $( -4, -27)$  
H. $(3, 10)$  
J. $(4, 27)$  
K. $(16,-15)$

55. For how many integers $x$ is the equation $3^{x+1} = 9^{x-2}$ true?

A. 0  
B. 1  
C. 2  
D. 3  
E. An infinite number
56. In $\triangle ABC$ shown below, the length of $AC$ and the measure of $\theta$ will remain constant. The length of $AC$ is 20 inches and the measure of $\angle C$ is equal to $\theta$. Initially, the length of $\overline{BC}$ is 15 inches, and the length of $\overline{BC}$ is the function given by $f(t) = 15 - 2t$, where $t$ is time, in seconds, since the length of $\overline{BC}$ began to decrease. What is the time, $t$, at which the resulting triangle will have an area that is $\frac{1}{2}$ the area of the original triangle?

(Note: The area of a triangle is $\frac{1}{2}ab \sin x$, where $a$ and $b$ are the lengths of the sides that form the interior angle with measure $x$.)

57. Which of the following expressions gives the number of distinct permutations of the letters in PEOPLE?

A. $6!$
B. $4(4!)$
C. $\frac{6!}{4!}$
D. $\frac{6!}{2!}$
E. $\frac{6!}{(2!)(2!)}$
58. Which of the following expressions is equivalent to 49x^2 + 81?
   F. (7x + 9)^2
   G. (7x + 9i)^2
   H. (7x - 9i)^2
   J. (7x - 9)(7x + 9)
   K. (7x - 9i)(7x + 9i)

59. A bivariate data set of observed values along with a line of best fit for the data set are shown in the standard (x,y) coordinate plane below. The set of 4 residuals for the model is given by y_i - y(x_i), for i = 1, 2, 3, 4, where y_i is the observed y-value corresponding to the input x_i and (x_i, y(x_i)) is on the line of best fit. What is the absolute value of the largest residual for this model?

A. 2.5
B. 6.8
C. 15.0
D. 20.0
E. 42.0
60. For the first 5 possible values of $x$, the table below gives the probability, $P(x)$, that a certain factory machine will make $x$ errors on any given workday.

<table>
<thead>
<tr>
<th>$x$ errors</th>
<th>$P(x)$</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>0.0823</td>
</tr>
<tr>
<td>1</td>
<td>0.2185</td>
</tr>
<tr>
<td>2</td>
<td>0.2712</td>
</tr>
<tr>
<td>3</td>
<td>0.2046</td>
</tr>
<tr>
<td>4</td>
<td>0.1238</td>
</tr>
</tbody>
</table>

Which of the following values is closest to the probability that this machine will make at least 1 error on any given workday?

F. 0.2185
G. 0.5996
H. 0.6992
J. 0.8181
K. 0.9177

END OF TEST 2
STOP! DO NOT TURN THE PAGE UNTIL TOLD TO DO SO.
DO NOT RETURN TO THE PREVIOUS TEST.
Passage I

PROSE FICTION: This passage is adapted from the novel The Fisher King by Paule Marshall (©2000 by Paule Marshall).

It was nearing the end of the second set, the jazz show winding down when Hattie heard Abe Kaiser at the microphone call Everett Payne’s name. Heard his name and, to her surprise, saw him slowly stand up in the bullpen up front. She hadn’t seen him join the other local musicians, including Shades Bowen with his tenor sax, in what was called the bullpen, which was simply a dozen or so chairs grouped near the bandstand. The young locals gathered there each Sunday evening, hoping for a chance to perform. Because toward the end of the final set, the custom was to invite one or two of them to sit in with the band. They sometimes even got to choose the tune they wanted to play.

This Sunday, Everett Payne, not long out of the army, was the one being invited to sit in.

Breath held, Hattie watched him separate himself from the hopefuls and approach the stand, taking his time, moving with what almost seemed a deliberate pause between each step. The crowd waiting.

That was his way, Hattie knew. His body moving absently through space, his head, his thoughts on something other than his surroundings, and his eyes like a curtain he occasionally drew aside a fraction of an inch to peer out at the world. A world far less interesting than the music inside his head.

She watched now as he slowly mounted the bandstand and conferred with the bassist and drummer, those two were all he would need. Then, without announcing the name of the tune he intended playing, without in any way acknowledging the audience, he sat down at the piano and brought his hands—large hands, the fingers long and splayed and slightly arched—down on the opening bars of “Sonny Boy Blue.”

“Sonny Boy Blue!” That hokey-doke tune!

Around her, the purists looked askance at each other from behind their regulation shades and slouched deeper in their chairs in open disgust.

At first, hokey though it was, he played the song straight through as written, the rather long introduction, verse, and chorus. And he did so with great care, although at a slower tempo than was called for and with a formality that lent the Tin Pan Alley tune a depth and thoughtfulness no one else would have accorded it.

Quickly taking their cue from him, the bassist reached for his bow, the drummer for his brushes, the two of them also treating the original as if it were a serious piece of music.

Everett Payne took his time paying his respects to the tune as written, and once that was done, he hunched closer to the piano, angled his head sharply to the left, completely closed the curtain of his gaze, and with his hands commanding the length and breadth of the keyboard he unleashed a dazzling pyrotechnic of chords (you could almost see their colors), polyrhythms, seemingly unrelated harmonies, and ideas—fresh, brash, outrageous ideas. It was an outpouring of ideas and feelings informed by his own brand of lyricism and lit from time to time by flashes of the recognizable melody. He continued to acknowledge the little simple-minded tune, while at the same time furiously recasting and reinventing it in an image all his own.

A collective in-suck of breath throughout the club.

Where, Hattie wondered, did he come by the dazzling array of ideas and wealth of feeling? What was the source? It had to do, she speculated, listening intently, with the way he held his head, angled to the left like that, tilted toward both heaven and earth. His right side, his right ear directed skyward, hearing up there, in the Upper Room among the stars Mahalia sang about, a new kind of music: splintered, atonal, profane, and possessing a wonderful dissonance that spoke to him, to his soul-case. For him, this was the true music of the spheres, of the maelstrom up there. When at the piano, he kept his right ear tuned to it at all times, letting it guide him, inspire him. His other ear? It remained earthbound, trained on the bedrock that for him was Bach and the blues.

Again and again he took them on a joyous, terrifying roller coaster of a ride it seemed to Hattie, and when he finally deposited them on terra firma after close to twenty minutes, everyone in Putnam Royal...
could only sit there as if they were in church and weren’t supposed to clap. Overcome. Until finally Alvin Edwards, who lived on Decatur Street and played trumpet in the school band, leaped to his feet and renamed him.

Alvin brought everyone up with him. Including the purists who normally refused to applaud even genius. They too stood up in languid praise of him.

1. It can reasonably be inferred from the passage that Shades Bowen:
   A. did not accompany Everett Payne as he played “Sonny Boy Blue.”
   B. had been in the army with Everett Payne.
   C. was the oldest musician in the bullpen.
   D. did not usually allow the local musicians to play with the band.

2. The main purpose of the statement in line 62 is to:
   F. illustrate the high expectations the audience initially had for Everett Payne’s performance.
   G. inform the reader of the audience’s reaction to Everett Payne’s performance.
   H. counteract the narrator’s description of Everett Payne’s performance.
   J. provide proof that Everett Payne was well known to the audience.

3. The passage most strongly suggests that the second set of the jazz shows at the club is:
   A. the final set.
   B. much longer than the first set.
   C. followed by a third set on Sunday nights.
   D. performed solely by the musicians in the bullpen.

4. Which of the following details is used in the passage to indicate how the purists in the audience initially reacted to Everett Payne’s choice of music?
   F. The overall silence of the audience, including the purists
   G. The description of the audience’s collective in-suck of breath
   H. The posture the purists assumed in their seats
   J. The fact that the purists stood up

5. According to the narrator, what did Hattie see Everett Payne do prior to playing “Sonny Boy Blue”?
   A. Move quickly from his seat to the bandstand
   B. Study the audience around him
   C. Confer with the bassist and the drummer
   D. Announce the name of the tune he was going to play

6. The passage initially portrays the purists most nearly as:
   F. knowledgeable and open minded.
   G. snobbish and intolerant.
   H. rational and well educated.
   J. inexperienced and uninhibited.

7. It can reasonably be inferred from the passage that Hattie believed Bach and the blues were the:
   A. musical influences that Everett Payne tried to avoid representing when he played piano.
   B. foundation of Everett Payne’s inventive piano playing.
   C. true music of the heavens that inspired Everett Payne’s creativity as a piano player.
   D. reason why Everett Payne’s piano-playing abilities limited him to Tin Pan Alley tunes.

8. According to the passage, when Everett Payne first played “Sonny Boy Blue” straight through, he did so:
   F. more slowly than was intended by the composer.
   G. after it had been suggested by Abe Kaiser.
   H. against the wishes of the bassist and drummer.
   J. without following the original tune.

9. According to the passage, Hattie speculated that the source of Everett Payne’s musical ideas and feelings during “Sonny Boy Blue” was in:
   A. the way he tilted his head.
   B. the simplemindedness of the song.
   C. his ability to play with great formality.
   D. his connection with the silent audience.

10. The narrator states that to Hattie, Everett Payne’s performance was:
    F. overly slow and formal.
    G. deliberate yet absentminded.
    H. like a song played in a church.
    J. a roller coaster of a ride.
At the time he gave the speech, Moe was president of the National Trust for Historic Preservation.

Drive down any highway leading into any town in the country, and what do you see? Fast-food outlets, office parks and shopping malls rising out of vast barren plains of asphalt. Residential subdivisions spreading like inkblots obliterating forests and farms in their relentless march across the landscape. Cars moving sluggishly down the broad ribs of pavement or halting in frustrated clumps at choked intersections. You see communities drowning in a destructive, soulless, ugly mess called sprawl.

Many of us have developed a frightening form of selective blindness that allows us to pass by the appalling mess without really seeing it. We’ve allowed our communities to be destroyed bit by bit, and most of us have shrugged off this destruction as “the price of progress.”

Development that destroys communities isn’t progress. It’s chaos. And it isn’t inevitable, it’s merely easy. Too many developers follow standard formulas, and too many government entities have adopted laws and policies that constitute powerful incentives for sprawl.

Why is an organization like the National Trust for Historic Preservation so concerned about sprawl? We’re concerned because sprawl devastates older communities, leaving historic buildings and neighborhoods underused, poorly maintained or abandoned. We’ve learned that we can’t hope to revitalize these communities without doing something to control the sprawl that keeps pushing further and further out from the center.

But our concern goes beyond that, because preservation today is about more than bricks and mortar. There’s a growing body of grim evidence to support our belief that the destruction of traditional downtowns and older neighborhoods—places that people care about—is corroding the very sense of community that helps bind us together as a people and as a nation.

One form of sprawl—retail development that transforms roads into strip malls—is frequently spurred on by discount retailers, many of whom are now concentrating on the construction of superstores with more than 200,000 square feet of space. In many small towns, a single new superstore may have more retail space than the entire downtown business district. When a store like that opens, the retail center of gravity shifts away from Main Street. Downtown becomes a ghost town.

Sprawl’s other most familiar form—spread-out residential subdivisions that “leapfrog” from the urban fringe into the countryside—is driven largely by the American dream of a detached home in the middle of a grassy lawn. Developers frequently claim they can build more “affordable” housing on the edge of town—but “affordable” for whom?

The developer’s own expenses may be less, and the home buyer may find the prices attractive—but who picks up the extra costs of fire and police protection, new roads and new utility infrastructure in these outlying areas? We all do, in the form of higher taxes for needless duplication of services and infrastructure that already exist in older parts of our cities and towns.

People who say that sprawl is merely the natural product of marketplace forces at work fail to recognize that the game isn’t being played on a level field. Government at every level is riddled with policies that mandate or encourage sprawl.

By prohibiting mixed uses and mandating inordinate amounts of parking and unreasonable setback requirements, most current zoning laws make it impossible—even illegal—to create the sort of compact walkable environment that attracts us to older neighborhoods and historic communities all over the world. These codes are a major reason why 82 percent of all trips in the United States are taken by car. The average American household now allocates more than 18 percent of its budget to transportation expenses, most of which are auto-related. That’s more than it spends for food and three times more than it spends for health care.

Our communities should be shaped by choice, not by chance. One of the most effective ways to reach this goal is to insist on sensible land-use planning. The way we zone and design our communities either opens up or forecloses alternatives to the automobile. Municipalities should promote downtown housing and mixed-use zoning that reduce the distances people must travel between home and work. The goal should be an integrated system of planning decisions and regulations that knit communities together instead of tearing them apart. We should demand land-use planning that exhibits a strong bias in favor of existing communities.
12. Among the following quotations from the passage, the one that best summarizes what the author would like to see happen is:
   F. “laws and policies that constitute powerful incentives for sprawl” (lines 20–22).
   G. “the destruction of traditional downtowns” (line 34).
   H. “‘affordable’ housing on the edge of town” (line 53).
   J. “an integrated system of planning decisions and regulations” (lines 87–88).

13. The last paragraph differs from the first paragraph in that in the last paragraph the author:
   A. asks a question and then answers it.
   B. uses more statistics to support his arguments.
   C. incorporates more emotional language.
   D. offers solutions rather than stating a problem.

14. In the passage, the author answers all of the following questions EXCEPT:
   F. How long has sprawl been happening in US cities?
   G. Is development synonymous with progress?
   H. What is one major reason that people in the United States use automobiles so much?
   J. What should communities do to combat sprawl?

15. The author states that one superstore may do all of the following EXCEPT:
   A. have more retail space than an entire downtown.
   B. lead to serious downtown renovations.
   C. make the downtown area into a ghost town.
   D. shift the center of gravity away from downtown.

16. The statistics cited by the author in the tenth paragraph (lines 67–79) are used to illustrate the concept that:
   F. allowing mixed uses of land leads to environmental destruction.
   G. current zoning laws help create a compact, walkable environment.
   H. land-use regulations now in effect increase the overall costs of transportation.
   J. Americans spend too much of their budgets on food and health care.

17. One form of sprawl the author describes is retail development that:
   A. adjoins existing downtown areas.
   B. utilizes historic buildings.
   C. turns roads into strip malls.
   D. promotes a sense of community around a superstore.

18. As it is used in line 51, the word detached most nearly means:
   F. objective.
   G. set apart.
   H. broken apart.
   J. taken away.

19. The author uses the statement “The game isn’t being played on a level field” (line 64) most nearly to mean that:
   A. cities needlessly duplicate essential services.
   B. higher taxes for some people make their lives more difficult.
   C. marketplace forces are at work.
   D. governmental decisions influence marketplace forces.

20. The phrase mixed uses (line 67) most likely refers to:
   F. having large parking lots around even larger stores.
   G. preserving and restoring historic neighborhoods.
   H. ensuring that automobiles cannot be driven to the various local businesses.
   J. allowing one area to contain various types of development.

GO ON TO THE NEXT PAGE.
There were, amazingly, arrived at a page where things looked right. Five the last of my friends had disappeared up the trail, I'd the Yellow part and began to flip through. By the time book's colored tabs. I turned in an authoritative way to hiking companions, "I'll be a minute . . ." Famous last guide for a test drive. "Go on ahead!" I said to my was a yellow flower, a nice opportunity to take my new along. Halfway up the mountain, there by the trailside with some friends up a little mountain, taking the book owned the Peterson's for about a week, I went on a hike was an easy affair for either of us. intimacy right away, however. This wasn't going to be indispensable as eyes or hands. I didn't arrive at this become my closest companion, a slice of worldview, as end of that week I had my own copy. I have it still. tape, its inside was full of drawings of flowers. By the cover said. Its backside was ruled like a measuring WILD FLOWERS—PETERSON & McKENNY, its revealed, and I reached for it. A FIELD GUIDE TO shadow of the tree, quivering, like a veil, the book was itself. It was a thing of power. In the thin summer through the woods. The book had been left there, by As it did, the book changed: its cover was stained by water and snack food, the spine grew invitingly lax, and some of the margins sprouted cryptic annotations.

By the time the next summer came, I had fully discovered the joy of the hunt, and every new species had its trophy of data—name and place and date—to be jotted down. If I'd found a flower before, I was happy to see it again. I often addressed it with enthusiasm: Hi there, Solidago hispida! I discovered early on that a plant's Latin name is a name of power by which the plant can be uniquely identified among different spoken tongues, across continents, and through time. The genus name lashes it firmly to its closest kin, while its species name describes a personal attribute—rubrum meaning red, officinale meaning medicinal, odoratus meaning smelly, and so on. It all makes such delightful sense!

My friend Julie and I identified individual plants in our rambles, but from the particulars we began to know wholes. Bogs held one community, montane forests held another, and the plants they held in common were clues to intricate dramas of climate change and continental drift. So from plant communities it followed that the grand schemes of things, when they came our way, arrived rooted in real place and personal experience: quaternary geology, biogeography, evolutionary biology all lay on the road that we had begun to travel.

Why I persisted in carrying it around and consulting its crowded pages at every opportunity, I have no idea. The book was stubborn; well, I was stubborn, too; that was part of it. And I had no choice, really, not if I wanted to get in. A landscape may be handsome in the aggregate, but this book led to the particulars, and that's what I wanted. A less complete guide would have been easier to start with, but more frustrating in the end. A more complete book would have been impossi-

For the rest of the text, please refer to the book or online source as the passage is too long to be included here. The passage is best described as being told from the point of view of someone who is:

- tracing her developing interest in identifying flowers and in the natural world.
- reexamining the event that led her to a lifelong fascination with asters.
- reviewing her relationships with people who have shared her interest in flowers.
- describing how her hobby of identifying flowers became a profitable career.
22. As portrayed by the author, the young man responded to her question about the flower with what is best described as:
   F. acceptance.
   G. surprise.
   H. condescension.
   J. anger.

23. What name, if any, does the author report assigning to the yellow flower she came across during a mountain hike?
   A. St. Johnswort
   B. Loosestrife
   C. Puccoon
   D. The passage doesn’t name the flower.

24. Looking back at her early experiences with the Peterson’s, the author most strongly implies that the guide was:
   F. daunting at first, but in retrospect preferable to either a more or a less complete guide.
   G. easy to use in the beginning, but more frustrating in the end than a more complete guide would have been.
   H. impossible for her to follow until she started pairing it with a different guide written for beginners.
   J. appealing initially until she realized how poorly illustrated its crowded pages were.

25. As it is used in line 56, the phrase get in most nearly means:
   A. arrive at a physical location.
   B. be chosen for group membership.
   C. truly understand the subject.
   D. be friendly with someone.

26. The passage best supports which of the following conclusions about Julie?
   F. She has more experience than the author has in identifying flowers.
   G. She owns a house that’s close to either a bog or a montane forest.
   H. She sees value in understanding the various communities of plants.
   J. She stopped using the Peterson’s as her primary source of flower information.

27. The author states that the Peterson’s became her closest companion over a period of several:
   A. days.
   B. weeks.
   C. months.
   D. years.

28. In the context of the passage, the author’s statement in lines 56–58 most nearly means that she:
   F. learned to understand landscapes by looking at their overall patterns rather than their details.
   G. found that landscapes lost their appeal the more she tried to understand them logically.
   H. hoped to paint attractive portraits of landscapes by paying careful attention to details.
   J. sought a deeper knowledge of landscapes through learning about their individual parts.

29. The details in lines 64–66 primarily serve to suggest the:
   A. poor craftsmanship the publishing company used in producing the Peterson’s.
   B. transformation the author’s copy of the Peterson’s underwent as a result of heavy use.
   C. strange writing the author often encountered in reading the Peterson’s.
   D. carelessness with which the author used the Peterson’s, much to her later regret.

30. The author refers to Solidago hispida as an example of a flower that she:
   F. had great trouble identifying the first time she stumbled upon it.
   G. hopes to finally come across on one of her nature walks.
   H. was pleased to encounter again after she had learned to identify it.
   J. feels has an inappropriate name given the plant’s characteristics.
Passage IV

NATURAL SCIENCE: This passage is adapted from the article “When Research Is a Snow Job” by Sarah Boyle ©2002 by National Wildlife.

The figure is beyond comprehension: Every year, 1,000,000,000,000,000,000,000,000 (1 septillion) snowflakes fall worldwide. As the crystals fall, they encounter different atmospheric conditions that produce flakes with unique attributes. The more complex those conditions are, the more elaborate the crystals.

Kenneth Libbrecht is a physicist at the California Institute of Technology. Along with the work of scientists at the U.S. Department of Agriculture’s Agricultural Research Service (ARS), his research is uncovering new information about the magical world of snow crystals—information that has practical applications in such diverse areas as agriculture and the production of electricity.

Snow crystals are individual crystals—usually in a hexagonal form—while snowflakes are collections of two or more snow crystals. Beginning as condensed water vapor, a crystal typically grows around a nucleus of dust. Its shape depends on how the six side facets—or faces—grow in relation to the top and bottom facets. If they grow relatively tall, the crystal appears column-like; if the side facets are short compared to the length of the bottom and top facets, the crystal looks platelike.

Currently Libbrecht is trying to crack the problem of why the crystal facets’ growth varies with temperature. He believes this may have something to do with the ice surface’s “quasi-liquid” layer, which affects how water molecules stick to the surface.

By manipulating the temperature and humidity within an incubation chamber (and by adding an electric current or various gases at times), Libbrecht creates “designer” snowflakes in his lab. Such experiments are helping him determine how crystals form.

William Wergin, a retired ARS research biologist, and a colleague, Eric Erbe, were using scanning electron microscopy to look at biological problems relating to agriculture. To avoid the laborious procedure that using such equipment usually entails, the two scientists decided to freeze the tissue they were working with and look at it in the frozen state.

“One day it happened to be snowing,” says Wergin, “and we were looking for a specimen. We imaged some snowflakes and were very surprised to see what we did.” It was the first time anyone had attempted to image snow crystals with scanning electron microscopy, which provides precise detail about the crystals’ shape, structural features and metamorphosed conditions (crystals often change once on the ground depending on the surrounding environment).

Wergin called another ARS colleague, hydrologist Albert Rango, to see if the snow crystal magnifications had any applications for his research. Rango now uses Wergin’s electron microscopy data, along with microwave satellite data, in the Snowmelt Runoff Model to predict the amount of water available in a winter snowpack. For western states such as Colorado, Montana, Utah and Wyoming, about 75 percent of the annual water supply comes from snowmelt. Snowmelt water is critical to crop irrigation and hydroelectric power, as well as recreation and domestic water supplies, fisheries management and flood control.

Before employing the scanning electron microscopy results, the forecasted amounts of snowpack water were inaccurate whenever the size and shape of the snow crystals varied much from the norm. “The more we know about crystals,” notes Rango, “the easier it will be to use microwave satellite data for predictions of the snow water equivalent.”

Currently, forecasts using the model are about 90 percent accurate. A 1980 study estimated that improving the prediction by 1 percent would save $38 million in irrigation and hydropower in the western United States.

Rango is also looking ahead at climate change predictions. “Following the estimates that have been made about what will happen by 2100, things are definitely warming up,” he says. Temperature increases will likely result in a reduction in stream flow as overall snow accumulation decreases, winter precipitation runs off as rain, and water evaporates at a quicker rate. The gap between water supply and demand will magnify even more, greatly increasing water’s economic value, anticipates Rango.

Not only does the crystal research help gauge snowmelt, it is also useful in predicting avalanches, designing artificial snow, and, perhaps in the near future, examining air pollution. “You can put snow in a scanning electron microscope and tell which elements are present, such as sulfur and nitrogen,” says Wergin. “You can then see what kind of pollution is in the area and possibly track the source.”

31. It can reasonably be inferred from the passage that the information about the scientific study of snow is presented primarily to:
A. emphasize the importance of communication among scientists.
B. explain how snow crystal facets influence the snowpack in some western states.
C. showcase the varied uses of the scanning electron microscope.
D. demonstrate some of the practical applications of the study of snow crystals.

GO ON TO THE NEXT PAGE.
32. According to the passage, the use of scanning electron microscopy can save money by:
   F. encouraging scientists to make estimates of water requirements far into the future.
   G. allowing forecasters to predict more accurately the quantity of water in the snowpack.
   H. helping agricultural researchers to identify biological problems.
   J. increasing the water supply for Colorado, Montana, Utah, and Wyoming by 75 percent.

33. It can reasonably be inferred that the phrase metamorphosed conditions (lines 47–48) refers to the:
   A. temperature and humidity at which crystals form.
   B. process by which snow crystals develop from a speck of dust and water vapor.
   C. state of snow crystals after they reach the ground.
   D. major changes in environmental conditions.

34. According to the passage, the addition of electron microscopy data to the Snowmelt Runoff Model allows scientists using the model to include in their predictions detailed information about:
   F. microwave satellite data.
   G. structural variations of snow crystals.
   H. locations having the most snowfall.
   J. biological problems related to agriculture.

35. According to Rango, one reason that water’s economic value is likely to increase by the year 2100 is that:
   A. more water will be polluted by then.
   B. less water will be wasted due to more accurate predictions of the water supply.
   C. the sulfur and nitrogen content in snow is likely to increase.
   D. predicted climate changes will reduce overall snow accumulation.

36. According to the passage, snowflakes have infinite variety because:
   F. enormous numbers of snow crystals fall worldwide.
   G. falling snow crystals meet with varied atmospheric conditions.
   H. snow crystals fall at various rates, creating unique snowflakes.
   J. complexities in the atmosphere slow snow crystal development.

37. The passage states that snowflakes differ from snow crystals in that snowflakes:
   A. grow around a nucleus of dust.
   B. combine to form snow crystals.
   C. grow in relation to top and bottom facets.
   D. are composed of more than one crystal.

38. The term “designer” snowflakes (line 32) refers directly to the fact that:
   F. no two snowflakes are alike.
   G. Libbrecht produces the snowflakes in his lab.
   H. snowflakes are part of the grand design of nature.
   J. Libbrecht’s snowflakes exhibit special beauty.

39. As it is used in line 59, the word critical most nearly means:
   A. evaluative.
   B. faultfinding.
   C. vital.
   D. acute.

40. The passage states that research about snow crystals has helped scientists do all of the following EXCEPT:
   F. extract pollutants from snow.
   G. gauge snowmelt.
   H. design artificial snow.
   J. predict avalanches.
Passage I

Two measures of water quality are the number of *Escherichia coli* bacteria present and the *biotic index*, BI (a numerical value based on the type, diversity, and pollution tolerance of aquatic invertebrate animals). Both of these measures can be affected by water flow.

*E. coli* levels that are above 100 colonies formed per 100 mL of water indicate reduced water quality. Figure 1 shows the *E. coli* levels on 5 collection days at Sites 1 and 2 in a river.

<table>
<thead>
<tr>
<th>Day</th>
<th>Site 1</th>
<th>Site 2</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>101</td>
<td>16</td>
</tr>
<tr>
<td>15</td>
<td>92</td>
<td>2</td>
</tr>
<tr>
<td>30</td>
<td>708</td>
<td>4</td>
</tr>
<tr>
<td>45</td>
<td>9</td>
<td>10</td>
</tr>
<tr>
<td>60</td>
<td>5</td>
<td>5</td>
</tr>
</tbody>
</table>

Figure 1

Table 2 shows how water quality rating varies with BI. Table 2 shows the average BI of each site during the collection period.

<table>
<thead>
<tr>
<th>BI</th>
<th>Water quality rating</th>
</tr>
</thead>
<tbody>
<tr>
<td>≥ 3.6</td>
<td>excellent</td>
</tr>
<tr>
<td>2.6 to 3.5</td>
<td>good</td>
</tr>
<tr>
<td>2.1 to 2.5</td>
<td>fair</td>
</tr>
<tr>
<td>1.0 to 2.0</td>
<td>poor</td>
</tr>
</tbody>
</table>

Table 1

1. If an *E. coli* level of over 400 colonies formed per 100 mL of water is unsafe for swimming, on which of the following collection days and at which site would it have been unsafe to swim?
   A. Day 1 at Site 1
   B. Day 30 at Site 1
   C. Day 1 at Site 2
   D. Day 30 at Site 2

2. Based on Figures 1 and 2, consider the average water flow and the average *E. coli* level for Site 1 and Site 2 over the collection period. Which site had the higher average water flow, and which site had the higher average *E. coli* level?

<table>
<thead>
<tr>
<th>Higher water flow</th>
<th>Higher <em>E. coli</em> level</th>
</tr>
</thead>
<tbody>
<tr>
<td>F.</td>
<td>Site 1</td>
</tr>
<tr>
<td>G.</td>
<td>Site 1</td>
</tr>
<tr>
<td>H.</td>
<td>Site 2</td>
</tr>
<tr>
<td>J.</td>
<td>Site 2</td>
</tr>
</tbody>
</table>

3. According to Table 1, what is the relationship between water quality and biotic index?
   A. As water quality improves, biotic index increases.
   B. As water quality improves, biotic index remains the same.
   C. As water quality degrades, biotic index increases.
   D. As water quality degrades, biotic index remains the same.

4. As water quality improves, the number of *stone fly larvae* (a type of aquatic invertebrate) increases. Students hypothesized that more *stone fly larvae* would be found at Site 1 than at Site 2. Are the data presented in Table 2 consistent with this hypothesis?
   F. Yes; based on BI, Site 1 had a water quality rating of good and Site 2 had a water quality rating of poor.
   G. Yes; based on BI, Site 1 had a water quality rating of excellent and Site 2 had a water quality rating of fair.
   H. No; based on BI, Site 1 had a water quality rating of poor and Site 2 had a water quality rating of good.
   J. No; based on BI, Site 1 had a water quality rating of fair and Site 2 had a water quality rating of excellent.

5. Which set of data best supports the claim that Site 1 has *lower* water quality than Site 2?
   A. Figure 1
   B. Figure 2
   C. Table 1
   D. Table 2

6. Suppose large amounts of fertilizer from adjacent fields begin to enter the river at Site 1. The BI of this site will most likely change in which of the following ways? The BI will:
   F. increase, because water quality is likely to increase.
   G. increase, because water quality is likely to decrease.
   H. decrease, because water quality is likely to increase.
   J. decrease, because water quality is likely to decrease.
Passage II

Aluminum water-based paints (AWPs) contain aluminum (Al) flakes that give surfaces a shiny, metallic appearance. If the flakes corrode, a dull coating of aluminum hydroxide forms on them:

$$2\text{Al} + 6\text{H}_2\text{O} \rightarrow 2\text{Al(OH)}_3 + 3\text{H}_2$$

Table 1 shows the volume of $\text{H}_2$ gas produced over time (at 25°C and 1 atm) from 100 mL samples of freshly made AWPs 1−3 in 3 separate trials. AWPs 1−3 were identical except that each had a different concentration of DMEA, an AWP ingredient that increases pH.

The AWP 3 trial was repeated 4 times, but for each trial, the sample had the same concentration of 1 of 4 corrosion inhibitors (see Figure 1).

<table>
<thead>
<tr>
<th>AWP</th>
<th>pH of AWP</th>
<th>Volume (mL) of $\text{H}_2$ produced by:</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td></td>
<td>Day 2</td>
</tr>
<tr>
<td>1</td>
<td>8</td>
<td>4</td>
</tr>
<tr>
<td>2</td>
<td>9</td>
<td>21</td>
</tr>
<tr>
<td>3</td>
<td>10</td>
<td>121</td>
</tr>
</tbody>
</table>

The AWP 3 trial was repeated 4 times, but for each trial, the sample had the same concentration of 1 of 4 corrosion inhibitors (see Figure 1).

8. Based on Table 1, if the volume of $\text{H}_2$ produced by Day 10 from the AWP 1 sample had been measured, it would most likely have been:
   F. less than 133 mL.
   G. between 133 mL and 461 mL.
   H. between 461 mL and 760 mL.
   J. greater than 760 mL.

9. According to Table 1, what volume of $\text{H}_2$ was produced by AWP 1 from the time the volume was measured on Day 6 until the time the volume was measured on Day 8?
   A. 52 mL
   B. 81 mL
   C. 133 mL
   D. 214 mL

10. In the trials represented in Table 1 and Figure 1, by measuring the volume of $\text{H}_2$, the experimenters were able to monitor the rate at which:
    F. $\text{H}_2\text{O}$ is converted to Al.
    G. Al is converted to $\text{H}_2\text{O}$.
    H. Al is converted to $\text{Al(OH)}_3$.
    J. $\text{Al(OH)}_3$ is converted to Al.

Figure 1

Figure 1 adapted from Bodo Müller, "Corrosion Inhibitors for Aluminum." ©1995 by Division of Chemical Education, Inc., American Chemical Society.
11. Based on the passage, is DMEA most likely an acid or a base?
   A. An acid, because DMEA decreases pH.
   B. An acid, because DMEA increases pH.
   C. A base, because DMEA decreases pH.
   D. A base, because DMEA increases pH.

12. Consider the volume of \( \text{H}_2 \) produced by Day 2 from the AWP 3 sample that contained no corrosion inhibitor. Based on Table 1 and Figure 1, the AWP 3 sample containing EDTA produced approximately the same volume of \( \text{H}_2 \) by which of the following days?
   F. Day 1
   G. Day 4
   H. Day 7
   J. Day 10
Passage III

Students studied forces by using 2 identical platform scales, Scale A and Scale B, one of which is shown in Figure 1.

The weight of the platform of each scale was insignificant. When a force (such as that produced by a weight) was exerted on the surface of the platform, the hand rotated clockwise away from the zero point on the dial. The amount of rotation was directly proportional to the strength of the force.

Study 1

Prior to each of Trials 1−3, the students set the dial readings of both Scales A and B to zero. In each of these 3 trials, Scale A was stacked on top of Scale B (see Figure 2). In Trial 1, no weight was placed on the platform of Scale A; in Trial 2, a 5.0 newton (N) weight was placed on the platform of Scale A; and in Trial 3, a 10.0 N weight was placed on the platform of Scale A. The dial readings for the 3 trials are also shown in Figure 2.

Study 2

The students placed a pencil on the platform of each scale and positioned on top of the pencils a board that spanned the 0.40 m distance between the 2 scales. Prior to each of Trials 4−6, the students set the dial readings of Scales A and B to zero (see Figure 3).

In each of these 3 trials, a 10.0 N weight was placed on the board at various distances from the pencil on Scale B (see Figure 4). In Trial 4, the weight was 0.10 m from the pencil; in Trial 5, the weight was 0.20 m from the pencil; and in Trial 6, the weight was 0.30 m from the pencil. The dial readings for the 3 trials are also shown in Figure 4.

13. In which of the trials in Study 2, if any, was the force of the 10.0 N weight equally distributed between Scales A and B?
   A. Trial 4
   B. Trial 5
   C. Trial 6
   D. None of the trials

14. Based on the results of Trials 1 and 2, Scale A and Scale B each weighed:
   F. 2.5 N.
   G. 5.0 N.
   H. 7.5 N.
   J. 10.0 N.
15. Assume that whenever a weight was placed on a scale’s platform, a spring inside the scale was compressed. Assume also that the greater the added weight, the greater the amount of compression. Was the amount of potential energy stored in Scale A’s spring greater in Trial 1 or in Trial 3?
   A. In Trial 1, because the amount of weight on the platform of Scale A was greater in Trial 1.
   B. In Trial 1, because the amount of weight on the platform of Scale A was less in Trial 1.
   C. In Trial 3, because the amount of weight on the platform of Scale A was greater in Trial 3.
   D. In Trial 3, because the amount of weight on the platform of Scale A was less in Trial 3.

16. In a new study, suppose Scale A were placed upside down atop Scale B, so that the platform of Scale A rested directly on the platform of Scale B. Which of the following drawings best represents the results that would most likely be obtained for this arrangement?
   F. 
   H. 
   G. 
   J. 

17. The main reason the pencils were placed on the scales in Study 2 was most likely:
   A. so that the line of contact between each pencil and its platform could be used as a reference line for distance measurements.
   B. so that the board would roll from side to side, rather than sliding from side to side over the scales’ platforms.
   C. to add additional weight to the scales.
   D. to provide extra room for air above each scale’s platform, so that the air pressure would be the same above and below the platform.

18. In Study 2, as the distance between the 10.0 N weight and the pencil on Scale B increased, the amount of force exerted on the surface of Scale B’s platform:
   F. remained the same.
   G. increased only.
   H. decreased only.
   J. varied, but with no general trend.

19. Which of the following statements most likely describes an important reason for setting the dial readings of both scales to zero after Study 1, prior to each of Trials 4–6?
   A. To add the weights of the scales to each weight measurement
   B. To add the weights of the board and pencils to each weight measurement
   C. To subtract the weights of the scales from each weight measurement
   D. To subtract the weights of the board and pencils from each weight measurement

GO ON TO THE NEXT PAGE.
Passage IV

The octane number of a fuel is a measure of how smoothly the fuel burns in a gasoline engine. Lower octane fuels knock (explode) when burned, which lowers fuel efficiency and can cause engine damage. Heptane knocks considerably when burned and is given an octane number of 0. Isooctane knocks very little and is given an octane number of 100.

Different proportions of heptane and isooctane were mixed to obtain mixtures with octane numbers between 0 and 100 (see Table 1).

<table>
<thead>
<tr>
<th>Volume of heptane (mL)</th>
<th>Volume of isooctane (mL)</th>
<th>Octane number</th>
</tr>
</thead>
<tbody>
<tr>
<td>0</td>
<td>100</td>
<td>100</td>
</tr>
<tr>
<td>10</td>
<td>90</td>
<td>90</td>
</tr>
<tr>
<td>25</td>
<td>75</td>
<td>75</td>
</tr>
<tr>
<td>50</td>
<td>50</td>
<td>50</td>
</tr>
<tr>
<td>90</td>
<td>10</td>
<td>10</td>
</tr>
<tr>
<td>100</td>
<td>0</td>
<td>0</td>
</tr>
</tbody>
</table>

Experiment 1

A sample of each fuel mixture listed in Table 1 was burned in a test engine at an engine speed of 600 revolutions per minute (rpm). The number of knocks per minute was determined for each mixture. This was done so that an octane number could be assigned to any fuel by measuring its knock rate.

Experiment 2

Adding tetraethyllead (TEL) to a fuel changes its octane number. Different amounts of TEL were added to 1,000 mL samples of isooctane. Each fuel mixture was tested under the same conditions used in Experiment 1, and the measured knock rate was used to determine the octane number (see Figure 1).

Table 2

<table>
<thead>
<tr>
<th>Engine speed (rpm)</th>
<th>EOR</th>
<th>Octane number in engine of:</th>
</tr>
</thead>
<tbody>
<tr>
<td>1,500</td>
<td>97.4</td>
<td>Fuel A 98.4  Fuel B 96.7</td>
</tr>
<tr>
<td>2,000</td>
<td>95.3</td>
<td>Fuel A 96.6  Fuel B 96.1</td>
</tr>
<tr>
<td>2,500</td>
<td>93.5</td>
<td>Fuel A 95.0  Fuel B 95.4</td>
</tr>
<tr>
<td>3,000</td>
<td>91.9</td>
<td>Fuel A 92.3  Fuel B 93.8</td>
</tr>
<tr>
<td>3,500</td>
<td>90.6</td>
<td>Fuel A 90.9  Fuel B 92.5</td>
</tr>
</tbody>
</table>

GO ON TO THE NEXT PAGE.
20. Based on Experiment 3, as engine speed increases, the minimum octane number of fuel required for an engine to operate without becoming damaged:
   F. increases only.
   G. decreases only.
   H. increases, then decreases.
   J. decreases, then increases.

21. Suppose a trial had been performed in Experiment 3 at an engine speed of 2,200 rpm. At this engine speed, which of the following sets of octane numbers would most likely have been determined for Fuel A and Fuel B?
   
<table>
<thead>
<tr>
<th>Fuel A</th>
<th>Fuel B</th>
</tr>
</thead>
<tbody>
<tr>
<td>95.0</td>
<td>95.4</td>
</tr>
<tr>
<td>96.1</td>
<td>95.8</td>
</tr>
<tr>
<td>96.6</td>
<td>96.1</td>
</tr>
<tr>
<td>97.6</td>
<td>96.4</td>
</tr>
</tbody>
</table>

22. Which of the following expressions is equal to the octane number of each fuel mixture listed in Table 1?
   F. \( \frac{\text{volume of isooctane}}{\text{volume of heptane}} \times 100 \)
   G. \( \frac{\text{volume of heptane}}{\text{volume of isooctane}} \times 100 \)
   H. \( \frac{\text{volume of isooctane}}{\text{\( \text{volume of heptane} + \text{volume of isooctane} \)}} \times 100 \)
   J. \( \frac{\text{volume of heptane}}{\text{\( \text{volume of heptane} + \text{volume of isooctane} \)}} \times 100 \)

23. Based on Table 1 and Experiment 2, if 3 mL of TEL were added to a mixture of 100 mL of heptane and 900 mL of isooctane, the octane number of the resulting fuel would most likely be:
   A. less than 55.
   B. between 55 and 90.
   C. between 90 and 125.
   D. greater than 125.

24. Which of the 2 fuels from Experiment 3 would be better to use in an engine that will run at all engine speeds between 1,500 rpm and 3,500 rpm?
   F. Fuel A, because its octane number was lower than the EOR at each of the engine speeds tested.
   G. Fuel A, because its octane number was higher than the EOR at each of the engine speeds tested.
   H. Fuel B, because its octane number was lower than the EOR at each of the engine speeds tested.
   J. Fuel B, because its octane number was higher than the EOR at each of the engine speeds tested.

25. Based on Table 1, if 2 mL of heptane were mixed with 8 mL of isooctane, the octane number of this mixture would be:
   A. 2.
   B. 8.
   C. 20.
   D. 80.

26. Suppose that 1 mL of TEL is added to 1,000 mL of heptane. Based on Experiment 2, one would predict that the octane number of the TEL/heptane mixture would be:
   F. higher than the octane number of pure heptane, but lower than 115.
   G. higher than the octane number of pure heptane, and higher than 115.
   H. lower than the octane number of pure heptane, but higher than 115.
   J. lower than octane number of pure heptane, and lower than 115.
Introduction

Comets are complex mixtures of ices and dust that orbit the Sun. They can be classified by orbital period as either long-period comets or short-period comets.

Long-period comets have orbital periods of more than 200 yr and originate within our solar system in the Oort Cloud, a spherical shell of many icy bodies located at an average distance of 40,000 A.U. from the Sun (1 A.U. = average distance of Earth from the Sun). Long-period comets approach the Sun from all directions.

Short-period comets have orbital periods of 200 yr or less, and their orbital planes have inclinations 30° or less with respect to the ecliptic plane, the plane of Earth’s orbit around the Sun. Portions of these planes are shown in Figure 1.

Scientist A

Short-period comets in our solar system originate within a thin ring-shaped region called the Kuiper Belt (KB). The KB has a small inclination with respect to the ecliptic plane and is located in the solar system between 30 A.U. and 50 A.U. from the Sun. The KB contains billions of icy bodies with diameters between 10 km and 30 km. These comet-size objects are too small to be clearly discerned at that distance with telescopes located on Earth’s surface. Such telescopes have gathered indirect evidence, but not clear images, of much larger icy bodies that are part of the KB. The small inclinations of short-period comets’ orbital planes with respect to the ecliptic plane are consistent with an origin in the KB. It has been discovered that other nearby stars have similar regions of icy bodies surrounding them.

Scientist B

The KB does not exist. Short-period comets were once long-period comets. Some long-period comets pass close enough to the giant planets (for example, Jupiter) to be influenced by the gravitational fields of the giant planets and are forced into orbits with orbital periods less than 200 yr. These altered orbits have orbital planes that have small inclinations with respect to the ecliptic plane. Also, most of the studied short-period comets have orbital planes with small inclinations with respect to the orbital planes of the giant planets, which, in turn, have small inclinations with respect to the ecliptic plane.
27. Which of the following generalizations about comets is most consistent with Scientist B’s viewpoint?
   A. Long-period comets cannot become short-period comets.
   B. Short-period comets cannot become long-period comets.
   C. Long-period comets can become short-period comets.
   D. No long-period comets or short-period comets orbit the Sun.

28. Scientist A would most likely suggest that a new telescope more powerful than previous telescopes be used to search which of the following regions of space for objects in the KB?
   F. The region 100,000 A.U. beyond our solar system
   G. The region 30 A.U. to 50 A.U. from the Sun at an angle of 90° with respect to the ecliptic plane
   H. The region 30 A.U. to 50 A.U. from the Sun at angles of 0° to 30° with respect to the ecliptic plane
   J. The region closely surrounding the planet Jupiter

29. Given the information about short-period comets in the introduction, which of the following inclinations with respect to the ecliptic plane would most likely NOT be observed for the orbital planes of short-period comets?
   A. 5°
   B. 15°
   C. 30°
   D. 45°

30. According to Scientist B, which of the following planets in our solar system is most likely capable of changing the orbit of a long-period comet over time?
   F. Mercury
   G. Earth
   H. Mars
   J. Saturn

31. Comet Halley currently has an orbital period of 76 yr. According to the information provided, Scientist B would most likely currently classify Comet Halley as a:
   A. short-period comet that originated in the Oort Cloud.
   B. short-period comet that originated in the KB.
   C. long-period comet that originated in the Oort Cloud.
   D. long-period comet that originated in the KB.

32. Based on Scientist A’s viewpoint, the “much larger icy bodies” in the KB most likely have diameters of:
   F. less than 10 km.
   G. between 10 km and 20 km.
   H. between 20 km and 30 km.
   J. greater than 30 km.

33. Suppose a study of 1 nearby star revealed that it had no spherical shell of material similar to the Oort Cloud surrounding it. How would this discovery most likely affect the scientists’ viewpoints, if at all?
   A. It would weaken Scientist A’s viewpoint only.
   B. It would strengthen Scientist B’s viewpoint only.
   C. It would strengthen both scientists’ viewpoints.
   D. It would have no effect on either scientist’s viewpoint.
Passage VI

Tomato plants grow poorly in high-salt environments. This effect is caused by 2 processes:

- A net movement of H₂O between the cytoplasm of the plants’ cells and the environment via osmosis
- An increase in the cytoplasmic Na⁺ concentration

The plant Arabidopsis thaliana carries a gene, AtNHX1. The product of this gene, VAC, facilitates uptake of cytoplasmic Na⁺ by the plant’s vacuoles.

A researcher created 4 genetically identical lines of tomato plants (L1–L4). An AtNHX1 gene from Arabidopsis thaliana was isolated and 2 identical copies of this gene were incorporated into L1’s genome. This process was repeated with L2 and L3 using a different AtNHX1 allele for each line, so that L1, L2, and L3 had different genotypes for AtNHX1. The researcher then did an experiment.

Experiment

Fifty seedlings from each of the 4 lines were grown in 10 L of nutrient solution for 80 days. The 10 L nutrient solution contained H₂O, 12 g of fertilizer, and 3 g of NaCl. The nutrient solution was replaced every 5 days. After 80 days, average height, average mass (without fruit), and average fruit mass (per plant) were measured (see Table 1).

| Table 1 |
|-----------------|-----------------|-----------------|
| 3 g of NaCl/10 L nutrient solution  | Height (cm) | Mass (kg) | Fruit mass (kg) |
| Line | | | |
| L1 | 124 | 1.2 | 2.1 |
| L2 | 128 | 1.2 | 2.0 |
| L3 | 120 | 1.2 | 2.1 |
| L4 | 124 | 1.2 | 2.0 |

This process was repeated except the 10 L nutrient solution contained 60 g of NaCl instead of 3 g of NaCl (see Table 2).

| Table 2 |
|-----------------|-----------------|-----------------|
| 60 g of NaCl/10 L nutrient solution  | Height (cm) | Mass (kg) | Fruit mass (kg) |
| Line | | | |
| L1 | 119 | 1.1 | 1.9 |
| L2 | 121 | 1.1 | 1.9 |
| L3 | 61 | 0.4 | 1.1 |
| L4 | 63 | 0.5 | 1.0 |

The process was repeated again except the 10 L nutrient solution contained 120 g of NaCl instead of 3 g of NaCl (see Table 3).

| Table 3 |
|-----------------|-----------------|-----------------|
| 120 g of NaCl/10 L nutrient solution  | Height (cm) | Mass (kg) | Fruit mass (kg) |
| Line | | | |
| L1 | 118 | 1.0 | 1.8 |
| L2 | 115 | 1.0 | 1.7 |
| L3 | 34 | 0.2 | 0 |
| L4 | 36 | 0.3 | 0 |

34. One plant produced no fruit and had a height of 21 cm. Which of the following most likely describes this plant?
   F. It was from L2 and was grown in a 10 L nutrient solution containing 60 g of NaCl.
   G. It was from L2 and was grown in a 10 L nutrient solution containing 120 g of NaCl.
   H. It was from L4 and was grown in a 10 L nutrient solution containing 60 g of NaCl.
   J. It was from L4 and was grown in a 10 L nutrient solution containing 120 g of NaCl.

35. During osmosis, water migrates through a semipermeable barrier. The osmosis referred to in the passage occurs through which of the following structures?
   A. Chromosomes
   B. Nuclear envelope
   C. Cell membrane
   D. Rough endoplasmic reticulum

36. For each line, as the concentration of salt in the nutrient solutions increased, average plant mass:
   F. increased only.
   G. decreased only.
   H. increased, then decreased.
   J. decreased, then increased.

37. Which of the following was an independent variable in the experiment?
   A. Whether a line received AtNHX1
   B. Whether a tomato plant was used
   C. Plant mass without fruit
   D. Plant height

38. Which of the following best characterizes the genotype of L1 for AtNHX1 after L1 was genetically modified?
   F. It was heterozygous, since its 2 AtNHX1 alleles were different.
   G. It was heterozygous, since its 2 AtNHX1 alleles were identical.
   H. It was homozygous, since its 2 AtNHX1 alleles were different.
   J. It was homozygous, since its 2 AtNHX1 alleles were identical.

39. Suppose the data for all of the plants were plotted on a graph with height on the x-axis and mass (without fruit) on the y-axis. Suppose also that the best-fit line for these data was determined. Which of the following would most likely characterize the slope of this line?
   A. The line would not have a slope, because the line would be vertical.
   B. The slope of the line would be zero.
   C. The slope of the line would be negative.
   D. The slope of the line would be positive.

40. The researchers included 1 of the 4 lines to serve as a control. This line was most likely which one?
   F. L1
   G. L2
   H. L3
   J. L4

END OF TEST 4
STOP! DO NOT RETURN TO ANY OTHER TEST.
You may wish to photocopy these sample answer document pages to respond to the practice ACT Writing Test.

Please enter the information at the right before beginning the Writing Test.

Use a soft lead No. 2 pencil only. Do NOT use a mechanical pencil, ink, ballpoint, or felt-tip pen.

BEGIN WRITING TEST here.

If you need more space, please continue on the next page.
If you need more space, please continue on the next page.
If you need more space, please continue on the next page.
STOP here with the Writing Test.
Directions

This is a test of your writing skills. You will have forty (40) minutes to read the prompt, plan your response, and write an essay in English. Before you begin working, read all material in this test booklet carefully to understand exactly what you are being asked to do.

You will write your essay on the lined pages in the answer document provided. Your writing on those pages will be scored. You may use the unlined pages in this test booklet to plan your essay. Your work on these pages will not be scored.

Your essay will be evaluated based on the evidence it provides of your ability to:

- analyze and evaluate multiple perspectives on a complex issue
- state and develop your own perspective on the issue
- explain and support your ideas with logical reasoning and detailed examples
- clearly and logically organize your ideas in an essay
- effectively communicate your ideas in standard written English

Lay your pencil down immediately when time is called.

DO NOT OPEN THIS BOOKLET UNTIL TOLD TO DO SO.
Vocational Education

For many years, public high schools in the United States emphasized vocational skills—the skills students would need to learn a trade and get a job. Classes in auto repair, office skills, and woodworking, for example, were common. The last few decades have seen career and technical training fall out of favor in public education, replaced gradually by additional academic courses. While many schools maintain a vocational program, these programs are often threatened with elimination when school budgets are strained. Given its uncertain status in many schools, it is worth considering what value vocational training adds to education.

Read and carefully consider these perspectives. Each suggests a particular way of thinking about the value of vocational training in education.

**Perspective One**
Schools must seek to prepare all students for their futures. Career training provides focus for many students and helps schools reach those who don’t excel in academic subjects.

**Perspective Two**
In every field, the skills workers need today are based on knowledge and communication. As such, schools should focus on academic subjects only.

**Perspective Three**
No one knows what jobs will be available in the future, so it is not wise to train today’s students for any specific career.

**Essay Task**
Write a unified, coherent essay in which you evaluate multiple perspectives on the value of vocational training in education. In your essay, be sure to:

- analyze and evaluate the perspectives given
- state and develop your own perspective on the issue
- explain the relationship between your perspective and those given

Your perspective may be in full agreement with any of the others, in partial agreement, or wholly different. Whatever the case, support your ideas with logical reasoning and detailed, persuasive examples.
Planning Your Essay

Your work on these prewriting pages will not be scored.

Use the space below and on the back cover to generate ideas and plan your essay. You may wish to consider the following as you think critically about the task:

Strengths and weaknesses of the three given perspectives
- What insights do they offer, and what do they fail to consider?
- Why might they be persuasive to others, or why might they fail to persuade?

Your own knowledge, experience, and values
- What is your perspective on this issue, and what are its strengths and weaknesses?
- How will you support your perspective in your essay?

If you need more space to plan, please continue on the back of this page.
Planning Your Essay

Use this page to continue planning your essay. Your work on this page will not be scored.
Scoring Your Practice Tests

Scoring practice test 2 and practice test 3 is covered in chapter 11.

Explanatory Answers
Passage I

Question 1. The best answer is C because the comma after tribe sets off what follows as a nonrestrictive appositive that describes what “the Miami tribe” is: “a Native American people with strong ties to territory in present-day Ohio, Indiana, and Illinois.”

The best answer is NOT:

A because it is missing the comma needed after tribe to set off the following nonrestrictive appositive from the noun tribe and because it places an unnecessary and confusing comma between the noun people and the series of prepositional phrases starting with “with strong ties” that follows and describes people.

B because it pointlessly separates with a comma the adjective Native American from the noun people.

D because it misuses the semicolon. The semicolon inappropriately implies that what will follow is an independent clause, as in “My family is part of the Miami tribe; we are a Native American people. . .”

Question 2. The best answer is F because “making freezer jam or researching tribal history” gives the most specific and vivid glimpse of what the grandmother was interested in.

The best answer is NOT:

G because “being actively involved in her pursuits” is vague and gives no suggestion of what those pursuits are.

H because “things I really hope she’ll teach me one day” gives no suggestion of what those things are.

J because “historical research as well as domestic projects” offers only a general notion of the interests that are more pointedly described in F.

Question 3. The best answer is D because the word rushed by itself is sufficient to express the idea “urged to hasten.”

The best answer is not:

A because the word rushed and the phrase “in a hurry” are redundant.

B because the words hurried and rushed are redundant.

C because the phrase “made to go faster” and the word rushed are redundant.
Question 4. The best answer is J because a comma is appropriate between the long introductory adverbial clause “if we were running late for an appointment” and the sentence’s main clause, which begins with she.

The best answer is NOT:

F because placing a period after the word appointment makes the introductory adverbial clause (subordinated by the conjunction if) into a sentence fragment and because doing so obscures how the ideas are related.

G because placing a semicolon after the word appointment makes the introductory adverbial clause into a sentence fragment and obscures how the ideas are related.

H because the coordinating conjunction and should not be used to join two unequal sentence elements, such as a subordinate clause and a main clause, as would be the case here.

Question 5. The best answer is A because it opens this paragraph with a general statement about the concept of Miami time and serves as the most logical link between the preceding paragraph and the subject of this paragraph.

The best answer is NOT:

B because the reference to the doctor’s appointment is only loosely related to the end of the preceding paragraph and to the subject of this paragraph, which is defining and describing the concept of Miami time.

C because the general reference to the relationship between the narrator and the grandmother is only loosely related to the subject of this paragraph, which is defining and describing the concept of Miami time.

D because the general reference to the son being curious about and having never met the grandmother is only loosely related to the subject of this paragraph, which is defining and describing the concept of Miami time.
Question 6. The best answer is G because the dependent clause “when time seemed to slow down or stand still” is necessary information to explain which moments are being referred to and thus should not be set off from the rest of the sentence by a comma.

The best answer is NOT:

F because the comma between the words moments and when identifies the information in the dependent clause “when time seemed to slow down or stand still” as unnecessary information when, in fact, the clause is vital to defining the moments of Miami time.

H because the comma between the words moments and as if identifies the information in the dependent clause “as if time seemed to slow down or stand still” as unnecessary information and because the conjunction as if does not appropriately link the ideas in this sentence.

J because the comma between the words moments and because identifies the information in the dependent clause “because time seemed to slow down or stand still” as unnecessary information and because the conjunction because does not appropriately link the ideas in this sentence.

Question 7. The best answer is A because the word words by itself is a sufficient, clear, and appropriate way to refer to what the grandmother had said.

The best answer is NOT:

B because the phrase “spoken statements to my ears” is clumsy, wordy, and overly formal for the tone of the essay.

C because the phrase “expressed opinions on the matter” is wordy and overly formal for the tone of the essay.

D because the phrase “verbal remarks in conversation” is wordy, redundant, and overly formal for the tone of the essay.

Question 8. The best answer is J because the past tense verb slipped appropriately describes an event that occurred in the past and is consistent with the other past tense verbs used throughout the essay.

The best answer is NOT:

F because the verb will slip describes a past event in future tense.

G because the verb slip describes a past event in present tense.

H because the verb are slipping describes a past event in present progressive tense.
Question 9. The best answer is C because thinking is the second half of a compound verb (was pushing and . . . thinking). The words I was are implied in front of thinking.

The best answer is NOT:

A because the plural verb were thinking doesn’t agree with the singular subject I.

B because the plural verb were having doesn’t agree with the singular subject I.

D because deleting the underlined portion would leave the second part of the sentence without a verb (“I was pushing Jeremy in his stroller and of the day ahead . . .”).

Question 10. The best answer is F because no punctuation should interrupt the compound subject “two does and three fawns” or separate it from the rest of the sentence.

The best answer is not:

G because it places an unnecessary comma between parts of the compound subject.

H because it places an unnecessary comma between the compound subject and the verb stood.

J because it places an unnecessary comma between parts of the compound subject.

Question 11. The best answer is A because sentence 3, which introduces the deer, fits logically between sentence 2’s reference to Jeremy squealing and pointing at the clearing and sentence 4’s reference to the movement of the deer’s ears.

The best answer is not:

B because the word there in sentence 3 would have no logical antecedent, leaving unclear where the deer are. Also, the setting for the paragraph, revealed in Sentence 1 (“a familiar trail near our house”), would not yet have been established.

C because the narration in the first part of the paragraph involves a surprise: the pair are out for a walk (sentence 1), then Jeremy suddenly squeals and points (sentence 2), and then the surprise is explained (sentence 3). Placing the revelation in sentence 3 ahead of what happens “suddenly” in sentence 2 removes the surprise.

D because the word there in sentence 3 would have no logical antecedent in sentence 4, leaving unclear what there refers to. Also, the more general introduction to the deer in sentence 3 (“two does and three fawns”) should occur before the more specific reference to the deer in sentence 4 (“five pairs of ears”).
Question 12. The best answer is G because the word *rustling* is parallel in form to *lazing* earlier in the sentence. Together, these two words help form the compound subject of the verb *surprised* (“Lizards lazing... and quail rustling... surprised us”).

The best answer is NOT:

**F** because *rustled* isn’t parallel in form to *lazing* previously in the sentence, and this lack of parallelism creates an ungrammatical sentence (“Lizards lazing in the sun and quail rustled through grasses surprised us”).

**H** because *were rustling* isn’t parallel in form to *lazing* previously in the sentence, and this lack of parallelism creates an ungrammatical sentence (“Lizards lazing in the sun and quail were rustling through grasses surprised us”).

**J** because deleting the underlined portion creates an ungrammatical, nonsensical sentence (“Lizards lazing in the sun and quail through grasses surprised us”).

Question 13. The best answer is D because no transition word or phrase is necessary here to make the sentence part of a list of sensory experiences the narrator and son had: seeing lizards and quail, eating wild blackberries, and smelling crushed eucalyptus leaves.

The best answer is NOT:

**A** because the phrase “For example” illogically suggests that the aroma of crushed eucalyptus leaves is an example of the taste of wild blackberries rather than being the third item in a list of sensory experiences.

**B** because the phrase “On the other hand” illogically suggests that the aroma of crushed eucalyptus leaves is somehow in opposition to the taste of wild blackberries rather than being the third item in a list of sensory experiences.

**C** because the phrase “Just in case” makes no sense in this context; it is unclear what smelling the aroma of crushed eucalyptus leaves would be designed to prevent.

Question 14. The best answer is J because “shorter than” is the correct comparative form to use to contrast how long the 3-hour hike seemed to take with how long the normal-length hike usually seemed.

The best answer is NOT:

**F** because the adverb *then* is incorrectly used instead of the preposition *than* to introduce the second part of the comparison.

**G** because *more shorter* is an incorrectly formed comparative term and because the adverb *then* is incorrectly used instead of the preposition *than* to introduce the second part of the comparison.

**H** because *shortest* is a superlative term used here incorrectly to compare two things.
Question 15. The best answer is A because most of the essay narrates a hike that took a long time but seemed short, the rhetorical aim being to illustrate one of the narrator's personal experiences with Miami time because that concept is defined in the early part of the essay.

The best answer is not:

B because although the essay has met the goal specified in the question, which was to convey a personal experience with Miami time, the reason given here is inaccurate. The essay doesn't reveal whether the narrator decided to live in Miami time, nor is it clear that one can actually choose to live always in Miami time.

C because the essay has met the goal specified in the question, which was to convey a personal experience with Miami time. That the grandmother's view of Miami time is represented doesn't detract from the fact that the essay still relates the narrator's personal experience.

D because the essay has met the goal specified in the question, which was to convey a personal experience with Miami time. It is unclear what it would mean for the term Miami time to belong to the grandmother; in any case, the essay indicates that the narrator and the grandmother came to share a similar sense of Miami time.

Passage II

Question 16. The best answer is H because the meaning here is clearest when the ideas are divided into two sentences, with the first sentence giving a general description of the artwork and the second describing the eight women in the artwork more specifically.

The best answer is not:

F because the relative pronoun that should be used to connect an adjectival clause to a main clause, not two main clauses. That in this position would logically refer to the immediately preceding noun, flowers, which makes no sense here.

G because the coordinating conjunction and creates a rambling sentence in which it's difficult to tell where one thought ends and the next begins, especially without a comma before and.

J because using only the comma after the word flowers to join two independent clauses creates a comma splice.
**Question 17. The best answer is D** because no transition word is necessary here to link the two questions posed at the end of the essay’s first paragraph with the answers that unfold beginning in the second paragraph.

The best answer is NOT:

A because the word *thus* illogically suggests that the fact that the answers to the questions posed at the end of the essay’s first paragraph can be found in the artwork itself is a result of the questions being posed.

B because the word *instead* illogically sets up a contrast between the questions posed at the end of the essay’s first paragraph and the fact that the answers can be found in the artwork itself.

C because the word *furthermore* illogically suggests that something additional but similar to the questions posed at the end of the essay’s first paragraph is coming next (mostly likely, more questions), when, in fact, the essay switches to discussing the answers to the questions.

**Question 18. The best answer is F** because the word order creates a clear, understandable sentence.

The best answer is NOT:

G because the placement of the phrase “the story” creates a nonsensical statement.

H because the placement of the phrase “of text” creates a nonsensical expression (“this gathering of text”).

J because the placement of the phrase “on two horizontal panels of text” divides the phrase “the story” from the prepositional phrase that describes the story, “of this gathering.”

**Question 19. The best answer is C** because *its* is the correct form of the singular possessive pronoun and agrees with its singular antecedent, understood to be the noun *piece*.

The best answer is NOT:

A because *it’s* is a contraction meaning “it is” rather than the singular possessive pronoun *its*, which is needed here.

B because *its’* is an incorrect form of the singular possessive pronoun *its*, which is needed here.

D because *their* is the plural possessive pronoun, which doesn’t agree with its singular antecedent, understood to be the noun *piece*. 
Question 20. The best answer is J because the interposed explanatory phrase “the story explains” is properly set off from the rest of the sentence by two commas, indicating that the phrase could be omitted without changing the basic meaning of the sentence.

The best answer is NOT:

F because the interposed explanatory phrase “the story explains” is not preceded by a comma, which would be needed to set the phrase off properly from the rest of the sentence.

G because the interposed explanatory phrase “the story explains” is improperly set off from the rest of the sentence by a comma before the phrase and a dash after the phrase. Either two commas or two dashes would be appropriate, but not one of each.

H because the interposed explanatory phrase “the story explains” is not preceded by a dash, which would be needed to set the phrase off properly from the rest of the sentence.

Question 21. The best answer is C because placing the underlined portion after the word cause is the only one of the four choices that wouldn’t be acceptable. This placement of the phrase “in their various ways” divides the phrase “the cause” from the prepositional phrase that describes the cause, “of justice.” Therefore, all of the choices would be acceptable EXCEPT C.

The best answer is NOT:

A because keeping the underlined portion where it is now creates a clear and correct sentence in English.

B because placing the underlined portion after the word support creates a clear and correct sentence in English.

D because placing the underlined portion after the word world (and before the period) creates a clear and correct sentence in English.

Question 22. The best answer is F because the rest of the paragraph explains that the women depicted in the artwork lived at different times and so couldn’t have sat together and made a quilt.

The best answer is NOT:

G because the phrase “in summary” illogically suggests that the sentence summarizes the preceding text, which it does not do.

H because the phrase “in addition” illogically suggests that the sentence directly adds to the preceding text, which it does not do.

J because the phrase “in contrast” illogically suggests that the sentence provides a direct contrast to the preceding text, which it does not do.
Question 23. The best answer is B because Ringgold is the only artist being referred to at this point; the singular possessive form of the noun artist’s is therefore required.

The best answer is NOT:

A because artists is a plural noun, not the singular possessive form of the noun artist’s that is required.

C because artists’ is a plural possessive form of the noun, not the singular possessive form artist’s that is required.

D because the phrase “artists imagination” uses the plural form of the noun artists instead of the singular possessive, artist’s, that is required, and because D includes an unnecessary comma after the word imagination.

Question 24. The best answer is J because the plural verb were agrees with the plural compound subject, “Sojourner Truth and Harriet Tubman.”

The best answer is NOT:

F because the singular verb was doesn’t agree with the plural compound subject “Sojourner Truth and Harriet Tubman.”

G because the singular verb was doesn’t agree with the plural compound subject “Sojourner Truth and Harriet Tubman.”

H because the singular verb was doesn’t agree with the plural compound subject “Sojourner Truth and Harriet Tubman.”

Question 25. The best answer is A because information about Wells speaking out for social and racial justice is highly relevant, given that the paragraph focuses on the causes championed by the women, including Wells, depicted in Ringgold’s artwork.

The best answer is NOT:

B because information about the man Wells married is only marginally relevant to the topic of the paragraph: the historical reality behind Ringgold’s artwork.

C because information about which newspapers Wells wrote for isn’t as relevant to the topic of the paragraph as the information in A.

D because information about Well’s birthplace, birth year, and siblings is only marginally relevant to the topic of the paragraph.
Question 26. The best answer is J because the word business is sufficient, together with the words her own earlier in the sentence, to indicate that Madam C. J. Walker established her own business.

The best answer is NOT:

F because the intensive pronoun herself is awkward and redundant with her own and because the comma between the noun business and the intensive herself is unnecessary and confusing.

G because the phrase “belonging to her” is awkward and redundant with “her own.”

H because the intensive pronoun herself is awkward and redundant with “her own” and because an intensifier, even when appropriate in a sentence, doesn’t need to be set off by commas from the rest of the sentence.

Question 27. The best answer is B because this sentence structure makes “Madam C. J. Walker” the subject of the sentence, which is necessary in order to have the introductory participial phrase “establishing her own hair products business in the first decade of the twentieth century” refer clearly to Walker.

The best answer is NOT:

A because this sentence structure makes the introductory participial phrase a dangling modifier that refers to “millions of dollars,” which doesn’t make sense.

C because this sentence structure makes the introductory participial phrase a dangling modifier that refers to “charities and educational institutions,” which doesn’t make sense.

D because this sentence structure makes the introductory participial phrase a dangling modifier that refers to “millions of dollars,” which doesn’t make sense.
Question 28. The best answer is H because no punctuation is warranted in this underlined portion. “Among the schools that benefited from this generosity” is an introductory adverbal phrase that, because it immediately precedes the verb it modifies, should not be set off by a comma. Had the sentence elements been arranged in the more typical subject-verb-object order (“Those [schools] that Mary McLeod Bethune opened and ran in order to provide a better education for Black students were among the schools that benefited from this generosity”), it would’ve been more obvious that no internal punctuation is required.

The best answer is NOT:

F because the comma after the word *generosity* is an unwarranted break between the prepositional phrase and the verb it modifies.

G because the semicolon after the word *generosity* creates two inappropriate sentence fragments, as neither what precedes nor what follows the semicolon is an independent clause.

J because the colon after the word *were* is unwarranted; what follows the colon is not a series, a list, an explanation, or a clarification.

Question 29. The best answer is D because the phrase “movement of” creates a clear, complete sentence, with the preposition *of* heading the phrase *of the 1950s and 1960s*.

The best answer is NOT:

A because “movement, it happened in” forms a second independent clause in the sentence joined to the original independent clause by only a comma, creating a comma splice.

B because “movement, it took place in” forms a second independent clause in the sentence joined to the original independent clause by only a comma, creating a comma splice.

C because “movement, that happened in” forms a second independent clause in the sentence joined to the original independent clause by only a comma, creating a comma splice.

Question 30. The best answer is F because the sentence under consideration interprets what the flowers represent (“seem to celebrate”) and makes a concluding reference to the main focus of the essay (“the women’s accomplishments and the beauty of their shared vision”).

The best answer is NOT:

G because the sentence under consideration makes no comparison of Ringgold to the women depicted in the artwork.

H because the sentence under consideration says nothing about a brushwork technique.

J because the sentence under consideration offers no evaluation of Ringgold’s artistic talent, only an interpretation of what the flowers represent (“seem to celebrate”).
The best answer is B because the plural present perfect verb *have allowed* agrees with the plural subject *times* and indicates appropriately that the creation of spectacular science fiction films continues.

The best answer is not:

A because the singular present perfect verb *has allowed* doesn’t agree with the plural subject *times*.

C because the singular verb *allows* doesn’t agree with the plural subject *times*.

D because the singular past progressive verb *was allowing* doesn’t agree with the plural subject *times* and incorrectly indicates that the creation of spectacular science fiction films ended in the past.

The best answer is F because the relative adverb *when* is appropriately used to follow a time expression (“in 1902”); no punctuation is needed.

The best answer is not:

G because the coordinating conjunction *and* treats a dependent clause (“when audiences first saw . . .”) as a second independent clause, creating a nonsensical sentence.

H because the relative pronoun *which* logically refers to 1902, both implying that audiences first saw the year 1902 (rather than first seeing a groundbreaking movie) and creating a garbled sentence.

J because the relative adverb *where* doesn’t fit logically into this context, since 1902 refers to time rather than place.

The best answer is C because *his* is the appropriate masculine singular pronoun to refer to the male magician Méliès.

The best answer is not:

A because the singular pronoun *its* refers to things, not people, and in the sentence would illogically refer to the camera rather than Méliès.

B because the plural pronoun *their* has no logical antecedent in the sentence.

D because *it’s* is a contraction meaning “it is,” which makes no sense in the sentence.
Question 34. The best answer is F because when a conjunctive adverb such as however is used in the middle of a sentence, it needs to be set off by commas.

   The best answer is NOT:

   G because the semicolon after the word however creates an abbreviated main clause (“he found out, however;”) followed by an inappropriate sentence fragment (“that the public preferred live magic acts to filmed versions”).

   H because the phrase “out, however” lacks the comma after the word however needed to set off the conjunctive adverb from the rest of the sentence.

   J because the phrase “out however,” lacks the comma after the word out needed to set off the conjunctive adverb from the rest of the sentence.

Question 35. The best answer is D because sentence 1 explains what Méliès did after he was undaunted by the discovery that people didn’t like filmed magic acts (sentence 5). He began instead to tell fantasy stories.

   The best answer is NOT:

   A because keeping sentence 1 where it is now would weaken the logic and coherence of the paragraph. The paragraph would begin with a reference to Méliès being undaunted and turning to fantasy stories instead before Méliès had been formally described in sentence 2 and before the incident that caused him to turn away from filmed magic acts had been related (sentences 3 to 5).

   B because placing sentence 1 after sentence 2 would weaken the logic and coherence of the paragraph. The words undaunted and instead in sentence 1 would make no sense, because there’s nothing in sentence 2 to suggest that Méliès had met with any problems.

   C because placing sentence 1 after sentence 3 would weaken the logic and coherence of the paragraph. The words undaunted and instead in sentence 1 would make no sense, because there’s nothing in sentences 2 or 3 to suggest that Méliès had met with any problems.
Question 36. The best answer is H because the sentence under consideration should NOT be deleted; it creates a transition between the preceding paragraph, about Méliès the magician, and this paragraph, which focuses on Méliès's exploration of special film effects.

The best answer is NOT:

F because the sentence under consideration mentions Méliès's “magician's eye” but doesn't otherwise describe his ability as a magician.

G because the sentence under consideration mentions “the basics of special effects” but doesn't begin to explain any of the techniques of trick photography.

J because the sentence under consideration doesn't indicate “that Méliès's interest in learning about trick photography existed before his interest in magic.” The preceding paragraph, in fact, describes Méliès's interests as beginning with magic, then moving into filmmaking.

Question 37. The best answer is D because perfecting “eerie film entrances and exits” is a specific example of Méliès's skill and inventiveness.

The best answer is NOT:

A because the clause “he was able to do interesting things” is vague and doesn't give any specific illustration of Méliès's skill and inventiveness.

B because the clause “he used effects commonly seen in his stage productions” doesn't suggest that Méliès was particularly skillful or inventive; on the contrary, it suggests that the best Méliès could do as a filmmaker was to copy himself.

C because “his actors could enter and leave the scene” shifts the focus away from Méliès to his actors, which doesn't effectively highlight Méliès's skill and inventiveness and because relative to D, C is imprecise.

Question 38. The best answer is J because the phrase “exceedingly high” appropriately uses the adverb exceedingly in front of the adjective it modifies, high, which in turn modifies the noun costs.

The best answer is NOT:

F because an adjective is needed to modify the noun costs, whereas the phrase “highly excessively” consists of two adverbs.

G because an adjective is needed to modify the noun costs, whereas the phrase “exceeding highly” consists of a participle and an adverb.

H because the phrase “high excessively” reverses conventional word order.
Question 39. The best answer is B because the verb fired is sufficient to indicate the action clearly.

The best answer is NOT:

A because the words fired, launched, and projected mean essentially the same thing in this context, making the phrasing redundant.

C because the words fired and projected mean essentially the same thing in this context, making the phrasing redundant.

D because the words fired and propelled mean essentially the same thing in this context, making the phrasing redundant.

Question 40. The best answer is F because the noun creatures is sufficient to indicate clearly what the terrain was filled with.

The best answer is NOT:

G because the clause “who they now realize live there” adds only wordiness to the sentence, which already strongly implies that the space travelers realize that the hostile creatures they encounter live in the strange terrain.

H because the clause “whom they are encountering” adds only wordiness to the sentence, which already clearly indicates that the space travelers encounter hostile creatures in the strange terrain.

J because the clause “who are found there” adds only wordiness to the sentence, which already clearly indicates that hostile creatures are found in the strange terrain.

Question 41. The best answer is C because for clarity this sequence of events should be divided into two sentences, the first indicating that the travelers fall off the edge of the moon to escape and the second establishing that the travelers land in the ocean and are eventually rescued.

The best answer is NOT:

A because using only a comma after the word moon to join two independent clauses creates a comma splice. (Alternatively, it’s possible to see the error here as a comma splice created by the comma after the word ocean.)

B because the phrase “moon after landing” creates a fused sentence. (Alternatively, it’s possible to see the error here as a comma splice created by the comma after the word ocean, with the sentence then suggesting illogically that the space travelers fell off the edge of the moon after landing in the ocean.)

D because using only a comma after the word moon to join two independent clauses creates a comma splice. (Alternatively, it’s possible to see the error here as a comma splice created by the comma after the word ocean.)
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Question 42. The best answer is J because the past perfect verb had begun is made up of the past tense form had and the past participle begun. Past perfect is called for here because Méliès produced A Trip to the Moon long before interplanetary explorations had taken place.

The best answer is NOT:

F because had began is an improperly formed past perfect verb that uses the past tense form began instead of the past participle begun.

G because would of begun is an improperly formed verb that uses the word of instead of have.

H because have began is an improperly formed present perfect verb that uses the past tense form began instead of the past participle begun. (Even if the present perfect verb had been formed properly, it still wouldn’t work in this context because the past perfect is needed to indicate that producing A Trip to the Moon occurred before interplanetary explorations had taken place.)

Question 43. The best answer is D because disturb is the only one of the four alternatives that, in the context of the sentence, can’t reasonably be used as a substitute for the underlined word (arouse). “Disturb his audience’s curiosity” is neither a conventional expression in standard English nor an appropriate innovation here. Therefore, disturb is the LEAST acceptable alternative to arouse.

The best answer is NOT:

A because the word whet, meaning here to stimulate or excite curiosity, is an acceptable, idiomatically appropriate alternative to the word arouse.

B because the word stimulate, meaning here to encourage or increase curiosity, is an acceptable, idiomatically appropriate alternative to the word arouse.

C because the word awaken, meaning here to stir up or stimulate curiosity, is an acceptable, idiomatically appropriate alternative to the word arouse.
Question 44. The best answer is G because the writer’s assertion that *A Trip to the Moon* “provided the genesis for a film genre”—science fiction—“that still packs theaters” is both specific and consistent with the writer’s point, made throughout the essay, that Méliès produced a landmark movie.

The best answer is NOT:

F because the assertion that “People are still going to theaters to see science fiction films” has no clear tie to Méliès’s role in science fiction filmmaking.

H because the assertion that “Méliès made an important contribution to filmmaking many years ago” is vague and doesn’t clearly express the writer’s viewpoint about Méliès’s role in science fiction filmmaking.

J because the assertion that “In Méliès’s production even the film crew knew a lot about space” shifts the focus away from Méliès’s own role in science fiction filmmaking.

Question 45. The best answer is B because the essay fulfills the specified goal by focusing on a single artist, Méliès, and explaining how he used his talents as a magician and filmmaker to produce the landmark film *A Trip to the Moon* and thereby inaugurated the genre of science fiction films.

The best answer is NOT:

A because although the essay fulfills the goal specified in the question, which was to highlight the contributions a single artist can make to a particular art form, the essay doesn’t assert that Méliès’s work as a magician never would have succeeded without the contributions of the artists in the film industry. Instead, the essay indicates that Méliès was a successful magician prior to having any association with film and filmmaking.

C because the essay fulfills the goal specified in the question and because the main focus of the essay is on a single artist, Méliès, and a specific film, *A Trip to the Moon*, not on the general process of making science fiction films.

D because the essay fulfills the goal specified in the question and because the essay doesn’t suggest that it took many artists working together to create Méliès’s success. Rather, the essay stresses Méliès’s accomplishments as a magician and his central role in creating the film *A Trip to the Moon*. 
Passage IV

**Question 46. The best answer is G** because the past perfect verb *had gone* is made up of the past tense form *had* and the past participle *gone*. Past perfect is called for here because if the Nancy Drew mystery series had gone out of style, it would have occurred prior to the events narrated here in past tense (“I thought . . .”). Furthermore, “gone out of style” is a conventional, idiomatic expression indicating that something has become unfashionable.

**The best answer is NOT:**

- **F** because *had went* is an improperly formed past perfect verb that uses the past tense form *went* instead of the past participle *gone*.
- **H** because *had went* is an improperly formed past perfect verb that uses the past tense form *went* instead of the past participle *gone* and because “went from style” isn’t a conventional, idiomatic expression in standard English.
- **J** because “gone from style” isn’t a conventional, idiomatic expression in standard English.

**Question 47. The best answer is B** because the context calls for the auxiliary verb *would* to express the presumption expressed by “I was sure” (and to parallel *would have* earlier in the sentence) and calls for the present perfect verb *have been retired* in the passive voice to indicate the idea that the “sleuth” received the action of being “retired” to the library’s back rooms.

**The best answer is NOT:**

- **A** because *would of been* is an improperly formed verb that uses the word *of* instead of *have*.
- **C** because *would of* is an improperly formed verb that uses the word *of* instead of *have*.
- **D** because deleting the underlined portion leaves just the simple past tense verb *retired*, which isn’t parallel to the other verb in the sentence, *would have*. 
Question 48. The best answer is J because the possessive form of the word library (library’s) is needed to indicate “the dusty back rooms of the library” and because no comma is needed between the words dusty and back since back rooms functions as a single unit (a compound noun) and dusty and back aren’t coordinate adjectives.

The best answer is NOT:

F because the comma between dusty and back is unnecessary since back rooms functions as a single unit (a compound noun) and dusty and back aren’t coordinate adjectives. (You couldn’t say “the library’s dusty and back rooms,” for example.)

G because the plural form libraries is incorrectly used in place of the possessive form library’s and because the comma between dusty and back is unnecessary since back rooms functions as a single unit (a compound noun) and dusty and back aren’t coordinate adjectives.

H because the plural form libraries is incorrectly used in place of the possessive form library’s.

Question 49. The best answer is C because of the four choices, the word hundreds provides the most specific information about the number of Nancy Drew novels in existence.

The best answer is NOT:

A because the word heaps is vague and too informal for the style and tone of the essay.

B because the phrase “a high number” is vague.

D because the word plenty is vague.

Question 50. The best answer is F because the comma after the word novels is needed to finish setting off the nonrestrictive appositive “the teenaged heroine of hundreds of young adult mystery novels” from Nancy Drew, the noun the appositive describes.

The best answer is NOT:

G because the comma after the word alive is unnecessary since the list of adjectives “alive and well and still on the job” is already linked by the coordinating conjunction and.

H because a comma is needed after the word novels to finish setting off the nonrestrictive appositive “the teenaged heroine of hundreds of young adult mystery novels” from Nancy Drew, the noun the appositive describes, and because the comma after the word alive is unnecessary since the list of adjectives “alive and well and still on the job” is already linked by the coordinating conjunction and.

J because a comma is needed after the word novels to finish setting off the nonrestrictive appositive “the teenaged heroine of hundreds of young adult mystery novels” from Nancy Drew, the noun the appositive describes.
Question 51. The best answer is B because the phrase “the mysteries” makes clear that the girls were reading Nancy Drew novels all summer long.

The best answer is NOT:

A because the pronoun that has no clear, logical antecedent. Though that is obviously intended to refer to the Nancy Drew novels the girls were reading all summer long, that is singular and novels is plural.

C because the pronoun that has no clear, logical antecedent. Though that is obviously intended to refer to the Nancy Drew novels the girls were reading all summer long, that is singular whereas novels is plural. Furthermore, “reading up on that” is an idiomatic phrase but one that doesn’t work in this context. To “read up on” something means to learn about a topic, not to read a number of novels for pleasure.

D because “Liana and her friends were reading it over all summer long” is confusing in more than one way. First, we again have to ask what they were reading, because it doesn’t logically refer to anything in the preceding sentence. Then “over all summer long” is a redundant phrase, with over being an extra, or superfluous, word.

Question 52. The best answer is G because the main clause of the sentence must have a subject (she) and a verb (had followed), and the verb must be in past perfect tense to indicate that Liana had already read the Nancy Drew novels The Spider Sapphire Mystery and The Secret of the Crossword Cipher before she went back to school.

The best answer is NOT:

F because “school and had” leaves the sentence without a main clause, creating an inappropriate sentence fragment.

H because “school, having” leaves the sentence without a main clause, creating an inappropriate sentence fragment.

J because “school, she” creates an inappropriate verb tense shift. The words “By the time” and “went back” signal that the past perfect verb had followed, rather than the simple past form followed, is needed to indicate that Liana had already read the Nancy Drew novels The Spider Sapphire Mystery and The Secret of the Crossword Cipher before she went back to school.
**Question 53. The best answer is A** because no punctuation is warranted between the verb solve and its direct object, “The Spider Sapphire Mystery.”

**The best answer is NOT:**

B because the colon between the verb solve and its direct object, “The Spider Sapphire Mystery,” is unnecessary and confusing.

C because the semicolon between the verb solve and its direct object, “The Spider Sapphire Mystery,” is unnecessary and confusing.

D because the comma between the verb solve and its direct object, “The Spider Sapphire Mystery,” is unnecessary and confusing.

**Question 54. The best answer is H** because this sentence names some specific settings for the Nancy Drew novels (Arizona, Argentina, Nairobi, New York) and uses the verb had chased, which suggests that Liana was so caught up in what she was reading that she felt like she was solving the mysteries along with Nancy Drew.

**The best answer is NOT:**

F because this sentence refers generally to “different places and various cultures all over the world” but doesn't specify any settings for the Nancy Drew novels and because the verb had read doesn't make clear that Liana was particularly interested in the novels.

G because this sentence refers generally to “many breathtaking adventures involving all sorts of colorful characters” but doesn't specify any settings for the Nancy Drew novels.

J because this sentence refers generally to “many new places around the world” but doesn't specify any settings for the Nancy Drew novels and because the phrases through her exposure to and learned about don't make clear that Liana was particularly interested in the novels.
Question 55. The best answer is C because the proposed sentence, concerning how many books are in one of the series featuring Nancy Drew, shouldn't be added at this point in the essay because it distracts the reader from the main point of the paragraph, which is about why the narrator and her childhood friends loved Nancy Drew so much.

The best answer is NOT:

A because while the proposed sentence does attest to the longevity and popularity of the Nancy Drew Mystery Story series, the sentence is out of place and largely irrelevant at this point in a paragraph mainly about the place Nancy Drew held in the narrator's childhood and that of her friends.

B because the proposed sentence, with its facts and figures, addresses the history of the Nancy Drew Mystery Story series, not why the narrator loved Nancy Drew, which is why the sentence is out of place and largely irrelevant at this point in a paragraph mainly about the place Nancy Drew held in the narrator's childhood and that of her friends.

D because while the proposed sentence shouldn't be added at this point, adding in information about the author of the Nancy Drew Mystery Story series would only make the sentence more out of place and irrelevant, given that the paragraph is mainly about the place Nancy Drew held in the narrator's childhood and that of her friends.

Question 56. The best answer is H because “her freedom to do what she wanted” is clear and is parallel with “her loyal companions” and “her bravado,” used previously in the sentence to identify two other things the narrator and her friends loved about Nancy Drew.

The best answer is NOT:

F because “there was a love for her freedom to do what she wanted” is not parallel with the two similar structures in the sentence (“her loyal companions,” “her bravado”) and is awkward, wordy, and redundant with “we loved.”

G because “a love for her freedom to do what she wanted” is not parallel with the two similar structures in the sentence (“her loyal companions,” “her bravado”) and is awkward and redundant with “we loved.”

J because “the freedom to do as one wants” is not parallel with the two similar structures in the sentence (“her loyal companions,” “her bravado”) and because the impersonal and rather formal pronoun one is stilted and out of place in a sentence focused on Nancy Drew’s qualities.
**Question 57. The best answer is B** because the word *therefore* is the only one of the four alternatives that, in the context of the sentence, can’t reasonably be used as a substitute for the underlined portion (*also*). *Therefore* introduces something that is a result of something else, but *also* only signals the addition of one or more things. Thus, *therefore* is the LEAST acceptable alternative to *also*.

The best answer is NOT:

A because the word *furthermore*, meaning “in addition,” is an acceptable alternative to the word *also*, as the two mean essentially the same thing in this context.

C because the word *likewise*, meaning “in a similar manner,” is an acceptable alternative to the word *also*, as the two mean essentially the same thing in this context.

D because deleting the underlined portion doesn’t change the meaning of the sentence much if at all. Even without the word *also*, the sentence is clearly adding to the list of qualities that the narrator and her friends loved about Nancy Drew.

**Question 58. The best answer is F** because the phrase “was able to solve crimes” effectively sets up a grammatically parallel list of notable things Nancy Drew was able to do: “solve crimes,” “win golf tournaments,” “kick bad guys in the shins,” and “impress her father’s distinguished clients.”

The best answer is NOT:

G because the phrase “was capable of solving crimes” doesn’t set up a parallel list of notable things Nancy Drew was able to do, as *solving* isn’t parallel with *win, kick, and impress*, nor is it standard to say that Drew “was capable of . . . win golf tournaments,” and so on.

H because the phrase “was good at crime solving” doesn’t set up a parallel list of notable things Nancy Drew was able to do, as *solving* isn’t parallel with *win, kick, and impress*, nor is it standard to say that Drew “was good at . . . win golf tournaments,” and so on.

J because the phrase “solved crimes” doesn’t set up a parallel list of notable things Nancy Drew was able to do, as *solved* isn’t parallel with *win, kick, and impress.*
Question 59. The best answer is C because the semicolon after the word *successful* is appropriately used to divide this sentence into two closely related independent clauses.

The best answer is NOT:

A because the lack of appropriate punctuation and/or a conjunction between the words *successful* and *they* creates a fused sentence.

B because the lack of appropriate punctuation and/or a conjunction between the words *successful* and *they* creates a fused sentence.

D because “successful, knowing” creates a confusing, possibly redundant sentence, as it’s not clear who knows what.

Question 60. The best answer is F because the phrase “those exciting adventure tales spiced with mystery” effectively supports the point in the first part of the sentence that what the girls in Liana’s generation “need and love” is entertaining fiction (“the stories themselves”).

The best answer is NOT:

G because the phrase “the answers to the mysteries of their lives” suggests that what the girls in Liana’s generation “need and love” are stories that teach the girls about themselves, whereas “the stories themselves,” used in the first part of the sentence, suggests that what the girls really want is entertaining fiction.

H because the phrase “a strong role model for their generation” suggests that what the girls in Liana’s generation “need and love” are stories that inspire them, whereas “the stories themselves,” used in the first part of the sentence, suggests that what the girls really want is entertaining fiction. The preceding two sentences in the paragraph also make the point that girls today don’t need a “successful girl detective” as a role model.

J because the phrase “the ability to overcome obstacles” clumsily suggests that what the girls in Liana’s generation “need and love” are stories that show a “successful girl detective” rising above adversity, whereas “the stories themselves,” used in the first part of the sentence, suggests that what the girls really want is entertaining fiction. The preceding two sentences in the paragraph also make the point that girls today don’t need a “successful girl detective” as a role model.
Passage V

**Question 61. The best answer is C** because the preposition *from* effectively sets up the long introductory phrase “From ancient Babylonian astronomers . . . to twentieth-century science fiction writers” that begins the sentence.

**The best answer is NOT:**

- **A** because the words “there were” introduce another independent clause into the sentence, resulting in ungrammatical and confusing sentence structure.

- **B** because the subordinating conjunction *when* creates a nonsensical introductory phrase and an ungrammatical sentence.

- **D** because the adjective *those* creates a nonsensical introductory phrase and an ungrammatical sentence.

**Question 62. The best answer is H** because the clause “who penned spine-tingling stories of ‘little green men from Mars’” is the most relevant to helping make the point that Mars “has often been a symbol of ill will and danger.”

**The best answer is NOT:**

- **F** because the fact that there are twentieth-century science fiction writers “whose works become best-sellers” isn’t relevant to making the point that Mars “has often been a symbol of ill will and danger.”

- **G** because the comment that there are twentieth-century science fiction writers who have “wild imaginations about outer space” is too vague to help explain why Mars “has often been a symbol of ill will and danger.”

- **J** because the fact that there are twentieth-century science fiction writers “who created images of Mars in literature” doesn’t say anything specific about the nature of those images or help explain why Mars “has often been a symbol of ill will and danger.”
Question 63. The best answer is B because this sentence effectively ties together the bad reputation Mars has often had (“such negative associations”), described in the preceding paragraph, and the more recent interest in robotic and human missions to Mars, discussed in this paragraph.

The best answer is not:

A because this sentence about the United States competing with other countries to explore space is at best only loosely relevant to the topic of this paragraph, which is recent interest in robotic and human missions to Mars, and is unconnected to the topic of the preceding paragraph, which is Mars’s impact on thought and culture.

C because this sentence about which year the United States founded its space agency is loosely relevant to the topic of this paragraph, which is recent interest in robotic and human missions to Mars, but is unconnected to the topic of the preceding paragraph, which is Mars’s impact on thought and culture.

D because this sentence about Earth and Mars being planets in the inner solar system offers encyclopedia- or textbook-style information that is only loosely related to the topic of this paragraph, which is recent interest in robotic and human missions to Mars, and the topic of the preceding paragraph, which is Mars’s impact on thought and culture.

Question 64. The best answer is G because the past perfect tense verb had sent is made up of the past tense form had and the past participle sent. Past perfect is called for here to indicate that one event in the past (NASA sending its thirtieth spacecraft to Mars) took place before another past event (“By 2003”).

The best answer is not:

F because would of sent is an improperly formed verb that uses the word of instead of have.

H because the simple past tense verb send is inappropriate given that a past perfect verb is needed to make clear that NASA had already sent its thirtieth spacecraft to Mars “by 2003.”

J because the present perfect tense verb have sent is inappropriate given that a past perfect verb is needed to make clear that NASA had already sent its thirtieth spacecraft to Mars “by 2003.”
Question 65. The best answer is C because the participial phrase “prompting speculation” modifies in a clear way the preceding clause: by sending thirty spacecraft to Mars by 2003, NASA had led people to think seriously about the possibility of a human mission to Mars.

The best answer is NOT:

A because the subject speculation and the verb has been prompted begin a second independent clause joined to the first by only the comma after the word planet, creating a comma splice.

B because the words “to which speculation has prompted” create a confusing and ungrammatical construction, partly because “speculation has prompted” isn’t a conventional, idiomatic expression and partly because the pronoun which has no logical antecedent.

D because the words “which is speculation” create a confusing construction because the pronoun which has no logical antecedent.

Question 66. The best answer is H because the phrase “Although few” begins a subordinate introductory clause that is set off from the sentence’s main clause with a comma, resulting in a complete and logical sentence.

The best answer is NOT:

F because the lack of a subordinating conjunction in front of the word Few turns the introductory clause into an independent clause joined to the sentence’s main clause by only the comma after the word exciting. The result is a comma splice.

G because the lack of a subordinating conjunction in front of the words “Maybe a few” turns the introductory clause into an independent clause joined to the sentence’s main clause by only the comma after the word exciting. The result is a comma splice.

J because the lack of a subordinating conjunction in front of the words “Few, if any,” turns the introductory clause into an independent clause joined to the sentence’s main clause by only the comma after the word exciting. The result is a comma splice.
Question 67. The best answer is A because the nonrestrictive appositive “the most ambitious NASA project yet” is nonessential explanatory information that needs to be set off by commas from the rest of the sentence.

The best answer is NOT:

B because a comma is needed after the word yet to finish setting off the nonrestrictive appositive “the most ambitious NASA project yet” from the rest of the sentence.

C because a comma, not a colon, is needed after the word yet to finish setting off the nonrestrictive appositive “the most ambitious NASA project yet” from the rest of the sentence.

D because a comma, not a dash, is needed after the word yet to finish setting off the nonrestrictive appositive “the most ambitious NASA project yet” from the rest of the sentence. Although a pair of dashes could have been used to set off the nonrestrictive appositive, the writer uses a comma after the word Station, so parallelism requires that a second comma follow the word yet.

Question 68. The best answer is F because the information should be added to the sentence; the explicit detail about the amount of money actually spent on constructing the space station—nearly double the already high projected cost of $17 billion—strengthens the sentence’s assertion that “NASA overspent on the International Space Station.”

The best answer is NOT:

G because although the information should be added to the sentence, nothing in the information suggests, let alone proves, that space flight will be more affordable in the future.

H because the information would strengthen, rather than weaken, the point made in the paragraph about the high cost of human flight to Mars. If the actual cost of constructing the International Space Station was almost double the projected cost, it’s reasonable to worry about the accuracy of the already high projections of the cost of sending humans to Mars. Thus, the information should be added to the sentence.

J because the essay’s focus isn’t on the human experience in travel to Mars but rather on the costs of manned and unmanned missions to the planet. The information isn’t a digression but instead strengthens the point made in the paragraph about the high cost of human flight to Mars. Thus, the information should be added to the sentence.
**Question 69.** The best answer is B because *what* is the logical introductory word in the noun clause functioning as the direct object of the verb *imagine*, resulting in “what the final price of a human voyage to Mars would be.” Turning this clause around reinforces the idea that *what* is the best answer: “The final price of a human voyage to Mars would be *what*?”

The best answer is NOT:

A because *if* is an illogical introductory word in the noun clause functioning as the direct object of the verb *imagine*. Turning the clause around makes this clear: “The final price of a human voyage to Mars would be *if*?”

C because *how* is an illogical introductory word in the noun clause functioning as the direct object of the verb *imagine*. Turning the clause around makes this clear: “The final price of a human voyage to Mars would be *how*?”

D because deleting the underlined portion results in an illogical, incomplete-sounding sentence: “One can only imagine the final price of a human voyage to Mars would be.”

**Question 70.** The best answer is F because “robotic spacecraft launched in 2003” offers an effective description of the Mars Rovers.

The best answer is NOT:

G because “which captured the imagination of the general public” doesn't offer any specific description of the Mars Rovers.

H because “the products described at length in the media” doesn't offer any specific description of the Mars Rovers.

J because “familiar to many who watched the news coverage at the time” doesn't offer any specific description of the Mars Rovers.

**Question 71.** The best answer is D because the word *capacity* is sufficient to refer to the capability of the Mars Rovers to examine soil and rocks.

The best answer is NOT:

A because the words *capacity* and *ability* are redundant; they mean basically the same thing in this context.

B because the adjective *genuine* in the phrase “genuine capacity” creates a confusing expression; *genuine* suggests there might be some doubt about the Rovers’ capability, but no doubts have been raised.

C because the phrase “potential capacity” is a confusing expression; *potential* suggests there might be some conditions or limits on the Rovers’ capability, but no conditions or limits have been mentioned.
Question 72. The best answer is J because age-old, which means having been around for a long time, is a conventional, idiomatic expression that makes sense in this context.

The best answer is NOT:

F because the words aging and older are redundant; they mean basically the same thing in this context. “Aging or older visions” is also not likely what the writer intends to say here, because the writer suggests in the essay that there’s a timeless appeal to the notion of human spaceflight.

G because “old age” creates a silly expression (“old age visions”) that implies that visions of human space travel are held only by old people.

H because “aging old” creates a nonsensical expression (“aging old visions”).

Question 73. The best answer is D because the phrase “Even so,” meaning “despite that,” effectively signals the contrast between the preceding sentence, which says that using only machines to explore Mars may take some of the romance out of space travel, and this sentence, which says that we nevertheless need to remember that the right machines can do as much as if not more than humans can and at a fraction of the cost.

The best answer is NOT:

A because the phrase “In other words” incorrectly indicates that this sentence restates or summarizes the preceding sentence. Instead, this sentence offers a contrast to the preceding one.

B because the phrase “For that reason alone” incorrectly indicates that this sentence offers a consequence following from a circumstance identified in the preceding sentence. Instead, this sentence offers a contrast to the preceding one.

C because the phrase “In that time frame” makes no sense in context, as no time frame is indicated in the preceding sentence. Instead, this sentence offers a contrast to the preceding one.
Question 74. The best answer is **G** because the word *at* creates a conventional, idiomatic expression (“at a fraction of the cost”) that makes sense in the context of the writer identifying an additional consideration (machines doing as much as if not more than humans *and* at a much lower cost).

The best answer is **not**:

**F** because the phrase *such as* creates a nonsensical expression (“such as a fraction of the cost”).

**H** because the phrase “but only” is missing the word *at* that would make it a conventional, idiomatic expression (“but only at a fraction of the cost”) and because *but* suggests a contrast with what precedes it in the sentence when what follows is an additional consideration (machines doing as much as if not more than humans and at a much lower cost). (The writer here might have used “at only,” for example, but not “but only.”)

**J** because deleting the underlined portion creates a nonsensical expression. “A fraction of the cost” suggests that what precedes it in the sentence identifies a cost (e.g., “… less than one billion dollars—a fraction of the cost [of a human mission]”), but this isn’t the case.

Question 75. The best answer is **D** because concluding the essay with the proposed sentence would blur the essay’s focus on Mars and the cost of sending humans there.

The best answer is **not**:

**A** because although the proposed sentence may capture the emotion that is the basis for the space exploration described in the essay, the sentence is out of place as a conclusion to an essay focused mainly on the expense of a human mission to Mars.

**B** because although the proposed sentence may invite the reader to reflect on the insignificance of money in relation to the mystery of space, the sentence is out of place as a conclusion to a paragraph and essay on the expense of a human mission to Mars.

**C** because although the proposed sentence shouldn’t be added at this point, the essay doesn’t contain a chronological history of people who traveled in space.
Question 1. The correct answer is E. You may want to make a sketch of this situation in your mind or, better yet, in the space in your test booklet. A sample sketch is shown in the following:

The vertical rod and the vertical flagpole each form a right angle with the level ground, resulting in two right triangles. The smaller right triangle (at left) is composed of the rod, the rod’s shadow, and the line of sight of the sun through the top of the rod. The larger right triangle (at right) is composed of the flagpole, the flagpole’s shadow, and the line of sight of the sun through the top of the flagpole. Because the angle of elevation of the sun is the same for each triangle, the two triangles are similar by the Angle-Angle Similarity property. Using the ratios of corresponding sides of the similar triangles, the proportion $\frac{h}{12} = \frac{4}{12}$ is solved to find the height of the flagpole, $h = 36$ feet.

Common errors in this problem result from relying on an incorrect mental image or labeling the dimensions on the sketch incorrectly. If you chose A, you might have set up and solved the proportion $\frac{h}{12} = \frac{4}{12}$. 

Question 2. The correct answer is K. If you knew the unknown score, you could check to see that it was correct by adding up all five scores, dividing by 5 to get the average, and checking to see that the result was 90. Let $x$ be the unknown score. Then the sum of all the scores is $85 + 95 + 93 + 80 + x$, and the average is $\frac{85 + 95 + 93 + 80 + x}{5}$. For the average to be 90, that means $\frac{85 + 95 + 93 + 80 + x}{5} = 90$. To solve that equation, you can multiply both sides by 5 to get $85 + 95 + 93 + 80 + x = 450$ and then subtract 353 from both sides to get $x = 97$.

$G$ is closest to the average of the four given scores, $\frac{85 + 95 + 93 + 80}{4} = 88.25$. To raise an average of 88.25 up to 90 would take an increase of about 2 points, but a single new score of 92 (answer choice J) would not raise the average much. You can check your answer to see that it is too low: $\frac{85 + 95 + 93 + 80 + 92}{5} = 445 = 89$. You can check any answer choice to see whether it is correct.
**Question 3. The correct answer is A.** Substituting –5 for \(x\) produces a numerator equal to \((-5)^2 - 1 = 25 - 1 = 24\) and a denominator equal to \(-5 + 1 = -4\). Therefore, \(\frac{x^2 - 1}{x + 1} = \frac{24}{-4} = -6\).

The most common wrong answer is C, which comes from forgetting the negative sign in the given \(x\)-value: \(\frac{5^2 - 1}{5 + 1} = \frac{24}{6} = 4\).

**Question 4. The correct answer is K.** To find the total distance, in miles, Kaya ran, you need the sum of 1 \(\frac{2}{5}\) and 2 \(\frac{1}{3}\). To add mixed numbers together, each fraction must have a common denominator. Because 3 and 5 do not have any common factors besides 1, the least common denominator is 3(5), or 15. To convert \(\frac{2}{5}\), you multiply by \(\frac{3}{3}\). The result is \(\frac{6}{15}\). To convert \(\frac{1}{3}\), you multiply by \(\frac{5}{5}\). The result is \(\frac{5}{15}\). To add \(1 \frac{6}{15}\) and \(2 \frac{5}{15}\), you first add 1 and 2 and then \(\frac{6}{15} + \frac{5}{15}\). The result is \(3 \frac{11}{15}\).

If you chose F, you probably added the whole number parts and multiplied the fractions. If you chose G, you probably added the whole number parts and added the numerators and the denominators separately: \(1 \frac{2}{5} + 2 \frac{1}{3}\). If you chose J, you probably converted \(\frac{2}{5}\) to \(\frac{2}{15}\) incorrectly and then added 1 + 2 and \(\frac{2}{15} + \frac{5}{15}\).

**Question 5. The correct answer is E.** Although you could try out various combinations of the given three statements and try to make a conclusion, it might be more straightforward to look at each of the answer choices to see whether it contradicts one of the given three statements or whether it could be deduced from the given three statements.

A and B each say that Insect I is an ant. This directly contradicts the second given statement, so A and B are false.

Consider C: if it is true (Insect I is attracted to honey), then the first given statement implies that Insect I is an ant. This contradicts the second given statement, so C is false.

D directly contradicts the third given statement, so D is false.

For E, consider Insect J. The third given statement tells you that Insect J is attracted to honey, and the first given statement tells you that, because all insects attracted to honey are ants, Insect J must be an ant. So E must be true.

**Question 6. The correct answer is G.** You can find the value of this expression by substituting the given values of \(x\) and \(m\) into the expression and then simplifying: \(\sqrt{-16} = \sqrt{-4}\).

You may have gotten F if you did \(\sqrt{-16} \Rightarrow -\sqrt{4}\).

You may have gotten H if you did \(\sqrt{-16} = \sqrt{8}\). You may have gotten J if you did \(\sqrt{-16} = \sqrt{-4}\).

You may have gotten K if you did \(\sqrt{-16} = \sqrt{-4}\).
**Question 7. The correct answer is B.** The amount collected from the sale of 142 tickets bought in advance is equal to ($6 per ticket)(142 tickets) = $852. The amount collected from the sale of \(d\) tickets bought at the door is equal to ($8 per ticket)(\(d\) tickets) = $8\(d\). The total amount collected from all ticket sales is $852 + 8\(d\). To determine the minimum number of tickets to produce $2,000 in ticket sales, you can set up an inequality: $852 + 8\(d\) \geq 2,000. Subtracting 852 from both sides and then dividing by 8 produces the equivalent inequality \(d \geq 143.5\). Keep in mind, however, that \(d\) must be a whole number of tickets, so you must select the whole number \(d\) to satisfy the inequality. This means you must round 143.5 up to obtain the correct answer. If you chose A, you probably rounded down to 143. If you chose D, you might have divided 2,000 by 8 without thinking carefully about what the numbers represent. If you chose C or E, you probably set up the inequality incorrectly.

**Question 8. The correct answer is J.** For each kind of bread, there are 5 kinds of meat, so that is \(3 \cdot 5\) combinations of bread and meat. For each of these 15 combinations of bread and meat, there are 3 kinds of cheese. That makes \(15 \cdot 3 = 45\) combinations of bread, meat, and cheese.

The tree diagram on page 574 shows all 45 combinations. It would take a lot of time to list all these cases, but you can imagine what the tree looks like without having to write it all out. You can see that parts of the tree repeat many times, and so you can use multiplication to help you count.
Question 9. The correct answer is E. Use of the Distributive Property gives the equivalent equation $12x - 132 = -15$. Adding 132 to both sides of the equation results in the equation $12x = 117$, implying that the solution is $x = \frac{117}{12}$, or $\frac{39}{4}$ when reduced to lowest terms. If you distributed 12 to only the first term, $x$, but forgot to distribute 12 to the second term, you probably got an answer of $-\frac{1}{3}$. 

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**Question 10.** The correct answer is J. The following figure illustrates the progression of angle measures found in determining the measure of $\angle BCE$.

Because $\overline{BD} \cong \overline{AD}$, $\Delta ABD$ is isosceles, so its base angles are congruent. Therefore, $m \angle BAD = m \angle ABD = 25^\circ$. Because the sum of the angle measures in $\Delta ABD$ must equal $180^\circ$, $m \angle ADB = 180^\circ - (25^\circ + 25^\circ) = 130^\circ$. Because $\angle ADB$ and $\angle BDC$ are a linear pair, $m \angle BDC = 180^\circ - 130^\circ = 50^\circ$. Because $\overline{BD} \cong \overline{BC}$, $\Delta BDC$ is isosceles, so its base angles are congruent: $m \angle BCD = m \angle BDC = 50^\circ$. Finally, $\angle BCD$ and $\angle BCE$ are a linear pair, so $m \angle BCE = 180^\circ - 50^\circ = 130^\circ$.

**Question 11.** The correct answer is C. When you substitute $-2$ for $x$, you get $9(-2)^2 + 5(-2) - 8 = 9(4) + (-10) - 8 = 18$. If you chose A, you probably evaluated $9(-2)^2$ as $-36$. If you chose E, you probably evaluated $5(-2)$ as $10$.

**Question 12.** The correct answer is J. One efficient way to solve this problem numerically is by listing the multiples of the largest of the 3 numbers (70) as a sequence and determining whether or not each succeeding term in the sequence is a multiple of both 20 and 30.

- 70 (multiple of neither)
- 140 (multiple of 20 only)
- 210 (multiple of 30 only)
- 280 (multiple of 20 only)
- 350 (multiple of neither)
- 420 (multiple of both 20 and 30)

The first term in the sequence that is a multiple of both 20 and 30 is 420, which is the least common multiple of 20, 30, and 70. You can also find the least common multiple by expressing each of the three numbers as a product of primes (with exponents), listing all bases of exponential expressions shown, and choosing for each base listed the highest-valued exponent shown.

- $30 = 2^1 \times 3^1 \times 5^1$
- $20 = 2^2 \times 5^1$
- $70 = 2^1 \times 5^1 \times 7^1$

The least common multiple is $2^2 \times 3^1 \times 5^1 \times 7^1 = 420$. 

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**Question 13. The correct answer is E.** You may want to choose an even integer as Tom’s initial number, follow his steps in obtaining the incorrect answer, and then determine what operation using what number is needed to obtain the desired number. For example:

1. Choose the integer 6 as the initial number.
2. When Tom “accidentally multiplies the number by 2,” he obtains an incorrect answer of 12.
3. Had Tom correctly divided the initial number by 2, he would have obtained 3 as the answer.
4. To convert his incorrect answer of 12 to the desired answer of 3, he must divide by 4.

You may want to confirm that E is the correct answer by choosing a different initial number and repeating the steps.

**Question 14. The correct answer is G.** The 8-sided figure in the problem consists of 5 congruent squares whose areas total 125 square inches. Therefore, each congruent square has an area of $125 \div 5 = 25$ square inches, so each side of each square is $\sqrt{25} = 5$ inches long. The perimeter of the 8-sided figure is composed of 12 of these sides, each of length 5 inches, as shown in the following figure. Therefore, the 8-sided figure has a perimeter of $12 \times 5 = 60$ inches.

![8-sided figure diagram]

**Question 15. The correct answer is A.** You can find the total number of USBs Hai can buy by dividing the total cost of $100 by the cost of 1 USB plus tax for 1 USB, $8 \times (1 + 0.07)$:

$$\frac{100}{1.07(8)}.$$ You cannot buy a partial USB; therefore, you must round down to 11 whole USBs. You may have gotten B if you did $\frac{100}{1.07(8)}$ and rounded up. You may have gotten C if you did $\frac{100}{1.08(7)}$ and rounded down. You may have gotten D if you did $\frac{100}{1.08(7)}$ and rounded up. You may have gotten E if you did $\frac{100 + 8}{7}$ and rounded down.
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**Question 16.** The correct answer is J. Because the item gives a unit rate, you can set up a proportional relationship and solve for $x$: \[ \frac{1.5 \times 10^8 \text{ calculations}}{1 \text{ second}} = \frac{6.0 \times 10^{16}}{x} \Rightarrow x = \frac{6.0 \times 10^{16}}{1.5 \times 10^8}. \]
You divide the coefficients and subtract the exponents because the bases are the same in each expression: $4.0 \times 10^{16-8} = 4.0 \times 10^8$.

You may have gotten F if you did $\frac{1.5 \times 10^8}{6.0 \times 10^{16}} = 0.25 \times 10^{-8}$. You may have gotten G if you did $6.0(1.5) \times 10$. You may have gotten H if you incorrectly simplified $\frac{6.0 \times 10^{16}}{1.5 \times 10^8}$ to be $4.0 \times 10^{8}$. You may have gotten K if you did $(1.5 \times 10^8)(6.0 \times 10^{16})$.

**Question 17.** The correct answer is E. Each answer choice is a linear equation in slope-intercept form; that is, $y = mx + b$, where the value of $m$ gives the slope of the line and the value of $b$ gives the $y$-intercept of the line. Only the equation shown in E represents a line having a $y$-intercept ($b = 5$), that matches the value of the $y$-intercept indicated by the given graph.

**Question 18.** The correct answer is K. To find the area of a square circumscribed about a circle with a radius of 7 feet, you would need to find the side length of the square. Because the diameter of the circle is the distance between 2 opposite sides of the square, the side length of the square is twice the radius, $2(7)$, or 14 feet. To find the area of the square, you square the side length, $14^2$, to get 196 square feet.

If you chose F, you probably thought 7 feet was the side length and squared 7 to get 49 square feet. If you chose J, you probably used the formula for the area of a circle, $\pi r^2$, where $r$ is the radius, to get $\pi r^2$, or $49\pi$ square feet.

**Question 19.** The correct answer is A. For $x$ years of full years' employment after being hired, Worker A's starting salary ($20,000) increases by $800 per year and Worker B's starting salary ($15,200) increases by $2,000 per year. After $x$ years, Worker A's salary has increased by $800x$ and Worker B's salary has increased by $2,000x$. So, for $x$ years of full years' employment after being hired, Worker A's yearly salary is represented by the expression $20,000 + 800x$ and Worker B's salary is represented by the expression $15,200 + 2,000x$. These 2 yearly salaries are equal at the value of $x$ for which the equation $20,000 + 800x = 15,200 + 2,000x$ is true.

**Question 20.** The correct answer is J. The figure shows a right triangle with two given side measures. To find the length of the third side, use the Pythagorean theorem:

$$(\text{length of the hypotenuse})^2 = (\text{length of one side of the triangle})^2 + (\text{length of the other side of the triangle})^2$$

In this problem, the 13-foot measure represents the length of the hypotenuse. So the formula gives the equation $13^2 = 12^2 + x^2$, where $x$ feet is the length of the missing side. To find $x^2$,
subtract $12^2$ from each side of the equation. The subtraction results in the equivalent equation $25 = x^2$, resulting in the solution $x = \pm 5$. Because the side length of a triangle must be positive, you can ignore the negative solution. If you chose F, you probably took the length of the hypotenuse and subtracted the length of the given leg, without applying the Pythagorean theorem at all. If you chose G, you probably doubled the lengths, rather than squaring them.

**Question 21.** The correct answer is E. To simplify this expression, use the Distributive Property: $7(x + 3) - 3(2x - 2) = 7x + (7)(3) + (-3)(2x) + (-3)(-2) = 7x + 21 + (-6x) + 6$. Then combine like terms to obtain $x + 27$. If you chose B, perhaps you forgot that $a - b = a + (-b)$, and so you distributed 3 rather than $-3$ to the $-2$ term in $(2x - 2)$. If you chose A, perhaps you forgot to distribute the 7 and the $-3$ to the second term in each set of grouping symbols, setting $7(x + 3)$ equal to $7x + 3$ and $-3(2x - 2)$ equal to $-6x - 2$.

**Question 22.** The correct answer is G. To find 75% of a number, $n$, for which 115% of $n$ is 460, you first set up an equation to find $n$ using the fact that 115% of $n$ is 460, or $1.15n = 460$. After dividing by 1.15, you find $n = 400$. Then, 75% of 400 is 400(0.75), or 300.

If you chose J, you probably found 75% of 460 as 460(0.75), or 345. If you chose K, you probably found $n$ using the equation $1.15n = 460$ by dividing by 1.15 and getting 400.

**Question 23.** The correct answer is C. This problem tests your knowledge of how to square a binomial. The expression $(2x - 3)^2$ can be expanded into the $ax^2 + bx + c$ form using the Distributive Property as shown in the following:

$$(2x - 3)^2 = (2x - 3)(2x - 3) = (2x)(2x) + (2x)(-3) + (-3)(2x) + (-3)(-3)
= 4x^2 - 6x - 6x + 9 = 4x^2 - 12x + 9$$

When the coefficients of $4x^2 - 12x + 9$ are matched with the coefficients of $ax^2 + bx + c$, you can see that $a = 4$, $b = -12$, and $c = 9$, and that $a + b + c = 4 + (-12) + 9 = 1$.

When you square a binomial, you must multiply two binomial expressions using the distributive property. Common errors result from reasoning that $(2x - 3)^2$ is equivalent to $(2x)^2 + (-3)^2$ or $(2x)^2 - (3)^2$, resulting in B or D.

**Question 24.** The correct answer is H. Two common approaches are often used in solving this problem.

In the first approach, the polygon can be divided into a 15 ft by 15 ft square and a 10 ft by 5 ft rectangle (see the following Figure 1). The area of the polygon is equal to the sum of the areas of the rectangle and the square: $(15)(15) + (10)(5) = 275$ square feet.

In the second approach, you take the rectangle formed by the 15 ft and 25 ft sides of the polygon and “cut away” a 10 ft by 10 ft square (see the following Figure 2). In this case, the area of the polygon is equal to the difference of the areas of the rectangle and the square: $(15)(25) - (10)(10) = 275$ square feet.
Question 25. The correct answer is B. The way to use the minimum number of blocks is to have a side of the block with the largest area face upward. That is the side that is 4” by 8”. The 4” width of the blocks will fit 3 to each foot. The 8” length of the blocks will fit 3 to each 2 feet. The blocks could be arranged as shown, with 24 block widths in one direction and 15 block lengths in the other direction. That makes 15 · 24 = 360 blocks. The blocks could be arranged in different patterns, but the top area of all the blocks has to equal the (8)(10) = 80-square-foot area Barb is covering.

An alternate way to work this problem is to calculate the total area, 80 square feet, and divide by the largest area a single block can cover, 32 square inches. The area to be covered is (8)(12) = 96 inches in one direction and (10)(12) = 120 inches in the other direction, which makes the total area (96)(120) = 11,520 square inches. If you divide this by the area of a single block, 32 square inches, you will get \[ \frac{11,520}{32} = 360 \] blocks.

If you got answer A, you may have calculated the area of the patio in square feet.
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Question 26. The correct answer is H. To find the slope, you can manipulate the equation $6y - 14x = 5$ algebraically in order to find its equivalent equation expressed in *slope-intercept form*, which is $y = mx + b$, where $m$ is the slope and $b$ is the $y$-intercept. The manipulations are shown in the following:

$$6y - 14x = 5 \Rightarrow 6y = 14x + 5 \Rightarrow y = \frac{14}{6}x + \frac{5}{6}$$

The slope of the line equals $\frac{14}{6}$, or $\frac{7}{3}$ when reduced to lowest terms.

Question 27. The correct answer is C. First we will show that $m < \sqrt{mn}$:

Because $m$ and $n$ are positive integers such that $m < n$, $n = m + k$ where $k$ is a positive integer and $m \geq 1$. For this reason, we know $\sqrt{mn} = \sqrt{m(m+k)} = \sqrt{m^2 + km}$. Because the square root function increases as its input increases and $m^2 + km > m^2$, $\sqrt{m^2 + km} > \sqrt{m^2}$, and $\sqrt{m^2} = m$. Thus, $\sqrt{mn} > m$.

Then, we will show that $\sqrt{mn} < n$ by a similar argument:

Start by solving $n = m + k$ for $n$: $n - k = m$. Then write $\sqrt{mn} = \sqrt{(n-k)n} = \sqrt{n^2 - kn}$. Because $\sqrt{n^2 - kn} < n^2$, $\sqrt{(n-k)n} > \sqrt{n^2}$, and $\sqrt{n^2} = n$. Thus, $\sqrt{mn} < n$.

We have shown $m < \sqrt{mn}$ and $\sqrt{mn} < n$; thus, $m < \sqrt{mn} < n$.

If you chose A or B, you might have not realized that $\sqrt{mn}$ must be larger than $m$. Notice that for $m = 1$ and $n = 4$, $\sqrt{1(4)} > 1$ because $2 > 1$. If you chose D, you might have not considered cases such as when $m = 1$ and $n = 2$. Notice that for this case $\sqrt{mn} = \sqrt{n}$; thus, $\sqrt{mn} < \sqrt{n}$ is false. If you chose E, you might have not considered cases such as when $m = 3$ and $n = 4$. Notice that for this case $\sqrt{mn} > \sqrt{m} + n$ because $\sqrt{12} > \sqrt{7}$; thus, $\sqrt{mn} < \sqrt{m} + n$ is false.

Question 28. The correct answer is J. Similar triangles are triangles whose corresponding sides are proportional. The solution, $x$, is found by setting up the following proportion:

$$\frac{\text{the perimeter of the smaller triangle}}{\text{the perimeter of the larger triangle}} = \frac{3}{5} = \frac{(3 + 5 + 7)}{x} \text{ cm}$$

To solve $\frac{3}{5} = \frac{15}{x}$ for $x$, cross-multiply to obtain the equivalent equation $3x = 75$, and divide by 3 to obtain $x = 25$.

Question 29. The correct answer is A. The area of the whole board is $\pi r^2 = \pi \cdot 10^2 = 100\pi$ square inches. The radius of the outside of the 20 ring is $10 - 2 = 8$ inches. The radius of the outside of the 30 ring is $8 - 2 = 6$ inches, so the area of
the circle that includes 30, 40, and 50 points is $\pi \cdot 6^2 = 36\pi$ square inches. If a dart hits at a random spot on the board, the chance of it hitting in a certain region is proportional to the area of that region. So, the percent chance of hitting inside a region that is worth at least 30 points is $\frac{36\pi}{100\pi} \cdot 100\% = 36\%$.

C is the percent chance of getting more than 30 points, using the 4-inch radius of the inside of the 30 ring.

**Question 30. The correct answer is G.** You can use translation skills to set up an algebraic equation that, when solved, yields the solution to the problem.

1. Let the variable $a$ represent the teacher's age.
2. “If you square my age” translates into “$a^2$.”
3. “23 times my age” translates into “23$a$.”
4. “then subtract 23 times my age” translates into “$a^2 - 23a$.” Because the words *than* and *from* do not appear in the sentence, the order of the terms “$a^2$” and “23$a$” is NOT reversed when translated into mathematical language.
5. “the result is 50” translates into “= 50.”

Therefore, the translation gives the equation $a^2 - 23a = 50$, which you may solve by subtracting 50 from both sides and factoring.

The equation $a^2 - 23a - 50 = 0$ is true, provided that $(a + 2)(a - 25) = 0$, which happens if $a = -2$ (but age cannot be negative) or $a = 25$.

**Question 31. The correct answer is B.** “If a car accelerates from a stop at the rate of 20 meters per second per second” implies that $a = 20$, and “travels a distance of 80 meters” implies that $d = 80$. Substituting these values into the equation $d = \frac{1}{2}at^2$ gives the equation $80 = \frac{1}{2} (20)t^2$ or, equivalently, $80 = 10t^2$, or $8 = t^2$. Therefore, $t = \sqrt{8} \approx 2.8$ seconds.
**Question 32.** The correct answer is F. To find the real numbers $x$ such that $x + 3 > x + 5$, you would subtract $x$ and 3 from both sides. The result is $0 > 2$, but that inequality is never true, so there is no solution for $x$. It is the empty set.

If you chose G, you probably switched the inequality and got $0 < 2$ after you subtracted $x$ and 3 from both sides. If you chose H, you probably got $0 > 2$ and then thought that a negative value for $x$ would change the inequality.

**Question 33.** The correct answer is D. You must first determine from the frequency bar graph the number of students in the class responding that they spent 0, 1, or 2 hours studying on the previous evening. The bars in the graph indicate that 2 students studied 0 hours, 5 students studied 1 hour, and 6 students studied 2 hours. Therefore, the fraction of students in the class that responded they had spent less than 3 hours studying is equal to

$$\frac{\text{the number of students studying less than 3 hours}}{\text{the number of students in the class}} = \frac{2 + 5 + 6}{20} = \frac{13}{20}.$$

If you chose B (the most common incorrect answer), perhaps you overlooked the phrase “less than” and selected the number of students studying exactly 3 hours as the numerator, obtaining the fraction $\frac{4}{20}$, or $\frac{1}{5}$.

**Question 34.** The correct answer is J. In the following figure, the shaded sector represents the 3-hour group:

For this circle graph, the ratio $\frac{\text{the area of the shaded sector}}{\text{the area of the circle}}$ is equivalent to the ratio $\frac{\text{the number of students in the 3-hour group}}{\text{the number of students in the class}}$. These ratios, in turn, are equivalent to the ratio $\frac{\text{the measure of the central angle of the sector representing the 3-hour group}}{\text{the measure of the angle covered by 1 complete circle}}$. Letting the numerator of this last ratio equal $x^\circ$, and using the fact that the denominator of this ratio is $360^\circ$, you obtain the proportions $\frac{4}{20} = \frac{\text{the number of students studying 3 hours}}{\text{the number of students in the class}} = \frac{x^\circ}{360^\circ}$, so $x = 72$. 
**Question 35. The correct answer is B.** Because this frequency bar graph gives the number of times each response was given, the frequency bar graph was constructed from the following 20 data values:

\[0, 0, 1, 1, 1, 1, 2, 2, 2, 2, 2, 3, 3, 3, 3, 3, 4, 4, 5\]

The average number of hours for the 20 responses is equal to the average of the data values, which is defined to be \(\frac{\text{sum of the data values}}{\text{number of data values}}\).

This is equal to \(\frac{0 + 0 + 1 + 1 + 1 + 1 + 1 + 2 + 2 + 2 + 2 + 2 + 2 + 3 + 3 + 3 + 3 + 4 + 4 + 5}{20}\), or, equivalently,

\[\frac{2(0) + 5(1) + 6(2) + 4(3) + 2(4) + 1(5)}{20} = \frac{42}{20} = 2.1.\]

**Question 36. The correct answer is H.** To find the number of diagonals the octagon has, you would label the 8 vertices as endpoints. Those segments (which are the diagonals) are \(AC, AD, AE, AF, AG, BD, BE, BF, BG, CE, CF, CG, CH, DF, DG, DH, EG, EH,\) and \(FH\). There are 20 diagonals.

If you chose F, you probably just found the number of vertices in an octagon. If you chose G, you probably just multiplied the number of vertices by the number of endpoints of a diagonal, \(8(s)\), or 16.

**Question 37. The correct answer is E.** As shown in the following figure, the tether line, the level ground, and a line segment representing the altitude of the bottom of the basket form a right triangle.

Let the length of the altitude equal \(h\) feet. You can use a trigonometric ratio to find \(h\). The tether line forms the hypotenuse of the right triangle, and the line segment representing the altitude is the side opposite the \(72^\circ\) angle. Therefore, the trigonometric ratio to be used with respect to the \(72^\circ\) angle is the sine ratio, which gives the following equation:

\[\sin 72^\circ = \frac{\text{length of the side opposite the } 72^\circ \text{ angle}}{\text{length of the hypotenuse}} = \frac{h}{144}\]

Multiplying both sides of the equation \(\frac{h}{144} = \sin 72^\circ\) by 144 yields the value of \(h\), which is 144 sin 72°.
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Question 38. The correct answer is G. The midpoint of a line segment is the point halfway between the two endpoints of the line segment. A formula for finding the midpoint \((x_m, y_m)\) of two points \((x_1, y_1)\) and \((x_2, y_2)\) in the standard \((x,y)\) coordinate plane is

\[
(x_m, y_m) = \left( \frac{x_1 + x_2}{2}, \frac{y_1 + y_2}{2} \right).
\]

The \(x\)-coordinate of the midpoint, \(x_m\), is the average of the \(x\)-coordinates of the endpoints of the line segment. In the case of \(GH\),

\[
x_m = \left( \frac{x_1 + x_2}{2} \right) = \frac{-8 + 2}{2} = -3.
\]

Question 39. The correct answer is E. To determine the value of \(8x + 9y\), find the solution \((x,y)\) to the system of two equations given in the problem. This system can be solved using an elimination method. First, determine which of the two variables would be easiest to eliminate. For this system, eliminating the \(y\)-variable would be easier. In order to eliminate the \(y\)-variable, the \(y\)-coefficients in each equation (or equivalent equation) must be opposite numbers (\(-6\) and \(6\) would be the best choice). Therefore, all terms in the upper equation should be multiplied by \(-2\) (Step 1 following) to form an equivalent equation with \(-6\) as the \(y\)-coefficient. Now the two equations have \(y\)-coefficients of \(-6\) and \(6\), respectively, so adding the equations will eliminate the \(y\)-variable (Step 2 following).

\[
\begin{align*}
2x + 3y &= 4 \\
5x + 6y &= 7
\end{align*}
\]

\[
\begin{align*}
\text{Step 1} & \Rightarrow -2(2x + 3y) = -2(4) \\
\text{Step 2} & \Rightarrow -4x - 6y = -8
\end{align*}
\]

Substituting into either of the two initial equations produces an equation that can be solved for \(y\); for example, letting \(x = -1\) in \(2x + 3y = 4\) gives \(2(-1) + 3y = 4\). Solving for \(y\), \(-2 + 3y = 4\), so \(3y = 6\). Therefore, \(y = 2\).

Substituting \(x = -1\) and \(y = 2\) into \(8x + 9y\) yields \(8(-1) + 9(2) = -8 + 18 = 10\).

Question 40. The correct answer is H. If we draw \(\theta\) in standard position and its terminal side intersects the unit circle at \((x,y)\), then \(\tan \theta = \frac{y}{x}\). Because we want to solve \(\tan \theta = -1\), we want the ratio \(\frac{y}{x} = -1\). This only happens when \(\theta = \frac{3\pi}{4}\) or \(\theta = \frac{7\pi}{4}\). Recall that \(\tan \theta < 0\) only when the terminal side of \(\theta\) is in Quadrants II or IV.

You may have gotten K if you solved \(\tan \theta = \pm 1\). You may have gotten F if you thought the tangent of an angle was negative when its terminal side was in Quadrants I and II. You may have gotten G if you thought the tangent of an angle was negative when its terminal side was in Quadrants II and III. You may have gotten J if you thought the tangent of an angle was negative when its terminal side was in Quadrants III and IV.
Question 41. The correct answer is B. By definition, $i^2 = -1$, so $i^4 = (i^2)^2 = (-1)^2 = 1$. Therefore, $i^x = 1$ for $x = 4$, so 1 is a possible value of $i^x$ when $x$ is an integer. More generally, when $x$ is an integer, the only values of $i^x$ possible are $i, -1, -i$, and 1, as shown in the following table:

<table>
<thead>
<tr>
<th>$x$</th>
<th>$i^0$</th>
<th>$i^1$</th>
<th>$i^2$</th>
<th>$i^3$</th>
<th>$i^4$</th>
<th>$i^5$</th>
<th>$i^6$</th>
<th>$i^7$</th>
<th>$i^8$</th>
<th>$i^9$</th>
<th>$i^{10}$</th>
<th>$i^{11}$</th>
<th>$i^{12}$</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>1</td>
<td>$-i$</td>
<td>1</td>
<td>$i$</td>
<td>1</td>
<td>$-i$</td>
<td>1</td>
<td>$i$</td>
<td>1</td>
<td>$-i$</td>
<td>1</td>
<td>$-i$</td>
<td>1</td>
</tr>
</tbody>
</table>

This rules out A, C, D, and E.

Question 42. The correct answer is F. Because the diameter of the can is 2 inches and the diameter of the glass is 3 inches, the radius of the can is 1 inch and the radius of the glass is 1.5 inches. Therefore, using $\pi r^2 h$, the volume of the can is $\pi (1^2)(6)$, or $6\pi$, and the volume of the glass is $\pi (1.5^2)h$, or $2.25\pi h$. Because the volume of the soda pop can and the volume of the glass are equal, $6\pi = 2.25\pi h$. Solving for $h$ gives us $h = 2\frac{2}{3}$.

You may have gotten G if you thought that height and diameter were directly proportional: $2(6) = 3h$. You may have gotten H if you thought that because the radius increased by 1 inch, then the height should decrease by 1 inch. You may have gotten J if you added all the values in the stem. You may have gotten K if you did $\frac{6\pi}{\frac{3}{2}\pi}$.

Question 43. The correct answer is C. The volume in cubic meters, $V$, of a right circular cylinder of radius $r$ meters and height $h$ meters is given by the formula $V = \pi r^2 h$. For the cylinder in this problem, $r = 5$ and $h = 6$. Therefore, $V = \pi (5^2)(6) = 150\pi$ cubic meters.

Question 44. The correct answer is F. The three triangles in the given figure ($\triangle ABC$, $\triangle ADE$, and $\triangle AFG$) can be shown to be similar by use of the Angle-Angle Similarity property.

Because $\triangle ABC \sim \triangle AFG$, the statement “The ratio of the perimeter of $\triangle ABC$ to the perimeter of $\triangle AFG$ is 1:3” implies that the ratio of $AC$ to $AG$ is 1:3. So if $AC = 1$ unit, then $AG = 3$ units (see the following Figure 1).

Because $\triangle ADE \sim \triangle AFG$, the statement “The ratio of $DE$ to $FG$ is 2:3” implies that the ratio of $AE$ to $AG$ is 2:3. So if $AG = 3$ units, then $AE = 2$ units (see the following Figure 2).

This means that $AE = 2$ units when $AC = 1$ unit, implying that $CE = 1$ unit (see the following Figure 3). Therefore, the ratio of $AC$ to $CE$ is 1:1.
**MATHEMATICS • PRACTICE TEST 3 • EXPLANATORY ANSWERS**

**Question 45.** The correct answer is E. The following Figure 1 shows the first phase, when the rocket traveled vertically for 30 kilometers.

Figure 2 shows the second phase, when the rocket traveled 40 km at 30° from the vertical. The three distances shown in Figure 2 are in the ratio 1:√3:2, a characteristic of 30°-60°-90° triangles. The vertical distance covered in the second phase is 20√3 km.

Figure 3 shows the third phase, when the rocket traveled 100 km at 45° from the vertical. The three distances shown in Figure 3 are in the ratio 1:1:√2, a characteristic of 45°-45°-90° triangles. The vertical distance covered in the third phase is 50√2 km.

Taking the sum of the vertical distances covered by each of the three phases gives the vertical distance of the rocket above the launch pad after the third phase.

**Question 46.** The correct answer is G. Let X be a random variable that can take on all and only the values of \(x_1, x_2, x_3, \ldots x_n\). The expected value of X is defined by

\[
EV(X) = x_1p_1 + x_2p_2 + \cdots + x_np_n
\]

where, for \(k = 1, 2, 3, \ldots n\), \(X\) takes the value of \(x_k\) with a probability of \(p_k\). Using this formula, we see \(EV(n) = 0(0.70) + 1(0.20) + 2(0.05) + 3(0.05) = 0.45\), G. If you chose either F or H, you probably did not recall the definition of the expected value of a random variable. If you chose J, you added the probabilities of the four possible values of \(n\). If you chose K, you found the mean of the four possible values of \(n\). In all four of these incorrect cases, please see the previously given definition of expected value.
MATHEMATICS • PRACTICE TEST 3 • EXPLANATORY ANSWERS

Question 47. The correct answer is E. We can find the factored form of the equation by first factoring out a GCF of –2, \( h = -2(t^2 - 5t - 24) \), and then further factoring the quadratic to \( h = -2(t + 3)(t - 8) \). The object reaches the ground when \( h = 0 \) and time is positive. By the zero product property, \( 0 = -2(t + 3)(t - 8) \) when \( t = -3 \) or \( t = 8 \). Because 8 is the positive value of \( t \) that is the solution to \( h = 0 \), the object will hit the ground at 8 seconds.

If you chose D, you might have picked the negative value of \( t \) in the solution to \( 0 = -2(t + 3)(t - 8) \) and then taken the absolute value. If you chose B or C, you might have confused the factored form of a quadratic equation with the vertex form. This equation can be written as \( h = -2(x - 2.5)^2 + 60.5 \), so the maximum height is 60.5 units. If you chose A, you might have not realized that the starting point is the value of \( h \) when \( t = 0 \), which is 48.

Question 48. The correct answer is H. Rewrite the values in the radicand as exponents, and then simplify.

\[
g^2 \sqrt{g^5 \cdot h^{2 \frac{4}{5} h^5}}
\]

\[
g^2 \sqrt{g^5} \cdot h^{2 \frac{4}{5} h^4}
\]

\[
g^{2 + \frac{4}{5}} \cdot h^{2 + \frac{5}{4}}
\]

\[
g \cdot \frac{9}{g^2} \cdot \frac{13}{h^4}
\]

\[
g^{4 \frac{1}{2}} \cdot h^{\frac{3}{4}}
\]

\[
g^4 h^{3 \frac{1}{5} g^2} h
\]

You probably got F if you did \( g^2 + \frac{2}{5} \cdot h^2 + \frac{2}{5} \). You probably got G if you did \( g^{\frac{21}{5}} \cdot h^{\frac{21}{5}} \). You probably got J if you did \( g^2 + \frac{5}{2} \cdot h^2 + \frac{5}{2} \). You probably got K if you did \( g^2 + 5 \cdot h^2 + 5 \).

Question 49. The correct answer is D. The value of \( \log_5(5^\frac{x}{2}) \) is found by solving the equation \( \log_5(5^\frac{x}{2}) = x \). By definition of logarithm to the base 5, this equation is equivalent to the equation \( 5^x = 5^{\frac{x}{2}} \). The equation \( 5^x = 5^{\frac{x}{2}} \) is equivalent to the equation \( x = \frac{\frac{x}{2}}{2} \), whose value is between 6 and 7.

Question 50. The correct answer is F. We need to find the percent decrease, which is found by using the formula for percent change.

\[
\text{percent change} = \frac{|\text{original cost} - \text{new cost}|}{\text{original cost}} \times 100
\]
The Size 3 unit is $100 per month, and the special rate is $1 for the first month. The original cost would have been 12(100), but because there is a special rate of $1 for the first month, Daria only needs to pay the original monthly fee for 11 months, 11(100) + 1. Use the formula to find the percent decrease.

\[
\frac{|12(100) - (11(100)+1)|}{12(100)} \times 100 = \frac{99}{12(100)} \times 100
\]

You may have gotten G if you did \(\frac{100}{12(100)} \times 100\). You may have gotten H if you did \(\frac{100+1}{12(100)} - 1 \times 100\). You may have gotten J if you did \(\frac{100-1}{11(100)} \times 100\). You may have gotten K if you did \(\frac{100}{11(100)} \times 100\).

**Question 51. The correct answer is E.** The Size 5 unit is 8 \(\times\) 16, and the Size 1 unit is 2 \(\times\) 4. One way to solve is to divide the width by width and length by length, if width \(\times\) length. We can see that the Size 1 unit’s width of 2 can fit into the Size 5 unit’s width of 8 four times, or \(\frac{8}{2}\). Similarly, we see that Size 1 unit’s length of 4 can fit into Size 5 unit’s length of 16 four times, or \(\frac{16}{4}\). Because we are dealing with area, we multiply \(\frac{8}{2} \times \frac{16}{4}\), or 4 \(\times\) 4, to get the maximum number of Size 1 units into Size 5 units. A drawing would also help you see this answer. A possible drawing:

You may have gotten A if you divided length from the Size 1 unit and width from the Size 5 unit as \(\frac{8}{4}\). You may have gotten B if you divided only the widths as \(\frac{8}{2}\). You may have gotten C if you did \(\frac{8}{2} + \frac{16}{4}\). You may have gotten D if you did \(\frac{16}{2} + \frac{8}{4}\).
Question 52. The correct answer is H. \( x \) = unit size number. The relationship between the unit size number and the area of each unit is as follows:

<table>
<thead>
<tr>
<th>( x )</th>
<th>Area</th>
<th>Pattern</th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>8</td>
<td>( 8 \times 2^0 )</td>
</tr>
<tr>
<td>2</td>
<td>16</td>
<td>( 8 \times 2^1 )</td>
</tr>
<tr>
<td>3</td>
<td>32</td>
<td>( 8 \times 2^2 )</td>
</tr>
<tr>
<td>4</td>
<td>64</td>
<td>( 8 \times 2^3 )</td>
</tr>
<tr>
<td>5</td>
<td>128</td>
<td>( 8 \times 2^4 )</td>
</tr>
</tbody>
</table>

Notice as the unit size number increases, the area increases exponentially. The pattern is shown in the table.

The expression that summarizes this pattern is \( 8 \times 2^{(x-1)} \) or \( 2^3 \times 2^{(x-1)} \). Using properties of exponents, the simplest form is \( 2^{(2+x)} \). You may have gotten F if you thought the pattern was \( 8 \times \) unit size number. You may have gotten G, J, or K if you did not understand the pattern.

Question 53. The correct answer is B. The graph of any trigonometric function of the form \( y = a \sin(bx + c) \) is cyclical. That is, the graph is composed of repeating, identical cycles. The shaded region in the following graph shows one such cycle. The period of the function is the width of the smallest interval of \( x \) on which one of these cycles appears. In the following graph, the period is the width of the shaded region, given by \( 2\pi - \pi = \pi \).

The period of \( y = \sin x \) is \( 2\pi \), which is C, the most common incorrect answer. If you chose E, you may have confused period with amplitude.
**Question 54. The correct answer is G.** The component form of \( w \) can be found by adding the opposite of the scalar horizontal components together and the opposite of the scalar vertical components together: 

\[
-2\langle 5, 3 \rangle + 3\langle 2, -7 \rangle = \langle -10 + 6, -6 - 21 \rangle.
\]

If you got F, you may have done 

\[
-2\langle 5, 3 \rangle - 3\langle 2, -7 \rangle = \langle -10 - 6, -6 + 21 \rangle.
\]

If you got H, you may have done 

\[
2\langle 5, 3 \rangle - 3\langle 2, -7 \rangle = \langle 10 - 6, 6 + 21 \rangle.
\]

If you got J, you may have done 

\[
2\langle 5, 3 \rangle - 3\langle 2, -7 \rangle = \langle 10 - 6, 6 + 21 \rangle.
\]

If you got K, you may have done 

\[
2\langle 5, 3 \rangle + 3\langle 2, -7 \rangle = \langle 10 + 6, 6 - 21 \rangle.
\]

**Question 55. The correct answer is B.** We can rewrite the bases as powers of a common base. The common base here is 3, because \( 3^1 = 3 \), and \( 3^2 = 9 \).

\[
\begin{align*}
3^x + 1 &= 3^{2(x-2)} \\
3^x + 1 &= 3^{2x-4} \\
x + 1 &= 2x - 4 \\
x &= 5
\end{align*}
\]

This is the one and only solution that makes the equation true.

If you chose A, you may have set the exponents equal to each other before finding a common base and found there was no solution, OR you may have not found a common base and tried instead to solve for \( x \). If you chose C, you may have rewritten 9 as \( 3^2 \) and misinterpreted the squared for two solutions. If you chose D, you may have done \( \frac{9}{2} \). If you chose E, you thought the exponential equation had an infinite number of solutions.

**Question 56. The correct answer is H.** The area of the original triangle is \( \frac{1}{2}(20)(15)\sin\theta \).

The area of the resulting triangle is \( \frac{1}{2}(20)(15 - 2t)\sin\theta \). To find the time, \( t \), when the resulting triangle has an area that is \( \frac{1}{2} \) the area of the original triangle, you need to set the area of the resulting triangle equal to \( \frac{1}{2} \) the area of the original triangle and solve for \( t \):

\[
\frac{1}{2}(20)(15 - 2t)\sin\theta = \frac{1}{2}\left(\frac{1}{2}(20)(15)\sin\theta\right)
\]

\[
\Leftrightarrow (20)(15 - 2t)\sin\theta = \frac{1}{2}(20)(15)\sin\theta
\]

\[
\Leftrightarrow (15 - 2t)\sin\theta = \frac{1}{2}(15)\sin\theta
\]

\[
\Leftrightarrow 15 - 2t = \frac{1}{2}(15)
\]

\[
\Leftrightarrow 30 - 4t = 15
\]

\[
\Leftrightarrow -4t = -15
\]

\[
\Leftrightarrow t = \frac{15}{4}
\]
If you chose F, you might have incorrectly set the area of the original triangle equal to the area of the resulting triangle and solved for \( t \): \( \frac{1}{2}(20)(15)\sin \theta = \frac{1}{2}(20)(15 - 2t)\sin \theta \). If you chose G, J, or K, you might have set up the problem correctly but made a mistake in your algebra. For G, you might not have distributed the four correctly:

\[
\frac{1}{2}(20)(15 - 2t)\sin \theta = \frac{1}{2}\left(\frac{1}{2}(20)(15)\sin \theta\right)
\]

\[
\iff \frac{1}{2}(15 - 2t) = \frac{1}{4}(15)
\]

\[
\iff 4\left(\frac{1}{2}(15 - 2t)\right) = 4\left(\frac{1}{4}(15)\right)
\]

\[
\iff 2(15) - 8t = 15
\]

For J, you might have dropped the \( \frac{1}{2} \) in the area of the original triangle:

\[
\frac{1}{2}(20)(15 - 2t)\sin \theta = \frac{1}{2}\left(\frac{1}{2}(20)(15)\sin \theta\right)
\]

\[
\iff (15 - 2t) = \frac{1}{4}(15)
\]

For K, you might have thought \( \frac{1}{2} \cdot \frac{1}{2} \) canceled out, incorrectly distributed the \( \frac{1}{2} \) in the area of the resulting triangle, and then dropped the negative:

\[
\frac{1}{2}(20)(15 - 2t)\sin \theta = \frac{1}{2}\left(\frac{1}{2}(20)(15)\sin \theta\right)
\]

\[
\iff \frac{1}{2}(15 - 2t) = 15
\]

\[
\iff \frac{1}{2}(15) - 2t = 30
\]

\[
\iff 15 - 4t = 60
\]

\[
\iff 4t = 45
\]

**Question 57.** The correct answer is E. Distinct permutations are permutations without repetition. We want to find how many unique orderings there are of the letters PEOPLE. The number of ways to order 6 different letters would be 6!. Because the P and the E are repeated twice, we must divide by 2! to account for the repeated P and again by 2! to account for the repeated E. Thus we get \( \frac{6!}{(2!)(2!)} \).

If you got A you probably didn’t account for letters P and E that cannot be repeated. If you got B you probably didn’t understand distinct permutations. If you got C you probably
considered the 6 letters in the word and 4 different letters in the word. If you got D you probably considered the 6 different letters in the word and that only 1 letter repeated.

**Question 58. The correct answer is K.** Complex conjugate pairs can be written in the form \((a + bi)(a - bi)\), which when simplified equals \(a^2 - b^2i^2 = a^2 + b^2\).

The value of \(i^2 = -1\); therefore, when \((7x - 9i)(7x + 9i)\) is simplified, it equals \(49x^2 - 81i^2 = 49x^2 - 81(-1) = 49x^2 + 81\). You may have gotten F if you took the square root of 49\(x^2\) and 81. Notice that \((7x + 9)^2 = 49x^2 + 126x + 81\). You may have gotten G or H if you forgot that a complex conjugate pair consists of one expression with an addition and its conjugate pair has subtraction. You may have gotten J if you forgot the \(i\) in the conjugate pairs.

**Question 59. The correct answer is B.** Given an input \(x_i\), the absolute value of the residual gives the vertical distance between the observed \(y_i\)-value and the \(y(x_i)\)-value predicted by the line of best fit. By inspecting the graph, the ordered pair (32, 135) appears to have the greatest vertical distance from the line of best fit. The absolute value of this residual is given by \(|135 - y(32)| = |135 - (1.1(32) + 93)| = |135 - 128.2| = 6.8\). The remaining residuals are \(|120 - y(27)| = |127 - (1.1(27) + 93)| = 2.7\), \(|140 - y(42)| = |140 - (1.1(42) + 93)| = 0.8\), and \(|130 - y(37)| = |130 - (1.1(37) + 93)| = 3.7\). If you chose A, you may have chosen the correct ordered pair (32, 135) but incorrectly computed the absolute value by adding 32 and 93 before multiplying by 1.1. If you chose C, you probably computed the difference in the 2 \(y_i\)-values 135 and 120. If you chose D, you may have incorrectly thought that the residual is the absolute value of the difference in the largest and smallest \(y_i\)-values, 140 and 120. If you chose E, you may have correctly identified the point farthest from the line but computed the vertical distance between 135 and the \(y\)-intercept of the line, 93.

**Question 60. The correct answer is K.** Making at least 1 error on any given day and making no errors are complementary events. Hence,

\[
P(x \geq 1) = 1 - P(x = 0)
\]

\[
\equiv P(x \geq 1) = 1 - 0.0823
\]

\[
\equiv P(x \geq 1) = 0.9177
\]

If you chose F, you might have thought that the probability of at least 1 error is the same as the probability of exactly 1 error, \(P(1)\). If you chose G or J, you might have thought that the table shows the probabilities for making any number of errors possible on a given day and not realized that it only shows the probabilities for making 0–4 errors. For G, you might have thought that the probability of at least 1 error is the same as the sum of the probabilities of 2–4 errors, \(P(2) + P(3) + P(4)\). For J, you might have thought that the probability of at least 1 error is the same as the sum of the probabilities of 1–4 errors, \(P(1) + P(2) + P(3) + P(4)\). If you chose H, you might have thought that the probability of making at least 1 error is equal to the complement of the sum of the probability of 1 error and the probability of no errors, \(1 - (P(1) + P(0)) = 1 - P(1) - P(0)\).
Passage I

**Question 1.** The best answer is A because the passage identifies Shades Bowen as one of the other local musicians in the “bullpen” (lines 5–6) and goes on to state that, of those local musicians, Everett Payne “was the one being invited to sit in” (line 15) and play with the band that night. In this context, “the one” indicates that only Everett was sitting in, and no mention is made in the passage of any other musician sitting in.

The best answer is not:

B because although the passage indicates that Everett Payne is “not long out of the army” (lines 14–15), the passage makes no mention of Shades Bowen having been in the army as well.

C because although the passage refers to all the people in the “bullpen” as “young locals” (line 9), the passage makes no mention of Shades Bowen's age.

D because the passage states that Everett Payne joined Shades Bowen in the “bullpen” (lines 5–7) where “young locals gathered . . . each Sunday evening, hoping for a chance to perform” (lines 9–10). This indicates that Shades Bowen was a local musician himself, and there is no indication in the passage that Shades Bowen had any role in deciding which other local musicians were allowed to play with the band.

**Question 2.** The best answer is G because the statement in question (line 62) describes the audience’s physical reaction to Everett Payne’s performance. This performance is described in great detail in the preceding paragraph (lines 48–61) as being impressive enough to warrant such a reaction.

The best answer is not:

F because the statement in question (line 62) refers to the audience’s physical reaction to the improvisational passages that Payne played after he had taken his time “paying his respects to the tune as written” (lines 48–49). This indicates that the audience reaction was not based on “initial expectations” but rather on later developments in the playing of the song “Sonny Boy Blue.”

H because the statement in question (line 62) supports, rather than counteracts, the narrator’s description of Payne’s performance.

J because there is no mention in the passage that Payne is well known by the audience.
**Question 3.** The *best answer is* A because the passage describes the jazz show as “winding down” (lines 1–2) near the end of the second set. This implies that the second set is the final set of the show.

*The best answer is NOT:*

B because there is no description in the passage of the first set or of the length of either the first or the second set.

C because the narrator mentions that the show is “winding down” (lines 1–2), which suggests that there will be no third set.

D because the passage states that the jazz show is “nearing the end of the second set” (line 1) when the musicians in the “bullpen” were called up to play. If the *entire* second set was performed solely by musicians from the “bullpen,” then they would not be “called up to play” only toward the end of that set.

**Question 4.** The *best answer is* H because the passage states that when the purists first heard Payne's choice of music, they “slouched deeper in their chairs in open disgust” (lines 36–37).

*The best answer is NOT:*

F because although the passage mentions the silence following Payne's performance (lines 81–83), there is no specific mention of the audience reacting to Payne's choice of music with silence.

G because the audience's in-suck of breath (line 62) is in response to Payne's performance, not to his choice of music.

J because the purists stood up at the end of Payne's performance “in languid praise” (line 88) of Payne, not as a reaction to Payne's choice of music.

**Question 5.** The *best answer is* C because the narrator describes how she watched as Payne “slowly mounted the bandstand and conferred with the bassist and drummer” (lines 26–27).

*The best answer is NOT:*

A because Payne did not move quickly to the bandstand. Rather, the narrator describes him as moving with “a deliberate pause between each step” (lines 18–19).

B because the narrator describes Payne as sitting down to play “without in any way acknowledging the audience” (line 30).

D because the narrator says that Payne sat down at the piano “without announcing the name of the tune he intended playing” (lines 28–29).
Question 6. The best answer is G because the purists are described as reacting negatively to Payne because of his choice of song (lines 35–37), suggesting intolerance. They are also described as usually refusing “to applaud even genius” (line 88), implying snobbishness.

The best answer is NOT:

F because although the term purist in the context of a jazz audience suggests that they may be knowledgeable about jazz music, the purists in this audience are described as reacting negatively to Payne because of his choice of song (lines 35–37), suggesting that they are intolerant rather than open-minded.

H because the passage makes no mention of whether or not the purists are educated. Additionally, the purists are not portrayed as rational, as they usually refuse to acknowledge a praiseworthy performance (lines 87–88).

J because although the purists may be “uninhibited” in that they visibly react or do not react to performances as they please, the passage makes no mention of their “inexperience” regarding jazz. In fact, the opposite impression is created by the purists’ initial disgust at the prospect of hearing a “hokey” (line 38), or old-fashioned, tune such as “Sonny Boy Blue.” Moreover, the term purist in general denotes someone devoted to the most essential or “pure” expression of a particular idea or practice, and such devotion usually indicates a deep familiarity with the object of their devotion rather than “inexperience.”

Question 7. The best answer is B because the narrator refers to Bach and the blues as being the “bedrock” on which Payne had been trained (lines 76–77).

The best answer is NOT:

A because there is nothing in the passage to suggest that Everett did anything to avoid representing Bach and the blues when he played piano.

C because the narrator describes Bach and the blues as being “earthbound” (line 76) and “the bedrock” (line 76) of Payne’s musical inspiration. Moreover, the narrator contrasts these influences, which Payne hears through “his other ear” (line 75) with “the true music of the spheres” (lines 72–73), which he hears through “his right ear directed skyward” (line 68).

D because the passage does not imply that Everett is limited to “Tin Pan Alley” tunes. Rather, the passage states that Everett “recast” and “reinvented” the Tin Pan Alley tune “Sonny Boy Blue” in an image all his own” (lines 60–61).
Question 8. The best answer is F because the passage indicates that Payne first played the song "at a slower tempo than was called for" (line 41).

The best answer is NOT:

G because there is no indication in the passage that Payne spoke with anyone other than the bassist and the drummer.

H because although the passage states that Payne conferred with the bassist and the drummer (line 27), there is no mention in the passage that either the bassist or the drummer had any reaction to what Payne said to them.

J because when Payne first played “Sonny Boy Blue,” he played the song “straight through as written” (line 39). The passage also states that throughout Payne's performance, he “continued to acknowledge the little simple-minded tune” (lines 59–60).

Question 9. The best answer is A because Hattie speculates that Payne's talent “had to do . . . with the way he held his head . . . tilted” (lines 65–67).

The best answer is NOT:

B because the narrator never mentions the simplemindedness of the tune as being related to Payne's musical ideas and feelings. Rather, the characterization of “Sonny Boy Blue” as a “little simple-minded tune” (lines 59–60) creates a contrast between Payne's elaborate and inventive improvisations and the simple and overly familiar song that he chooses as a vehicle for those improvisations.

C because although the narrator mentions Payne's formality in playing through the parts of “Sonny Boy Blue” the first time (lines 42–43), the narrator does not identify this formality as the source of the musical ideas and feelings showcased in Payne's improvisations.

D because the passage makes no mention of any connection Payne feels with his audience. Rather, the passage states that Payne does not even acknowledge his audience before playing (line 30).

Question 10. The best answer is J because the passage states that Payne's performance seemed to Hattie “a joyous, terrifying roller coaster of a ride” (lines 78–79).

The best answer is NOT:

F because although the passage states that Payne's rendition of the song began slowly and formally (lines 41–43), the passage goes on to contrast this beginning with a lengthy improvisational section described in terms that indicate that Hattie found the performance as a whole anything but formal (lines 48–61).
G because there is no indication in the passage that Hattie considers Payne’s musical performance absent-minded. Instead, she describes his body “moving absentmindedly through space” as he approaches the bandstand to play (lines 20–21).

H because the narrator does not describe Payne’s performance of “Sonny Boy Blue” as resembling a song played in church. Rather, she describes the audience reacting to Payne’s performance “as if they were in church and weren’t supposed to clap” (lines 82–83).

Passage II

**Question 11. The best answer is A** because the passage as a whole presents a cohesive argument that sprawl is both unpleasant and harmful (lines 9–10, 25–27, 33–37, 44–47, 59–61, 74–79); that its destructive effects are too often ignored (lines 11–16); that characterizations of sprawl as either inevitable or desirable are flawed (lines 17–19, 52–54, 62–66); that policies currently in place encourage sprawl to continue (lines 19–22, 66–74); and that there are a set of alternative policies that, if adopted, would resist sprawl and reduce these harmful effects (lines 80–91). The overall effect of these linked propositions is to persuade the reader that a choice must be made between a proven harm and a beneficial alternative. Moreover, the language used to describe sprawl throughout the passage is consistently negative, including, for example, the initial identification of sprawl as a “destructive, soulless, ugly mess” (lines 9–10). In contrast to these descriptions, communities without sprawl are described as “places that people care about” (line 35) or characterized as representing a “compact walkable environment” (70–71). Drawing a contrast between attractive and unattractive descriptions, as this passage does, is a common tactic of persuasive rhetoric.

**The best answer is not:**

B because although the author explains what sprawl is, the main purpose of the passage is not merely to explain what sprawl is but to argue for measures that would control sprawl and “knit communities together” (line 89).

C because although the author does describe sprawl throughout the passage, these descriptions are more often colorful and emotional than they are precise and exact. For example, sprawl is initially characterized as a “destructive, soulless mess” (lines 9–10). By contrast, communities without sprawl are described as “places that people care about” (line 35) or characterized as representing a “compact walkable environment” (lines 70–71). Drawing a contrast between attractive and unattractive descriptions, as this passage does, is a common tactic of persuasive rather than descriptive rhetoric. Therefore the principal aim of the passage is persuasive rather than descriptive.

D because the passage does not tell a story. Rather, it informs the reader of a problem and urges the reader not only to see sprawl as a problem as well but also to take measures to solve the problem.
Question 12. The best answer is J because after describing the effect of sprawl on communities, and criticizing policies that encourage sprawl, the author proposes the adoption of policies that discourage sprawl, such as “downtown housing and mixed-use zoning” (lines 85–86) and goes on to explain that “the goal should be an integrated system of planning decisions and regulations that knit communities together instead of tearing them apart” (lines 87–90). Therefore, in the context of the sentence in which it appears and in the context of the entire passage, the establishment of “an integrated system of planning decisions and regulations” is clearly something that the author would like to see happen.

The best answer is NOT:

F because the full sentence in question reads “Too many developers follow standard formulas, and too many government entities have adopted laws and policies that constitute powerful incentives for sprawl” (lines 19–22). The author’s opposition to the laws in question is signaled within the sentence by the assertion that “too many government entities” enact them. In the context of the sentence in which it appears and in the context of the author’s criticism of sprawl throughout the passage, the enactment of “laws . . . that provide powerful incentives for sprawl” is not something that the author would like to see happen.

G because “the destruction of traditional downtowns” (line 34) is presented as an end result of sprawl and as something that “is corroding the very sense of community that helps bind us together as a people and as a nation” (lines 35–37). In the context of the sentence in which it appears and in the context of the author’s criticism of sprawl throughout the passage, “the destruction of traditional downtowns” is not something that the author would like to see happen.

H because the author explains that “affordable’ housing on the edge of town” (line 53) is only more affordable for developers (line 55), and that the construction of this housing, which is a familiar form of sprawl (lines 48–50), requires “higher taxes for needless duplication of services and infrastructure” (lines 59–60). In the context of the sentence in which it appears and in the context of the author’s criticism of sprawl throughout the passage, construction of this housing is not something that the author would like to see happen.
Question 13. The best answer is D because in the first paragraph the author defines sprawl as a problem, and in the last paragraph, the author offers possible solutions to this problem, including “sensible land-use planning” (line 82), “mixed-use zoning” (lines 85–86), and “an integrated system of planning decisions and regulations” (lines 87–88).

The best answer is NOT:

A because the author does not ask a question at any point in the final paragraph. Rather, the author offers solutions to the problem explained throughout the passage.

B because the author mentions no specific statistics in the final paragraph.

C because the final paragraph does not incorporate more emotional language than the first. If anything, the opposite may be true. In the first paragraph, the author uses emotionally loaded language to encourage the reader to agree that the “destructive, soulless, ugly mess called sprawl” (lines 9–10) is a serious problem. By contrast, the last paragraph, while arguing that “our communities should be shaped by choice, not by chance” (lines 80–81), uses more precise and less emotional language to describe possible solutions to the problem of sprawl, such as “an integrated system of planning decisions and regulations” (lines 87–88). This less emotional language encourages the reader to agree that these solutions may be effective.

Question 14. The best answer is F because the passage makes no mention of how long the problem of sprawl has been happening in US cities.

The best answer is NOT:

G because the author answers this question in lines 17–18: “Development that destroys communities isn’t progress. It’s chaos.”

H because the author argues that current zoning laws, which make construction of a “walkable environment” impossible, “are a major reason why 82 percent of all trips taken in the United States are taken by car” (lines 69–74).

J because the author offers solutions to the problem of what to do to combat sprawl in the final paragraph in the passage.
Question 15. The best answer is B because the passage does not support the idea that the opening of a superstore leads to downtown renovations. Rather, the passage states that, after a superstore opens in a small town, “downtown becomes a ghost town” (lines 46–47).

The best answer is NOT:

A because the author states that “in many small towns, a single new superstore may have more retail space than the entire downtown business district” (lines 42–44).

C because the author states that, after a superstore opens in a small town, “downtown becomes a ghost town” (lines 46–47).

D because the author states that, when a superstore opens in a small town, “the retail center of gravity shifts away from Main Street” (lines 45–46).

Question 16. The best answer is H because the statistics in question (lines 73–76) show that a significant majority of all trips taken in the United States are taken by car, and that American families spend a significant portion of their budget on transportation expenses. The author argues that these statistics regarding automobile transportation and its costs represent the effects of land-use regulations that make it impossible to construct a “compact walkable environment” (lines 69–71).

The best answer is NOT:

F because the statistics in question (lines 73–76) do not support the idea that mixed-use zoning leads to environmental destruction. Rather, they show that a significant majority of all trips taken in the United States are taken by car, and that American families spend a significant portion of their budget on transportation. According to the author, the dependence on automobile transportation is a result of current zoning laws “prohibiting mixed uses” (line 67). Because this dependence on automobile transportation is associated with sprawl, which is associated with environmental destruction throughout the passage, the statistics in question support the argument that it is the prohibition of mixed-use zoning, rather than mixed-use zoning itself, that creates environmental destruction (line 67).

G because the statistics in question (lines 73–76) show that a significant majority of all trips taken in the United States are taken by car, and that American families spend a significant portion of their budget on transportation expenses. The author argues that these statistics regarding automobile transportation and its costs represent the effects of land-use regulations that make it impossible to construct a “compact walkable environment” (lines 69–71).

J because the statistics in question do not support the idea that Americans spend too much of their budgets on food and health care. Rather, the passage states that “the average American household now allocates more than 18 percent of its budget to transportation expenses” and that this is “more than it spends for food and three times more than it spends for health care” (lines 74–79). This strongly suggests that Americans spend too much on transportation, rather than suggesting that they spend too much on food and health care.
Question 17. The best answer is C because the passage refers to “retail development that transforms roads into strip malls” (lines 38–39).

The best answer is NOT:

A because the author discusses the type of sprawl that develops far away from town centers (line 30), not adjacent to them.

B because the author argues that the development of sprawl leads to the neglect of historic buildings in towns (lines 26–27), not that sprawl leads to the utilization of these buildings.

D because the author argues that the construction of superstores is part of a process whereby “the retail center of gravity shifts away from Main Street” and “downtown becomes a ghost town” (lines 45–47). This strongly suggests that superstores are associated with the destruction, rather than the promotion, of a sense of community in the towns in which they are constructed.

Question 18. The best answer is G because the sentence is describing how residential subdivisions are driven “by the American dream of a detached home in the middle of a grassy lawn” (lines 50–52). Since a grassy lawn surrounds the home being referred to, it is reasonable to assume there is space between the home and other structures. In other words, the home is “set apart.”

The best answer is NOT:

F because although the word detached can indicate an objective point of view, detached is used in this context to describe a house, which does not have a point of view.

H because the passage does not provide a clear sense of what “broken apart” would mean in the context of this sentence.

J because there is nothing in the passage to suggest that the home being referred to was “taken away” from another location.
Question 19. The best answer is D because the statement in question is preceded by, and is intended to counter, the claim made by some people that “sprawl is merely the natural product of marketplace forces at work” (lines 62–63). Therefore, the author is arguing that people who make this claim “fail to recognize” (line 63) that those market forces are influenced by governmental decisions. The author’s rhetoric here assumes that the reader will recognize “a level playing field” as a popular expression for conditions governed purely by market forces, and will understand that a playing field that “isn’t level” (line 64) refers to conditions in which governmental decisions do influence market forces.

The best answer is NOT:

A because the “needless duplication of services and infrastructure” (line 60) referred to in the passage is identified as a result of sprawl, whereas the phrase “the game isn’t being played on a level field” (line 64) is used to identify the influence of governmental decisions on market forces, and not market forces alone, as a cause of sprawl.

B because the “higher taxes” (line 59) referred to in the passage are identified as a result of sprawl, whereas the phrase “the game isn’t being played on a level field” (line 64) is used to identify the influence of governmental decisions on market forces, and not market forces alone, as a cause of sprawl.

C because the phrase “the game isn’t being played on a level field” (line 64) is used to identify the influence of governmental decisions on market forces, and not market forces alone, as a cause of sprawl. The author’s rhetoric here assumes that the reader will recognize “a level playing field” as a popular expression for conditions governed purely by market forces, and will understand that a playing field that “isn’t level” (line 64) refers to conditions in which governmental decisions do influence market forces.
Question 20. The best answer is J because the passage identifies zoning laws that prohibit “mixed uses” (line 67) as a primary cause of the separation of urban commercial zones and residential subdivisions described in the three paragraphs that immediately precede the sentence in question (lines 48–66). That separation of commercial and residential land use is contrasted, in the following sentences, with “the sort of compact walkable environment that attracts us to older neighborhoods and historic communities all over the world” (lines 70–72). Therefore the phrase “mixed uses” can be understood as referring to zoning that allows one area to contain various types of development.

The best answer is NOT:

F because the passage identifies both large parking lots (lines 3–4) and large retail stores (lines 38–42) as being characteristic of sprawl, which is encouraged by the prohibition of “mixed uses” (line 67). Furthermore, parking lots and retail stores are both understood to be commercial uses of land, and therefore the phrase “mixed uses” is unlikely to refer to them.

G because although the passage states that the prohibition of “mixed uses” (line 67) makes it “impossible—even illegal—to create the sort of compact walkable environment that attracts us to older neighborhoods and historic communities” (lines 69–72), the phrase “mixed uses” itself is not directly associated with historic preservation in any way. Rather, “mixed uses” refers to the designation of land use as residential, commercial, or industrial under zoning laws.

H because although “mixed uses” (line 67) are understood within the context of the passage as encouraging the creation of a “walkable environment” (line 71), there is no association between the phrase “mixed uses” and the prohibition of driving or parking.
Passage III

**Question 21.** The best answer is A because the passage begins with the narrator’s description of an incident in which she first became interested in identifying flowers and in the natural world (lines 1–24), and the remainder of the passage describes how this early interest developed into a larger part of her life.

The best answer is NOT:

- B because although the identification of an aster is part of the incident (lines 1–24) that leads to the narrator’s lifelong interest in flowers and the natural world, there is no mention in the passage of the author having a lifelong fascination for asters in particular. Rather, the incident in question leads to a lifelong fascination with identifying flowers in general.

- C because although the author briefly mentions hiking with companions (lines 31–32) and identifying flowers with a friend (lines 81–82), the primary focus of the passage is on the author’s individual interest in flowers and how that interest developed.

- D because the author does not discuss her career in the passage.

**Question 22.** The best answer is H because the author describes the young man’s answer to her question as containing “the hint of a sniff” (line 7), which indicates that she detected disdain or condescension in the tone of the young man’s answer.

The best answer is NOT:

- F because there is nothing in the passage to suggest that the guide treated the author with acceptance. Rather, his reaction to her question about the flower is described as containing “the hint of a sniff” (line 7), which indicates disdain or condescension, qualities that are incompatible with acceptance.

- G because there is no mention in the passage of the guide being surprised by the author’s question. Rather, his reaction is described as containing “the hint of a sniff” (line 7), which indicates disdain or condescension and not surprise.

- J because there is no mention in the passage of the guide becoming angry with the author. Rather, his reaction to her question about the flower is described as containing “the hint of a sniff” (line 7), which indicates disdain or condescension and not anger.
Question 23. **The best answer is D** because although the author describes her efforts to identify a yellow flower on a particular hike (lines 30–51), she does not name the flower in question. Rather, she uses the description of this incident to explain her developing “intimacy” (line 28) with the book *A Field Guide to Wild Flowers*.

**The best answer is NOT:**

A because although the author mentions St. John's Wort, loosestrife, and puccoon as “five-petaled yellow flowers” (lines 50–51) similar to the one she is trying to identify, she does not identify the flower in question as St. John's Wort.

B because although the author mentions St. John's Wort, loosestrife, and puccoon as “five-petaled yellow flowers” (lines 50–51) similar to the one she is trying to identify, she does not identify the flower in question as loosestrife.

C because although the author mentions St. John's Wort, loosestrife, and puccoon as “five-petaled yellow flowers” (lines 50–51) similar to the one she is trying to identify, she does not identify the flower in question as puccoon.

Question 24. **The best answer is F** because the author states that though daunting at first, the book was neither too frustrating as a more basic book would have become nor too daunting as a more complex one would have been (lines 58–61).

**The best answer is NOT:**

G because the author indicates that the book was not easy to use in the beginning. Rather, it was difficult for her, but she “persisted in wrestling” (line 61) with the book until it became easier.

H because the author makes no mention in the passage of any other guide she used.

J because the author makes no negative statements about the illustrations in the guide.
**Question 25.** The best answer is C because the sentence in question reads “I had no choice, really, not if I wanted to get in” (lines 55–56), and the surrounding sentences indicate that the matter she had no choice in was the use of the field guide, which “led to the particulars” (line 57), or deepened her understanding, of the landscape. Therefore, in this context, to “get in” to a subject can be understood as meaning to fully understand that subject.

The best answer is NOT:

A because the sentence in question reads “I had no choice, really, not if I wanted to get in” (lines 55–56), and there is no indication in the surrounding lines that the matter she has no choice in is her arrival in a specific location. Rather, she wants to figuratively, and not literally, arrive at a deeper understanding of the landscape, and she has no choice but to use the field guide in order to do so (lines 55–58).

B because the sentence in question reads “I had no choice, really, not if I wanted to get in” (lines 55–56), and there is no indication in the surrounding lines or the passage as a whole that the matter she has no choice in has anything to do with membership in any group. Rather, she wants to figuratively, and not literally, “get in” to a deeper understanding of the landscape, and she has no choice but to use the field guide in order to do so (lines 55–58).

D because the sentence in question reads “I had no choice, really, not if I wanted to get in” (lines 55–56), and there is no indication in the surrounding lines or the passage as a whole that the matter she has no choice in has anything to do with being friendly with someone. Rather, she wants to figuratively, and not literally, “get in” to a deeper understanding of the landscape, and she has no choice but to use the field guide in order to do so (lines 55–58).

**Question 26.** The best answer is H because the author states that she and Julie began to see that their understanding of plant communities was valuable because it led to a greater understanding of larger issues such as “climate change and continental drift” (lines 85–86).

The best answer is NOT:

F because there is no information in the passage about Julie's level of experience in identifying plant life.

G because there is no information in the passage about Julie owning a house near a bog.

J because there is no information in the passage about whether or not Julie used the Peterson's guide.
Question 27. The best answer is D because the author states that “over the next several years this field guide would become my closest companion” (lines 25–26), specifying that she measures the period in question in “years.”

The best answer is NOT:

A because the author states that “over the next several years this field guide would become my closest companion” (lines 25–26), specifying “years” and not days as the way in which she measures the period in question.

B because the author states that “over the next several years this field guide would become my closest companion” (lines 25–26), specifying “years” and not weeks as the way in which she measures the period in question.

C because the author states that “over the next several years this field guide would become my closest companion” (lines 25–26), specifying “years” and not months as the way in which she measures the period in question.

Question 28. The best answer is J because the author’s statement that “a landscape may be handsome in the aggregate, but this book led to the particulars, and that’s what I wanted” (lines 56–58) contrasts the surface appeal of a landscape seen at a distance with the deeper knowledge of a landscape that only comes from familiarity with the “particulars,” or individual parts, and specifies that this deeper knowledge of the landscape is what she sought.

The best answer is NOT:

F because the author’s statement that “a landscape may be handsome in the aggregate, but this book led to the particulars, and that’s what I wanted” (lines 56–58) specifies that she was more interested in the deeper knowledge of the landscape that comes from familiarity with the “particulars,” or individual parts, than she was in an understanding of a landscape that might come from looking at its overall patterns.

G because although the passage does relate the way in which the field guide helps the author break landscapes down logically into their “particulars” (line 57), or individual parts, there is no indication that this made landscapes lose their appeal. Rather, she states that this kind of understanding was “what [she] wanted” (line 58) and that the logically ordered classifications in the field guide all made “such delightful sense” (lines 79–80).

H because there is no indication in the passage that the deeper understanding of landscapes that she sought through knowledge of their “particulars” (line 57), or individual parts, was in any way related to painting portraits of those landscapes.
Question 29. The best answer is B because the details in question describe the ways in which the field guide “changed” (line 64) as she figuratively, and not literally, “persisted in wrestling” (line 61) with it “by slow degrees” (line 62). In this context, these details indicate that this transformation occurred because of heavy use over a long period of time.

The best answer is NOT:

A because there is no indication that the transformation of the book described by the details in question (lines 64–66) takes place because of poor craftsmanship. Rather, the details in question describe the ways in which the field guide “changed” (line 64) as she, figuratively and not literally “persisted in wrestling” (line 61) with it “by slow degrees” (line 62). In this context, these details indicate that this transformation occurred because of heavy use over a long period of time.

C because the passage implies that the “cryptic annotations” (line 66) in the guide were made by the author herself.

D because the details in question describe the ways in which the field guide “changed” (line 64) as she, figuratively and not literally “persisted in wrestling” (line 61) with it “by slow degrees” (line 62). Although this indicates that the book’s condition was transformed because of heavy use, there is no specific indication of carelessness and no mention anywhere in the passage of any regret the author has regarding her use of the field guide.

Question 30. The best answer is H because the author mentions Solidago hispida in order to exemplify her practice of addressing flowers that she has encountered before by their Latin name after she has learned to identify them (lines 70–72).

The best answer is NOT:

F because the passage makes no mention of any trouble the author had initially identifying Solidago hispida.

G because the author mentions Solidago hispida as an example of a flower she has addressed in the past with great enthusiasm, meaning she has already come across the flower in her nature walks.

J because there is no indication anywhere in the passage that the author feels the name Solidago hispida is inappropriate. Rather, the author mentions Solidago hispida only in order to exemplify her practice of addressing flowers by their Latin name (lines 70–72).
Passage IV

**Question 31. The best answer is D** because the passage states that information gained from the study of snow crystals “has practical applications in such diverse areas as agriculture and the production of electricity” (lines 12–14). Specific details about these practical applications are presented in the final five paragraphs (lines 50–91) of the passage.

**The best answer is not:**

A because although the passage does mention the fact that scientists have communicated with each other during the course of studying snow crystals (lines 50–54), communication is secondary to the main point of the passage, which is to explain the practical applications of such a study.

B because although the passage does discuss the role of snow crystal facets in the formation of snow crystals (lines 19–23) and also discusses the winter snowpack in some Western states (lines 56–61), the passage makes no specific connection between the snow crystal facets and the snowpack and does not indicate that either one is the primary reason for presenting information about the scientific study of snow.

C because although the passage does tell the story of the first time a scanning electron microscope was used in the scientific study of snow (lines 34–49), it tells this story in the context of presenting information about the practical applications of the scientific study of snow and does not explicitly discuss the varied uses of the scanning electron microscope.

**Question 32. The best answer is G** because the passage states that “before employing the scanning electron microscopy results, the forecasted amounts of snowpack water were inaccurate” (lines 62–64) and that “improving the prediction [of snowpack water] by 1 percent would save $38 million” in costs (lines 71–72). Improving a prediction can be understood as making that prediction more accurate, which establishes a connection between the use of the scanning electron microscope and saving money.

**The best answer is not:**

F because although the passage mentions future predictions in the context of less snowfall expected (lines 75–80), those future predictions are not linked to any money saved.

H because as the passage states, the two scientists (who were looking at biological problems) froze the tissue they were using in order “to avoid the laborious procedure” (lines 37–38) that the use of scanning electron microscopes usually entailed. The passage does not state that the scientists were saving money by using these microscopes when looking for these biological problems.

J because although the passage states that snowmelt accounts for 75 percent of the annual water supply of these western states (lines 56–58), the passage mentions nothing about increasing the water supply of these states as a means of saving money.
Question 33. The best answer is C because the phrase in question is immediately followed by a statement in parentheses explaining that “crystals often change once on the ground depending on the surrounding environment” (lines 48–49). Because metamorphosed means “changed,” and conditions and environment have similar meanings, we can read the parenthetical statement as clarifying the fact that “metamorphosed conditions” refers to the state of snow crystals after they reach the ground.

The best answer is NOT:

A because the passage does not establish a direct connection between the phrase “metamorphosed conditions” (lines 47–48) and the temperature and humidity at which crystals form. Rather, the phrase in question is immediately followed by a statement in parentheses explaining that “crystals often change once on the ground depending on the surrounding environment” (lines 48–49). Read in context, the parenthetical statement, which makes no mention of the temperature and humidity at which crystals form, can be understood as defining the phrase “metamorphosed conditions.”

B because the passage does not establish a direct connection between the phrase “metamorphosed conditions” (lines 47–48) and the process by which snow crystals develop from a speck of dust and water vapor. Rather, the phrase in question is immediately followed by a statement in parentheses explaining that “crystals often change once on the ground depending on the surrounding environment” (lines 48–49). Read in context, the parenthetical statement, which makes no mention of the formation of snow crystals, can be understood as defining the term “metamorphosed conditions.”

D because the phrase in question (lines 47–48) is immediately followed by a statement in parentheses explaining that “crystals often change once on the ground depending on the surrounding environment” (lines 48–49). This clarification indicates that the phrase “metamorphosed conditions” refers to changes in the snowflake that occur as a result of changes in the environment and not directly to changes in the environment.
Question 34. The best answer is G because the passage explains that “before employing the scanning electron microscopy results, the forecasted amounts of snowpack water were inaccurate whenever the size and shape of the snow crystals varied much from the norm” (lines 62–65). This indicates that the addition of scanning electron microscopy data allowed scientists using the model to include more detailed information about structural variations in snow crystals in their predictions, making those predictions more accurate.

The best answer is NOT:

F because the passage does not specify that the addition of scanning microscopy data allowed scientists using the Snowmelt Runoff Model to include more detailed information about microwave satellite data. Rather, the passage states that Albert Rango “now uses Wergin’s electron microscopy data, along with microwave satellite data, in the Snowmelt Runoff Model to predict the amount of water available in a winter snowpack” (lines 52–56). This indicates that scanning electron microscopy data and microwave satellite data are used in conjunction with each other, not that one allows the inclusion of more detailed information about the other.

H because the passage makes no mention of electron microscopy in helping provide detailed information about locations having the highest amount of snowfall.

J because although the passage mentions that William Wergin and Eric Erbe were looking for biological problems related to agriculture (lines 34–37), there is no mention of biological problems in the discussion of the Snowmelt Runoff Model, which occupies the last five paragraphs of the passage (lines 50–91).

Question 35. The best answer is D because the passage states that, because of temperature increases, less snow will fall, thus “greatly increasing water’s economic value” (lines 77–82).

The best answer is NOT:

A because although the passage mentions an increased ability to track water pollution via the use of crystal research (lines 90–91), the passage makes no mention of an increase of pollution as a cause of an increase in water’s value.

B because the passage makes no mention of water conservation leading to an increase in water’s value.

C because although the passage mentions the ability of scanning electron microscopes to detect sulfur and nitrogen in snow (lines 87–89), the passage makes no mention of a predicted increase in sulfur and nitrogen levels in snow.
Question 36. The best answer is G because the passage states that “as the crystals fall, they encounter different atmospheric conditions that produce flakes with unique attributes” (lines 3–5).

The best answer is NOT:

F because although the passage does state that 1 septillion snowflakes fall worldwide each year (lines 1–3), the passage does not make any connection between that enormous number and the infinite variety of snowflakes. Rather, the passage states that “as the crystals fall, they encounter different atmospheric conditions that produce flakes with unique attributes” (lines 3–5).

H because the passage makes no connection between the rate at which snowflakes fall and the infinite variety of snowflakes. Rather, the passage states that “as the crystals fall, they encounter different atmospheric conditions that produce flakes with unique attributes” (lines 3–5).

J because although the passage does state that more complex atmospheric conditions produce more elaborate and therefore more varied snow crystals (lines 5–6), the passage makes no connection between those complex atmospheric conditions and the speed at which snow crystals develop, and the passage makes no connection between the speed at which snow crystals develop and the infinite variety of snowflakes.

Question 37. The best answer is D because the passage states that “snowflakes are collections of two or more snow crystals” (lines 16–17).

The best answer is NOT:

A because the passage does not state that snowflakes grow around a nucleus of dust. Rather, the passage states that “snowflakes are collections of two or more snow crystals” (lines 16–17) and that a crystal “typically grows around a nucleus of dust” (lines 18–19).

B because the snowflakes do not combine to form snow crystals. Rather, according to the passage, the opposite is true: snow crystals combine to form snowflakes (lines 16–17).

C because although the passage states that the shape of a snow crystal “depends on how the six side facets—or faces—grow in relation to the top and bottom facets” (lines 19–20), there is no mention of any direct relation between top and bottom facets and the growth of snowflakes.
Question 38. The best answer is G because the passage specifies that the physicist Kenneth Libbrecht “creates ‘designer’ snowflakes in his lab” (lines 31–32).

The best answer is NOT:

F because the passage makes no connection between the term “‘designer’ snowflakes” (line 32) and the fact that no two snowflakes are alike. Rather, the passage specifies that the physicist Kenneth Libbrecht “creates ‘designer’ snowflakes in his lab” (lines 31–32).

H because the passage makes no mention of the grand design of nature. Rather, the passage specifies that the physicist Kenneth Libbrecht “creates ‘designer’ snowflakes in his lab” (lines 31–32).

J because although the passage does state that the physicist Kenneth Libbrecht “creates ‘designer’ snowflakes in his lab” (lines 31–32), the passage makes no mention of the beauty of Libbrecht's snowflakes.

Question 39. The best answer is C because the sentence in question states that “snowmelt water is critical to crop irrigation and hydroelectric power, as well as recreation and domestic water supplies, fisheries management and flood control” (lines 58–61). In context, this is understood to mean that snowmelt water is vital, or very important, to these processes and practices.

The best answer is NOT:

A because the sentence in question states that “snowmelt water is critical to crop irrigation and hydroelectric power, as well as recreation and domestic water supplies, fisheries management and flood control” (lines 58–61). In this context critical cannot be read as meaning “evaluative” because snowmelt water cannot evaluate anything or anyone.

B because the sentence in question states that “snowmelt water is critical to crop irrigation and hydroelectric power, as well as recreation and domestic water supplies, fisheries management and flood control” (lines 58–61). In this context critical cannot be read as meaning “faultfinding” because snowmelt water cannot find fault with anything or anyone.

D because the sentence in question states that “snowmelt water is critical to crop irrigation and hydroelectric power, as well as recreation and domestic water supplies, fisheries management and flood control” (lines 58–61). In context, the adjective critical is understood to mean that snowmelt water is vital, or very important, to these processes and practices. Although it is also an adjective and can sometimes be understood to mean vital or important, acute cannot be substituted for critical in this sentence because it would be neither grammatical nor logical to say “water is acute to crop irrigation.”
Question 40. The best answer is F because although the passage does state that research about snow crystals has helped scientists to identify and possibly track the source of pollutants in snow (lines 90–91), the passage does not make any connection between research about snow crystals and the extraction of pollutants from snow.

The best answer is NOT:

G because one meaning of gauge is “to measure,” and the term snowmelt refers to water generated by a melting snowpack; therefore, when the passage states that research about snow crystals has helped scientists to “predict the amount of water available in a winter snowpack” (lines 55–56), that statement means that research about snow crystals has helped scientists to gauge (measure) the probable amount of snowmelt. Lines 84–85 specifically state that “the crystal research help[s] gauge snowmelt.”

H because the passage states that, in the process of conducting research about snow crystals, physicist Kenneth Libbrecht “creates ‘designer’ snowflakes in his lab” (lines 31–32).

J because the passage states that research about snow crystals “is also useful in predicting avalanches” (line 85).
Passage I

1. **The best answer is B.** According to Figure 1, the only site with *E. coli* levels above 400 colonies per 100 mL was Day 30 at Site 1. **A** is incorrect; the *E. coli* level on Day 1 at Site 1 was 101 colonies formed per 100 mL. **B** is correct; the *E. coli* level on Day 30 at Site 1 was 708 colonies formed per 100 mL. **C** is incorrect; the *E. coli* level on Day 1 at Site 2 was 16 colonies formed per 100 mL. **D** is incorrect; the *E. coli* level on Day 30 at Site 2 was 173 colonies formed per 100 mL.

2. **The best answer is F.** According to Figure 1, the *E. coli* levels were much higher at Site 1 than Site 2 on 3 of the five days measured and nearly the same on the other two days measured, indicating that the average *E. coli* levels were higher at Site 1 than at Site 2 over the collection period. According to Figure 2, the water flow was greater for Site 1 than Site 2 on all five days that measurements were taken, indicating that the average water flow was higher for Site 1 than Site 2 over the collection period. **F** is correct; both the water flow and *E. coli* levels were greater for Site 1 than Site 2. **G, H, and J** are incorrect.

3. **The best answer is A.** According to Table 1, the better the water quality rating, the greater the value for BI. Therefore, **A** is correct. **B, C, and D** are incorrect; biotic index is neither independent of water quality nor does it increase as water quality degrades.

4. **The best answer is G.** According to Table 2, the average BI for Site 1 was 6.3, indicating that the water quality rating for Site 1 was excellent. The average BI for Site 2 was 2.5, indicating that the water quality rating for Site 2 was fair. One would expect more stone fly larvae at the site with the higher water quality, which is Site 1. The results are consistent with the students’ hypothesis. **F** is incorrect; Site 1 had a water quality rating of excellent, and Site 2 had a water quality rating of fair. **G** is correct. **H and J** are incorrect; Site 1 had a better water quality rating.

5. **The best answer is A.** According to the passage, *E. coli* levels above 100 colonies formed per 100 mL indicate reduced water quality. According to Figure 1, on Days 1 and 30, Site 1 had *E. coli* levels above 100 colonies formed per 100 mL. **A** is correct; Figure 1 contains the information about *E. coli* levels. **B** is incorrect; Figure 2 contains information about water flow, and no relationship is given between water flow and water quality. **C** is incorrect; Table 1 shows how water quality rating varies with BI. Table 1 contains no information about Sites 1 or 2. **D** is incorrect; according to Table 2, Site 1 has a higher water quality rating than does Site 2.
6. **The best answer is J.** In order to answer this item, the examinee must know that the introduction of large amounts of fertilizer may cause eutrophication, leading to reduction in water quality. A higher BI corresponds to a higher water quality rating. A reduction in water quality after the introduction of the fertilizer would therefore cause a decrease in the BI. F and G are incorrect; the BI will decrease, not increase. H is incorrect; the water quality will decrease. J is correct.

**Passage II**

7. **The best answer is B.** According to Table 1, AWP 2 produced 21 mL of H\textsubscript{2} by Day 2, 187 mL by Day 4, 461 mL by Day 6, and 760 mL by Day 8. A is incorrect; this figure shows the production of more than 200 mL of H\textsubscript{2} by Day 4. B is correct. C and D are incorrect; both show a decrease in the volume of H\textsubscript{2} over time.

8. **The best answer is G.** According to Table 1, AWP 1 produced 4 mL of H\textsubscript{2} in the first 2 days, 29 mL of H\textsubscript{2} in the next 2 days, 48 mL of H\textsubscript{2} in the next 2 days, and 52 mL of H\textsubscript{2} in the last 2 days. If the volume had been measured on Day 10, it is likely that the additional amount of H\textsubscript{2} produced would have been no more than 50–60 mL. This would have resulted in a total volume of no more than 200 mL H\textsubscript{2} produced. F is incorrect; 133 mL of H\textsubscript{2} had been produced by Day 8. G is correct. H and J are incorrect; a total volume of H\textsubscript{2} greater than 461 mL would require the formation of 328 mL from Day 8 to Day 10, which is very unlikely based on the rate of H\textsubscript{2} formation seen in Days 2–8.

9. **The best answer is A.** According to Table 1, 133 mL of H\textsubscript{2} was produced by AWP 1 on Day 8, and 81 mL of H\textsubscript{2} was produced by AWP 1 on Day 6. The amount produced between those measurements was 133 – 81 = 52 mL. A is correct. B, C, and D are incorrect; 52 mL of H\textsubscript{2} was produced.

10. **The best answer is H.** In order to answer this item, the examinee must have a basic understanding of chemical equations. H\textsubscript{2} is one of the reaction products and is formed at half the rate that Al(OH)\textsubscript{3} is formed. Measuring the volume of H\textsubscript{2} that forms would therefore give information about the rate of formation of Al(OH)\textsubscript{3}. F and G are incorrect; H\textsubscript{2}O and Al are both reactants and are not converted into one another. H is correct; Al is converted to Al(OH)\textsubscript{3}. J is incorrect; Al is converted to Al(OH)\textsubscript{3}.

11. **The best answer is D.** In order to answer this item, the examinee must understand that a base will increase the pH of water (and realize that the passage states that AWPs are water-based). The passage states that DMEA is an AWP ingredient that increases pH. Therefore, DMEA is a base. A, B, and C are incorrect; DMEA is a base because it increases pH. D is correct.
Taking Additional Practice Tests

The ONLY Official Prep Guide from the Makers of the ACT

SCIENCE • PRACTICE TEST 3 • EXPLANATORY ANSWERS

12. The best answer is J. According to Table 1, on Day 2 the AWP 3 sample had produced 121 mL of H₂. According to Figure 1, the sample containing EDTA produced 121 mL of H₂ on approximately Day 10. F and G are incorrect; the volume of H₂ was not greater than 100 mL until Day 7. H is incorrect; only 100 mL of H₂ had been produced on Day 7. J is correct; on Day 10 approximately 121 mL of H₂ had been produced.

Passage III

13. The best answer is B. Figure 4 shows that for Trial 5 both scales had equal readings, indicating that the weight was equally distributed. A is incorrect; in Trial 4, Scale B had a higher reading than did Scale A. B is correct; in Trial 5, both scales had equal readings. C is incorrect; in Trial 6, Scale A had a higher reading than did Scale B. D is incorrect; the weight was equally distributed in Trial 5.

14. The best answer is G. Figure 2 (Trial 1) shows that Scale A caused the hand on Scale B to move ¼ of the way around the dial. Figure 2 (Trial 2) shows that a 5.0 N weight causes the hand on Scale A to move ¼ of the way around the dial. Scale B has a weight of 5.0 N. F, H, and J are incorrect; the scales have a weight of 5.0 N. G is correct.

15. The best answer is C. In order to answer this item, the examinee must know that as a spring is compressed, the potential energy stored in the spring increases. The stored potential energy would therefore be greatest when the spring is compressed the most, and the spring would be compressed the most when the heaviest weight is placed on the scale. In Trial 1, there is no weight on Scale A; thus the spring would not be compressed at all. In Trial 3, there is a 10.0 N weight on Scale A, and the spring would be compressed. A and B are incorrect; the potential energy stored in the spring of Scale A would be greater in Trial 3. C is correct. D is incorrect; the amount of weight was greater in Trial 3.

16. The best answer is F. According to Figure 2, the weight of Scale A is 5.0 N (the hand on the scale moves ¼ of the way around the dial). Scale B should read 5.0 N whether Scale A is right side up or upside down. When Scale A is upside down, the spring in Scale A is also compressed by the weight of Scale A; therefore, Scale A should also read 5.0 N. F is correct; both scales read 5.0 N with the hands ¼ of the way around the dials. G is incorrect; Scale B reads 10.0 N with the hand ½ of the way around the dial. H is incorrect; Scale A reads 10.0 N with the hand ½ of the way around the dial. J is incorrect; both scales read 10.0 N.
17. **The best answer is A.** The description of Study 2 states that the distance between Scale B and the 10.0 N weight was measured from the pencil to the weight. Therefore, the pencils were most likely intended to be used as a convenient visual reference from which to measure distance, so A is correct. B is incorrect; any side-to-side motion of the board would have been contrary to the design of Study 2. C is incorrect; the students intentionally zeroed out the weights of the pencils and the board. D is incorrect; air pressure would have been equal above and below each platform regardless of whether the pencils had been included or not.

18. **The best answer is H.** According to Figure 4, when the distance between the weight and the pencil on Scale B was 0.10 m, Scale B read approximately 7.5 N. When the distance between the weight and the pencil was 0.20 m, Scale B read 5.0 N, and when the distance was 0.30 m, Scale B read 2.5 N. As the distance increased, the amount of force exerted on Scale B decreased. F, G, and J are incorrect. H is correct.

19. **The best answer is D.** In Trials 4–6, pencils were placed on each scale and a board was placed on top. In order to measure only the amount of force exerted by the weight and not the force exerted by the pencils and the board, the scales were zeroed. A is incorrect; setting the dial readings to zero would not add in the weights of the scales. B is incorrect; the weights of the board and pencils were subtracted, not added. C is incorrect; setting the dial readings to zero would not subtract the weights of the scales. D is correct; the students were interested only in the force exerted by the weight and not the pencils and board.

**Passage IV**

20. **The best answer is G.** According to the passage, the EOR is the minimum octane number of a fuel required for an engine to operate without becoming damaged. According to Table 2, as engine speed increases the EOR decreases. F, H, and J are incorrect. G is correct.

21. **The best answer is B.** According to Table 2, as the engine speed increases, the octane numbers for each fuel decrease. At an engine speed of 2,000 rpm, the octane number for Fuel A was 96.6, and the octane number for Fuel B was 96.1. At an engine speed of 2,500 rpm, the octane number for Fuel A was 95.0, and the octane number for Fuel B was 95.4. At an engine speed of 2,200 rpm the octane number for Fuel A should be between 95.0 and 96.6, and the octane number for Fuel B should be between 95.4 and 96.1. A is incorrect; the octane numbers for both fuels should be higher. B is correct. C and D are incorrect; the octane numbers for both fuels should be lower.
22. **The best answer is H.** According to Table 1, the octane number is equal to the percent isooctane in the mixture. The percent isooctane for a given mixture is:

\[
\text{percent isooctane} = \left( \frac{\text{volume of isooctane}}{\text{volume of isooctane} + \text{volume of heptane}} \right) \times 100
\]

F is incorrect; taking the first entry in the table as an example, \(100 \div 0 \neq 0\). G is incorrect; taking the first entry in the table as an example, \(0 \div 100 \neq 100\). H is correct; taking the first entry in the table as an example, \((100 \div 100) \times 100 = 100\). J is incorrect; taking the first entry in the table as an example, \((0 \div 100) \times 100 \neq 100\).

23. **The best answer is C.** Based on the information in Table 1, a mixture containing 100 mL of heptane and 900 mL of isooctane would have an octane number of 90. According to the results of Experiment 2, adding 4 mL of TEL to 1,000 mL of isooctane increased the octane number from 100 to 125. One would predict that adding 3 mL of TEL to the heptane/isoctane mixture would increase the octane number to some value greater than 90 but less than 125. A and B are incorrect; the octane number would be increased to a value greater than 90. C is correct. D is incorrect; upon addition of the TEL, the octane number of pure isooctane was increased to 125; the octane number of the mixture containing 90% isooctane would not be greater than 125.

24. **The best answer is G.** According to the passage, the minimum octane number of a fuel required for an engine to run without being damaged is the EOR. The best fuel would be that which has an octane number greater than the EOR at all engine speeds between 1,500 rpm and 3,500 rpm. Fuel A has an octane number greater than the EOR at all engine speeds. The octane number for Fuel B at 1,500 rpm is 96.7, and the EOR is 97.4. Fuel A would be the best choice. A is incorrect; the octane number for Fuel A is higher than the EOR at each engine speed tested. G is correct. H and J are incorrect; the octane number for Fuel B at 1,500 rpm is lower than the EOR.

25. **The best answer is D.** In order to answer this item, the examinee should understand solution properties. According to Table 1, the octane number decreases as the percentage of isooctane in the mixture decreases. A solution containing 80% isooctane should have an octane number between those of a solution containing 90% isooctane (90) and 75% isooctane (75). A, B, and C are incorrect; the octane number should be between 75 and 90. D is correct; a solution that is 80% isooctane would have an octane number of 80.
26. The best answer is F. The results of Experiment 2 indicate that adding 1 mL of TEL to 1,000 mL of isooctane increased the octane number from 100 to 115. It is reasonable to predict that if 1 mL of TEL were added to 1,000 mL of heptane, the octane number would likewise increase. However, because Table 1 indicates that pure heptane has an octane number of zero, the addition of such a small volume of TEL is unlikely to increase the octane number to 115 or greater. Therefore, it is most reasonable to predict that a mixture of 1 mL of TEL and 1,000 mL of heptane would have an octane number that is higher than that of pure heptane but lower than 115. F is correct. G, H, and J are incorrect; it is unlikely that adding 1 mL of TEL to 1,000 mL of heptane would result in the octane number either decreasing to less than that of pure heptane or increasing to greater than 115.

Passage V

27. The best answer is C. Scientist B argues that short-period comets were once long-period comets. A is incorrect; Scientist B claims that long-period comets do become short-period comets. B is incorrect; Scientist B does not discuss whether or not short-period comets can become long-period comets. C is correct. D is incorrect; Scientist B agrees that both long-period and short-period comets orbit the Sun.

28. The best answer is H. Scientist A states that the KB is 30 AU to 50 AU from the Sun and has a small inclination with respect to the ecliptic plane. Scientists should search this region of space for objects in the KB. F is incorrect; this region would be too far away to find objects in the KB. G is incorrect; the region at smaller angles with respect to the ecliptic plane should be searched. H is correct. J is incorrect; Scientist A does not suggest that the region surrounding Jupiter would be part of the KB.

29. The best answer is D. According to the introduction, the orbital planes of short-period comets have inclinations of 30° or less with respect to the ecliptic plane. A, B, and C are incorrect; one would expect short-period comets to have orbital planes with inclinations of 30° or less with respect to the ecliptic plane. D is correct; one would not expect the orbital plane of a short-period comet to be as large as 45° with respect to the ecliptic plane.

30. The best answer is J. In order to answer this item, the examinee should know that Saturn is one of the “giant planets” of our solar system. Scientist B states that the orbits of long-period comets are affected by the gravitational fields of the giant planets. F, G, and H are incorrect; these are smaller planets and may not be large enough to affect the orbits of the long-period comets. J is correct; Saturn is a giant planet.
### 31. The best answer is A.

According to the introduction, short-period comets have orbital periods of 200 years or less. Scientist B claims that short-period comets were once long-period comets. The introduction states that long-period comets originate in the Oort cloud. Scientist B would most likely agree that Comet Halley is a short-period comet that originated in the Oort cloud. A is correct. B is incorrect; Scientist B claims that the KB does not exist. C is incorrect; because the orbital period of Comet Halley is less than 200 years, it is a short-period comet. D is incorrect; Comet Halley is a short-period comet, and Scientist B claims that the KB does not exist.

### 32. The best answer is J.

Scientist A states that the icy bodies in the KB with diameters between 10 km and 30 km are too small to be seen with telescopes on Earth's surface. The much larger icy bodies must have diameters greater than 30 km. F, G, and H are incorrect; the diameters should be greater than 30 km. J is correct.

### 33. The best answer is D.

The two scientists do not dispute the presence of the Oort cloud around our solar system. The absence of a spherical shell similar to the Oort cloud near a similar star would not affect either viewpoint. A, B, and C are incorrect. D is correct.

### Passage VI

34. The best answer is J. The plant in question has a height of only 21 cm, and it produced no fruit. According to the results of the experiment, these properties are most consistent with the data shown for the L4 plants that were grown in a nutrient solution containing 120 g of NaCl. The L2 and L4 plants grown in nutrient solutions containing 60 g of NaCl had both greater average plant heights and non-zero average fruit masses. Likewise, for the L2 plants grown in a nutrient solution containing 120 g of NaCl. Therefore, F, G, and H are incorrect. J is correct.

35. The best answer is C. In order to answer this item, the examinee must know that the cell membrane separates the cell’s cytoplasm from the environment. According to the passage, the H₂O moved between the cytoplasm of the plants’ cells and the environment. If the H₂O was passing from the cell to the environment, then it passed through the cell membrane. A, B, and D are incorrect; in order for water to pass between the cytoplasm into the environment, it must pass through the cell membrane. C is correct.

36. The best answer is G. In order to answer this item, the examinee must know that NaCl is a salt. According to Tables 1, 2, and 3, as the amount of NaCl added to the nutrient solution increased, the plant mass decreased. F is incorrect; the mass did not increase. G is correct. H and J are incorrect; the plant mass decreased only.
37. **The best answer is A.** The researchers controlled which lines received the *AtNHX1* gene. **A** is correct. **B** is incorrect; only tomato plants were used, so this was not a variable. **C** is incorrect; the plant mass was a dependent variable. **D** is incorrect; the plant height was a dependent variable.

38. **The best answer is J.** In order to answer this item, the examinee must understand the concept of an allele and the relationship between homozygosity and genotype. The passage indicates that two identical alleles of the *AtNHX1* gene were incorporated into L1’s genome. An organism that has two identical alleles for a given gene is homozygous for that gene. Therefore, **F**, **G**, and **H** are incorrect. **J** is correct.

39. **The best answer is D.** According to the information in Tables 1, 2, and 3, as the height decreased, the mass decreased. A plot of this data would result in a line with a positive slope. **A** and **B** are incorrect; the line would have a slope because the mass changed as the height changed. **C** is incorrect; the line would have a positive slope because the mass increased as the height increased. **D** is correct.

40. **The best answer is J.** L1, L2, and L3 all had *AtNHX1* introduced. L4 did not have *AtNHX2* introduced; L4 was the control. **F**, **G**, and **H** are incorrect; L1, L2, and L3 all contained different genotypes for *AtNHX1*. **J** is correct; L4 was not altered.
Chapter 11: Scoring the Additional Practice Tests

After taking the ACT practice test 2 or the ACT practice test 3, you are ready to score the test to see how you did. In this chapter, you learn how to determine your raw score, convert raw scores to scale scores, compute your Composite score, determine your estimated percentile ranks for each of your scale scores, and score your practice writing test essay. Assuming you already scored practice test 1 (see chapter 3), you should be familiar with the scoring procedures.

When scoring each practice test and reviewing your scores, remember that your scores on the practice tests are only estimates of the scores that you will obtain on the ACT. If your score isn’t as high as you expected, the cause could be related to any number of factors. Maybe you need to review important content and skills. Maybe you should work a little faster, or more slowly and carefully, when taking the test. Perhaps you simply weren’t doing your best work on the test. Or maybe you need to take more challenging courses to be better prepared. Keep in mind that a test score is just one indicator of your level of academic knowledge and skills. You know your own strengths and weaknesses better than anyone else, so keep them in mind as you evaluate your performance.
Scoring Your Practice Tests

For the multiple-choice tests (English, mathematics, reading, and science), the number of questions you answer correctly is called a raw score. To figure out your raw scores for the practice tests in this book count the number of correct answers for each test using the scoring keys provided in the following sections. Then you can convert your raw scores into scale scores. Scale scores are the scores that ACT reports to students, high schools, colleges, and scholarship agencies. A scale score is a raw score that is converted to a scale score to enhance score interpretation and allow comparability across different forms. After you’ve converted your raw scores for the practice tests to scale scores, you’ll want to convert your scale scores to percentile ranks. Percentile ranks, which are explained in the following pages, are useful for interpreting your scores relative to the scores of others who have taken the ACT.

If you took the optional practice writing test, use the scoring rubric in chapter 3 to evaluate your essay and estimate your writing test score. Being objective about one’s own work is difficult, and you have not had the extensive training provided to actual readers of the ACT writing test. However, it is to your advantage to read your own writing critically. Becoming your own editor helps you grow as a writer and as a reader, so it makes sense for you to evaluate your own practice essay. That having been said, it may also be helpful for you to give your practice essay to another reader to get another perspective: perhaps that of a classmate, a parent, or an English teacher, for example. To rate your essay, you and your reader should be familiar with the scoring rubric in chapter 3 and the sample essays and scoring explanations in chapter 9, and then assign your practice essay a score of 1 (low) through 6 (high) in each of the four writing domains (ideas and analysis, development and support, organization, and language use).

Your writing test should be based on two ratings, so you may either multiply your own rating times two, or sum your rating and another reader’s rating to calculate your domain scores (2–12 for each domain). Your raw score is the sum of your domain scores and will be in a range of 8 to 48.

Finally, convert your writing test raw score to a scale score and to percentile ranks using the procedures described. Percentile ranks enable you to compare your writing test score to those of others who have taken the writing test.

You can find the most current information on scoring the ACT writing test in the bonus online content.
Scoring Practice Test 2

Scoring the Multiple-Choice Tests

To score each of your multiple-choice practice tests, starting with the English test, follow these six steps:

**STEP 1.** Write a “1” in the blank for each question that you answered correctly. An example is provided in the following box:

<table>
<thead>
<tr>
<th>Key</th>
<th>Your answer was</th>
</tr>
</thead>
<tbody>
<tr>
<td>1.</td>
<td>A</td>
</tr>
<tr>
<td>2.</td>
<td>J</td>
</tr>
<tr>
<td>3.</td>
<td>B</td>
</tr>
<tr>
<td>4.</td>
<td>G</td>
</tr>
</tbody>
</table>

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**English Scoring Key**

<table>
<thead>
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<th>Key</th>
<th>Key</th>
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<tbody>
<tr>
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<td>27.</td>
</tr>
<tr>
<td>7.</td>
<td>A</td>
<td>32.</td>
</tr>
<tr>
<td>9.</td>
<td>A</td>
<td>34.</td>
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<tr>
<td>10.</td>
<td>J</td>
<td>35.</td>
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<td>11.</td>
<td>C</td>
<td>36.</td>
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<td>15.</td>
<td>C</td>
<td>40.</td>
</tr>
<tr>
<td>17.</td>
<td>D</td>
<td>42.</td>
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<tr>
<td>18.</td>
<td>G</td>
<td>43.</td>
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<tr>
<td>19.</td>
<td>A</td>
<td>44.</td>
</tr>
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<td>20.</td>
<td>G</td>
<td>45.</td>
</tr>
<tr>
<td>22.</td>
<td>G</td>
<td>47.</td>
</tr>
<tr>
<td>24.</td>
<td>F</td>
<td>49.</td>
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</tbody>
</table>
STEP 2. Add the numbers you entered in Step 1 and write this total in the following shaded box. This is your raw score.

| Number Correct (Raw Score) for: |
| English test (75 questions) |

STEP 3. Repeat Steps 1 and 2 for the ACT mathematics, reading, and science tests using the scoring keys on the following pages.

**Mathematics Scoring Key Practice Test 2**

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<td>32. G</td>
<td>52. F</td>
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<td>35. B</td>
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</tr>
<tr>
<td>20. G</td>
<td>40. G</td>
<td>60. F</td>
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</table>

| Number Correct (Raw Score) for: |
| Mathematics test (60 questions) |
## Reading Scoring Key | Practice Test 2

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Number Correct (Raw Score) for:

**Reading test (40 questions)**

---

## Science Scoring Key | Practice Test 2

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<tbody>
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</table>

Number Correct (Raw Score) for:

**Science test (40 questions)**
**STEP 4.** On each of the four tests, the total number of correct responses yields a raw score. Use the conversion table on the following page to convert your raw scores to scale scores. For each of the four tests, locate and circle your raw score or the range of raw scores that includes it in the conversion table. Then, read across to either outside column of the table and circle the scale score that corresponds to that raw score. As you determine your scale scores, enter them in the blanks provided below. The highest possible scale score for each test is 36. The lowest possible scale score for any of the four tests is 1.

<table>
<thead>
<tr>
<th>Your Scale Scores</th>
</tr>
</thead>
<tbody>
<tr>
<td>English</td>
</tr>
<tr>
<td>Mathematics</td>
</tr>
<tr>
<td>Reading</td>
</tr>
<tr>
<td>Science</td>
</tr>
<tr>
<td>Sum of Scores</td>
</tr>
<tr>
<td>Composite Score (sum ÷ 4)</td>
</tr>
</tbody>
</table>

**STEP 5.** Compute your Composite score by averaging the four scale scores. To do this, add your four scale scores and divide the sum by 4. If the resulting number ends in a fraction, round it off to the nearest whole number. (Round down any fraction less than one-half; round up any fraction that is one-half or more.) Enter this number in the appropriate blank below. This is your Composite score. The highest possible Composite score is 36. The lowest possible Composite score is 1.

<table>
<thead>
<tr>
<th>Your Scale Scores</th>
</tr>
</thead>
<tbody>
<tr>
<td>English</td>
</tr>
<tr>
<td>Mathematics</td>
</tr>
<tr>
<td>Reading</td>
</tr>
<tr>
<td>Science</td>
</tr>
<tr>
<td>Sum of Scores</td>
</tr>
<tr>
<td>Composite Score (sum ÷ 4)</td>
</tr>
</tbody>
</table>
## Scale Score Conversion Table: Practice Test 2

<table>
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<th>Scale Score</th>
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<th>Reading</th>
<th>Science</th>
<th>Scale Score</th>
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</table>

**STEP 6.** Use the table on page 630 to determine your estimated percentile ranks (percent at or below) for each of your scale scores. In the far left column of the table, circle your scale score for the English test (from page 628). Then read across to the percentile rank column for that test; circle or put a checkmark beside the corresponding percentile rank. Use the same procedure for the other three tests (from page 628). Using the right-hand column of scale scores for your science test and Composite scores may be easier. As you mark your percentile ranks, enter them in the blanks provided. You may also find it helpful to compare your performance with the national mean (average) score for each of the four tests and the Composite as shown at the bottom of the table.
## National Distributions of Cumulative Percents for ACT Test Scores

ACT-Tested High School Graduates from 2013, 2014 and 2015

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### Mean

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<th>READING</th>
<th>SCIENCE</th>
<th>COMPOSITE</th>
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### S.D.

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Note: These national norms are the source of U.S. Ranks, for multiple-choice tests, displayed on ACT reports during the 2015-2016 testing year.

These norms with a sample size of 5,569,466, are based on 2013, 2014 and 2015 graduates.
**Scoring Your Practice Writing Test 2 Essay**

To score your practice writing test essay, follow these steps:

**STEP 1.** Use the guidelines from the writing test scoring rubric in chapter 3 to score your essay. Because many essays do not fit the exact description at each score point, read each description and try to determine which paragraph in the rubric best describes most of the characteristics of your essay.

**STEP 2.** Because your writing test domain scores are the sum of two readers’ ratings of your essay, multiply your own 1–6 rating from step 1 by 2. Or, have both you and someone else read and score your practice essay and add those ratings together. In either case, record the total in the blank in step 3.

**STEP 3.** Enter your writing test domain scores in the following box:

<table>
<thead>
<tr>
<th>Domain Score</th>
<th>Ideas and Analysis</th>
<th>Development and Support</th>
<th>Organization</th>
<th>Language Use and Conventions</th>
</tr>
</thead>
<tbody>
<tr>
<td>x 2 =</td>
<td>x 2 =</td>
<td>x 2 =</td>
<td>x 2 =</td>
<td></td>
</tr>
</tbody>
</table>

**STEP 4.** Enter the sum of the second-column scores here ______. This is your raw score (value between 8 and 48).

**STEP 5.** Use the table on page 632 to find the scaled writing subject score that corresponds to your raw score.

You can find the most current information on scoring the ACT writing test in the bonus online content.
## Scale Score Conversion Table: Writing Practice Test 2

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<td>–</td>
</tr>
<tr>
<td>1</td>
<td>8</td>
</tr>
</tbody>
</table>

**STEP 6.** Use the table on page 633 to determine your estimated percentile rank (percent at or below) for your writing test subscore. Circle your writing test subscore, this time using the column headed “Writing.” As you mark your percentile ranks, enter them in the blanks provided in the following table. You may also find it helpful to compare your performance with the national mean (average) score of the writing test subscore as shown at the bottom of the table on page 633.

You can find the most current information on scoring the ACT writing test in the bonus online content.
Taking Additional Practice Tests

Scoring the Additional Practice Tests

The ONLY Official Prep Guide from the Makers of the ACT

<table>
<thead>
<tr>
<th>Score</th>
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<th>Writing</th>
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</thead>
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</tbody>
</table>

<table>
<thead>
<tr>
<th>Mean</th>
<th>21.1</th>
<th>19.4</th>
<th>17.2</th>
</tr>
</thead>
<tbody>
<tr>
<td>S.D.</td>
<td>5.1</td>
<td>5.4</td>
<td>6.6</td>
</tr>
</tbody>
</table>

Note: These national norms are the source of U.S. Ranks, for the STEM and ELA scores and for the writing test displayed on ACT reports for students who test beginning September 2015.

STEM norms with a sample size of 5,569,466, is based on 2013, 2014 and 2015 graduates.

ELA and writing norms are initially based on one special study.

Starting in September 2015, ACT has introduced enhancements to the ACT writing test. Key differences between the former and the enhanced designs can be found at:

http://www.actstudent.org/writing/enhancements/
Scoring Practice Test 3

Scoring the Multiple-Choice Tests

To score each of your multiple-choice practice tests, starting with the English test, follow these six steps:

**STEP 1.** Write a “1” in the blank for each question that you answered correctly. An example is provided in the following box:

<table>
<thead>
<tr>
<th>Key</th>
<th>Your answer was</th>
</tr>
</thead>
<tbody>
<tr>
<td>1. A</td>
<td>Incorrect</td>
</tr>
<tr>
<td>2. J</td>
<td>Correct</td>
</tr>
<tr>
<td>3. B</td>
<td>Correct</td>
</tr>
<tr>
<td>4. G</td>
<td>Incorrect</td>
</tr>
</tbody>
</table>

**English Scoring Key**

<table>
<thead>
<tr>
<th>Key</th>
<th>Key</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>2. F</td>
<td>27. B</td>
<td>52. G</td>
</tr>
<tr>
<td>5. A</td>
<td>30. F</td>
<td>55. C</td>
</tr>
<tr>
<td>7. A</td>
<td>32. F</td>
<td>57. B</td>
</tr>
<tr>
<td>9. C</td>
<td>34. F</td>
<td>59. C</td>
</tr>
<tr>
<td>10. F</td>
<td>35. D</td>
<td>60. F</td>
</tr>
<tr>
<td>15. A</td>
<td>40. F</td>
<td>65. C</td>
</tr>
<tr>
<td>17. D</td>
<td>42. J</td>
<td>67. A</td>
</tr>
<tr>
<td>18. F</td>
<td>43. D</td>
<td>68. F</td>
</tr>
<tr>
<td>20. J</td>
<td>45. B</td>
<td>70. F</td>
</tr>
<tr>
<td>22. F</td>
<td>47. B</td>
<td>72. J</td>
</tr>
<tr>
<td>25. A</td>
<td>50. F</td>
<td>75. D</td>
</tr>
</tbody>
</table>
**STEP 2.** Add the numbers you entered in step 1 and write this total in the following shaded box. This is your raw score.

<table>
<thead>
<tr>
<th>Number Correct (Raw Score) for:</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>English test (75 questions)</td>
<td></td>
</tr>
</tbody>
</table>

**STEP 3.** Repeat steps 1 and 2 for the ACT mathematics, reading, and science tests using the scoring keys on the following pages.

### Mathematics Scoring Key Practice Test 3

<table>
<thead>
<tr>
<th>Key</th>
<th>Key</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>2.</td>
<td>K</td>
<td>22.</td>
</tr>
<tr>
<td>3.</td>
<td>A</td>
<td>23.</td>
</tr>
<tr>
<td>4.</td>
<td>K</td>
<td>24.</td>
</tr>
<tr>
<td>7.</td>
<td>B</td>
<td>27.</td>
</tr>
<tr>
<td>12.</td>
<td>J</td>
<td>32.</td>
</tr>
<tr>
<td>17.</td>
<td>E</td>
<td>37.</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Number Correct (Raw Score) for:</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Mathematics test (60 questions)</td>
<td></td>
</tr>
</tbody>
</table>
### Reading Scoring Key ■ Practice Test 3

<table>
<thead>
<tr>
<th>Key</th>
<th>Key</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>13. D</td>
<td>27. D</td>
<td></td>
</tr>
</tbody>
</table>

Number Correct (Raw Score) for:
Reading test (40 questions) _____________

### Science Scoring Key ■ Practice Test 3

<table>
<thead>
<tr>
<th>Key</th>
<th>Key</th>
<th>Key</th>
</tr>
</thead>
<tbody>
<tr>
<td>3. A</td>
<td>17. A</td>
<td>31. A</td>
</tr>
<tr>
<td>5. A</td>
<td>19. D</td>
<td>33. D</td>
</tr>
<tr>
<td>13. B</td>
<td>27. C</td>
<td></td>
</tr>
</tbody>
</table>

Number Correct (Raw Score) for:
Science test (40 questions) _____________
STEP 4. On each of the four tests, the total number of correct responses yields a raw score. Use the conversion table on the following page to convert your raw scores to scale scores. For each of the four tests, locate and circle your raw score or the range of raw scores that includes it in the conversion table. Then, read across to either outside column of the table and circle the scale score that corresponds to that raw score. As you determine your scale scores, enter them in the blanks provided below. The highest possible scale score for each test is 36. The lowest possible scale score for any of the four tests is 1.

<table>
<thead>
<tr>
<th>Your Scale Scores</th>
</tr>
</thead>
<tbody>
<tr>
<td>English</td>
</tr>
<tr>
<td>Mathematics</td>
</tr>
<tr>
<td>Reading</td>
</tr>
<tr>
<td>Science</td>
</tr>
<tr>
<td>Sum of Scores</td>
</tr>
<tr>
<td>Composite Score (sum ÷ 4)</td>
</tr>
</tbody>
</table>

STEP 5. Compute your Composite score by averaging the four scale scores. To do this, add your four scale scores and divide the sum by 4. If the resulting number ends in a fraction, round it off to the nearest whole number. (Round down any fraction less than one-half; round up any fraction that is one-half or more.) Enter this number in the appropriate blank below. This is your Composite score. The highest possible Composite score is 36. The lowest possible Composite score is 1.

<table>
<thead>
<tr>
<th>Your Scale Scores</th>
</tr>
</thead>
<tbody>
<tr>
<td>English</td>
</tr>
<tr>
<td>Mathematics</td>
</tr>
<tr>
<td>Reading</td>
</tr>
<tr>
<td>Science</td>
</tr>
<tr>
<td>Sum of Scores</td>
</tr>
<tr>
<td>Composite Score (sum ÷ 4)</td>
</tr>
</tbody>
</table>
### Scale Score Conversion Table:
**Practice Test 3**

<table>
<thead>
<tr>
<th>Scale Score</th>
<th>Raw Score</th>
<th>Scale Score</th>
</tr>
</thead>
<tbody>
<tr>
<td>36</td>
<td>75</td>
<td>36</td>
</tr>
<tr>
<td>35</td>
<td>73–74</td>
<td>35</td>
</tr>
<tr>
<td>34</td>
<td>72</td>
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<td>31</td>
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</tr>
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<td>68</td>
<td>30</td>
</tr>
<tr>
<td>29</td>
<td>66–67</td>
<td>29</td>
</tr>
<tr>
<td>28</td>
<td>65</td>
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<td>3</td>
<td>2</td>
</tr>
<tr>
<td>1</td>
<td>0–2</td>
<td>1</td>
</tr>
</tbody>
</table>

**English** | **Mathematics** | **Reading** | **Science**
**Scoring Your Practice Writing Test 3 Essay**

To score your practice writing test essay, follow these steps:

**STEP 1.** Use the guidelines from the writing test scoring rubric in chapter 3 to score your essay. Because many essays do not fit the exact description at each score point, read each description and try to determine which paragraph in the rubric best describes most of the characteristics of your essay.

**STEP 2.** Because your writing test domain scores are the sum of two readers’ ratings of your essay, multiply your own 1–6 rating from step 1 by 2. Or, have both you and someone else read and score your practice essay and add those ratings together. In either case, record the total in the blank in step 3.

**STEP 3.** Enter your writing test domain scores in the following box:

<table>
<thead>
<tr>
<th>Domain Score</th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>Ideas and Analysis</td>
<td>x 2 =</td>
</tr>
<tr>
<td>Development and Support</td>
<td>x 2 =</td>
</tr>
<tr>
<td>Organization</td>
<td>x 2 =</td>
</tr>
<tr>
<td>Language Use and Conventions</td>
<td>x 2 =</td>
</tr>
</tbody>
</table>

**STEP 4.** Enter the sum of the second-column scores here. This is your raw score (value between 8 and 48).

**STEP 5.** Use the table on page 640 to find the scaled writing subject score that corresponds to your raw score.

You can find the most current information on scoring the ACT writing test in the bonus online content.
## Scale Score Conversion Table: Writing Practice Test 3

<table>
<thead>
<tr>
<th>Scale Score</th>
<th>Raw Score</th>
</tr>
</thead>
<tbody>
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<td>46</td>
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<td>44–45</td>
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<tr>
<td>33</td>
<td>41–43</td>
</tr>
<tr>
<td>32</td>
<td>40</td>
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<td>28</td>
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<td>–</td>
</tr>
<tr>
<td>3</td>
<td>9</td>
</tr>
<tr>
<td>2</td>
<td>–</td>
</tr>
<tr>
<td>1</td>
<td>8</td>
</tr>
</tbody>
</table>

**STEP 6.** Use the table on page 630 to determine your estimated percentile rank (percent at or below) for your writing test subscore. Circle your writing test subscore, this time using the column headed “Writing.” As you mark your percentile ranks, enter them in the blanks provided in the following table. You may also find it helpful to compare your performance with the national mean (average) score of the writing test subscore as shown at the bottom of the table on page 633.

You can find the most current information on scoring the ACT writing test in the bonus online content.
After taking any test, students are eager to see how they’ve done. Assuming you took and scored ACT practice test 1 in chapter 3 or took other practice tests in chapter 10 and scored them in chapter 11, you have a great deal of information to consider when determining how well you did.

- **Raw scores**: ACT does not provide raw scores, but you have raw scores for the practice tests in this book.

- **Scale scores** are the scores that ACT reports to students, high schools, colleges, and scholarship agencies.

- **Composite score** is a scale score that reflects your overall performance on all of the multiple choice tests—English, math, reading, and science.

- **Ranks** indicate the approximate percentage of ACT-tested students who scored at or below each of your scores; for example, if your mathematics rank is 85%, then you scored as well or better than 85% of the other students who took the mathematics test.
If you took the ACT you receive the *ACT Student Report*, which includes scale scores, the Composite score, and the rank for each score. The sample report image below was used during the 2015–2016 academic school year and may be updated; to view the current report please visit www.act.org.

In this chapter, we explain how to interpret your scores and use them as a tool to help inform your education and career decisions. We encourage you to look at your ACT test scores and ranks with additional information to help guide your future education and career planning.

**Understanding Your ACT Test Results**

Your scores, Composite score, and ranks provide a good indication of how well you did on the test, but you can interpret these scores on a deeper level to find out more about how well prepared you are to tackle a certain course of studies or pursue a specific career. In the following sections, we help you put your scores and ranks in perspective to make them more meaningful and relevant to your education and career planning.
**How ACT Scores Your Multiple-Choice Tests**

ACT scores the multiple-choice tests the same way you scored your ACT practice tests in chapters 3 and 11. The first step is to do exactly what you did for your practice tests: count the number of questions you answered correctly to determine your raw score. No points are deducted for incorrect answers.

The raw score is converted to a scale score to enhance score interpretation and allow comparability across different forms. Scale scores range from 1 (low) to 36 (high) for each of the four individual tests and for the Composite score, which is the average of the four test scores.

**How ACT Scores Your Writing Test**

Two trained readers score each writing test based on the scoring rubric presented on pages 109–110. Each reader scores your essay on a scale from 1 (low) to 6 (high) on each domain. If their scores differ by more than 1 point on any of the four domains, a third reader scores your essay to resolve the discrepancy. This method is designed to be as impartial as possible. The writing score is calculated from your domain scores and is reported on a 1 to 36 scale.

**Recognizing That Test Scores Are Estimates of Educational Achievement**

No test, including the ACT, is an exact measure of your educational achievement. We estimate the amount of imprecision using the “standard error of measurement.” On the ACT, the standard error of measurement (SEM) is 2 points for each of the multiple-choice tests, 4 points for the writing test, and 1 point for the Composite score.

Because no test score is an exact measure of your achievement, think of each of your ACT scores as a range of scores rather than as a precise number. The SEM can be used to estimate ranges for your scores. To do this, just add the SEM to, and subtract it from, each of your scores. For example, if your score on the English test is 22, your true achievement is likely in the score range of 20 to 24 (22 plus or minus 2 points).

**Using Ranks to Interpret Your Scores**

The US and state ranks for a score tell you how your scores compare to those earned by recent high school graduates who took the ACT. The numbers indicate the cumulative percent of students who scored at or below a given score. For example, if your rank is 63%, then 63% of recent high school graduates who took the ACT scored at or below your score.

You can find the most current information on scoring the ACT writing test in the bonus online content.
**Comparing Your Test Scores to Each Other**

Another way to interpret your ACT test scores is by comparing them to each other using the ranks. You may find it interesting, for example, to compare your ranks for the science and mathematics tests to your ranks for the reading and English tests. Perhaps you felt more comfortable and successful in some subject areas than in others. Making comparisons among your ACT test ranks can be especially helpful as you make decisions about the courses you will take in high school and college. A high rank in a particular area indicates that you compare well to other ACT test-takers in that subject. A low rank may indicate that you need to develop your skills more in that area.

Keep in mind, however, that scale scores from the different individual tests can’t be directly compared to each other. Scoring 23 on the ACT English and mathematics tests, for example, doesn’t necessarily mean that your levels of skill and knowledge in English are the same as they are in mathematics. The percentile ranks corresponding to the scores—not the scores themselves—are probably best for making comparisons among subject areas.

**Comparing Your Scores and Ranks to Your High School Grades**

After you take the ACT and receive your student report, compare your scores and ranks to your high school grades. Are your highest grades and highest ACT test scores and ranks in the same content areas? If so, you might want to consider college majors that would draw on your areas of greatest strength or seek to improve your knowledge and skills in weaker subject areas. However, if your grades and scores differ significantly, talk with your counselor about possible reasons for the differences.

**Comparing Your Scores to Those of Enrolled First-Year College Students**

Another way to understand your ACT test scores and ranks is by comparing them to those of students enrolled at colleges or universities you’re interested in attending. This information can be very useful as you make decisions about applying for college. Keep in mind that admissions offices use a number of measures—including high school grades, recommendations, and extracurricular activities—to determine how students are likely to perform at their schools. Still, knowing that your ACT test scores are similar to those of students already enrolled at a college or university you’re considering may make you more confident in applying for admission there.

You can also use ACT Profile’s score explorer to determine if your ACT score is in the score range typically accepted by the colleges you are considering. Score explorer is a free service found at www.actprofile.com.
After you calculate your scores, you may wonder what your test scores mean regarding how well you are prepared to tackle college-level courses. In other words, what do your test scores tell you about your knowledge and skills in English, math, reading, and science? One way to understand this is to consider your scores from the perspective of what students who have that score are likely to know and be able to do. ACT developed the College and Career Readiness Standards to tell you exactly that.

**What Are the ACT College and Career Readiness Standards?**

The ACT College and Career Readiness Standards are sets of statements that describe what students are likely to know and be able to do in each content area based on their scores on each of the tests (English, mathematics, reading, science, and writing). The statements serve as
score descriptors and reflect a progression of skills and knowledge in a particular content area. The College and Career Readiness Standards are reported in terms of score range, so that the statements describe the knowledge and skills that students typically demonstrate who score in these different ranges on the multiple-choice tests: 13–15, 16–19, 20–23, 24–27, 28–32, 33–36. A score of 1–12 indicates the student is most likely beginning to develop the knowledge and skills described in the 13–15 score range for that particular test. All the College and Career Readiness Standards are cumulative, meaning that students typically can also demonstrate the skills and knowledge described in the score ranges below the range in which they scored.

**How Can the ACT College and Career Readiness Standards Help You?**

The purpose of the ACT College and Career Readiness Standards is to help you and others better understand what your ACT scores indicate about the knowledge and skills you likely have and what areas might need further development for you to be better prepared for college.

Because the ACT College and Career Readiness Standards provide statements that describe what you are likely to know and be able to do, you can use that information to help zero in on what specific steps you should take to further develop your college readiness. If, for example, you scored in the 16–19 range on the English test, you might infer that you are likely able to do and know the skills and knowledge described in the 13–15 and in the 16–19 range. You might choose to take a closer look at the standards in the 20–23 and higher score ranges to see what courses to take, or what instruction you might need, to develop those particular areas in order to be better prepared for college. In other words, you can use the ACT College and Career Readiness Standards to help you select courses and instruction that will focus on preparing you for college.

**ACT College Readiness Benchmarks**

ACT has identified the minimum score needed on each ACT test to indicate a 50% chance of obtaining a B or higher or about a 75% chance of obtaining a C or higher in the corresponding first-year college course. Your score report will have a visual representation of where you scored compared to the ACT College Readiness Benchmark. See figure on previous page.

<table>
<thead>
<tr>
<th>ACT Test</th>
<th>ACT Benchmark Score</th>
<th>College Course</th>
</tr>
</thead>
<tbody>
<tr>
<td>English</td>
<td>18</td>
<td>English Composition</td>
</tr>
<tr>
<td>Mathematics</td>
<td>22</td>
<td>Algebra</td>
</tr>
<tr>
<td>Reading</td>
<td>22</td>
<td>Social Sciences/Humanities</td>
</tr>
<tr>
<td>Science</td>
<td>23</td>
<td>Biology</td>
</tr>
</tbody>
</table>

To increase your college readiness, consider taking additional rigorous course work before you enter college. When you meet with your academic advisor to plan your first-year college courses, select courses that are appropriate for your academic background and reflect your planned curriculum. On the ACT writing test, ACT’s research to date suggests that examinees with a writing subscore of 7 or higher possess sufficient general writing skills to be ready for college-level writing assignments.
Planning Your Education and Career

The ACT Student Report includes a College and Career Planning section that helps you explore college majors and occupations, consider your options, and develop plans. The information in this section is all about you. Majors and occupations you may want to explore have been listed here, because they are related to the interests you expressed or occupations you said you were considering.

To explore and find opportunities that might be a good fit for you, visit ACT’s free college and career planning website at www.actprofile.org. After creating an account, you can use the site to explore these options:

- **Occupations suggested by your interests.** Career areas related to your interests are listed on the back of your score report. Use ACT Profile’s interactive career map to obtain more detailed information about the occupations in these career areas and others, including salary, training, and growth.

- **College majors.** The back of your score report lists the college major you selected, as well as related majors. ACT Profile has more detailed information about the major you selected, along with hundreds of majors to explore using the interactive major map.

- **Schools.** ACT Profile enables you to learn more about over 7,000 schools and find schools based on your preferences or search for schools by major, size, location, ACT score, and more.

Create your free account today to identify majors that fit your interests, find occupations that align with your values and abilities, compare college costs, and engage in other education and career planning activities at www.actprofile.org.

Seeking Additional Information and Guidance

Your ACT Student Report will provide additional information to help you understand your ACT test results and use them to make important decisions about college and to explore possible future careers.

As you approach decisions about college and careers, be sure to take advantage of all the assistance you can find. Talk to your parents, counselors, and teachers; visit your local library; and talk directly to personnel at colleges in which you’re interested. The more you can find out about all the educational options available to you and the level of your academic skills and knowledge (using such information as your ACT test results), the better prepared you’ll be to make informed college and career choices.
ACT College and Career Readiness Standards—English

These standards describe what students who score in specific score ranges on the English test are likely to know and be able to do.

- Students who score in the 1–12 range are most likely beginning to develop the knowledge and skills assessed in the other ranges.
- The ACT College Readiness Benchmark for English is 18. Students who achieve this score on the ACT English test have a 50% likelihood of achieving a B or better in a first-year English composition course at a typical college. The knowledge and skills highly likely to be demonstrated by students who meet the benchmark are shaded.

Production of Writing

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Production of Writing: Topic Development in Terms of Purpose and Focus (TOD)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>TOD 201. Delete material because it is obviously irrelevant in terms of the topic of the essay</td>
</tr>
</tbody>
</table>
| 16–19       | TOD 301. Delete material because it is obviously irrelevant in terms of the focus of the essay  
TOD 302. Identify the purpose of a word or phrase when the purpose is simple (e.g., identifying a person, defining a basic term, using common descriptive adjectives)  
TOD 303. Determine whether a simple essay has met a straightforward goal |
| 20–23       | TOD 401. Determine relevance of material in terms of the focus of the essay  
TOD 402. Identify the purpose of a word or phrase when the purpose is straightforward (e.g., describing a person, giving examples)  
TOD 403. Use a word, phrase, or sentence to accomplish a straightforward purpose (e.g., conveying a feeling or attitude) |
| 24–27       | TOD 501. Determine relevance of material in terms of the focus of the paragraph  
TOD 502. Identify the purpose of a word, phrase, or sentence when the purpose is fairly straightforward (e.g., identifying traits, giving reasons, explaining motivations)  
TOD 503. Determine whether an essay has met a specified goal  
TOD 504. Use a word, phrase, or sentence to accomplish a fairly straightforward purpose (e.g., sharpening an essay's focus, illustrating a given statement) |
### Production of Writing: Topic Development in Terms of Purpose and Focus (TOD) (continued)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Production of Writing: Topic Development in Terms of Purpose and Focus (TOD) (continued)</th>
</tr>
</thead>
</table>
| 28–32       | TOD 601. Determine relevance when considering material that is plausible but potentially irrelevant at a given point in the essay  
                         TOD 602. Identify the purpose of a word, phrase, or sentence when the purpose is subtle (e.g., supporting a later point, establishing tone) or when the best decision is to delete the text in question  
                         TOD 603. Use a word, phrase, or sentence to accomplish a subtle purpose (e.g., adding emphasis or supporting detail, expressing meaning through connotation) |
| 33–36       | TOD 701. Identify the purpose of a word, phrase, or sentence when the purpose is complex (e.g., anticipating a reader’s need for background information) or requires a thorough understanding of the paragraph and essay  
                         TOD 702. Determine whether a complex essay has met a specified goal  
                         TOD 703. Use a word, phrase, or sentence to accomplish a complex purpose, often in terms of the focus of the essay |

### Production of Writing: Organization, Unity, and Cohesion (ORG)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Production of Writing: Organization, Unity, and Cohesion (ORG)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>ORG 201. Determine the need for transition words or phrases to establish time relationships in simple narrative essays (e.g., then, this time)</td>
</tr>
</tbody>
</table>
| 16–19       | ORG 301. Determine the most logical place for a sentence in a paragraph  
                         ORG 302. Provide a simple conclusion to a paragraph or essay (e.g., expressing one of the essay’s main ideas) |
| 20–23       | ORG 401. Determine the need for transition words or phrases to establish straightforward logical relationships (e.g., first, afterward, in response)  
                         ORG 402. Determine the most logical place for a sentence in a straightforward essay  
                         ORG 403. Provide an introduction to a straightforward paragraph  
                         ORG 404. Provide a straightforward conclusion to a paragraph or essay (e.g., summarizing an essay’s main idea or ideas)  
                         ORG 405. Rearrange the sentences in a straightforward paragraph for the sake of logic |

(continued)
<table>
<thead>
<tr>
<th>Score Range</th>
<th>Production of Writing: Organization, Unity, and Cohesion (ORG) (continued)</th>
</tr>
</thead>
<tbody>
<tr>
<td>24–27</td>
<td>ORG 501. Determine the need for transition words or phrases to establish subtle logical relationships within and between sentences (e.g., <em>therefore</em>, <em>however</em>, <em>in addition</em>)</td>
</tr>
<tr>
<td></td>
<td>ORG 502. Provide a fairly straightforward introduction or conclusion to or transition within a paragraph or essay (e.g., supporting or emphasizing an essay’s main idea)</td>
</tr>
<tr>
<td></td>
<td>ORG 503. Rearrange the sentences in a fairly straightforward paragraph for the sake of logic</td>
</tr>
<tr>
<td></td>
<td>ORG 504. Determine the best place to divide a paragraph to meet a particular rhetorical goal</td>
</tr>
<tr>
<td></td>
<td>ORG 505. Rearrange the paragraphs in an essay for the sake of logic</td>
</tr>
<tr>
<td>28–32</td>
<td>ORG 601. Determine the need for transition words or phrases to establish subtle logical relationships within and between paragraphs</td>
</tr>
<tr>
<td></td>
<td>ORG 602. Determine the most logical place for a sentence in a fairly complex essay</td>
</tr>
<tr>
<td></td>
<td>ORG 603. Provide a subtle introduction or conclusion to or transition within a paragraph or essay (e.g., echoing an essay’s theme or restating the main argument)</td>
</tr>
<tr>
<td></td>
<td>ORG 604. Rearrange the sentences in a fairly complex paragraph for the sake of logic and coherence</td>
</tr>
<tr>
<td>33–36</td>
<td>ORG 701. Determine the need for transition words or phrases, basing decisions on a thorough understanding of the paragraph and essay</td>
</tr>
<tr>
<td></td>
<td>ORG 702. Provide a sophisticated introduction or conclusion to or transition within a paragraph or essay, basing decisions on a thorough understanding of the paragraph and essay (e.g., linking the conclusion to one of the essay’s main images)</td>
</tr>
<tr>
<td>Score Range</td>
<td>Production of Writing: Knowledge of Language (KLA)</td>
</tr>
<tr>
<td>-------------</td>
<td>--------------------------------------------------</td>
</tr>
<tr>
<td>13–15</td>
<td>KLA 201. Revise vague, clumsy, and confusing writing that creates obvious logic problems</td>
</tr>
<tr>
<td></td>
<td>KLA 301. Delete obviously redundant and wordy material</td>
</tr>
<tr>
<td></td>
<td>KLA 302. Revise expressions that deviate markedly from the style and tone of the essay</td>
</tr>
<tr>
<td>16–19</td>
<td>KLA 401. Delete redundant and wordy material when the problem is contained within a single phrase (e.g., “alarmingly startled,” “started by reaching the point of beginning”)</td>
</tr>
<tr>
<td></td>
<td>KLA 402. Revise expressions that deviate from the style and tone of the essay</td>
</tr>
<tr>
<td></td>
<td>KLA 403. Determine the need for conjunctions to create straightforward logical links between clauses</td>
</tr>
<tr>
<td></td>
<td>KLA 404. Use the word or phrase most appropriate in terms of the content of the sentence when the vocabulary is relatively common</td>
</tr>
<tr>
<td>20–23</td>
<td>KLA 501. Revise vague, clumsy, and confusing writing</td>
</tr>
<tr>
<td></td>
<td>KLA 502. Delete redundant and wordy material when the meaning of the entire sentence must be considered</td>
</tr>
<tr>
<td></td>
<td>KLA 503. Revise expressions that deviate in subtle ways from the style and tone of the essay</td>
</tr>
<tr>
<td></td>
<td>KLA 504. Determine the need for conjunctions to create logical links between clauses</td>
</tr>
<tr>
<td></td>
<td>KLA 505. Use the word or phrase most appropriate in terms of the content of the sentence when the vocabulary is uncommon</td>
</tr>
<tr>
<td>24–27</td>
<td>KLA 601. Revise vague, clumsy, and confusing writing involving sophisticated language</td>
</tr>
<tr>
<td></td>
<td>KLA 602. Delete redundant and wordy material that involves fairly sophisticated language (e.g., “the outlook of an aesthetic viewpoint”) or that sounds acceptable as conversational English</td>
</tr>
<tr>
<td></td>
<td>KLA 603. Determine the need for conjunctions to create subtle logical links between clauses</td>
</tr>
<tr>
<td></td>
<td>KLA 604. Use the word or phrase most appropriate in terms of the content of the sentence when the vocabulary is fairly sophisticated</td>
</tr>
<tr>
<td>28–32</td>
<td>KLA 701. Delete redundant and wordy material that involves sophisticated language or complex concepts or where the material is redundant in terms of the paragraph or essay as a whole</td>
</tr>
<tr>
<td></td>
<td>KLA 702. Use the word or phrase most appropriate in terms of the content of the sentence when the vocabulary is sophisticated</td>
</tr>
<tr>
<td>Score Range</td>
<td>Conventions of Standard English Grammar, Usage, and Punctuation Sentence Structure and Formation (SST)</td>
</tr>
<tr>
<td>-------------</td>
<td>------------------------------------------------------------------------------------------------</td>
</tr>
</tbody>
</table>
| 13–15       | SST 201. Determine the need for punctuation or conjunctions to join simple clauses  
SST 202. Recognize and correct inappropriate shifts in verb tense between simple clauses in a sentence or between simple adjoining sentences |
| 16–19       | SST 301. Determine the need for punctuation or conjunctions to correct awkward-sounding fragments and fused sentences as well as obviously faulty subordination and coordination of clauses  
SST 302. Recognize and correct inappropriate shifts in verb tense and voice when the meaning of the entire sentence must be considered |
| 20–23       | SST 401. Recognize and correct marked disturbances in sentence structure (e.g., faulty placement of adjectives, participial phrase fragments, missing or incorrect relative pronouns, dangling or misplaced modifiers, lack of parallelism within a simple series of verbs) |
| 24–27       | SST 501. Recognize and correct disturbances in sentence structure (e.g., faulty placement of phrases, faulty coordination and subordination of clauses, lack of parallelism within a simple series of phrases)  
SST 502. Maintain consistent and logical verb tense and pronoun person on the basis of the preceding clause or sentence |
| 28–32       | SST 601. Recognize and correct subtle disturbances in sentence structure (e.g., danglers where the intended meaning is clear but the sentence is ungrammatical, faulty subordination and coordination of clauses in long or involved sentences)  
SST 602. Maintain consistent and logical verb tense and voice and pronoun person on the basis of the paragraph or essay as a whole |
<p>| 33–36       | SST 701. Recognize and correct very subtle disturbances in sentence structure (e.g., weak conjunctions between independent clauses, run-ons that would be acceptable in conversational English, lack of parallelism within a complex series of phrases or clauses) |</p>
<table>
<thead>
<tr>
<th>Score Range</th>
<th>Conventions of Standard English Grammar, Usage, and Punctuation Usage Conventions (USG)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>USG 201. Form the past tense and past participle of irregular but commonly used verbs</td>
</tr>
<tr>
<td></td>
<td>USG 202. Form comparative and superlative adjectives</td>
</tr>
<tr>
<td>16–19</td>
<td>USG 301. Determine whether an adjective form or an adverb form is called for in a given situation</td>
</tr>
<tr>
<td></td>
<td>USG 302. Ensure straightforward subject-verb agreement</td>
</tr>
<tr>
<td></td>
<td>USG 303. Ensure straightforward pronoun-antecedent agreement</td>
</tr>
<tr>
<td></td>
<td>USG 304. Use idiomatically appropriate prepositions in simple contexts</td>
</tr>
<tr>
<td></td>
<td>USG 305. Use the appropriate word in frequently confused pairs (e.g., <em>there and their, past and passed, led and lead</em>)</td>
</tr>
<tr>
<td>20–23</td>
<td>USG 401. Use the correct comparative or superlative adjective or adverb form depending on context (e.g., “He is the oldest of my three brothers”)</td>
</tr>
<tr>
<td></td>
<td>USG 402. Ensure subject-verb agreement when there is some text between the subject and verb</td>
</tr>
<tr>
<td></td>
<td>USG 403. Use idiomatically appropriate prepositions, especially in combination with verbs (e.g., <em>long for, appeal to</em>)</td>
</tr>
<tr>
<td></td>
<td>USG 404. Recognize and correct expressions that deviate from idiomatic English</td>
</tr>
<tr>
<td>24–27</td>
<td>USG 501. Form simple and compound verb tenses, both regular and irregular, including forming verbs by using <em>have</em> rather than <em>of</em> (e.g., “would have gone,” not “would of gone”)</td>
</tr>
<tr>
<td></td>
<td>USG 502. Ensure pronoun-antecedent agreement when the pronoun and antecedent occur in separate clauses or sentences</td>
</tr>
<tr>
<td></td>
<td>USG 503. Recognize and correct vague and ambiguous pronouns</td>
</tr>
<tr>
<td>28–32</td>
<td>USG 601. Ensure subject-verb agreement in some challenging situations (e.g., when the subject-verb order is inverted or when the subject is an indefinite pronoun)</td>
</tr>
<tr>
<td></td>
<td>USG 602. Correctly use reflexive pronouns, the possessive pronouns <em>its</em> and <em>your</em>, and the relative pronouns <em>who</em> and <em>whom</em></td>
</tr>
<tr>
<td></td>
<td>USG 603. Use the appropriate word in less-common confused pairs (e.g., <em>allude and elude</em>)</td>
</tr>
<tr>
<td>33–36</td>
<td>USG 701. Ensure subject-verb agreement when a phrase or clause between the subject and verb suggests a different number for the verb</td>
</tr>
<tr>
<td></td>
<td>USG 702. Use idiomatically and contextually appropriate prepositions in combination with verbs in situations involving sophisticated language or complex concepts</td>
</tr>
<tr>
<td>Score Range</td>
<td>Conventions of Standard English Grammar, Usage, and Punctuation Conventions (PUN)</td>
</tr>
<tr>
<td>-------------</td>
<td>---------------------------------------------------------------------------------</td>
</tr>
<tr>
<td>13–15</td>
<td>PUN 201. Delete commas that create basic sense problems (e.g., between verb and direct object)</td>
</tr>
</tbody>
</table>
| 16–19       | PUN 301. Delete commas that markedly disturb sentence flow (e.g., between modifier and modified element)  
          | PUN 302. Use appropriate punctuation in straightforward situations (e.g., simple items in a series) |
| 20–23       | PUN 401. Delete commas when an incorrect understanding of the sentence suggests a pause that should be punctuated (e.g., between verb and direct object clause)  
          | PUN 402. Delete apostrophes used incorrectly to form plural nouns  
          | PUN 403. Use commas to avoid obvious ambiguity (e.g., to set off a long introductory element from the rest of the sentence when a misreading is possible)  
          | PUN 404. Use commas to set off simple parenthetical elements |
| 24–27       | PUN 501. Delete commas in long or involved sentences when an incorrect understanding of the sentence suggests a pause that should be punctuated (e.g., between the elements of a compound subject or compound verb joined by \textit{and})  
          | PUN 502. Recognize and correct inappropriate uses of colons and semicolons  
          | PUN 503. Use punctuation to set off complex parenthetical elements  
          | PUN 504. Use apostrophes to form simple possessive nouns |
| 28–32       | PUN 601. Use commas to avoid ambiguity when the syntax or language is sophisticated (e.g., to set off a complex series of items)  
          | PUN 602. Use punctuation to set off a nonessential/nonrestrictive appositive or clause  
          | PUN 603. Use apostrophes to form possessives, including irregular plural nouns  
          | PUN 604. Use a semicolon to link closely related independent clauses |
| 33–36       | PUN 701. Delete punctuation around essential/restrictive appositives or clauses  
          | PUN 702. Use a colon to introduce an example or an elaboration |
ACT College and Career Readiness Standards—Mathematics

These standards describe what students who score in specific score ranges on the math test are likely to know and be able to do. For more information about the ACT College and Career Readiness Standards in mathematics, go to www.act.org/standard/planact/math/mathnotes.html.

- Students who score in the 1–12 range are most likely beginning to develop the knowledge and skills assessed in the other ranges.
- The ACT College Readiness Benchmark for mathematics is 22. Students who achieve this score on the ACT mathematics test have a 50% likelihood of achieving a B or better in a first-year college algebra course at a typical college. The knowledge and skills highly likely to be demonstrated by students who meet the benchmark are shaded.

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Number and Quantity (N)</th>
</tr>
</thead>
</table>
| 13–15       | N 201. Perform one-operation computation with whole numbers and decimals  
N 202. Recognize equivalent fractions and fractions in lowest terms  
N 203. Locate positive rational numbers (expressed as whole numbers, fractions, decimals, and mixed numbers) on the number line |
| 16–19       | N 301. Recognize one-digit factors of a number  
N 302. Identify a digit’s place value  
N 303. Locate rational numbers on the number line  
Note: A matrix as a representation of data is treated here as a basic table. |
| 20–23       | N 401. Exhibit knowledge of elementary number concepts such as rounding, the ordering of decimals, pattern identification, primes, and greatest common factor  
N 402. Write positive powers of 10 by using exponents  
N 403. Comprehend the concept of length on the number line, and find the distance between two points  
N 404. Understand absolute value in terms of distance  
N 405. Find the distance in the coordinate plane between two points with the same x-coordinate or y-coordinate  
N 406. Add two matrices that have whole number entries |
| 24–27       | N 501. Order fractions  
N 502. Find and use the least common multiple  
N 503. Work with numerical factors  
N 504. Exhibit some knowledge of the complex numbers  
N 505. Add and subtract matrices that have integer entries |

(continued)
Score Range | Number and Quantity (N) (continued)
--- | ---
28–32 | N 601. Apply number properties involving prime factorization
N 602. Apply number properties involving even/odd numbers and factors/multiples
N 603. Apply number properties involving positive/negative numbers
N 604. Apply the facts that \( \pi \) is irrational and that the square root of an integer is rational only if that integer is a perfect square
N 605. Apply properties of rational exponents
N 606. Multiply two complex numbers
N 607. Use relations involving addition, subtraction, and scalar multiplication of vectors and of matrices

33–36 | N 701. Analyze and draw conclusions based on number concepts
N 702. Apply properties of rational numbers and the rational number system
N 703. Apply properties of real numbers and the real number system, including properties of irrational numbers
N 704. Apply properties of complex numbers and the complex number system
N 705. Multiply matrices
N 706. Apply properties of matrices and properties of matrices as a number system

Because algebra and functions are closely connected, some standards apply to both categories.

Score Range | Algebra (A) | Functions (F)
--- | --- | ---
13–15 | AF 201. Solve problems in one or two steps using whole numbers and using decimals in the context of money
A 201. Exhibit knowledge of basic expressions (e.g., identify an expression for a total as \( b + g \))
A 202. Solve equations in the form \( x + a = b \), where \( a \) and \( b \) are whole numbers or decimals
F 201. Extend a given pattern by a few terms for patterns that have a constant increase or decrease between terms

16–19 | AF 301. Solve routine one-step arithmetic problems using positive rational numbers, such as single-step percent
AF 302. Solve some routine two-step arithmetic problems
AF 303. Relate a graph to a situation described qualitatively in terms of familiar properties such as before and after, increasing and decreasing, higher and lower
AF 304. Apply a definition of an operation for whole numbers (e.g., \( a \bullet b = 3a - b \))

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Algebra (A)</th>
<th>Functions (F)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>A 301. Substitute whole numbers for unknown quantities to evaluate expressions</td>
<td>F 301. Extend a given pattern by a few terms for patterns that have a constant factor between terms</td>
</tr>
<tr>
<td></td>
<td>A 302. Solve one-step equations to get integer or decimal answers</td>
<td></td>
</tr>
<tr>
<td></td>
<td>A 303. Combine like terms (e.g., $2x + 5x$)</td>
<td></td>
</tr>
<tr>
<td>20–23</td>
<td>AF 401. Solve routine two-step or three-step arithmetic problems involving concepts such as rate and proportion, tax added, percentage off, and estimating by using a given average value in place of actual values</td>
<td>AF 401. Evaluate linear and quadratic functions, expressed in function notation, at integer values</td>
</tr>
<tr>
<td></td>
<td>AF 402. Perform straightforward word-to-symbol translations</td>
<td></td>
</tr>
<tr>
<td></td>
<td>AF 403. Relate a graph to a situation described in terms of a starting value and an additional amount per unit (e.g., unit cost, weekly growth)</td>
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<tr>
<td></td>
<td>A 401. Evaluate algebraic expressions by substituting integers for unknown quantities</td>
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<tr>
<td></td>
<td>A 402. Add and subtract simple algebraic expressions</td>
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</tr>
<tr>
<td></td>
<td>A 403. Solve routine first-degree equations</td>
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</tr>
<tr>
<td></td>
<td>A 404. Multiply two binomials</td>
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</tr>
<tr>
<td></td>
<td>A 405. Match simple inequalities with their graphs on the number line (e.g., $x &gt; -3$)</td>
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<tr>
<td></td>
<td>A 406. Exhibit knowledge of slope</td>
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</tr>
<tr>
<td>24–27</td>
<td>AF 501. Solve multistep arithmetic problems that involve planning or converting common derived units of measure (e.g., feet per second to miles per hour)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>AF 502. Build functions and write expressions, equations, or inequalities with a single variable for common pre-algebra settings (e.g., rate and distance problems and problems that can be solved by using proportions)</td>
<td></td>
</tr>
<tr>
<td></td>
<td>AF 503. Match linear equations with their graphs in the coordinate plane</td>
<td></td>
</tr>
</tbody>
</table>

(continued)
<table>
<thead>
<tr>
<th>Score Range</th>
<th>Algebra (A)</th>
<th>Functions (F)</th>
</tr>
</thead>
<tbody>
<tr>
<td>A 501.</td>
<td>Recognize that when numerical quantities are reported in real-world contexts, the numbers are often rounded</td>
<td>F 501. Evaluate polynomial functions, expressed in function notation, at integer values</td>
</tr>
<tr>
<td>A 502.</td>
<td>Solve real-world problems by using first-degree equations</td>
<td>F 502. Find the next term in a sequence described recursively</td>
</tr>
<tr>
<td>A 503.</td>
<td>Solve first-degree inequalities when the method does not involve reversing the inequality sign</td>
<td>F 503. Build functions and use quantitative information to identify graphs for relations that are proportional or linear</td>
</tr>
<tr>
<td>A 504.</td>
<td>Match compound inequalities with their graphs on the number line (e.g., $-10.5 &lt; x &lt; 20.3$)</td>
<td>F 504. Attend to the difference between a function modeling a situation and the reality of the situation</td>
</tr>
<tr>
<td>A 505.</td>
<td>Add, subtract, and multiply polynomials</td>
<td>F 505. Understand the concept of a function as having a well-defined output value at each valid input value</td>
</tr>
<tr>
<td>A 506.</td>
<td>Identify solutions to simple quadratic equations</td>
<td>F 506. Understand the concept of domain and range in terms of valid input and output, and in terms of function graphs</td>
</tr>
<tr>
<td>A 507.</td>
<td>Solve quadratic equations in the form $(x + a)(x + b) = 0$, where $a$ and $b$ are numbers or variables</td>
<td>F 507. Interpret statements that use function notation in terms of their context</td>
</tr>
<tr>
<td>A 508.</td>
<td>Factor simple quadratics (e.g., the difference of squares and perfect square trinomials)</td>
<td>F 508. Find the domain of polynomial functions and rational functions</td>
</tr>
<tr>
<td>A 509.</td>
<td>Work with squares and square roots of numbers</td>
<td>F 509. Find the range of polynomial functions</td>
</tr>
<tr>
<td>A 510.</td>
<td>Work with cubes and cube roots of numbers</td>
<td>F 510. Find where a rational function's graph has a vertical asymptote</td>
</tr>
<tr>
<td>A 511.</td>
<td>Work with scientific notation</td>
<td>F 511. Use function notation for simple functions of two variables</td>
</tr>
<tr>
<td>A 512.</td>
<td>Work problems involving positive integer exponents</td>
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</tr>
<tr>
<td>A 513.</td>
<td>Determine when an expression is undefined</td>
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</tr>
<tr>
<td>A 514.</td>
<td>Determine the slope of a line from an equation</td>
<td></td>
</tr>
<tr>
<td>Score Range</td>
<td>Algebra (A)</td>
<td>Functions (F)</td>
</tr>
<tr>
<td>-------------</td>
<td>-----------------------------------------------------------------------------</td>
<td>-----------------------------------------------------------------------------</td>
</tr>
</tbody>
</table>
| 28–32       | AF 601. Solve word problems containing several rates, proportions, or percentages  
AF 602. Build functions and write expressions, equations, and inequalities for common algebra settings (e.g., distance to a point on a curve and profit for variable cost and demand)  
AF 603. Interpret and use information from graphs in the coordinate plane  
AF 604. Given an equation or function, find an equation or function whose graph is a translation by a specified amount up or down | F 601. Relate a graph to a situation described qualitatively in terms of faster change or slower change  
F 602. Build functions for relations that are inversely proportional  
F 603. Find a recursive expression for the general term in a sequence described recursively  
F 604. Evaluate composite functions at integer values |
| 33–36       | AF 701. Solve complex arithmetic problems involving percent of increase or decrease or requiring integration of several concepts (e.g., using several ratios, comparing percentages, or comparing averages)  
AF 702. Build functions and write expressions, equations, and inequalities when the process requires planning and/or strategic manipulation  
AF 703. Analyze and draw conclusions based on properties of algebra and/or functions  
AF 704. Analyze and draw conclusions based on information from graphs in the coordinate plane  
AF 705. Identify characteristics of graphs based on a set of conditions or on a general equation such as $y = ax^2 + c$  
AF 706. Given an equation or function, find an equation or function whose graph is a translation by specified amounts in the horizontal and vertical directions |
<table>
<thead>
<tr>
<th>Score Range</th>
<th>Algebra (A)</th>
<th>Functions (F)</th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>A 701. Solve simple absolute value inequalities</td>
<td>F 701. Compare actual values and the values of a modeling function to judge model fit and compare models</td>
</tr>
<tr>
<td></td>
<td>A 702. Match simple quadratic inequalities with their graphs on the number line</td>
<td>F 702. Build functions for relations that are exponential</td>
</tr>
<tr>
<td></td>
<td>A 703. Apply the remainder theorem for polynomials, that ( P(a) ) is the remainder when ( P(x) ) is divided by ( (x - a) )</td>
<td>F 703. Exhibit knowledge of geometric sequences</td>
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<td></td>
<td>F 704. Exhibit knowledge of unit circle trigonometry</td>
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<tr>
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<td></td>
<td>F 705. Match graphs of basic trigonometric functions with their equations</td>
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<td>F 706. Use trigonometric concepts and basic identities to solve problems</td>
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<td>F 707. Exhibit knowledge of logarithms</td>
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<td>F 708. Write an expression for the composite of two simple functions</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Geometry (G)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>G 201. Estimate the length of a line segment based on other lengths in a geometric figure</td>
</tr>
<tr>
<td></td>
<td>G 202. Calculate the length of a line segment based on the lengths of other line segments that go in the same direction (e.g., overlapping line segments and parallel sides of polygons with only right angles)</td>
</tr>
<tr>
<td></td>
<td>G 203. Perform common conversions of money and of length, weight, mass, and time within a measurement system (e.g., dollars to dimes, inches to feet, and hours to minutes)</td>
</tr>
<tr>
<td>16–19</td>
<td>G 301. Exhibit some knowledge of the angles associated with parallel lines</td>
</tr>
<tr>
<td></td>
<td>G 302. Compute the perimeter of polygons when all side lengths are given</td>
</tr>
<tr>
<td></td>
<td>G 303. Compute the area of rectangles when whole number dimensions are given</td>
</tr>
<tr>
<td></td>
<td>G 304. Locate points in the first quadrant</td>
</tr>
<tr>
<td>Score Range</td>
<td>Geometry (G)</td>
</tr>
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</tbody>
</table>
| 20–23       | G 401. Use properties of parallel lines to find the measure of an angle  
G 402. Exhibit knowledge of basic angle properties and special sums of angle measures (e.g., 90°, 180°, and 360°)  
G 403. Compute the area and perimeter of triangles and rectangles in simple problems  
G 404. Find the length of the hypotenuse of a right triangle when only very simple computation is involved (e.g., 3–4–5 and 6–8–10 triangles)  
G 405. Use geometric formulas when all necessary information is given  
G 406. Locate points in the coordinate plane  
G 407. Translate points up, down, left, and right in the coordinate plane |
| 24–27       | G 501. Use several angle properties to find an unknown angle measure  
G 502. Count the number of lines of symmetry of a geometric figure  
G 503. Use symmetry of isosceles triangles to find unknown side lengths or angle measures  
G 504. Recognize that real-world measurements are typically imprecise and that an appropriate level of precision is related to the measuring device and procedure  
G 505. Compute the perimeter of simple composite geometric figures with unknown side lengths  
G 506. Compute the area of triangles and rectangles when one or more additional simple steps are required  
G 507. Compute the area and circumference of circles after identifying necessary information  
G 508. Given the length of two sides of a right triangle, find the third when the lengths are Pythagorean triples  
G 509. Express the sine, cosine, and tangent of an angle in a right triangle as a ratio of given side lengths  
G 510. Determine the slope of a line from points or a graph  
G 511. Find the midpoint of a line segment  
G 512. Find the coordinates of a point rotated 180° around a given center point |

(continued)
<table>
<thead>
<tr>
<th>Score Range</th>
<th>Geometry (G) (continued)</th>
</tr>
</thead>
</table>
| 26–32       | G 601. Use relationships involving area, perimeter, and volume of geometric figures to compute another measure (e.g., surface area for a cube of a given volume and simple geometric probability)  
G 602. Use the Pythagorean theorem  
G 603. Apply properties of $30^\circ$–$60^\circ$–$90^\circ$, $45^\circ$–$45^\circ$–$90^\circ$, similar, and congruent triangles  
G 604. Apply basic trigonometric ratios to solve right-triangle problems  
G 605. Use the distance formula  
G 606. Use properties of parallel and perpendicular lines to determine an equation of a line or coordinates of a point  
G 607. Find the coordinates of a point reflected across a vertical or horizontal line or across $y = x$  
G 608. Find the coordinates of a point rotated $90^\circ$ about the origin  
G 609. Recognize special characteristics of parabolas and circles (e.g., the vertex of a parabola and the center or radius of a circle) |

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Statistics and Probability (S)</th>
</tr>
</thead>
</table>
| 13–15       | S 201. Calculate the average of a list of positive whole numbers  
S 202. Extract one relevant number from a basic table or chart, and use it in a single computation |
| 16–19       | S 301. Calculate the average of a list of numbers  
S 302. Calculate the average given the number of data values and the sum of the data values  
S 303. Read basic tables and charts  
S 304. Extract relevant data from a basic table or chart and use the data in a computation  
S 305. Use the relationship between the probability of an event and the probability of its complement |
<table>
<thead>
<tr>
<th>Score Range</th>
<th>Statistics and Probability (S) (continued)</th>
</tr>
</thead>
<tbody>
<tr>
<td>20–23</td>
<td>S 401. Calculate the missing data value given the average and all data values but one</td>
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<tr>
<td></td>
<td>S 402. Translate from one representation of data to another (e.g., a bar graph to a circle graph)</td>
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<tr>
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<td>S 403. Determine the probability of a simple event</td>
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<td>S 404. Describe events as combinations of other events (e.g., using and, or, and not)</td>
</tr>
<tr>
<td></td>
<td>S 405. Exhibit knowledge of simple counting techniques</td>
</tr>
<tr>
<td>24–27</td>
<td>S 501. Calculate the average given the frequency counts of all the data values</td>
</tr>
<tr>
<td></td>
<td>S 502. Manipulate data from tables and charts</td>
</tr>
<tr>
<td></td>
<td>S 503. Compute straightforward probabilities for common situations</td>
</tr>
<tr>
<td></td>
<td>S 504. Use Venn diagrams in counting</td>
</tr>
<tr>
<td></td>
<td>S 505. Recognize that when data summaries are reported in the real world, results are often rounded and must be interpreted as having appropriate precision</td>
</tr>
<tr>
<td></td>
<td>S 506. Recognize that when a statistical model is used, model values typically differ from actual values</td>
</tr>
<tr>
<td>28–32</td>
<td>S 601. Calculate or use a weighted average</td>
</tr>
<tr>
<td></td>
<td>S 602. Interpret and use information from tables and charts, including two-way frequency tables</td>
</tr>
<tr>
<td></td>
<td>S 603. Apply counting techniques</td>
</tr>
<tr>
<td></td>
<td>S 604. Compute a probability when the event and/or sample space are not given or obvious</td>
</tr>
<tr>
<td></td>
<td>S 605. Recognize the concepts of conditional and joint probability expressed in real-world contexts</td>
</tr>
<tr>
<td></td>
<td>S 606. Recognize the concept of independence expressed in real-world contexts</td>
</tr>
<tr>
<td>33–36</td>
<td>S 701. Distinguish among mean, median, and mode for a list of numbers</td>
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<tr>
<td></td>
<td>S 702. Analyze and draw conclusions based on information from tables and charts, including two-way frequency tables</td>
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<td>S 703. Understand the role of randomization in surveys, experiments, and observational studies</td>
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<tr>
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<td>S 704. Exhibit knowledge of conditional and joint probability</td>
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<tr>
<td></td>
<td>S 705. Recognize that part of the power of statistical modeling comes from looking at regularity in the differences between actual values and model values</td>
</tr>
</tbody>
</table>
ACT College and Career Readiness Standards—Reading

These standards describe what students who score in specific score ranges on the reading test are likely to know and be able to do.

- Students who score in the 1–12 range are most likely beginning to develop the knowledge and skills assessed in the other ranges.
- The ACT College Readiness Benchmark for reading is 22. Students who achieve this score on the ACT reading test have a 50% likelihood of achieving a B or better in a first-year social science course at a typical college. The knowledge and skills highly likely to be demonstrated by students who meet the benchmark are shaded.

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Close Reading (CLR)</th>
</tr>
</thead>
</table>
| 13–15       | CLR 201. Locate basic facts (e.g., names, dates, events) clearly stated in a passage  
CLR 202. Draw simple logical conclusions about the main characters in somewhat challenging literary narratives |
| 16–19       | CLR 301. Locate simple details at the sentence and paragraph level in somewhat challenging passages  
CLR 302. Draw simple logical conclusions in somewhat challenging passages |
| 20–23       | CLR 401. Locate important details in somewhat challenging passages  
CLR 402. Draw logical conclusions in somewhat challenging passages  
CLR 403. Draw simple logical conclusions in more challenging passages  
CLR 404. Paraphrase some statements as they are used in somewhat challenging passages |
| 24–27       | CLR 501. Locate and interpret minor or subtly stated details in somewhat challenging passages  
CLR 502. Locate important details in more challenging passages  
CLR 503. Draw subtle logical conclusions in somewhat challenging passages  
CLR 504. Draw logical conclusions in more challenging passages  
CLR 505. Paraphrase virtually any statement as it is used in somewhat challenging passages  
CLR 506. Paraphrase some statements as they are used in more challenging passages |
### Score Range | Close Reading (CLR) (continued)
--- | ---
28–32 | CLR 601. Locate and interpret minor or subtly stated details in more challenging passages  
CLR 602. Locate important details in complex passages  
CLR 603. Draw subtle logical conclusions in more challenging passages  
CLR 604. Draw simple logical conclusions in complex passages  
CLR 605. Paraphrase virtually any statement as it is used in more challenging passages
--- | ---
33–36 | CLR 701. Locate and interpret minor or subtly stated details in complex passages  
CLR 702. Locate important details in highly complex passages  
CLR 703. Draw logical conclusions in complex passages  
CLR 704. Draw simple logical conclusions in highly complex passages  
CLR 705. Draw complex or subtle logical conclusions, often by synthesizing information from different portions of the passage  
CLR 706. Paraphrase statements as they are used in complex passages

### Score Range | Central Ideas, Themes, and Summaries (IDT)
--- | ---
13–15 | IDT 201. Identify the topic of passages and distinguish the topic from the central idea or theme
--- | ---
16–19 | IDT 301. Identify a clear central idea in straightforward paragraphs in somewhat challenging literary narratives
--- | ---
20–23 | IDT 401. Infer a central idea in straightforward paragraphs in somewhat challenging literary narratives  
IDT 402. Identify a clear central idea or theme in somewhat challenging passages or their paragraphs  
IDT 403. Summarize key supporting ideas and details in somewhat challenging passages
--- | ---
24–27 | IDT 501. Infer a central idea or theme in somewhat challenging passages or their paragraphs  
IDT 502. Identify a clear central idea or theme in more challenging passages or their paragraphs  
IDT 503. Summarize key supporting ideas and details in more challenging passages

(continued)
### Central Ideas, Themes, and Summaries (IDT) (continued)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Central Ideas, Themes, and Summaries (IDT)</th>
</tr>
</thead>
</table>
| 28–32       | IDT 601. Infer a central idea or theme in more challenging passages or their paragraphs  
               IDT 602. Summarize key supporting ideas and details in complex passages |
| 33–36       | IDT 701. Identify or infer a central idea or theme in complex passages or their paragraphs  
               IDT 702. Summarize key supporting ideas and details in highly complex passages |

### Relationships (REL)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Relationships (REL)</th>
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</thead>
</table>
| 13–15       | REL 201. Determine when (e.g., first, last, before, after) an event occurs in somewhat challenging passages  
               REL 202. Identify simple cause-effect relationships within a single sentence in a passage |
| 16–19       | REL 301. Identify clear comparative relationships between main characters in somewhat challenging literary narratives  
               REL 302. Identify simple cause-effect relationships within a single paragraph in somewhat challenging literary narratives |
| 20–23       | REL 401. Order simple sequences of events in somewhat challenging literary narratives  
               REL 402. Identify clear comparative relationships in somewhat challenging passages  
               REL 403. Identify clear cause-effect relationships in somewhat challenging passages |
| 24–27       | REL 501. Order sequences of events in somewhat challenging passages  
               REL 502. Understand implied or subtly stated comparative relationships in somewhat challenging passages  
               REL 503. Identify clear comparative relationships in more challenging passages  
               REL 504. Understand implied or subtly stated cause-effect relationships in somewhat challenging passages  
               REL 505. Identify clear cause-effect relationships in more challenging passages |
### Relationships (REL) (continued)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Relationships (REL) (continued)</th>
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</thead>
<tbody>
<tr>
<td>28–32</td>
<td>REL 601. Order sequences of events in more challenging passages</td>
</tr>
<tr>
<td></td>
<td>REL 602. Understand implied or subtly stated comparative relationships in more challenging passages</td>
</tr>
<tr>
<td></td>
<td>REL 603. Identify clear comparative relationships in complex passages</td>
</tr>
<tr>
<td></td>
<td>REL 604. Understand implied or subtly stated cause-effect relationships in more challenging passages</td>
</tr>
<tr>
<td></td>
<td>REL 605. Identify clear cause-effect relationships in complex passages</td>
</tr>
<tr>
<td>33–36</td>
<td>REL 701. Order sequences of events in complex passages</td>
</tr>
<tr>
<td></td>
<td>REL 702. Understand implied or subtly stated comparative relationships in complex passages</td>
</tr>
<tr>
<td></td>
<td>REL 703. Identify clear comparative relationships in highly complex passages</td>
</tr>
<tr>
<td></td>
<td>REL 704. Understand implied or subtly stated cause-effect relationships in complex passages</td>
</tr>
<tr>
<td></td>
<td>REL 705. Identify clear cause-effect relationships in highly complex passages</td>
</tr>
</tbody>
</table>

### Craft and Structure: Word Meanings and Word Choice (WME)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Craft and Structure: Word Meanings and Word Choice (WME)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>WME 201. Understand the implication of a familiar word or phrase and of simple descriptive language</td>
</tr>
<tr>
<td>16–19</td>
<td>WME 301. Analyze how the choice of a specific word or phrase shapes meaning or tone in somewhat challenging passages when the effect is simple</td>
</tr>
<tr>
<td></td>
<td>WME 302. Interpret basic figurative language as it is used in a passage</td>
</tr>
<tr>
<td>20–23</td>
<td>WME 401. Analyze how the choice of a specific word or phrase shapes meaning or tone in somewhat challenging passages</td>
</tr>
<tr>
<td></td>
<td>WME 402. Interpret most words and phrases as they are used in somewhat challenging passages, including determining technical, connotative, and figurative meanings</td>
</tr>
</tbody>
</table>

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<table>
<thead>
<tr>
<th>Score Range</th>
<th>Craft and Structure: Word Meanings and Word Choice (WME) (continued)</th>
</tr>
</thead>
<tbody>
<tr>
<td>24–27</td>
<td>WME 501. Analyze how the choice of a specific word or phrase shapes meaning or tone in somewhat challenging passages when the effect is subtle</td>
</tr>
<tr>
<td></td>
<td>WME 502. Analyze how the choice of a specific word or phrase shapes meaning or tone in more challenging passages</td>
</tr>
<tr>
<td></td>
<td>WME 503. Interpret virtually any word or phrase as it is used in somewhat challenging passages, including determining technical, connotative, and figurative meanings</td>
</tr>
<tr>
<td></td>
<td>WME 504. Interpret most words and phrases as they are used in more challenging passages, including determining technical, connotative, and figurative meanings</td>
</tr>
<tr>
<td>28–32</td>
<td>WME 601. Analyze how the choice of a specific word or phrase shapes meaning or tone in complex passages</td>
</tr>
<tr>
<td></td>
<td>WME 602. Interpret virtually any word or phrase as it is used in more challenging passages, including determining technical, connotative, and figurative meanings</td>
</tr>
<tr>
<td></td>
<td>WME 603. Interpret words and phrases in a passage that makes consistent use of figurative, general academic, domain-specific, or otherwise difficult language</td>
</tr>
<tr>
<td>33–36</td>
<td>WME 701. Analyze how the choice of a specific word or phrase shapes meaning or tone in passages when the effect is subtle or complex</td>
</tr>
<tr>
<td></td>
<td>WME 702. Interpret words and phrases as they are used in complex passages, including determining technical, connotative, and figurative meanings</td>
</tr>
<tr>
<td></td>
<td>WME 703. Interpret words and phrases in a passage that makes extensive use of figurative, general academic, domain-specific, or otherwise difficult language</td>
</tr>
</tbody>
</table>

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Craft and Structure: Text Structure (TST)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>TST 201. Analyze how one or more sentences in passages relate to the whole passage when the function is stated or clearly indicated</td>
</tr>
<tr>
<td>16–19</td>
<td>TST 301. Analyze how one or more sentences in somewhat challenging passages relate to the whole passage when the function is simple</td>
</tr>
<tr>
<td></td>
<td>TST 302. Identify a clear function of straightforward paragraphs in somewhat challenging literary narratives</td>
</tr>
</tbody>
</table>
### Craft and Structure: Text Structure (TST) (continued)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Craft and Structure: Text Structure (TST) (continued)</th>
</tr>
</thead>
</table>
| 20–23       | TST 401. Analyze how one or more sentences in somewhat challenging passages relate to the whole passage  
|             | TST 402. Infer the function of straightforward paragraphs in somewhat challenging literary narratives  
|             | TST 403. Identify a clear function of paragraphs in somewhat challenging passages  
|             | TST 404. Analyze the overall structure of somewhat challenging passages |
| 24–27       | TST 501. Analyze how one or more sentences in somewhat challenging passages relate to the whole passage when the function is subtle  
|             | TST 502. Analyze how one or more sentences in more challenging passages relate to the whole passage  
|             | TST 503. Infer the function of paragraphs in somewhat challenging passages  
|             | TST 504. Identify a clear function of paragraphs in more challenging passages  
|             | TST 505. Analyze the overall structure of more challenging passages |
| 28–32       | TST 601. Analyze how one or more sentences in complex passages relate to the whole passage  
|             | TST 602. Infer the function of paragraphs in more challenging passages  
|             | TST 603. Analyze the overall structure of complex passages |
| 33–36       | TST 701. Analyze how one or more sentences in passages relate to the whole passage when the function is subtle or complex  
|             | TST 702. Identify or infer the function of paragraphs in complex passages  
|             | TST 703. Analyze the overall structure of highly complex passages |

### Craft and Structure: Purpose and Point of View (PPV)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Craft and Structure: Purpose and Point of View (PPV)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>PPV 201. Recognize a clear intent of an author or narrator in somewhat challenging literary narratives</td>
</tr>
<tr>
<td>16–19</td>
<td>PPV 301. Recognize a clear intent of an author or narrator in somewhat challenging passages</td>
</tr>
</tbody>
</table>
| 20–23       | PPV 401. Identify a clear purpose of somewhat challenging passages and how that purpose shapes content and style  
<p>|             | PPV 402. Understand point of view in somewhat challenging passages |</p>
<table>
<thead>
<tr>
<th>Score Range</th>
<th>Craft and Structure: Purpose and Point of View (PPV) (continued)</th>
</tr>
</thead>
</table>
| 24–27       | PPV 501. Infer a purpose in somewhat challenging passages and how that purpose shapes content and style  
PPV 502. Identify a clear purpose of more challenging passages and how that purpose shapes content and style  
PPV 503. Understand point of view in more challenging passages |
| 28–32       | PPV 601. Infer a purpose in more challenging passages and how that purpose shapes content and style  
PPV 602. Understand point of view in complex passages |
| 33–36       | PPV 701. Identify or infer a purpose in complex passages and how that purpose shapes content and style  
PPV 702. Understand point of view in highly complex passages |

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Integration of Knowledge and Ideas: Arguments (ARG)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>ARG 201. Analyze how one or more sentences in passages offer reasons for or support a claim when the relationship is clearly indicated</td>
</tr>
<tr>
<td>16–19</td>
<td>ARG 301. Analyze how one or more sentences in somewhat challenging passages offer reasons for or support a claim when the relationship is simple</td>
</tr>
</tbody>
</table>
| 20–23       | ARG 401. Analyze how one or more sentences in somewhat challenging passages offer reasons for or support a claim  
ARG 402. Identify a clear central claim in somewhat challenging passages |
| 24–27       | ARG 501. Analyze how one or more sentences in more challenging passages offer reasons for or support a claim  
ARG 502. Infer a central claim in somewhat challenging passages  
ARG 503. Identify a clear central claim in more challenging passages |
| 28–32       | ARG 601. Analyze how one or more sentences in complex passages offer reasons for or support a claim  
ARG 602. Infer a central claim in more challenging passages |
| 33–36       | ARG 701. Analyze how one or more sentences in passages offer reasons for or support a claim when the relationship is subtle or complex  
ARG 702. Identify or infer a central claim in complex passages  
ARG 703. Identify a clear central claim in highly complex passages |
## Integration of Knowledge and Ideas: Multiple Texts (SYN)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Integration of Knowledge and Ideas: Multiple Texts (SYN)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>SYN 201. Make simple comparisons between two passages</td>
</tr>
<tr>
<td>16–19</td>
<td>SYN 301. Make straightforward comparisons between two passages</td>
</tr>
<tr>
<td>20–23</td>
<td>SYN 401. Draw logical conclusions using information from two literary narratives</td>
</tr>
<tr>
<td>24–27</td>
<td>SYN 501. Draw logical conclusions using information from two informational texts</td>
</tr>
<tr>
<td>28–32</td>
<td>SYN 601. Draw logical conclusions using information from multiple portions of two literary narratives</td>
</tr>
<tr>
<td>33–36</td>
<td>SYN 701. Draw logical conclusions using information from multiple portions of two informational texts</td>
</tr>
</tbody>
</table>

### Text Complexity Rubric—Reading

This rubric describes reading passages for ACT Aspire™ Grade 8, ACT Aspire Early High School, and the ACT.

**Literary Narratives: Stories and Literary Nonfiction**

<table>
<thead>
<tr>
<th></th>
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<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td></td>
<td>• Have a largely straightforward purpose (chiefly literary nonfiction)</td>
<td>• Have a largely straightforward to somewhat complex purpose (chiefly literary nonfiction)</td>
<td>• Have a somewhat complex purpose; apparent purpose may differ from real purpose (chiefly literary nonfiction)</td>
<td>• Have a complex purpose; apparent purpose may differ from real purpose (chiefly literary nonfiction)</td>
</tr>
<tr>
<td></td>
<td>• Contain literal and inferential levels of meaning (chiefly stories)</td>
<td>• Contain literal, inferential, and interpretive levels of meaning (chiefly stories)</td>
<td>• Contain literal, inferential, and interpretive levels of meaning (chiefly stories)</td>
<td>• Contain literal, inferential, and interpretive levels of meaning (chiefly stories)</td>
</tr>
</tbody>
</table>

(continued)
### Structure

<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>• Use a mostly straightforward structure and a wide range of transitions (chiefly literary nonfiction)</td>
<td>• Use a somewhat complex structure and a full range of transitions (chiefly literary nonfiction)</td>
<td>• Use a complex structure (chiefly literary nonfiction)</td>
<td>• Use a highly complex structure (chiefly literary nonfiction)</td>
</tr>
<tr>
<td>• Offer insights into people, situations, and events (e.g., motives)</td>
<td>• Offer deep insights into people, situations, and events (e.g., motives in conflict)</td>
<td>• Offer sophisticated and profound insights into people, situations, and events (e.g., philosophical commentary)</td>
<td>• Offer sophisticated and profound insights into people, situations, and events (e.g., philosophical commentary)</td>
</tr>
<tr>
<td>• May contain subplots, flashbacks, and flash-forwards (chiefly stories)</td>
<td>• May contain numerous subplots, flashbacks, and flash-forwards as well as parallel and nonlinear plots; may lack clear resolution (chiefly stories)</td>
<td>• May contain numerous subplots, flashbacks, and flash-forwards as well as parallel and nonlinear plots; may lack clear resolution (chiefly stories)</td>
<td>• May contain plots that are intricate, nonlinear, and/or difficult to discern; may lack resolution or may not be plot driven (chiefly stories)</td>
</tr>
<tr>
<td>• Explore largely straightforward conflicts that may be internal or external (chiefly stories)</td>
<td>• Explore subtle conflicts that may be internal or external (chiefly stories)</td>
<td>• Explore complex conflicts that are largely internal and lack an obvious or easy resolution (e.g., moral dilemmas) (chiefly stories)</td>
<td>• Explore complex conflicts that are largely internal and lack an obvious or easy resolution (e.g., moral dilemmas) (chiefly stories)</td>
</tr>
<tr>
<td>• May have multiple narrators, with switches clearly signaled; main characters exhibit growth and change (chiefly stories)</td>
<td>• May have multiple narrators; main characters are well rounded (chiefly stories)</td>
<td>• May have multiple and/or unreliable narrator(s); main characters are well rounded (chiefly stories)</td>
<td>• May have multiple and/or unreliable narrator(s); main characters are well rounded (chiefly stories)</td>
</tr>
</tbody>
</table>
### Interpreting Your ACT Test Scores and Ranks

#### Taking Additional Practice Tests

<table>
<thead>
<tr>
<th></th>
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<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>• Use some uncommon words and phrases (e.g., general academic [tier 2] words, archaic words, dialect)</td>
<td>• Use some uncommon words and phrases (e.g., general academic [tier 2] words, archaic words, dialect)</td>
<td>• Consistently use uncommon words and phrases (e.g., general academic [tier 2] words, archaic words, dialect)</td>
<td>• Extensively use uncommon words and phrases (e.g., general academic [tier 2] words, archaic words, dialect)</td>
</tr>
<tr>
<td>• Use varied sentence structures significantly more or less formal than in everyday language</td>
<td>• Use varied, often complex, and formal sentence structures, with texts from earlier time periods containing structures uncommon in more modern reading</td>
<td>• Use varied, often complex, and formal sentence structures, with texts from earlier time periods containing structures uncommon in more modern reading</td>
<td>• Use varied, often complex, and formal sentence structures, with texts from earlier time periods containing structures uncommon in more modern reading</td>
</tr>
<tr>
<td>• Use some somewhat challenging nonliteral and figurative language and literary devices (e.g., symbols, irony)</td>
<td>• Consistently use somewhat challenging nonliteral and figurative language and literary devices (e.g., symbols, irony)</td>
<td>• Consistently use challenging nonliteral and figurative language and literary devices (e.g., extended metaphors, satire, parody)</td>
<td>• Extensively use challenging nonliteral and figurative language and literary devices (e.g., extended metaphors, satire, parody)</td>
</tr>
<tr>
<td>• Observe language conventions (e.g., standard paragraph breaks) (chiefly stories)</td>
<td>• Largely observe language conventions, with some unconventional elements possible (e.g., dialogue marked with dashes) (chiefly stories)</td>
<td>• May use unconventional language structures (e.g., stream-of-consciousness)</td>
<td>• Use unconventional language structures (e.g., stream-of-consciousness)</td>
</tr>
</tbody>
</table>

(continued)
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>• Depict some abstract ideas and concepts that may be important to understanding the text</td>
<td>• Depict several abstract ideas and concepts that are essential to understanding the text</td>
<td>• Depict numerous abstract ideas and concepts that are essential to understanding the text</td>
<td>• Depict numerous abstract ideas and concepts that are essential to understanding the text</td>
<td></td>
</tr>
<tr>
<td>Density (chiefly literary nonfiction)</td>
<td>• Have moderate information/concept density</td>
<td>• Have moderately high information/concept density</td>
<td>• Have high information/concept density</td>
<td>• Have very high information/concept density</td>
</tr>
<tr>
<td>Knowledge Demands: Textual Analysis, Life Experiences, Cultural and Literary Knowledge</td>
<td>• Assume readers can read on literal and inferential levels • Assume readers can handle somewhat challenging themes and subject matter with some maturity and objectivity • Assume readers can relate to experiences outside of their own • Call on cultural or literary knowledge to some extent</td>
<td>• Assume readers can read on literal, inferential, and interpretive levels • Assume readers can handle somewhat challenging themes and subject matter with some maturity and objectivity • Assume readers can relate to experiences distinctly different from their own</td>
<td>• Assume readers can read on literal, inferential, and interpretive levels • Assume readers can handle complex themes and subject matter with maturity and objectivity • Assume readers can relate to experiences distinctly different from their own</td>
<td>• Assume readers can read on literal, inferential, and interpretive levels • Assume readers can handle complex themes and subject matter with maturity and objectivity • Assume readers can relate to experiences distinctly different from their own • Require cultural or literary knowledge for full comprehension</td>
</tr>
</tbody>
</table>
(continued)

|-----------------------------------------|--------------------------------------|----------------------------|----------------------------------|
| • Have low intertextuality (i.e., make no/few or unimportant connections to other texts); drawing connections between texts at the level of theme may enhance understanding and appreciation | • Call on cultural or literary knowledge to some extent  
• Have moderate intertextuality (i.e., make some important connections to other texts); drawing connections between texts may enhance understanding and appreciation | • Have moderate intertextuality (i.e., make some important connections to other texts); drawing connections between texts may enhance understanding and appreciation | • Have high intertextuality (i.e., make many important connections to other texts); drawing connections between texts is essential for full understanding and appreciation |

<table>
<thead>
<tr>
<th>Informational Texts: Social Science, Humanities, and Natural Science</th>
</tr>
</thead>
<tbody>
<tr>
<td><strong>Purpose</strong></td>
</tr>
<tr>
<td>Somewhat Challenging Informational Texts</td>
</tr>
<tr>
<td>• Have a largely straightforward purpose</td>
</tr>
<tr>
<td>More Challenging Informational Texts</td>
</tr>
<tr>
<td>• Have a largely straightforward to somewhat complex purpose</td>
</tr>
<tr>
<td>Complex Informational Texts</td>
</tr>
<tr>
<td>• Have a somewhat complex to complex purpose; apparent purpose may differ from real purpose</td>
</tr>
<tr>
<td>Highly Complex Informational Texts</td>
</tr>
<tr>
<td>• Have a complex purpose; apparent purpose may differ from real purpose</td>
</tr>
</tbody>
</table>

(continued)
### Structure

- Use a mostly straightforward structure and a wide range of transitions
- Exhibit norms and conventions of a general discipline (e.g., natural science)

- Use a somewhat complex structure and a full range of transitions
- Exhibit norms and conventions of a general discipline (e.g., natural science)

- Use a complex structure
- Exhibit norms and conventions of a general discipline (e.g., natural science)

- Use a highly complex and possibly highly formalized structure (e.g., journal article)
- Exhibit norms and conventions of a specific discipline (e.g., biology)

### Language

- Use some general academic [tier 2] and domain-specific [tier 3] words and phrases
- Use varied and some long and complicated sentence structures

- Consistently use general academic [tier 2] and domain-specific [tier 3] words and phrases
- Use varied and often complex sentence structures, with consistent use of long and complicated structures

- Consistently use general academic [tier 2] and domain-specific [tier 3] words and phrases
- Use varied and often complex sentence structures, with consistent use of long and complicated structures

- Extensively use general academic [tier 2] and domain-specific [tier 3] words and phrases
- Use varied and often complex sentence structures, with consistent use of long and complicated structures

### Abstractness

- Depict some abstract ideas and concepts that may be important to understanding the text

- Depict several abstract ideas and concepts that are essential to understanding the text

- Depict numerous abstract ideas and concepts that are essential to understanding the text

- Depict numerous abstract ideas and concepts that are essential to understanding the text

### Density

- Have moderate information/concept density

- Have moderately high information/concept density

- Have high information/concept density

- Have very high information/concept density
<table>
<thead>
<tr>
<th>Knowledge Demands: Textual Analysis, Life Experiences, Content and Discipline Knowledge</th>
<th>Somewhat Challenging Informational Texts</th>
<th>More Challenging Informational Texts</th>
<th>Complex Informational Texts</th>
<th>Highly Complex Informational Texts</th>
</tr>
</thead>
<tbody>
<tr>
<td>• Assume readers can read on literal and inferential levels</td>
<td>• Assume readers can read on literal, inferential, and evaluative levels</td>
<td>• Assume readers can read on literal, inferential, and evaluative levels</td>
<td>• Assume readers can read on literal, inferential, and evaluative levels</td>
<td></td>
</tr>
<tr>
<td>• Assume readers can handle somewhat challenging subject matter, including perspectives, values, and ideas unlike their own, with some maturity and objectivity</td>
<td>• Assume readers can handle somewhat challenging subject matter, including perspectives, values, and ideas unlike their own, with some maturity and objectivity</td>
<td>• Assume readers can handle challenging subject matter, including perspectives, values, and ideas in opposition to their own, with maturity and objectivity</td>
<td>• Assume readers can handle complex subject matter, including perspectives, values, and ideas in opposition to their own, with maturity and objectivity</td>
<td></td>
</tr>
<tr>
<td>• Assume readers have everyday knowledge and some broad content knowledge, with texts at the high end of the range assuming some content knowledge</td>
<td>• Assume readers have some content knowledge, with texts at the high end of the range assuming some discipline-specific content knowledge</td>
<td>• Assume readers have some discipline-specific content knowledge</td>
<td>• Assume readers have extensive discipline-specific content knowledge, often in specialized subjects or areas</td>
<td></td>
</tr>
<tr>
<td>• Have low intertextuality (i.e., make no/few or unimportant connections to other texts); drawing connections between texts at the level of general concept may enhance understanding</td>
<td>• Have moderate intertextuality (i.e., make some important connections to other texts); drawing connections between texts may enhance understanding</td>
<td>• Have moderate intertextuality (i.e., make some important connections to other texts); drawing connections between texts may enhance understanding</td>
<td>• Have high intertextuality (i.e., make many important connections to other texts); drawing connections between texts is essential for full understanding</td>
<td></td>
</tr>
</tbody>
</table>
ACT College and Career Readiness Standards—Science

These standards describe what students who score in specific score ranges on the science test are likely to know and be able to do.

- Students who score in the 1–12 range are most likely beginning to develop the knowledge and skills assessed in the other ranges.
- The ACT College Readiness Benchmark for science is 23. Students who achieve this score on the ACT science test have a 50% likelihood of achieving a B or better in a first-year biology course at a typical college. The knowledge and skills highly likely to be demonstrated by students who meet the benchmark are shaded.

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Interpretation of Data (IOD)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>IOD 201. Select one piece of data from a simple data presentation (e.g., a simple food web diagram)</td>
</tr>
<tr>
<td></td>
<td>IOD 202. Identify basic features of a table, graph, or diagram (e.g., units of measurement)</td>
</tr>
<tr>
<td></td>
<td>IOD 203. Find basic information in text that describes a simple data presentation</td>
</tr>
<tr>
<td>16–19</td>
<td>IOD 301. Select two or more pieces of data from a simple data presentation</td>
</tr>
<tr>
<td></td>
<td>IOD 302. Understand basic scientific terminology</td>
</tr>
<tr>
<td></td>
<td>IOD 303. Find basic information in text that describes a complex data presentation</td>
</tr>
<tr>
<td></td>
<td>IOD 304. Determine how the values of variables change as the value of another variable changes in a simple data presentation</td>
</tr>
<tr>
<td>20–23</td>
<td>IOD 401. Select data from a complex data presentation (e.g., a phase diagram)</td>
</tr>
<tr>
<td></td>
<td>IOD 402. Compare or combine data from a simple data presentation (e.g., order or sum data from a table)</td>
</tr>
<tr>
<td></td>
<td>IOD 403. Translate information into a table, graph, or diagram</td>
</tr>
<tr>
<td></td>
<td>IOD 404. Perform a simple interpolation or simple extrapolation using data in a table or graph</td>
</tr>
<tr>
<td>24–27</td>
<td>IOD 501. Compare or combine data from two or more simple data presentations (e.g., categorize data from a table using a scale from another table)</td>
</tr>
<tr>
<td></td>
<td>IOD 502. Compare or combine data from a complex data presentation</td>
</tr>
<tr>
<td></td>
<td>IOD 503. Determine how the values of variables change as the value of another variable changes in a complex data presentation</td>
</tr>
<tr>
<td></td>
<td>IOD 504. Determine and/or use a simple (e.g., linear) mathematical relationship that exists between data</td>
</tr>
<tr>
<td></td>
<td>IOD 505. Analyze presented information when given new, simple information</td>
</tr>
</tbody>
</table>
### Interpretation of Data (IOD) (continued)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Interpretation of Data (IOD)</th>
<th>Description</th>
</tr>
</thead>
<tbody>
<tr>
<td>28–32</td>
<td>IOD 601.</td>
<td>Compare or combine data from a simple data presentation with data from a complex data presentation</td>
</tr>
<tr>
<td></td>
<td>IOD 602.</td>
<td>Determine and/or use a complex (e.g., nonlinear) mathematical relationship that exists between data</td>
</tr>
<tr>
<td></td>
<td>IOD 603.</td>
<td>Perform a complex interpolation or complex extrapolation using data in a table or graph</td>
</tr>
<tr>
<td>33–36</td>
<td>IOD 701.</td>
<td>Compare or combine data from two or more complex data presentations</td>
</tr>
<tr>
<td></td>
<td>IOD 702.</td>
<td>Analyze presented information when given new, complex information</td>
</tr>
</tbody>
</table>

### Scientific Investigation (SIN)

<table>
<thead>
<tr>
<th>Score Range</th>
<th>Scientific Investigation (SIN)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>SIN 201. Find basic information in text that describes a simple experiment</td>
</tr>
<tr>
<td></td>
<td>SIN 202. Understand the tools and functions of tools used in a simple experiment</td>
</tr>
<tr>
<td>16–19</td>
<td>SIN 301. Understand the methods used in a simple experiment</td>
</tr>
<tr>
<td></td>
<td>SIN 302. Understand the tools and functions of tools used in a complex experiment</td>
</tr>
<tr>
<td></td>
<td>SIN 303. Find basic information in text that describes a complex experiment</td>
</tr>
<tr>
<td>20–23</td>
<td>SIN 401. Understand a simple experimental design</td>
</tr>
<tr>
<td></td>
<td>SIN 402. Understand the methods used in a complex experiment</td>
</tr>
<tr>
<td></td>
<td>SIN 403. Identify a control in an experiment</td>
</tr>
<tr>
<td></td>
<td>SIN 404. Identify similarities and differences between experiments</td>
</tr>
<tr>
<td></td>
<td>SIN 405. Determine which experiments used a given tool, method, or aspect of design</td>
</tr>
<tr>
<td>24–27</td>
<td>SIN 501. Understand a complex experimental design</td>
</tr>
<tr>
<td></td>
<td>SIN 502. Predict the results of an additional trial or measurement in an experiment</td>
</tr>
<tr>
<td></td>
<td>SIN 503. Determine the experimental conditions that would produce specified results</td>
</tr>
<tr>
<td>28–32</td>
<td>SIN 601. Determine the hypothesis for an experiment</td>
</tr>
<tr>
<td></td>
<td>SIN 602. Determine an alternate method for testing a hypothesis</td>
</tr>
<tr>
<td>33–36</td>
<td>SIN 701. Understand precision and accuracy issues</td>
</tr>
<tr>
<td></td>
<td>SIN 702. Predict the effects of modifying the design or methods of an experiment</td>
</tr>
<tr>
<td></td>
<td>SIN 703. Determine which additional trial or experiment could be performed to enhance or evaluate experimental results</td>
</tr>
</tbody>
</table>

*(continued)*
<table>
<thead>
<tr>
<th>Score Range</th>
<th>Evaluation of Models, Inferences, and Experimental Results (EMI)</th>
</tr>
</thead>
<tbody>
<tr>
<td>13–15</td>
<td>EMI 201. Find basic information in a model (conceptual)</td>
</tr>
<tr>
<td>16–19</td>
<td>EMI 301. Identify implications in a model</td>
</tr>
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<td></td>
<td>EMI 302. Determine which models present certain basic information</td>
</tr>
<tr>
<td>20–23</td>
<td>EMI 401. Determine which simple hypothesis, prediction, or conclusion is, or is not, consistent with a data presentation, model, or piece of information in text</td>
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<tr>
<td></td>
<td>EMI 402. Identify key assumptions in a model</td>
</tr>
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<td>EMI 403. Determine which models imply certain information</td>
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<tr>
<td></td>
<td>EMI 404. Identify similarities and differences between models</td>
</tr>
<tr>
<td>24–27</td>
<td>EMI 501. Determine which simple hypothesis, prediction, or conclusion is, or is not, consistent with two or more data presentations, models, and/or pieces of information in text</td>
</tr>
<tr>
<td></td>
<td>EMI 502. Determine whether presented information, or new information, supports or contradicts a simple hypothesis or conclusion, and why</td>
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<td></td>
<td>EMI 503. Identify the strengths and weaknesses of models</td>
</tr>
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<td></td>
<td>EMI 504. Determine which models are supported or weakened by new information</td>
</tr>
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<td></td>
<td>EMI 505. Determine which experimental results or models support or contradict a hypothesis, prediction, or conclusion</td>
</tr>
<tr>
<td>28–32</td>
<td>EMI 601. Determine which complex hypothesis, prediction, or conclusion is, or is not, consistent with a data presentation, model, or piece of information in text</td>
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<tr>
<td></td>
<td>EMI 602. Determine whether presented information, or new information, supports or weakens a model, and why</td>
</tr>
<tr>
<td></td>
<td>EMI 603. Use new information to make a prediction based on a model</td>
</tr>
<tr>
<td>33–36</td>
<td>EMI 701. Determine which complex hypothesis, prediction, or conclusion is, or is not, consistent with two or more data presentations, models, and/or pieces of information in text</td>
</tr>
<tr>
<td></td>
<td>EMI 702. Determine whether presented information, or new information, supports or contradicts a complex hypothesis or conclusion, and why</td>
</tr>
</tbody>
</table>
ACT College and Career Readiness Standards for science are measured in rich and authentic contexts based on science content that students encounter in science courses. This content includes the following:

### Life Science/Biology
- Animal behavior
- Animal development and growth
- Body systems
- Cell structure and processes
- Ecology
- Evolution
- Genetics
- Homeostasis
- Life cycles
- Molecular basis of heredity
- Origin of life
- Photosynthesis
- Plant development, growth, structure
- Populations
- Taxonomy

### Physical Science/Chemistry, Physics
- Atomic structure
- Chemical bonding, equations, nomenclature, reactions
- Electrical circuits
- Elements, compounds, mixtures
- Force and motions
- Gravitation
- Heat and work
- Kinetic and potential energy
- Magnetism
- Momentum
- The periodic table
- Properties of solutions
- Sound and light
- States, classes, and properties of matter
- Waves

### Earth and Space Science
- Earthquakes and volcanoes
- Earth’s atmosphere
- Earth’s resources
- Fossils and geological time
- Geochemical cycles
- Groundwater
- Lakes, rivers, oceans
- Mass movements
- Plate tectonics
- Rocks, minerals
- Solar system
- Stars, galaxies, and the universe
- Water cycle
- Weather and climate
- Weathering and erosion
Part Five:
Moving Forward to Test Day

In This Part

Even when you are fully prepared, mentally and physically, to take the ACT, you may need additional guidance to handle the logistics of arriving at the test center on time and with the necessary items. This part helps you avoid any unpleasant surprises on test day that might cause confusion and anxiety, which could negatively affect your performance. Specifically, in this part, you learn how to do the following:

- Register for a convenient test date and test center in plenty of time to have your scores reported to the colleges and scholarship agencies of your choice by their deadlines
- Map a route and choose a means of travel that ensure you arrive at the test center on time
- Dress for comfort to ensure that you are not too hot or too cold when taking the test
- Pack everything you need for test day, so you are admitted to the testing room and have the items you need to take the test
- Find out what to expect at the test center in terms of check-in procedures, rules, and maintaining your composure and energy
- Obtain additional information you may need, including how to void your answer documents on test day, retake the test, and gather additional information
Chapter 13: Registering, Planning, and Packing for Test Day

When you feel ready to take the actual ACT, the time has come to register, plan, and pack for the upcoming day. Your goal is to avoid any unpleasant surprises on test day, such as getting lost on the way to the test center, showing up without your ACT admission ticket and a valid ID, or wearing the wrong clothing and being physically uncomfortable during the entire test. Such surprises distract you from what should be your sole focus on test day—doing your very best on the test.

In this chapter, we help you register for the ACT, avoid the most common pitfalls that test-takers encounter leading up to test day, offer guidance on how to dress and what to pack for test day, explain what you can expect at the test center, and give you a heads up about posttest concerns, such as voiding your test documents on test day, retaking the test, and reporting your scores.
National Testing Program versus School/District/State Testing

ACT makes the test available via national testing centers and through certain schools, school districts, or states. Registration for and administration of the test varies accordingly. For example, if your school, district, or state offers the test, you do not need to register to take the test at a national testing center on a Saturday. Instead, your school, district, or state registers for the test and chooses a school day on which to administer it. Check with your counselor to find out whether your school offers the ACT or whether you must register individually to take the ACT at a national testing center.

Registering for the ACT

If your school, district, or state offers the ACT, you do not need to register to take the test on a Saturday through the ACT national testing program. Instead, your school, district, or state takes the following registration steps for you prior to test day, and you can skip ahead to the section “Planning and Packing for Test Day”:

- Selects a test date (typically a school day)
- Chooses whether students will take the ACT with or without the writing test

Note: If you have a diagnosed disability and documentation of receiving an accommodation in school, you may be eligible to take the ACT with that accommodation. Work with your school counselor or accommodations coordinator to determine if they have submitted the required accommodation documentation.

If your school does not offer the ACT, you must register for it through the ACT national testing program and receive an admission ticket as proof of your registration. In the following sections, we lead you through the process of choosing a national test date and test option (ACT with or without the writing test) and registering for the test. We also address special circumstances that could affect your registration.

Selecting a National Testing Date and Location

Prior to registering for the ACT through the ACT national testing program, choose the date on which you want to take the test. When choosing a date, consider the following:

- Available test dates and test centers near you
- College and scholarship application deadlines
- Where you stand in your high school course work
- Whether you may want to take the ACT more than once

Let’s look at each of these considerations in turn.
Checking Available Test Dates and Test Centers

The ACT is offered nationally and internationally several times a year. However, it’s not offered at every test center on each test date. If you need to take the ACT on a day other than Saturday (for religious reasons), you’ll want to be especially attentive in selecting a test date when a test center near you is open on a non-Saturday date.

One of the first things you should find out, then, is where and when the ACT is being offered in your area. A quick and easy way to access available test dates and find test centers is to visit ACT’s website at www.actstudent.org. Search for test dates and deadlines to find test dates and registration deadlines. You can also look at nearby ACT test centers by searching for ACT test centers.

Note: You may not receive scores from more than one test taken on a scheduled national or international test date and one of the alternate test dates associated with that date. For example, suppose you take the test on Saturday and then again on the non-Saturday date associated with that Saturday. We will report only the scores from the first test. The second set of scores will be cancelled without refund.

Considering College and Scholarship Application Deadlines

Colleges and scholarship agencies may require that ACT test scores be submitted sometime during your junior year of high school. Find out what these deadlines are and then make absolutely sure that you take the test early enough to ensure that the colleges and scholarship agencies you’re applying to receive your ACT test scores by those deadlines.

Score reports are usually ready about 3 to 8 weeks after the test date. To be on the safe side, consider taking your ACT at least 10 weeks prior to the earliest deadline.

You may not be certain yet which school or program you’ll decide on. That’s okay. Just be sure you’re doing everything, including taking the ACT, early enough to keep all options open.

Gauging Where You Stand in Your High School Course Work and Whether You May Want to Take the ACT More Than Once

Another consideration in deciding when to take the ACT is where you stand in your high school course work. If you’re in a college-prep program and taking a lot of courses in English, mathematics, and science in your sophomore and junior years, taking the ACT in your junior year, while those subjects are still fresh in your memory, is probably best.

Perhaps you’ll decide to take the ACT more than once, in hopes of improving your score. In that case, it’s better to take the exam early in the spring of your junior year to allow time for a second try. If you find you’re studying a significant amount of material covered on the ACT during your senior year, you may plan on retaking the ACT in your senior year, based on the reasonable assumption that your scores will reflect your improved knowledge and skills.
Taking the ACT in your junior year has several advantages:

- You probably will have completed much of the course work corresponding to the material covered on the ACT.
- You will have your ACT scores and other information in time to help make decisions about your final year of high school course work. (For example, you may decide to take additional classes in an area in which your test score was lower than you wanted it to be.)
- Colleges will know of your interest and have your scores in time to contact you during the summer before your senior year, when many of them like to send information about admissions, scholarships, advanced placement, and special programs to prospective students.
- You’ll have your ACT scores and information from colleges in time to make decisions about visiting campuses or contacting schools.
- You’ll have the opportunity to take the ACT again if you feel your scores don’t accurately reflect your achievement.

**Selecting a Test Option**

When you register, you must choose one of two test options—the ACT (which includes the four multiple-choice tests: English, mathematics, reading, and science), or the ACT with the optional writing test (which includes the four multiple-choice tests plus a 40-minute writing test). Taking the writing test does not affect your composite score.

Not all institutions require the ACT writing test. Check directly with the institutions you are considering to find out their requirements, or ask your high school counselor which test option you should take.

**Registering**

The fastest and easiest way to register to take the ACT through its national testing program is online at www.actstudent.org. When you register on the web, you will know immediately if your preferred test center has space for you, and you can print your admission ticket. Read all the information on your admission ticket carefully to make sure it is correct.

You are guaranteed a seat and test booklet at a test center only if you register by the deadline for a test date. If you miss the late registration deadline, you can try to test as a “standby” examinee. Testing as a standby costs more and does not guarantee you a seat or test booklet. If you decide to take your chance as a standby, be sure to follow the instructions for standby testing on the ACT website. You must print a copy of your standby ticket and bring it with you to the test center, along with acceptable identification. Standby examinees will be admitted only after all registered students have been seated for their test option.
Registering, Planning, and Packing for Test Day

However you register, you are encouraged to create your free ACT web account. You can use your ACT web account to do several things:

- View your scores and score report on the web at no charge
- Send your scores to additional colleges
- Receive e-mail updates from ACT about changes to your registration
- Make changes to your student profile
- Print your admission ticket

Registering Under Special Circumstances

See the website or our online registration brochure for instructions if special circumstances apply to you—for example, if your religious beliefs prevent you from taking the exam on Saturday and no test centers in your area offer non-Saturday test dates or if you have a diagnosed disability and require special accommodations.

If you have a diagnosed disability and documentation of receiving an accommodation in school, you may be eligible to take the ACT with that accommodation. Details about the procedures for applying to test with and accommodations are provided on the ACT website.

Planning and Packing for Test Day

At least one week before your scheduled test date, start planning and packing for test day. You need to know where you’re going, how you’re getting there, how much time the trip will take you, how to dress, and what to pack. In the following sections, we help you plan and pack for test day.

Getting to the Test Center

If your school is administering the ACT on a school day, you simply need to arrive at your school at the start of the school day. Testing will be the first activity of the day.

Under no circumstances will you be admitted to the test after the test booklets have been distributed, so be sure to arrive on time.

If you registered to take the test through the ACT national testing program, you’ll be asked to report to the test center by 8:00 AM on your test date. Under no circumstances will you be admitted after the test booklets have been distributed so be sure to arrive on time by 8:00 AM.

You may need to walk a few blocks to get to the test center or drive several hours, perhaps to an unfamiliar city. Whatever your situation, be certain to allow plenty of time. We recommend that you plan to arrive 15 to 30 minutes early just in case you experience an unexpected delay.
Test centers vary considerably. You may be taking the ACT in your own high school, at a local community college, or in a large building on a nearby university campus. Your surroundings may be quite familiar or they may be new. If they're new, allow yourself a few extra minutes to get acclimated. Then try to forget about your surroundings so that you can concentrate on the test.

To ensure that you arrive on time, map your route to the test center and choose a means of travel—car, train, bus, taxi, bicycle, carpool with a friend...whatever works best for you.

One week prior to test day, travel to the testing center using the selected means of travel. By doing a test run on the same day and at the same time (but a week early), you gain a better sense of what traffic will be like, what your parking options will be, whether the buses are running during those times, and so on.

**Dressing for Test Day**

The night before the test, set out the clothes you want to wear. Dress in layers so that you can adjust to the temperature in your testing room.

Keep in mind that you're going to be sitting in the same place for more than three hours. Wearing something you're especially comfortable in may make you better able to relax and concentrate on the test. For many people, what they're wearing can make a difference in how they feel about themselves. Picking something you like and feel good wearing may boost your confidence.

**Packing for Test Day: What to Bring**

Bring with you only what you'll need that morning, because other materials will be in your way and may be prohibited in the test room. Be sure to bring these:

- **Your paper admission ticket** (if you are taking the test on a national or international ACT test date). You will *not* be admitted to the test without it. If your school, district, or state is administering the test, you will not receive (or need) an admission ticket.

- **Acceptable photo identification**. Examples of acceptable identification include current identification issued by your school or city/state/federal government on which both your name and current photograph appear (for example, driver's license or passport). Without acceptable identification, you will not be allowed to take the test. (See www.actstudent.org for details on what constitutes acceptable and unacceptable identification.)

- Several sharpened **soft-lead no. 2 pencils with good erasers** (no mechanical pencils or ink pens). Test the erasers to make sure they erase cleanly without leaving any residue.
• **A watch without an alarm function** to pace yourself. If your watch has an alarm function and the alarm goes off, it will disturb the other students, you will be dismissed, and your answer document will not be scored. Although the test supervisor will announce when 5 minutes remain on each test, not all test rooms have wall clocks for pacing yourself in the meantime.

• **A permitted calculator** if you wish to use one on the mathematics test only (for a list of permitted and prohibited calculators, visit www.actstudent.org). You are solely responsible for knowing whether a particular calculator is permitted.

• **A snack and a drink** to consume outside the test room only during the break.

### Obtaining Additional Test Details
On certain national test dates, if you test at a national test center, you may request and pay for a copy of the test questions used to determine your score, a copy of your answers, a list of correct answers, and scoring instructions. If you take the writing test, you will also receive a copy of the prompt, the scoring rubric, and the scores assigned by the two readers. You’ll also get information about requesting an actual copy of your answer document for an additional fee. These services are not offered for all test dates, so if you’re interested in receiving any of these services, you’ll need to check the dates on ACT’s website (www.actstudent.org) to be sure you’re choosing a test date on which the desired service is available.

### At the Test Center
Knowing ahead of time what to expect at the test center can alleviate any anxiety you may feel, ensure that you do everything ACT requires in terms of checking in and obeying the rules, and help you maintain your composure. In the following sections, we describe the check-in procedure, present the rules, encourage you to communicate with the testing staff (if necessary), and provide tips on maintaining your composure and energy level.

### Checking In
The way **check-in procedures** are handled may vary from location to location. You may find that all students are met at a central location and directed from there to different classrooms. Signs may be posted, telling you that everyone whose last name falls between certain letters should report directly to a particular room. However this part of the check-in is handled at your location, you can anticipate that certain check-in procedures will be performed, including verification of your identity.

In the room you’ll be directed to a seat by a member of the testing staff. If you are left-handed, let the testing staff know so that an appropriate desk or table may be made available to you.
Following the Rules
The following behaviors are prohibited. You will be dismissed and your answer document will not be scored if you are found doing any of the following:

- Filling in or altering responses on a test section on your answer sheet or continuing to complete the essay after time has been called on that test section; this means that you cannot make any changes to a test section outside of the designated time for that section, even to fix a stray mark or accidental keystroke
- Looking back at a test section on which time has already been called
- Looking ahead in the test booklet
- Looking at another person’s test booklet or answer document
- Giving or receiving assistance by any means
- Discussing or sharing test content, test form identification numbers, or answers during test administration, during breaks, or after the test
- Using a prohibited calculator
- Using a calculator on any test section other than mathematics
- Sharing a calculator with another person
- Using a watch with recording, Internet, or communication capabilities
- Using any electronic device at any time during testing or during breaks other than an approved calculator or watch; all other electronic devices, including cell phones and wearable devices, must be turned off and placed out of reach from the time you are admitted to test until you are dismissed after testing concludes
- Attempting to memorize test-related information or otherwise remove test materials, including questions or answers, from the test room in any way
- Using highlight pens, colored pens or pencils, notes, dictionaries, or other aids
- Using scratch paper (unless an exception applies)
  - Specific instructions will be provided on test day if ACT authorized you to use scratch paper, including the section(s) on which ACT has authorized its use.
  - If you are permitted to use scratch paper, you may use only paper that ACT has authorized and/or provided to you.
- Not following instructions or abiding by the rules of the test center
Exhibiting confrontational, threatening, or unruly behavior, or violating any laws; if ACT suspects you are engaging in criminal activities, such activities will be reported to law enforcement agencies

Allowing an alarm to sound in the test room or creating any other disturbance

All items brought into the test center, such as hats, purses, backpacks, cell phones, calculators, and other electronic devices, may be searched at the discretion of ACT and its testing staff. ACT and its testing staff may confiscate and retain for a reasonable period of time any item suspected of having been used, or being capable of being used, in violation of this list of prohibited behaviors. ACT may also provide such items to third parties in connection with an investigation conducted by ACT or others. ACT and its testing staff shall not be responsible for lost, stolen, or damaged items.

Examinees who are dismissed because of prohibited behavior forfeit their registration for that test date. There are no options for refunds or appeals in situations involving prohibited behavior.

Eating, drinking, and the use of tobacco are not allowed in the test room. You may bring a snack to eat or drink before the test or during the break, but any food or beverage you bring must be put away during testing and must be consumed outside the test room.

**Communicating with the Testing Staff**

Although you are required to work silently during the test, you may need to communicate with the testing staff under certain circumstances, such as the following:

- **If you have problems with the testing environment, let the testing staff know immediately.** Possible problems include being seated below, over, or next to a heating or cooling vent that is making you too warm or too cold; having a defective chair or desk; poor lighting that makes reading difficult; or excessive noise.

- **If any aspect of the test-taking procedure is not perfectly clear to you, request clarification.** Testing staff will be available throughout the exam. In fact, they’ll be moving quietly around the room while you’re working. If you have a question about the administration of the test (not about any of the test questions), raise your hand and quietly ask for information.

- **If you need to use the restroom, ask.** Bathroom breaks are permitted during the test or between tests, but you’re not allowed to make up the lost time.

- **If you become ill during the test, you may turn in your test materials and leave, if necessary.** Let the testing staff know that you are ill and whether you wish to have your answer document scored. One caution: once you leave the test center, you won’t be allowed to return and continue—so be sure that leaving is what you want to do. You might try closing your eyes or putting your head on the desk for a minute first; then if you feel better, you’ll be able to continue.
Maintaining Your Composure and Energy

While you’re waiting for the test to begin, you may find yourself getting anxious or jittery. That’s perfectly normal. Most of us get nervous in new situations. People handle this nervousness in different ways.

Some people find it helpful to practice mental and physical relaxation techniques. If this appeals to you, try alternately flexing and relaxing your muscles, beginning at your toes and moving up through your shoulders, neck, and arms. Meanwhile, imagine yourself in a quiet, peaceful place: at the beach, in the mountains, or just in your favorite lounge chair. Breathe deeply and evenly.

Other people like to redirect that nervous energy and turn it to their advantage. For them, concentrating on the task at hand and shutting everything else out of their minds is the most helpful strategy. If this is your style, you may even want to close your eyes and imagine yourself already working on the exam, thinking about how it will feel to move confidently and smoothly through the tests.

If you have the chance, try out the two approaches on some classroom tests and see which one works better for you. The important thing is to keep the ACT in perspective. Try not to let it become larger than life. Remember, it’s just one part of a long academic and professional career. If you begin to feel tired during the test, check your posture to make sure you’re sitting up straight. Getting enough air in your lungs is difficult when you’re slouching. You’ll stay more alert and confident if your brain receives a steady supply of oxygen.

You might want to practice those relaxation techniques again, too, because tension contributes to fatigue. As you start a new test, you might find it helpful to stretch your neck and shoulder muscles, rotate your shoulders, stretch back in your chair and take some long, deep breaths.

You can expect a short break (approximately 10 to 15 minutes) after the second test. During this break, it’s a good idea to stand up, walk around a little, stretch, and relax. You may wish to get a drink, have a snack, or use the restroom. Keep in mind, though, that you still have work ahead of you that requires concentrated effort. Eat lightly and return to the room quickly. The third test will start promptly, and you’ll need to be back at your desk and ready to go on time.

Voiding Your Answer Documents on Test Day

If you have to leave the test center before completing all tests, you must decide whether you want your answer document scored and then inform your supervisor if you do not want your answer document scored; otherwise, your answer document will be scored.

Once you break the seal on your multiple-choice test booklet, you cannot request a test date change. If you do not complete all your tests and want to test again, you will have to pay the full fee for your test option again. If you want to take the ACT again, see www.actstudent.org for your options. Once you begin filling out your answer document, you cannot change from one test option to another.
Testing More Than Once
The following text is from www.actstudent.org with some changes. If you think you can improve your scores, you can retake the ACT. (You can take the ACT no more than 12 times total.) Many students take the test twice, once as a junior and again as a senior. Of the students who took the ACT more than once:

- 57% increased their Composite score
- 21% had no change in their Composite score
- 22% decreased their Composite score

You determine which set of scores are sent to colleges or scholarship programs. ACT will release only the scores from the test date (month and year) and test location (e.g., national, state, school) you designate. This protects you and ensures that you direct the reporting of your scores.

However, you cannot mix and match scores. For example, ACT will not send your mathematics test results from one test and your English test results from another.
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